

Computer-Aided VLSI System Design

Final Project:

Elliptic Curve Cryptographic Processor

lecturer: Liang-Hsin Lin

Graduate Institute of Electronics Engineering, National Taiwan University



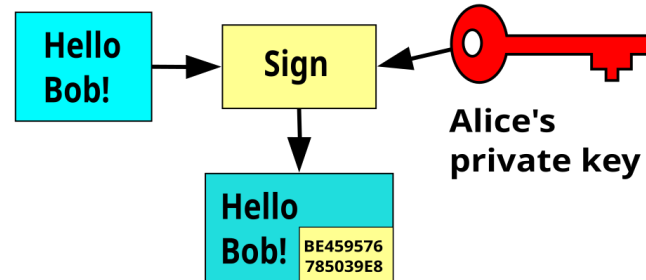
NTU GIEE



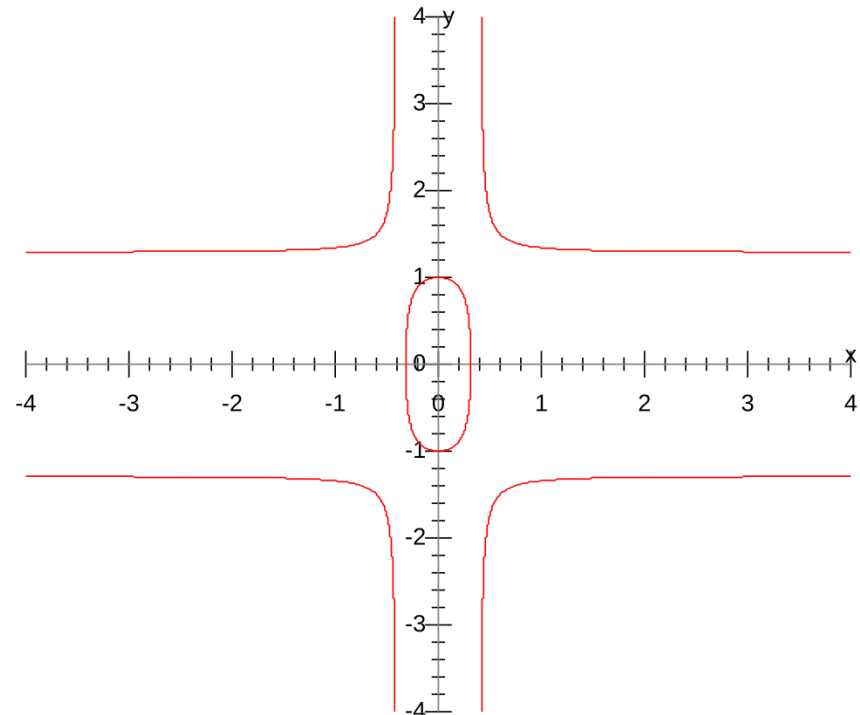
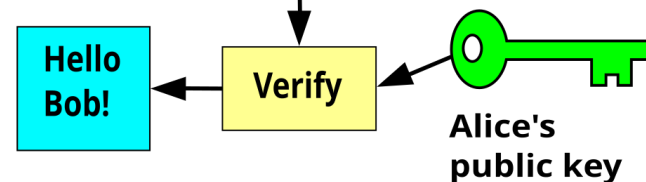
Overview

- Edwards-curve Digital Signature Algorithm (EdDSA) [1] is frequently used for data authentication nowadays
- Based on a mathematical structure: twisted Edward curve [2]
 - A special type of elliptic curve with strong security

Alice



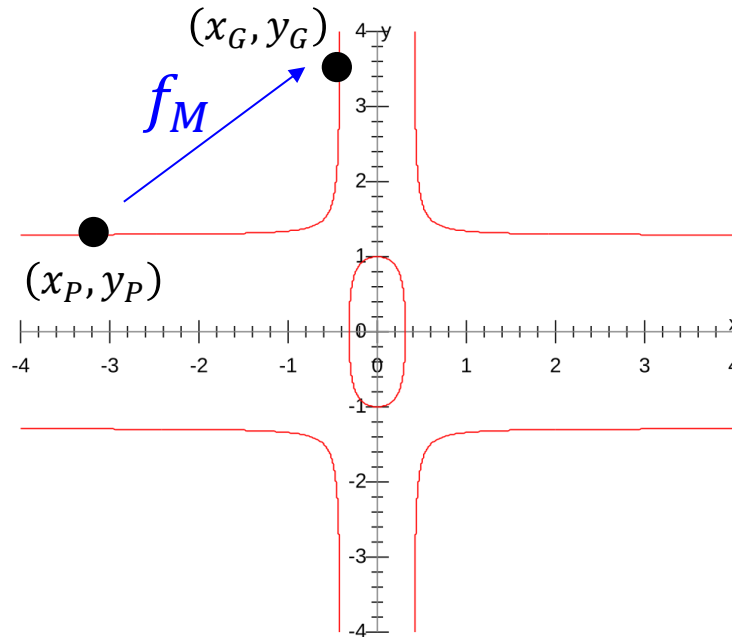
Bob





System Model

- **Project Goal:** Accelerate the core function in EdDSA
 - Given a point $P = (x_P, y_P)$ on a twisted Edwards curve
 - Compute another point $G = (x_G, y_G) = f_M(x_P, y_P)$

