

# Solving the phase boundary between two solid phases

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# Outline

$F(V)$ ,  $G(P)$  and pressure of intersection. Thermal evolution

Shapes of  $G$ ,  $F$ ,  $\mathcal{E}$

Shape of  $H(P; T)$

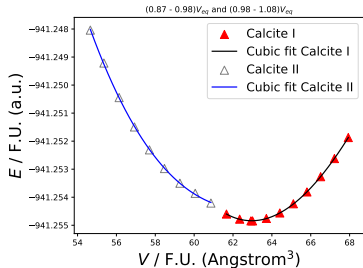
# Outline I

$F(V)$ ,  $G(P)$  and pressure of intersection. Thermal evolution

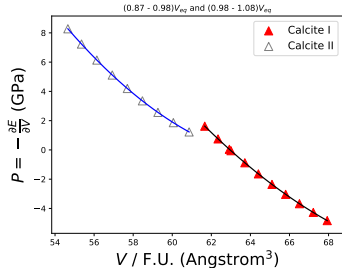
Shapes of  $G$ ,  $F$ ,  $\mathcal{E}$

Shape of  $H(P; T)$

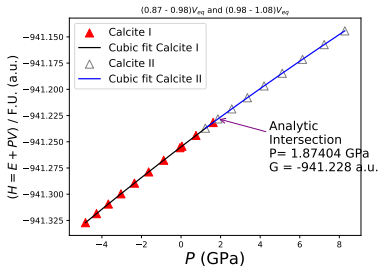
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



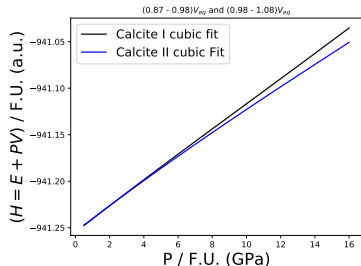
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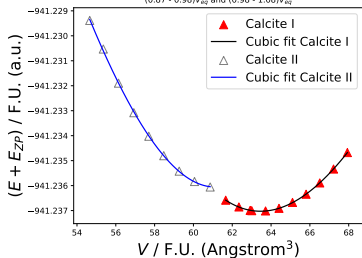
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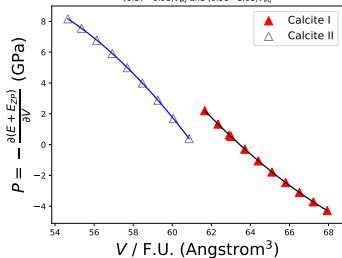
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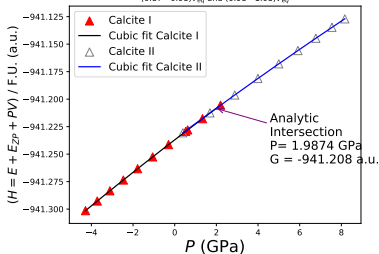
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8  
(0.87 - 0.98) $V_{eq}$  and (0.98 - 1.08) $V_{eq}$



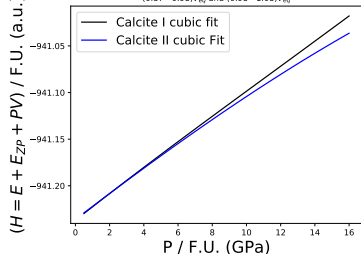
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8  
(0.87 - 0.98) $V_{eq}$  and (0.98 - 1.08) $V_{eq}$

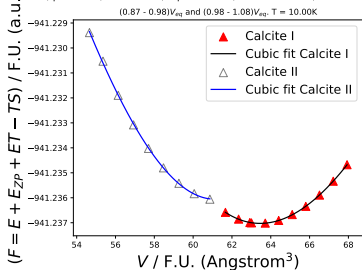


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8  
(0.87 - 0.98) $V_{eq}$  and (0.98 - 1.08) $V_{eq}$

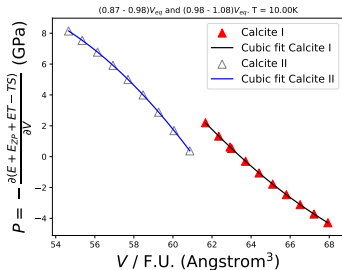


$$T = 10.00K$$

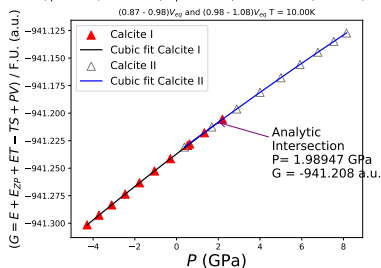
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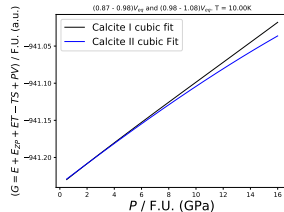
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

