

CS314 Spring 2014

Assignment 9

WILL NOT BE GRADED

Sample solution will be posted by Monday, May 5

Problem 1 – Vectorization

A statement-level dependence graph represents the dependences between statements in a loop nest. Nodes represent single statements, and edges dependences between statements. An edge is generated by a pair of array references that have a dependence. Edges are directed from the source of the dependence to its sink. For example, for a true dependence, the source is a write reference, and the sink is a read reference. There may be multiple edges (i.e., dependences) between two nodes in the graph.

```
      for i = 2, 99
S1:      a(i) = b(i-1) + c(i+1);
S2:      b(i) = c(i) + 3;
S3:      c(i) = c(i-1) + a(i);
      endfor;
```

Here is a basic vectorization algorithm based on a statement-level dependence graph:

1. Construct statement-level dependence graph considering true, anti, and output dependences; in the final dependence graph, the type of the dependence is not important any more
2. Detect strongly connected components (SCC) over the dependence graph; represent SCC as summary nodes; walk resulting graph in topological order; For each visited node do
 - (a) If SCC has more than one statement in it, distribute loop with statements of SCC as its body, and keep the code sequential.
 - (b) If SCC is a single statement and has no dependence cycle, distribute loop around it and “collapse” loop into a vector instruction. For example, the loop

```
      for i=1, 100
          a(i) = b(i) + 1;
      endfor
```

can be “collapsed” into a single vector instruction

$a(1:100) = b(1:100) + 1;$

. If there is a dependence cycle on the single statement, distribute the loop around the statement and keep loop sequential.

1. Show the statement-level dependence graph for the loop with its strongly connected components.
2. Show the generated code by the vectorization algorithm described above.

Problem 2 – Type Systems

Assume that E is a type environment that maps variables and constants to their type expressions. Assume that the environment already contains the following mappings

$E = \{ (1 \rightarrow \text{integer}), (2 \rightarrow \text{integer}), (\text{true} \rightarrow \text{boolean}), (\text{false} \rightarrow \text{boolean}) \}$

1. integer addition:

$$\frac{E \vdash e_1 : \text{integer} \quad E \vdash e_2 : \text{integer}}{E \vdash (+ e_1 e_2) : \text{integer}}$$

2. Polymorphic cons:

$$\frac{E \vdash e_1 : \alpha \quad E \vdash e_2 : \text{list}(\alpha)}{E \vdash (\text{cons } e_1 e_2) : \text{list}(\alpha)}$$

3. Polymorphic car:

$$\frac{E \vdash e : \text{list}(\alpha)}{E \vdash (\text{car } e) : \alpha}$$

4. Polymorphic '():

$$E \vdash '() : \text{list}(\alpha)$$

1. Give type rules for polymorphic function **cdr** and polymorphic function **null?** functions.
2. Apply the above type inference rules to determine whether the following programs can be typed. List every step explicitly. In case of a type error, show the situation where no rule can be applied any more, i.e., where your type inference process get's stuck.

(a) (car (cons (+ 1 2) '()))

- (b) `(cons true (cons 1 '()))`
- (c) `(cdr (cons 1 (cons 2 '())))`
- (d) `(cons 1 2)`
- (e) `(cons true '())`
- (f) `(null? '(1))`