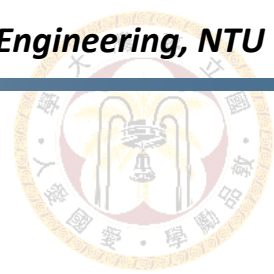


- However, **integers** instead of real numbers are used



Finite Field F_p

- Twisted Edward curve is based on finite field
- Given prime q , the set $F_q = \{0, 1, \dots, q - 1\}$ is called a finite field
- The operations between arbitrary $x, y \in F_q$ are defined by
 - Addition: $x + y \bmod q$
 - Subtraction: $x - y \bmod q$
 - Multiplication: $x \times y \bmod q$
 - Division: $x \times y^{-1}$ where $y^{-1} \in F_q$ s.t. $y \times y^{-1} \bmod q = 1$
- The “ $\bmod q$ ” is neglected in the following context for elements in F_q



Twisted Edwards Curve

- Given constant $a, d \in F_q$, the curve is defined by a set of points

$$E = \{(x \in F_q, y \in F_q) | ax^2 + y^2 = 1 + dx^2y^2\}$$

- The addition between two points $(x_1, y_1), (x_2, y_2)$ is defined by

$$(x_1, y_1) + (x_2, y_2) = \left(\frac{x_1y_2 + x_2y_1}{1 + dx_1x_2y_1y_2}, \frac{y_1y_2 - ax_1x_2}{1 - dx_1x_2y_1y_2} \right)$$



Projective Coordinates

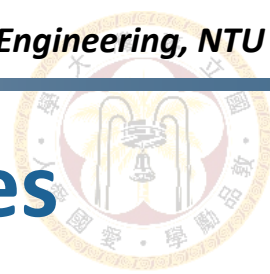
- Use (X_1, Y_1, Z_1) to represent $(x_1 = X_1/Z_1, y_1 = Y_1/Z_1)$
- The addition formula becomes

$$(X_1, Y_1, Z_1) + (X_2, Y_2, Z_2) = (X_3, Y_3, Z_3)$$

$$X_3 = Z_1 Z_2 (X_1 Y_2 + X_2 Y_1) (Z_1^2 Z_2^2 - d X_1 X_2 Y_1 Y_2)$$

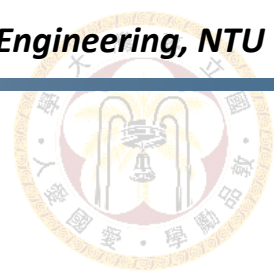
$$Y_3 = Z_1 Z_2 (Y_1 Y_2 - a X_1 X_2) (Z_1^2 Z_2^2 + d X_1 X_2 Y_1 Y_2)$$

$$Z_3 = (Z_1^2 Z_2^2 - d X_1 X_2 Y_1 Y_2) (Z_1^2 Z_2^2 + d X_1 X_2 Y_1 Y_2)$$



Advantage of Projective Coordinates

- Less modular divisions
- Example: $(x_1, y_1) + (x_1, y_1) + (x_1, y_1)$
 - **Without** projective coordinate (4 divisions):
 - $(x_2, y_2) = (x_1, y_1) + (x_1, y_1)$: 2 divisions
 - $(x_3, y_3) = (x_1, y_1) + (x_2, y_2)$: 2 divisions
 - **With** projective coordinate (2 divisions)
 - $(X_2, Y_2, Z_2) = (x_1, y_1, 1) + (x_1, y_1, 1)$: 0 division
 - $(X_3, Y_3, Z_3) = (X_2, Y_2, Z_2) + (x_1, y_1, 1)$: 0 division
 - $(X_3, Y_3, Z_3) \rightarrow (x_3, y_3)$: 2 divisions



EdDSA

- The core operation in EdDSA involves the following procedure
 - Given an integer M and a point $P = (x_p, y_p)$ on a Twisted Edward Curve

- Compute

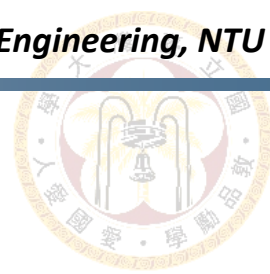
$$f_M(x, y) = M \times P = \underbrace{(x_p, y_p) + (x_p, y_p) + \cdots + (x_p, y_p)}_M$$

- Ed25519 is a EdDSA scheme based on the twisted Edward curve

$$E_{25519} = \{(x \in F_q, y \in F_q) | ax^2 + y^2 = 1 + dx^2y^2\}$$

where $q = 2^{255} - 19$, $a = q - 1$, and $d =$

0x52036cee2b6ffe738cc740797779e89800700a4d4141d8ab75eb4dca135978a3



Ed25519 System Overview

- Input: scalar M , point $P = (x_P, y_P) \in E_{25519}$
- Output: another point $G = (x_G, y_G) = M \times P$
- Three operation levels for Ed25519