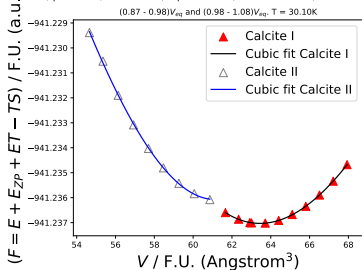


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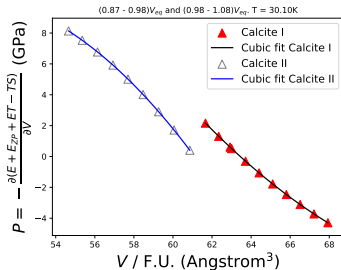


$$T = 30.10K$$

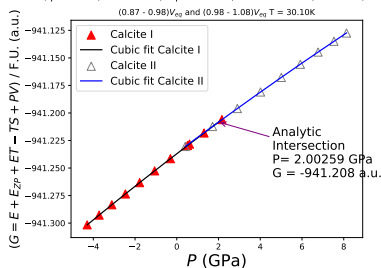
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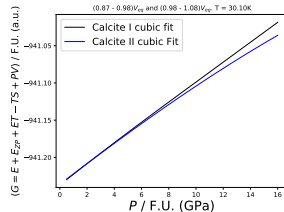
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

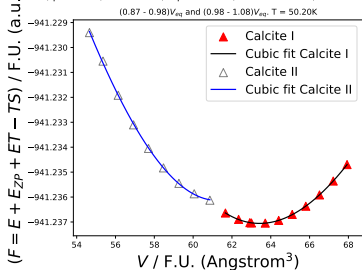


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

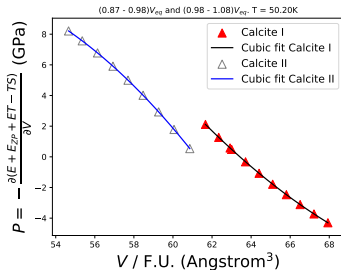


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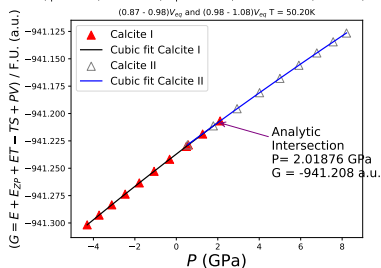
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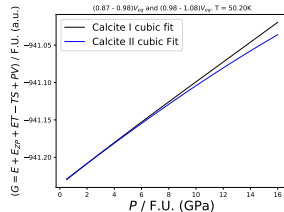
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



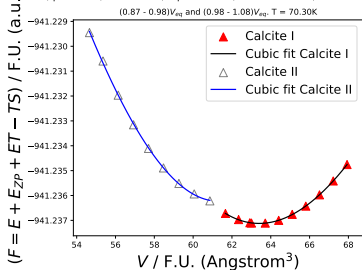
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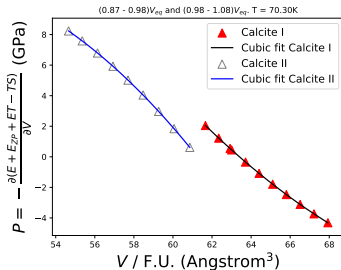


$$T = 70.30K$$

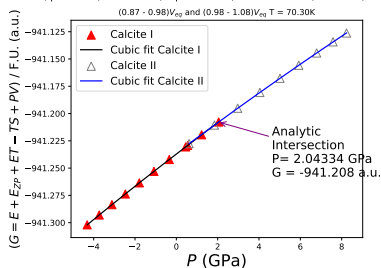
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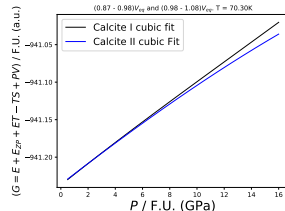
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

