

## Class Information

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- Seventh homework submission extension: Friday, April 18, before class.
- Second project extension: **Monday, April 21, 11:59pm**. There will be a chilled water outage during parts of April 15 and April 16.

## Review: Dependence — Overview

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**Definition** — There is a data dependence from statement  $S_1$  to statement  $S_2$  ( $S_1 \delta S_2$ ) if

1. Both statements access the same memory location, and
2. There is a run-time execution path from  $S_1$  to  $S_2$ .

### Data dependence classification

“ $S_2$  depends on  $S_1$ ” —  $S_1 \delta S_2$

**true (flow) dependence**

occurs when  $S_1$  writes a memory location that  $S_2$  later reads

**anti dependence**

occurs when  $S_1$  reads a memory location that  $S_2$  later writes

**output dependence**

occurs when  $S_1$  writes a memory location that  $S_2$  later writes

**input dependence**

occurs when  $S_1$  reads a memory location that  $S_2$  later reads. Note: Input dependences do not restrict statement (*load/store*) order!

## Review: Dependence — Basics

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### Theorem

Any reordering transformation that preserves every dependence (i.e., visits first the source, and then the sink of the dependence) in a program preserves the meaning of that program.

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Note: Dependence starts with the notion of a sequential execution, i.e., starts with a sequential program.

## Dependence — Where do we need it?

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We restrict our discussion to data dependence for scalar and subscripted variables (no pointers and no control dependence).

Examples:

do I = 1, 100	do I = 1, 99
do J = 1, 100	do J = 1, 100
A(I,J) = A(I,J) + 1	A(I,J) = A(I+1,J) + 1
enddo	enddo
enddo	enddo

### vectorization

$A(1:100:1, 1:100:1) = A(1:100:1, 1:100:1) + 1$   
 $A(1:99, 1:100) = A(2:100, 1:100) + 1$

### parallelization

doall I = 1, 100	do I = 1, 99
doall J = 1, 100	doall J = 1, 100
A(I,J) = A(I,J) + 1	A(I,J) = A(I+1,J) + 1
enddo	enddo
<i>implicit barrier sync.</i>	<i>implicit barrier sync.</i>
enddo	enddo
<i>implicit barrier sync.</i>	

# Dependence Analysis

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## Question

Do two variable references never/maybe/always access the same memory location?

## Benefits

- improves alias analysis
- enables loop transformations

## Motivation

- classic optimizations
- instruction scheduling
- data locality (register/cache reuse)
- vectorization, parallelization

## Obstacles

- array references
- pointer references

## Vectorization vs. Parallelization

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**vectorization** — Find parallelism in innermost loops;  
fine-grain parallelism

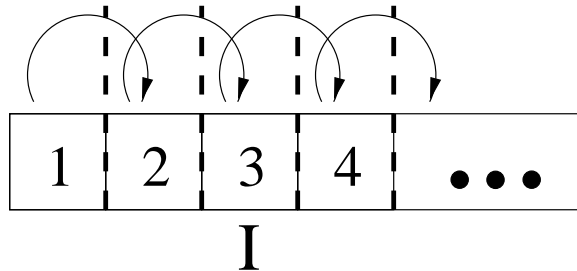
**parallelization** — Find parallelism in outermost loops;  
coarse-grain parallelism

- Parallelization is considered more complex than vectorization, since finding coarse-grain parallelism requires more analysis (e.g., interprocedural analysis).
- Automatic vectorizers have been very successful

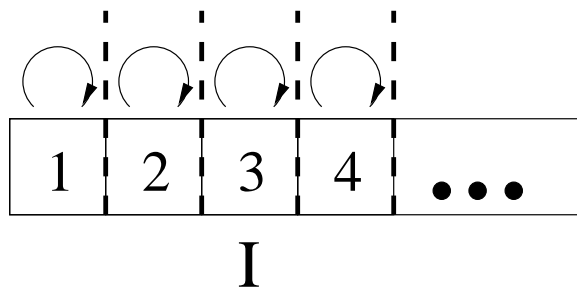
# Dependence Analysis for Array References

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```
do I = 1, 100
  A(I) =
    = A(I-1)
enddo
```



```
do I = 1, 100
  A(I) =
    = A(I)
enddo
```



A **loop-independent** dependence exists regardless of the loop structure. The source and sink of the dependence occur on the same loop iteration.

A **loop-carried** dependence is induced by the iterations of a loop. The source and sink of the dependence occur on different loop iterations.

*Loop-carried dependences can inhibit parallelization and loop transformations*