**Scalar
Multiplication**

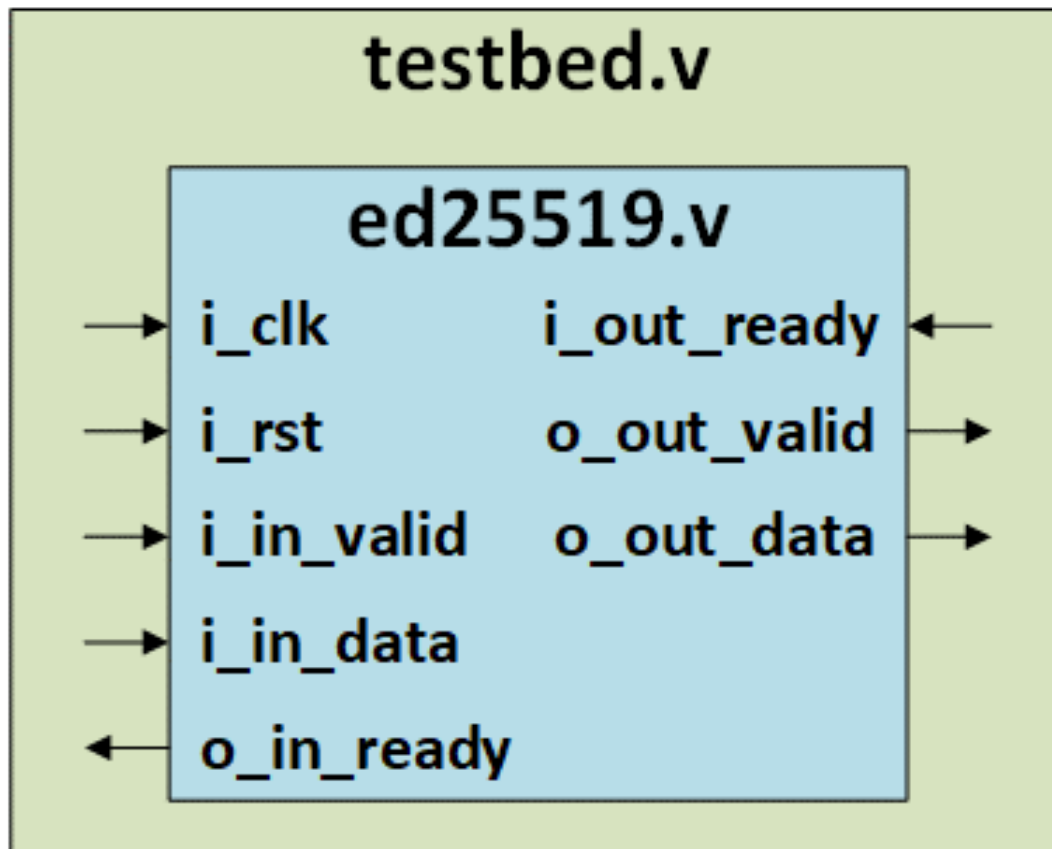
**Point addition
on Curve25519**

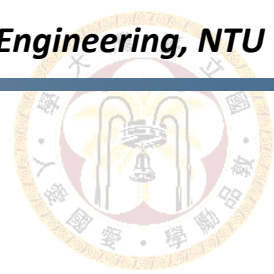
Modular operation

- $M \times P = M \times (x_P, y_P)$
- $(X_1, Y_1, Z_1) + (X_2, Y_2, Z_2)$
with projective coordinates
- $+, -, \times, \div$ on finite field F_q