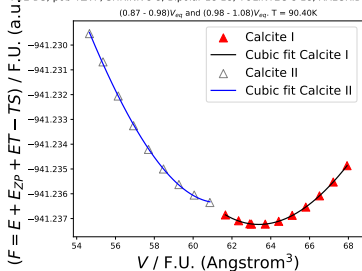


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

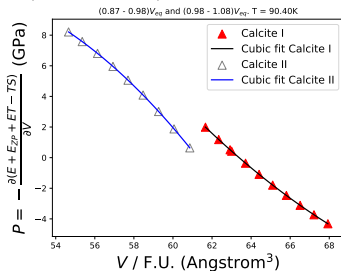


$$T = 90.40K$$

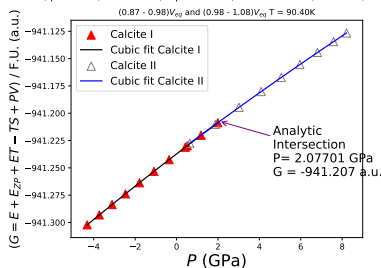
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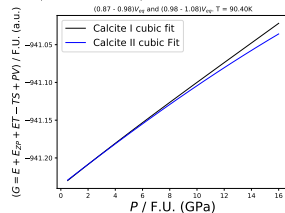
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

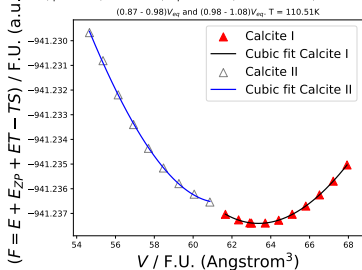


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

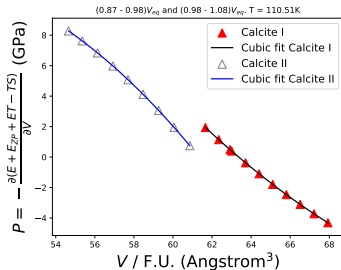


# $T = 110.51K$

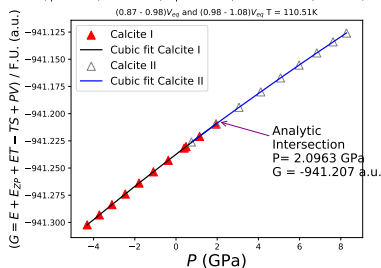
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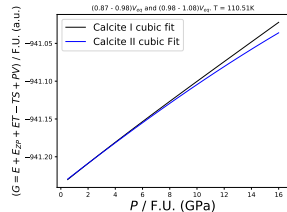
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

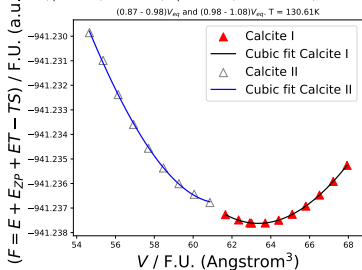


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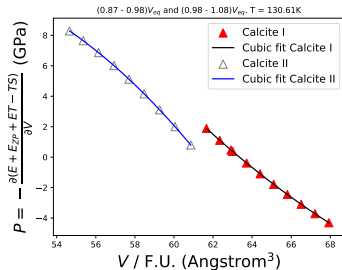


# $T = 130.61K$

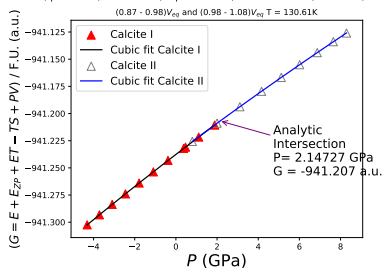
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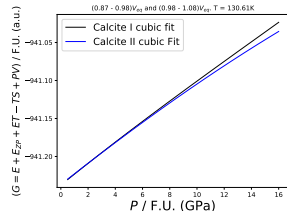
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