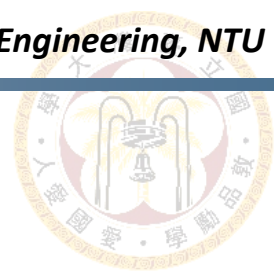
Block Diagram





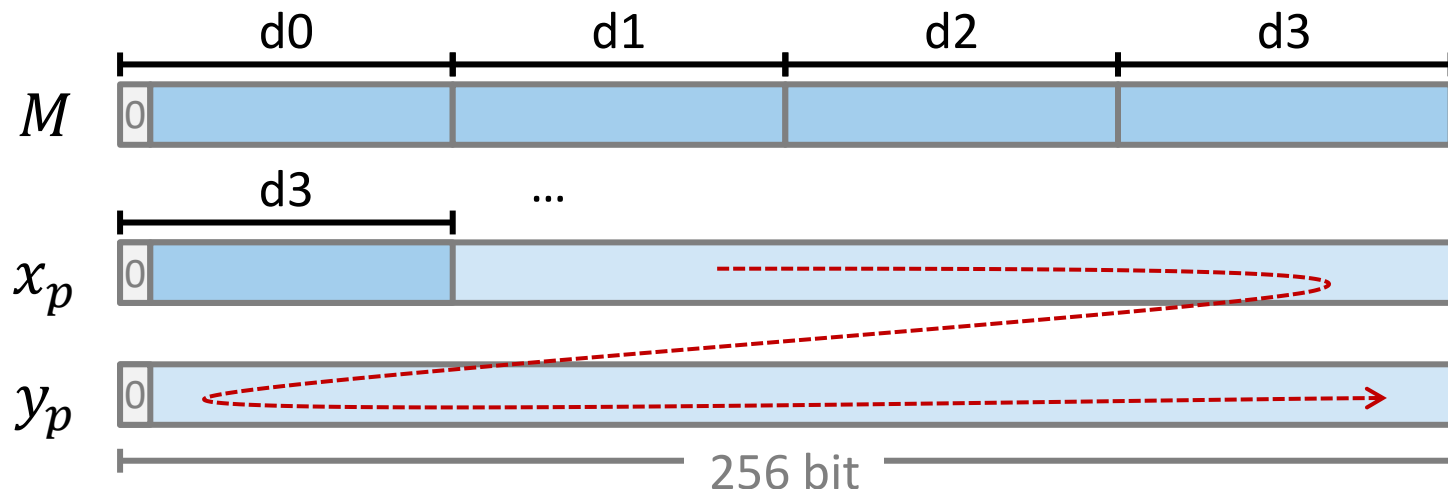
Input/Output

Signal Name	I/O	Width	Description
i_clk	I	1	System clock signal, synchronized on the rising edge
i_rst	I	1	Synchronous active high reset signal
i_in_valid	I	1	When high, indicates that i_in_data contains valid data
i_in_data	I	64	64-bit input data bus
i_out_ready	I	1	When high, indicates that testbench is ready to receive output data
o_in_ready	O	1	When high, indicates that the module is ready to accept input data
o_out_valid	O	1	When high, indicates that o_out_data contains valid output data
o_out_data	O	64	64-bit output data bus

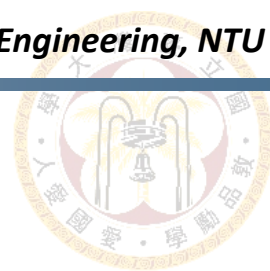


I/O Data Sequence

- The I/O data port is 64-bit
- Input sequence order: $M \rightarrow x_P \rightarrow y_P$
- Output sequence order: $x_G \rightarrow y_G$
- Each 255-bit data is expanded to 256 bits by adding 0 as the MSB
- Each data unit is transmitted starting from the MSB down to the LSB in 64-bit chunks



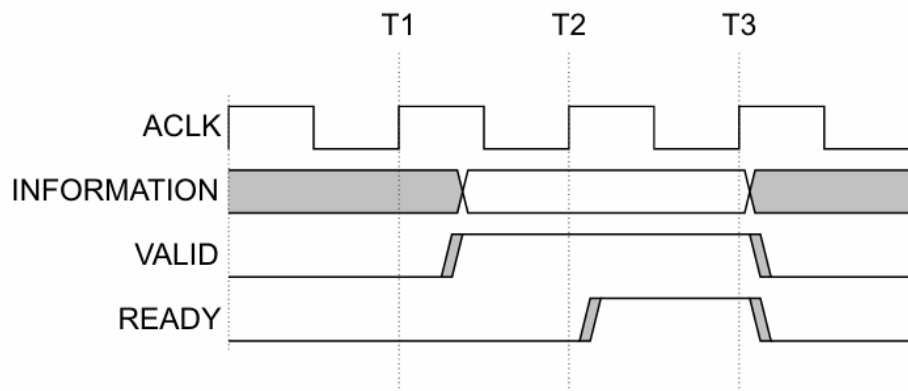
*Sequence: $d0, d1, d2, d3, \dots$



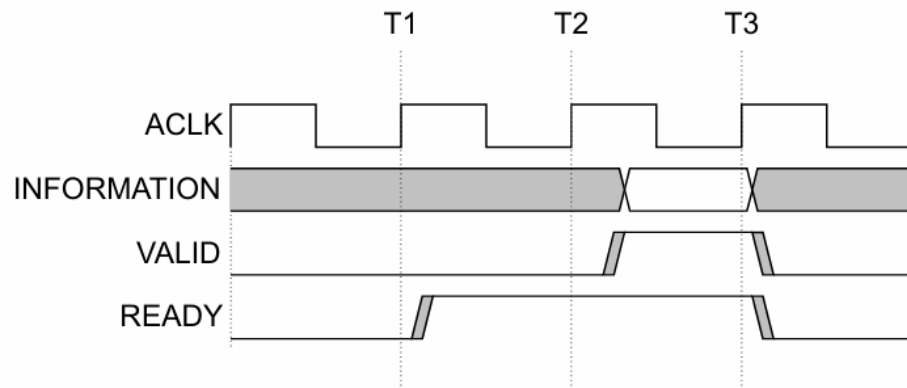
I/O Handshake

- The source generates the **VALID** signal to indicate when the data is available
- The destination generates the **READY** signal to indicate that it can accept the information
- Transfer occurs only when both the **VALID** and **READY** signals are HIGH
- There must be no combinatorial paths between input and output signals

VALID before READY handshake



READY before VALID handshake

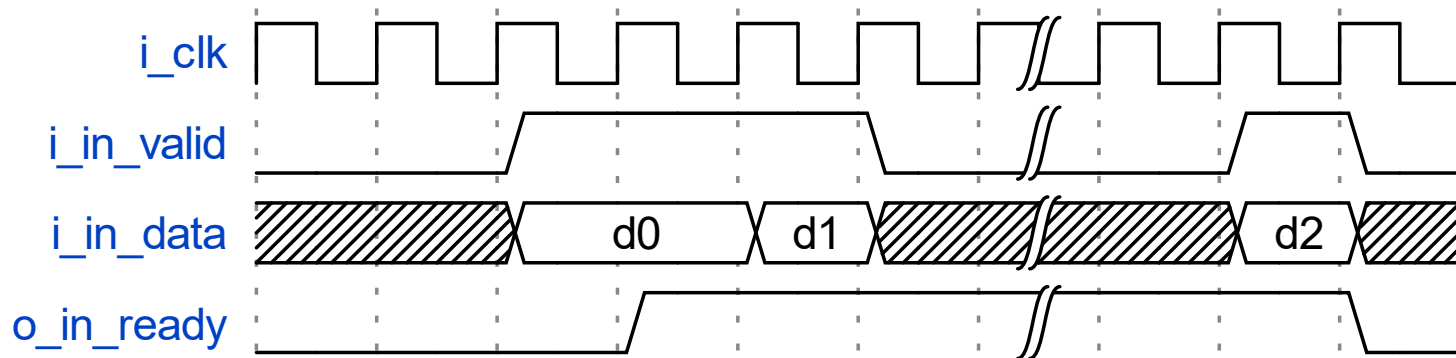


Reference: AMBA AXI and ACE Protocol Specification [5]

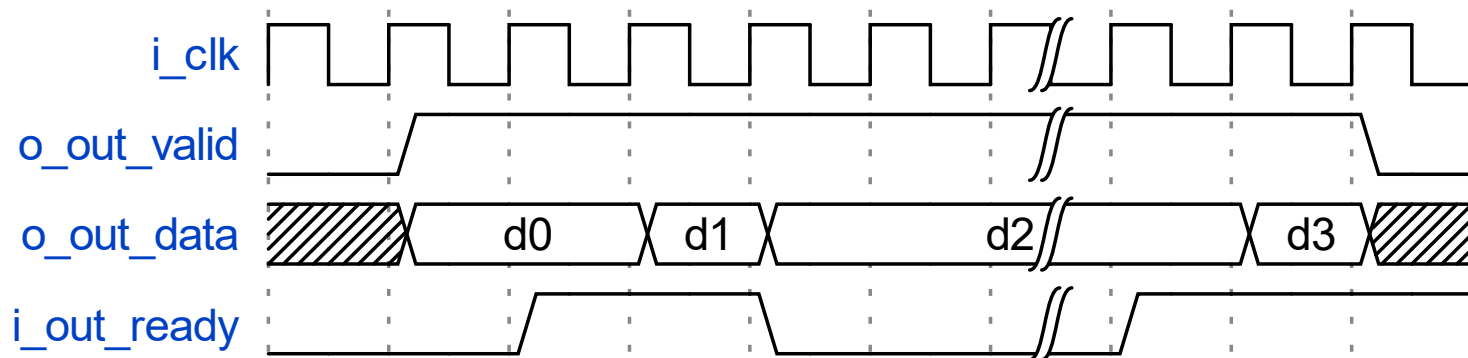


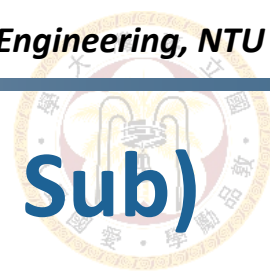
I/O Waveform

Input Interface



Output Interface





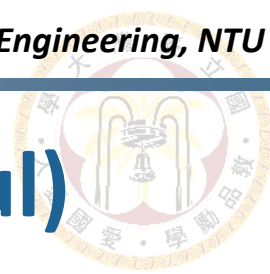
HW Implementation: Mod. Op. (Add & Sub)

- Let $x, y \in F_q$
- Modular addition:

$$x + y \bmod q = \begin{cases} x + y, & \text{if } x + y < q \\ x + y - q, & \text{otherwise} \end{cases}$$

- Modular subtraction:

$$x - y \bmod q = \begin{cases} x - y, & \text{if } x \geq y \\ x + (q - y), & \text{otherwise} \end{cases}$$



HW Implementation: Mod. Op. (Mul)

- Let $x, y \in F_q$, $R = 2^{255}$, q^{-1} be the inverse of q modular R ($q \times q^{-1} \bmod R = 1$)

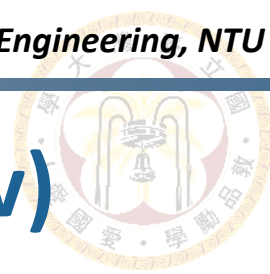
- Montgomery multiplication (MM): 512 → 255

$$MM(x, y) = \frac{xy}{R} \bmod q = \begin{cases} t - q, & \text{if } t \geq q \\ t, & \text{otherwise} \end{cases}$$

$$t = \frac{xy - (xyq^{-1} \bmod R)q}{R} \quad \text{255}$$

- Modular multiplication:

$$x \times y \bmod q = \underline{MM(MM(x, y), R^2 \bmod q)}$$



HW Implementation: Mod. Op. (Div)