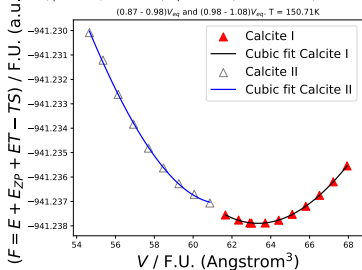


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

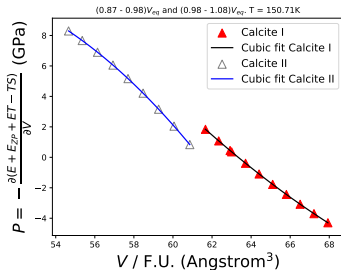


# $T = 150.71K$

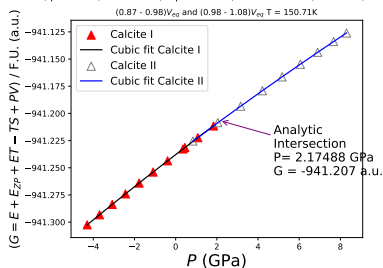
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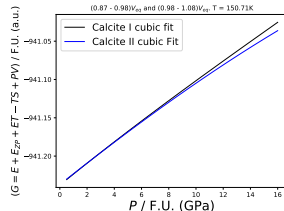
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

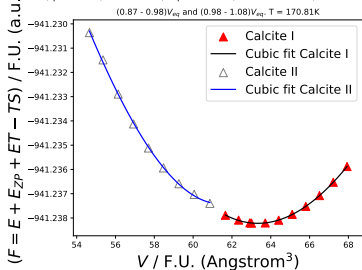


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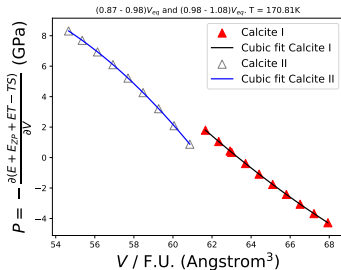


$$T = 170.81K$$

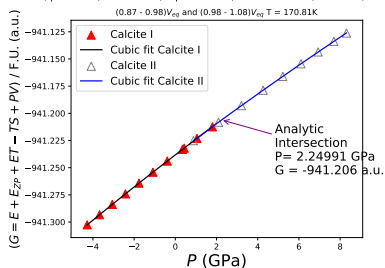
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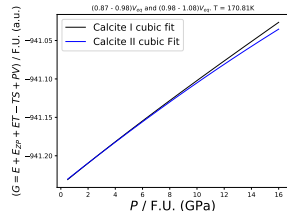
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

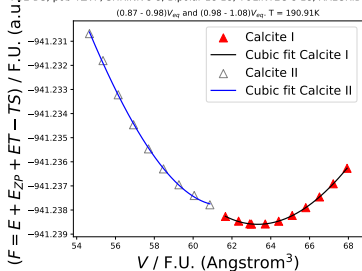


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

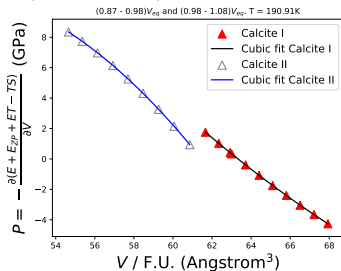


$$T = 190.91\text{K}$$

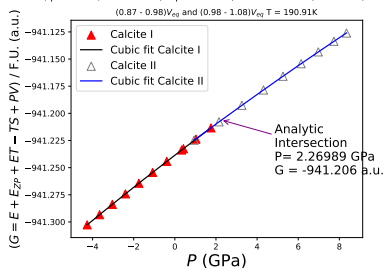
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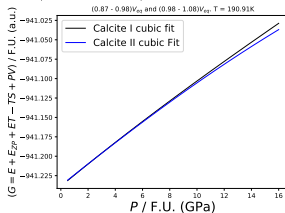
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

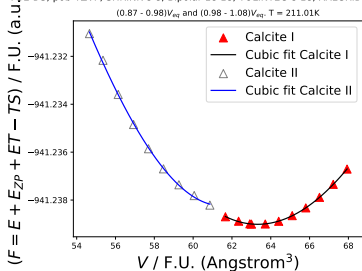


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

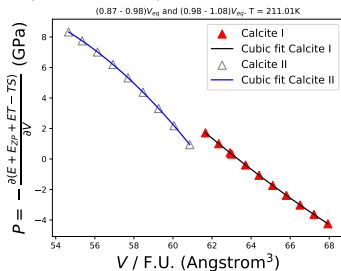


$$T = 211.01\text{K}$$

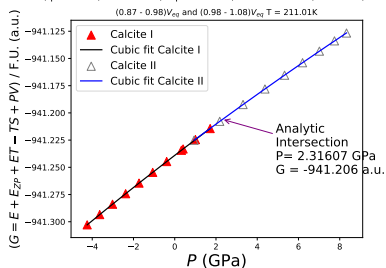
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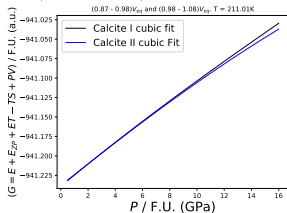
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



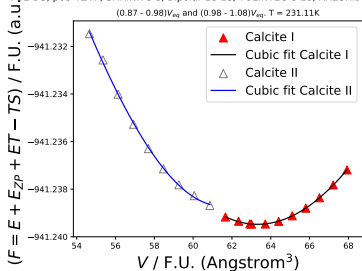
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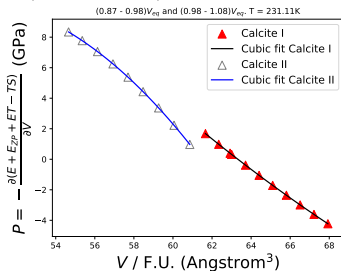


$$T = 231.11\text{K}$$

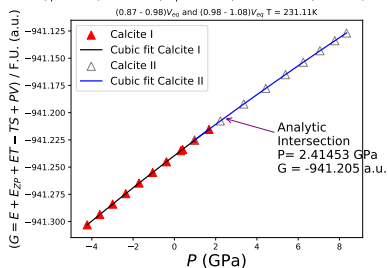
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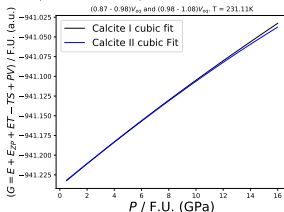
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

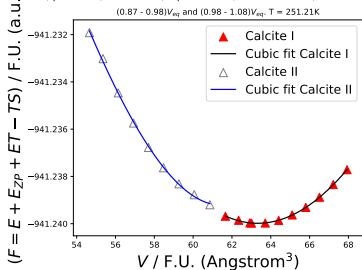


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

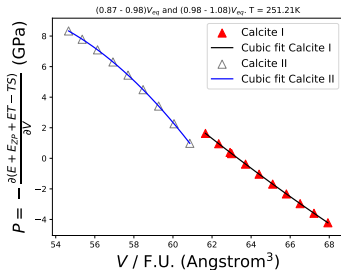


$$T = 251.21\text{K}$$

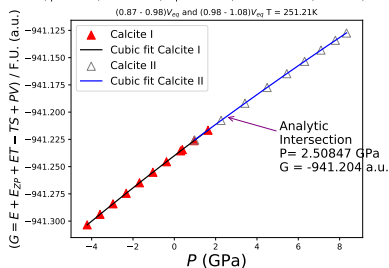
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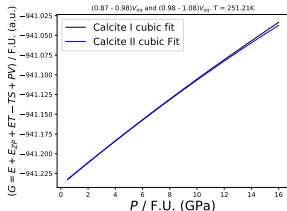
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

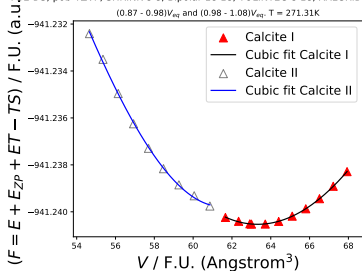


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

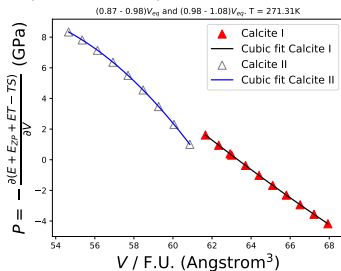


$$T = 271.31\text{K}$$

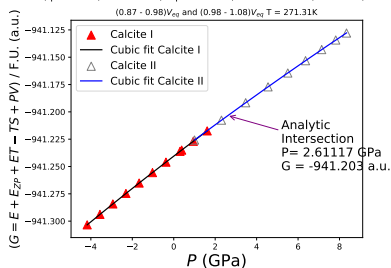
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



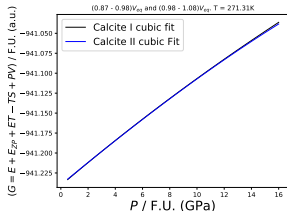
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PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