- Let $a, b \in F_q$, $q = 2^{255} - 19$
- Modular division: modular multiplication + modular inversion

$$a/b \bmod q = a \otimes b^{-1} \bmod q$$

- Modular inversion (by Fermat's little theorem)

$$b^{-1} \bmod q = b^{q-2} \bmod q$$

Algorithm 1: Modular Inversion

Parameter: $q = 2^{255} - 19$

Input : $b \in F_q$

Output : $b^{-1} \bmod q \in F_q$

$r = 1$

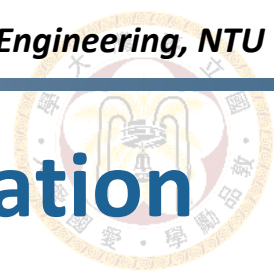
for $i = 255$ **to** 1 **do**

$r = r^2 \bmod q$

if i th bit of $q - 2$ is 1 **then**

$r = rb \bmod q$

return r



HW Implementation: Scalar Multiplication

- Using addition formula in projective coordinate

$$M \times (x_P, y_P) = M \times (x_P, y_P, 1) = \underbrace{(x_P, y_P, 1) + \cdots + (x_P, y_P, 1)}_M$$

Algorithm 2: Scalar Multiplication

Parameter: Curve E_{25519}

Input : 255-bit scalar M and point $P = (x_P, y_P) \in E_{25519}$

Output : point $G = (x_G, y_G) = M \times P$

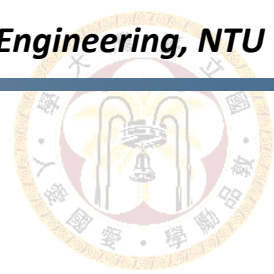
$r = (0, 1, 1)$ // zero point in projective coordinate

$P = (x_P, y_P, 1)$ // point P in projective coordinate

for $i = 255$ **to** 1 **do**

	$r = r + r$	// point addition
	if i th bit of M is 1 then	
	$r = r + P$	// point addition

return r



Coordinate Reduction

- Reduce extra coordinate Z in projective coordinates
 - Let $MP = (X_{MP}, Y_{MP}, Z_{MP})$ be the result of scalar multiplication (Algorithm 2)
 - Find the point in normal coordinate

$$(x_{MP}, y_{MP}) = (X_{MP}/Z_{MP}, Y_{MP}/Z_{MP})$$

- Make sure x_{MP} and y_{MP} are both even

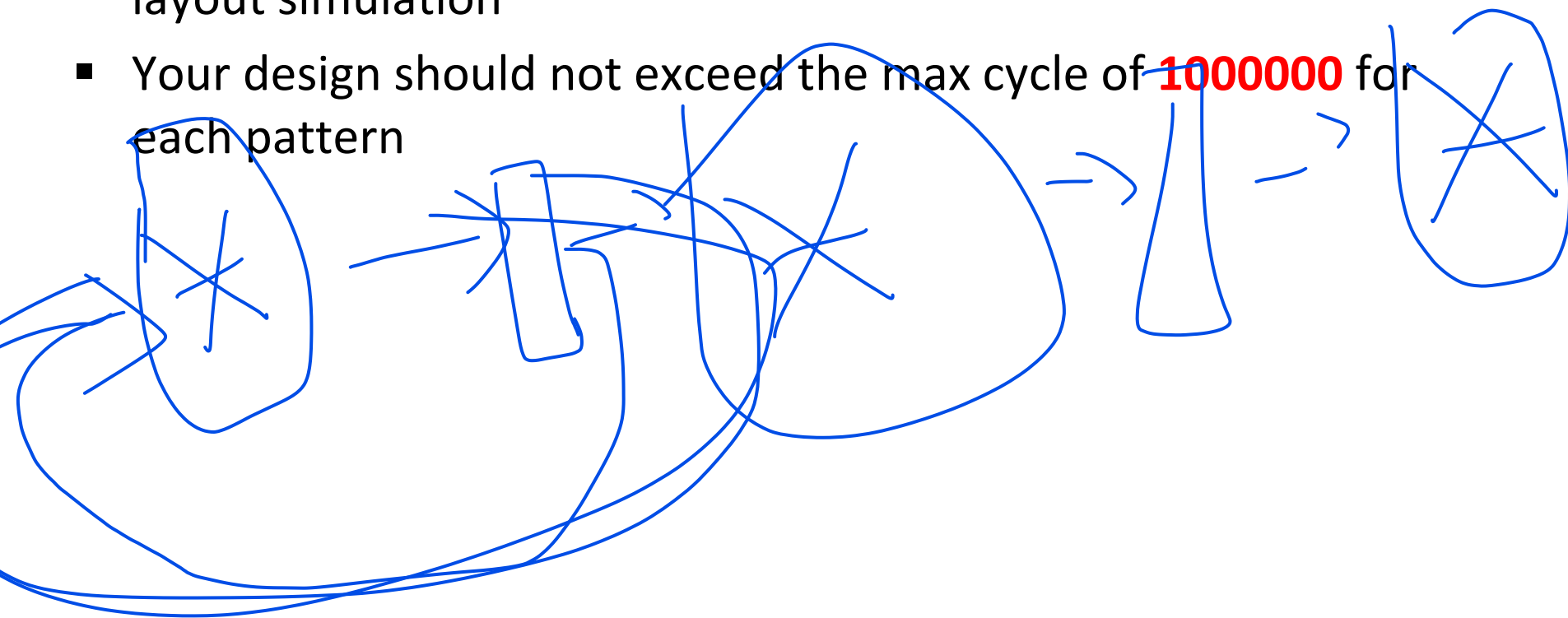
$$x_G = \begin{cases} x_{MP}, & x_{MP} \text{ is even} \\ -x_{MP} \bmod q, & x_{MP} \text{ is odd} \end{cases} \quad y_G = \begin{cases} y_{MP}, & y_{MP} \text{ is even} \\ -y_{MP} \bmod q, & y_{MP} \text{ is odd} \end{cases}$$

- Derive point $G = (x_G, y_G)$



Timing Specification

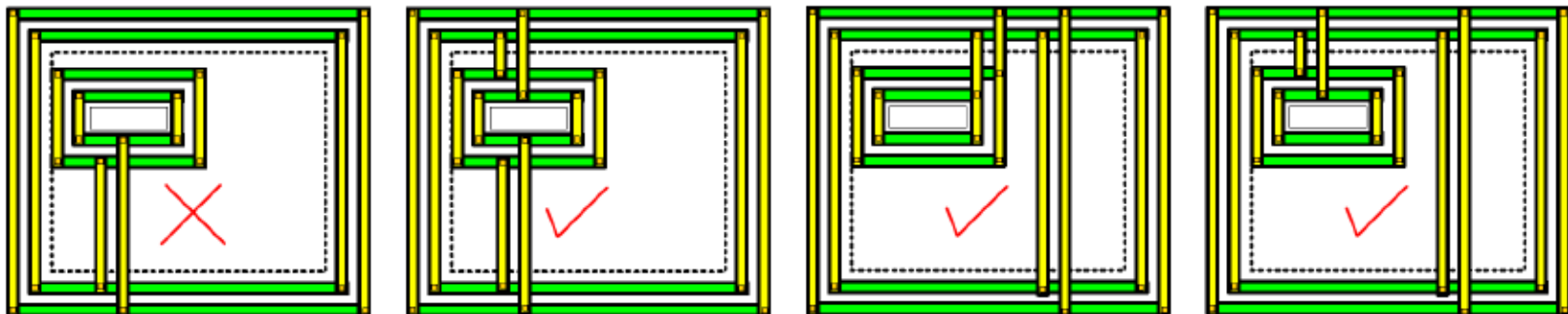
- Only the worst-case library is used for synthesis
- The slack for setup time should be non-negative
- **No timing violation** for the gate level simulation and post-layout simulation
- Your design should not exceed the max cycle of **1000000** for each pattern





APR Specifications (1)

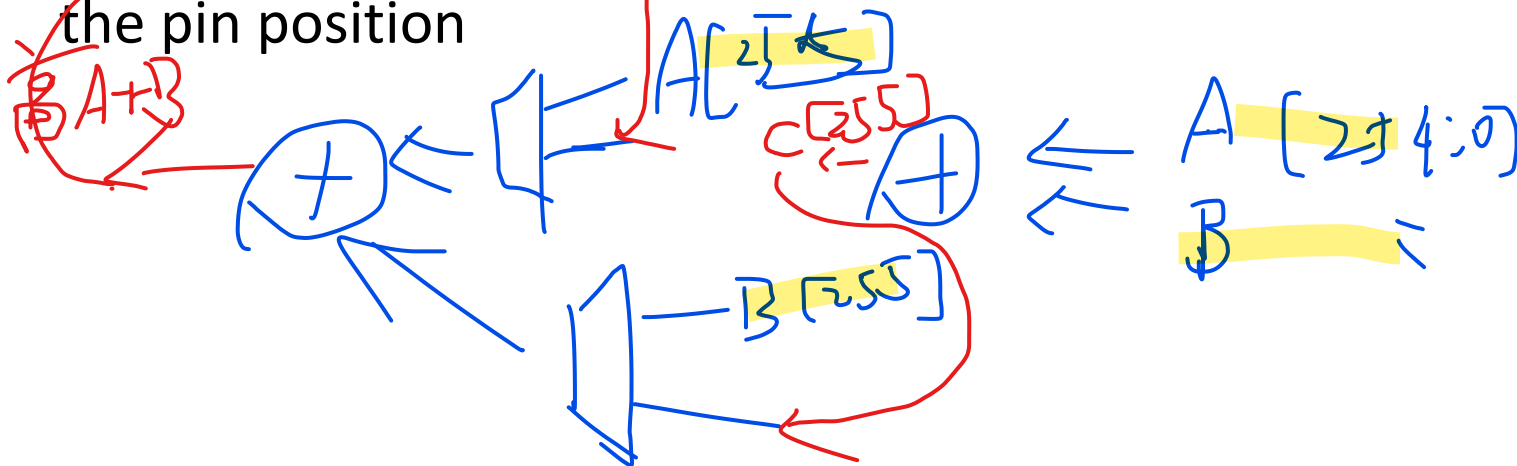
- Only the **macro layout** is needed
 - IO pads and bonding pads are not required
- **VDD** and **VSS** **power rings** should each be **2 μm wide**, with only one ring required for each
- **Power stripes**
 - At least one set, with **VDD** and **VSS** stripes each **2 μm wide**
 - Vertical power stripes require at least one set (horizontal power stripes are optional)





APR Specifications (2)

- Remember to add the **Power Rail** (follow pin)
- **Dummy metal layers** are not needed
- **Core Filler** must be added
- The **GDSII** file after APR must be generated
- Ensure that the APR DRC/LVS is completely **error-free**
- You can generate the ioc file first, and then reload the file to set the pin position