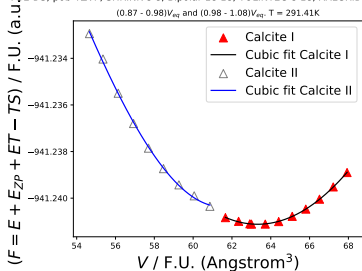


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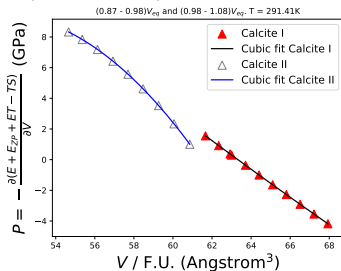


$$T = 291.41\text{K}$$

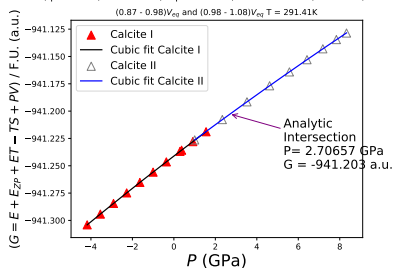
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



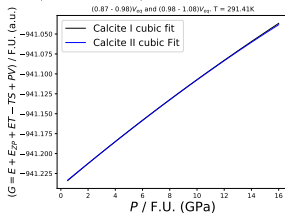
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

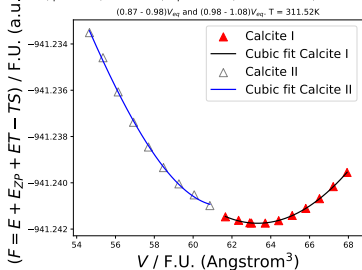


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

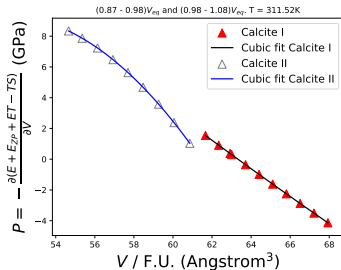


$$T = 311.52\text{K}$$

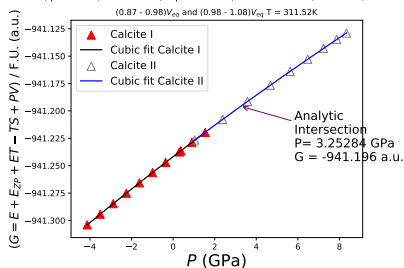
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



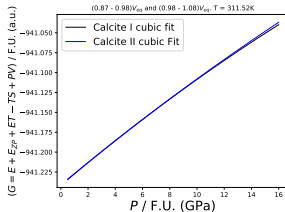
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

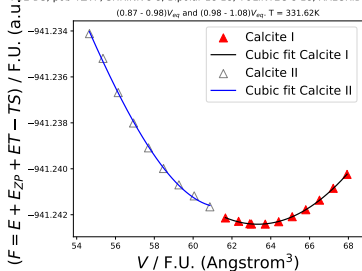


PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8

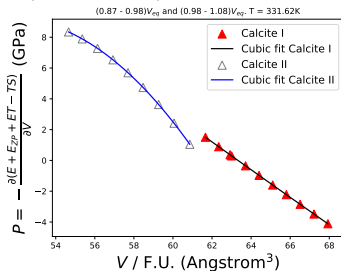


$$T = 331.62K$$

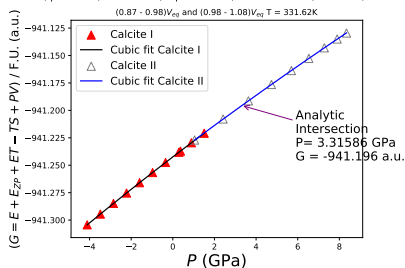
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



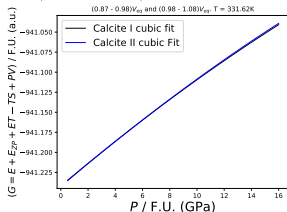
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



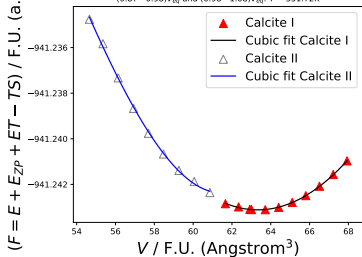
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



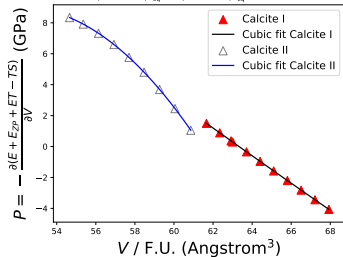
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



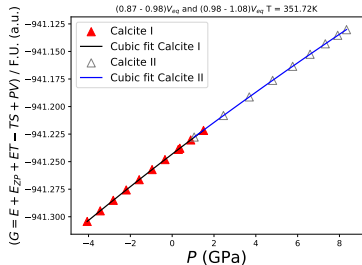
PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8  
(0.87 - 0.98) $V_{eq}$  and (0.98 - 1.08) $V_{eq}$ , T = 351.72K



PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8  
(0.87 - 0.98) $V_{eq}$  and (0.98 - 1.08) $V_{eq}$ , T = 351.72K



PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8  
(0.87 - 0.98) $V_{eq}$  and (0.98 - 1.08) $V_{eq}$ , T = 351.72K



# Outline I

$F(V)$ ,  $G(P)$  and pressure of intersection. Thermal evolution

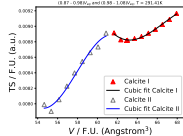
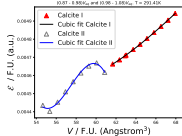
Shapes of  $G$ ,  $F$ ,  $\mathcal{E}$

Shape of  $H(P; T)$



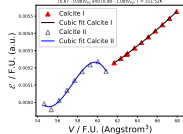
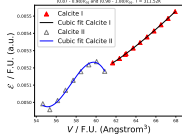
**T = 291.41K:**

PBE-O3, p66-TZVP, SHRINK 8 8, Bipolar 18 18, TOLNTEG 8 18, XXLGRID, TOLDEE 8  
 (0.87 : 0.88) $\epsilon_{\infty}$  and (0.96 : 1.00) $\epsilon_{\infty}$  T = 291.41K



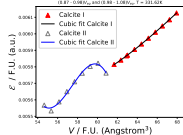
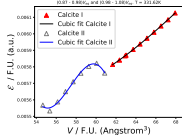
**T = 311.52K:**

PBE-O3, p66-TZVP, SHRINK 8 8, Bipolar 18 18, TOLNTEG 8 18, XXLGRID, TOLDEE 8  
 (0.87 : 0.88) $\epsilon_{\infty}$  and (0.96 : 1.00) $\epsilon_{\infty}$  T = 311.52K



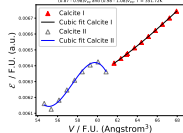
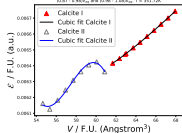
**T = 331.62K:**

PBE-O3, p66-TZVP, SHRINK 8 8, Bipolar 18 18, TOLNTEG 8 18, XXLGRID, TOLDEE 8  
 (0.87 : 0.88) $\epsilon_{\infty}$  and (0.96 : 1.00) $\epsilon_{\infty}$  T = 331.62K



**T = 351.72K:**

PBE-O3, p66-TZVP, SHRINK 8 8, Bipolar 18 18, TOLNTEG 8 18, XXLGRID, TOLDEE 8  
 (0.87 : 0.88) $\epsilon_{\infty}$  and (0.96 : 1.00) $\epsilon_{\infty}$  T = 351.72K



# Outline I

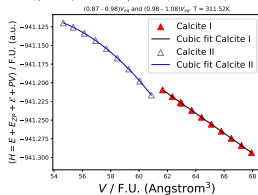
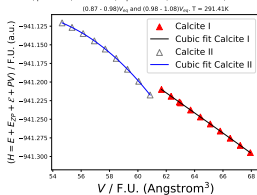
$F(V)$ ,  $G(P)$  and pressure of intersection. Thermal evolution

Shapes of  $G$ ,  $F$ ,  $\mathcal{E}$

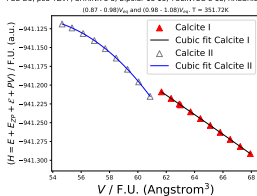
Shape of  $H(P; T)$

When  $H(P; T) = E + E_{ZP} + \mathcal{E}(T) + PV$ :

PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



PBE-D3, pob-TZVP, SHRINK 8 8, Bipolar 18 18, TOLINTEG 8 18, XXLGRID, TOLDEE 8



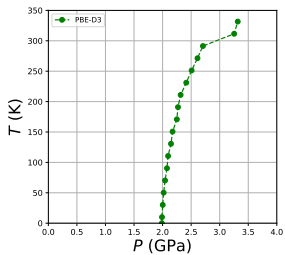


Figure 1: Pressure-temperature phase boundary