Simulation Settings

- Run the simulations using 01_run, 03_run, and 05_run
- You can only edit the bottom section of each *_sim.f file

```
// =====  
//           Your Can Only Modify The Below Part  
// =====  
  
// Your Design Files  
// -----  
./ed25519.sv  
  
// Define Flags  
// -----  
+define+RANDOM_IO_HANDSHAKE
```

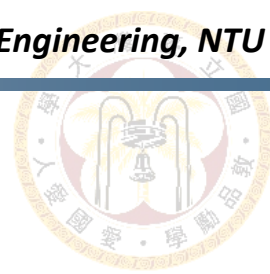
- There is a define flag RANDOM_IO_HANDSHAKE
 - Randomized valid/ready signal for testing in the testbench
 - Each pattern will be tested with this flag enabled
 - Performance (time) is evaluated without this flag



Submission (1)

- Create a folder named **teamID_final** with the structure below:

```
team01_final/  
├── 01_RTL  
│   ├── ed25519.v (and other Verilog files)  
│   └── rtl_sim.f (include all your Verilog files)  
├── 02_SYN  
│   ├── ed25519_syn.area  
│   ├── ed25519_syn.timing_min  
│   └── ed25519_syn.timing_max  
├── 03_GATE  
│   ├── ed25519_syn.v  
│   ├── ed25519_syn.sdf  
│   └── gate_sim.f  
├── 04_APR  
│   ├── final (saved APR design)  
│   ├── final.dat (design database)  
│   └── ed25519.gds  
├── 05_POST  
│   ├── ed25519_pr.v  
│   ├── ed25519_pr.sdf  
│   └── post_sim.f  
└── reports  
    ├── design.spec  
    └── team01_report.pdf
```

Submission (2)

- **Deadline:** 2024/12/17 **13:59:59** (UTC+8)
- Compress the folder **teamID_final** (**all lowercase**) in a tar file named **teamID_final_vk.tar** (k: version number, e.g., 1,2,...)
- Ensure all required files are submitted
 - **10-point deduction** for each missing file
- Submit to **NTU Cool**



Report Requirements

1. APR Results

- Show the screenshot of the layout and DRC/LVS results

2. Algorithm Design

- Clearly describe the algorithm analysis and the optimization techniques employed

3. Hardware Implementation

- Provide specifics about the hardware architecture, including the design of key modules and optimization techniques

4. Performance Evaluation

- Assess the efficiency of your design, including metrics such as speed and area.



Grading Policy

- **Baseline** 50% + **Performance** 40% + **Report** 10%

Item	%	Description
RTL Simulation	20	Pass all pattern simulations (3 public + 1 hidden)
Synthesis	10	Pass gate-level simulation
APR	20	Finish APR with no DRC/LVS errors Pass post-layout simulation
Performance	40	Area x Time
Report	10	See Page 19 for more details

- **Performance = 0 if**
 - DRC/LVS errors occur
 - Post-layout simulation fails



Grading Policy

- **No late submission is allowed**
 - Any submissions after the deadline will receive 0 points
- **5-point deduction** for incorrect naming or format
 - Pack all files into a single folder and compress the folder
 - Ensure that the files submitted can be decompressed and executed without issues
- **No plagiarism**
 - Plagiarism in any form, including copying from online sources, is strictly prohibited



Discussion

- **NTU Cool Discussion Forum**

- For any questions not related to assignment answers or privacy concerns, please use the NTU Cool discussion forum
- TAs will prioritize answering questions on the NTU Cool discussion forum

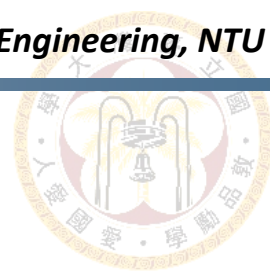
- **Email: d10943004@ntu.edu.tw**

- Title should start with [CVSD 2024 Fall Final Project]
- Email with wrong title will be moved to trash automatically



Final Project Presentation

- **Date:** December 24, 2024
- **Time:** 14:20 - 17:20
- Top-performing teams will be invited to present their design optimization strategies
- Bonus points will be awarded for presentations
- Additional information will be provided later



Hints for HW Optimizations

- Point doubling $P + P$ is faster than point addition $P + P'$ ($P \neq P'$) [3]
- Minimize the # of modular operations in point doubling/addition [3]
- Try different coordinate representation [3]
 - Projective, Extended, Inverted, ...
- Try different algorithms for faster scalar multiplication [4]
 - Double-and-Add (Algorithm 2), Windowed, Sliding-window, ...
- Reduce # of Montgomery multiplications with factor $R^2 \bmod q$
- Design a Montgomery multiplier with low hardware complexity



Reference

- [1] <https://zh.wikipedia.org/zh-tw/EdDSA>
- [2] https://en.wikipedia.org/wiki/Twisted_Edwards_curve
- [3] <https://www.hyperelliptic.org/EFD/g1p/auto-twisted.html>
- [4] https://en.wikipedia.org/wiki/Elliptic_curve_point_multiplication
- [5] AMBA AXI and ACE Protocol Specification, Arm.