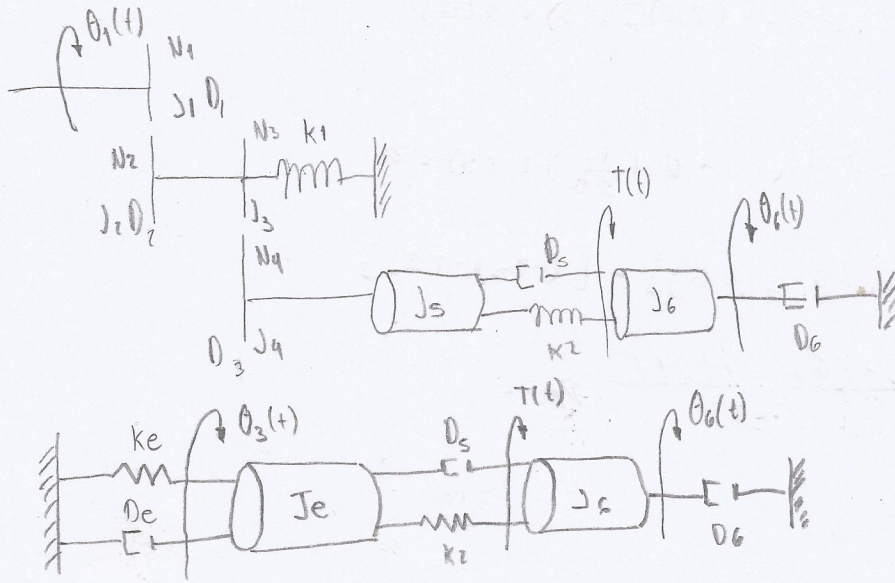


Para el sistema rotacional de la fig encuentre las ecuaciones dinámicas $N_1 = N_3 = 8$, $N_2 = 16$, $N_4 = 24$,
 D = último dígito de número de cuenta, si es cero usar 1, k_2 = penúltimo número de cuenta, si es cero usar
 2 , todos los $J = 1$ $k_1 = k_2$



$$J_e = [J_4 + J_5 + (J_2 + J_3) \left(\frac{N_4}{N_3}\right)^2 + J_1 \left(\frac{N_4}{N_3}\right)^2 \left(\frac{N_2}{N_1}\right)^2] \quad K_e = k_1 \left(\frac{N_4}{N_3}\right)^2$$

$$D_e = D_1 \left(\frac{N_2}{N_1}\right)^2 \left(\frac{N_4}{N_3}\right)^2 + D_2 \left(\frac{N_4}{N_3}\right)^2 + D_3$$

$$(J_e s^2 + D_e s + K_e + D_5 s + k_2) \theta_3(s) - (D_5 s + k_2) \theta_6(s) = 0 \dots ①$$

$$-(D_5 s + k_2) \theta_3(s) + (D_5 + D_6) s + k_2 + J_6 s^2 \theta_6(s) = T(s) \dots ②$$

Sustituyendo:

$$J_e = (1 + 1 + (2) \left(\frac{24}{8}\right)^2 + (1) \left(\frac{24}{8}\right)^2 \left(\frac{16}{8}\right)^2) = 56$$

$$D_e = 6 \left(\frac{16}{8}\right)^2 \left(\frac{24}{8}\right)^2 + 6 \left(\frac{24}{8}\right)^2 + 6 = 276$$

$$K_e = 9 \left(\frac{24}{8}\right)^2 = 81$$

Sust en ①

$$(56 s^2 + 276 s + 81 + 6 s + 9) \theta_3(s) - (6 s + 9) \theta_6(s) = 0$$

$$(56 s^2 + 282 s + 90) \theta_3(s) - (6 s + 9) \theta_6(s) = 0$$

Sust en ②:

$$(-6 s - 9) \theta_3(s) + (12 s + 9 + s^2) \theta_6(s) = T(s)$$

Datos:

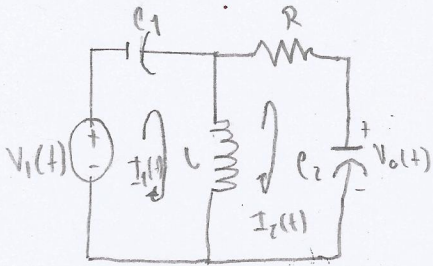
$$N_1 = N_3 = 8 \quad N_4 = 24$$

$$N_2 = 16 \quad D = 6$$

$$k_1 = k_2 = 9 \quad J = 1$$

2) Escriba la función de transferencia para el voltaje de entrada V_i y el voltaje de la resistencia R $G(s) = V_r(s)/V_i(s)$, $C_1=1$, $L=2$, $C_2=2$, $R=$ último dígito de número de cuenta si es cero $R=3$

$$V = R I_2$$



Malla 1:

$$\left(\frac{1}{s} + 2s\right) I_1(s) - (2s) I_2(s) = V_i(s)$$

Malla 2:

$$-(2s) I_1(s) + \left(2s + 6 + \frac{1}{2s}\right) I_2(s) = 0$$

$$\begin{vmatrix} \left(\frac{1}{s} + 2s\right) & -2s \\ (-2s) & \left(2s + \frac{1}{2s} + 6\right) \end{vmatrix} \begin{bmatrix} I_1(s) \\ I_2(s) \end{bmatrix} = \begin{bmatrix} V_i(s) \\ 0 \end{bmatrix}$$

$$\left[\left(\frac{1}{s} + 2s\right) \left(2s + \frac{1}{2s} + 6\right) \right] - [(-2s)(-2s)]$$

$$= \frac{24s^3 + 6s^2 + 12s + 1}{2s^2} \Delta_T$$

$$= \frac{24s^3 + 6s^2 + 12s + 1}{2s^2} \Delta_T$$

$$\begin{vmatrix} \frac{1}{s} + 2s & -2s \\ -2s & \left(2s + \frac{1}{2s} + 6\right) \end{vmatrix} \begin{bmatrix} I_1(s) \\ I_2(s) \end{bmatrix} = \begin{bmatrix} V_i(s) \\ 0 \end{bmatrix}$$

$$= +2s V_i(s)$$

$$\Rightarrow I_2 = \frac{+2s V_i(s)}{\frac{24s^3 + 6s^2 + 12s + 1}{2s^2}}$$

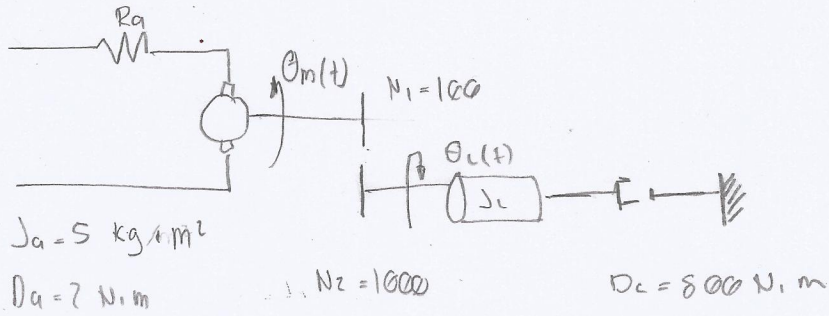
$$I_2 = \frac{+ V_i(s)}{s(24s^3 + 6s^2 + 12s + 1)}$$

$$G(s) = \frac{R I_2}{V_i(s)} = \frac{+6 V_i(s)}{s(24s^3 + 6s^2 + 12s + 1) V_i(s)}$$

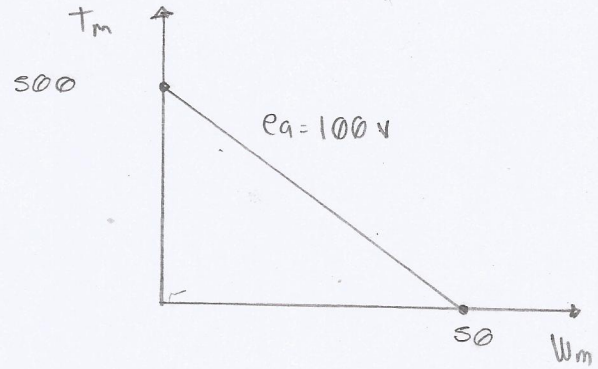
$$G(s) = \frac{+6/s}{s(24s^3 + 6s^2 + 12s + 1)}$$

Para el siguiente sist, encontrar una función de transferencia donde la salida sea

$$\omega_L(s)/V_e(s)$$



$$J_L = 700$$



$$J_m = J_a + J_L \left(\frac{N_1}{N_2} \right)^2 = 5 + 700 \left(\frac{100}{1000} \right)^2 = 12$$

$$D_m = D_a + D_L \left(\frac{N_1}{N_2} \right)^2 = 2 + 800 \left(\frac{100}{1000} \right)^2 = 10$$

$$T_{\text{PARMAX}} = 500 \text{ N} \cdot \text{m}$$

$$V_e = 100 \text{ V}$$

$$\omega_{\text{SN CARGA}} = 50 \text{ rad/s}$$

Sabemos:

$$\frac{K_T}{R_M} = \frac{T_{\text{PARMAX}}}{V_e} \Rightarrow \frac{K_T}{R_M} = \frac{500}{100} = 5$$

$$\frac{N_1}{N_2} = 0.1$$

Sabemos:

$$K_b = \frac{V_o}{\omega_{\text{SN CARGA}}} = K_b = \frac{100}{50} = 2$$

Sabemos:

$$\frac{\theta_m(s)}{V_e(s)} = \frac{\frac{K_T}{R_M J_m}}{s \left[s + \frac{1}{J_m} \left(D_m + \frac{K_T R_e}{R_M} \right) \right]} = \frac{(5)/(5)/(12)}{s \left[s + \frac{1}{(12)} (10 + (5)(2)) \right]} = \frac{s/12}{s \left[s + s/3 \right]}$$

$$\frac{\theta_m(s)}{V_e(s)} = \frac{s/12}{s^2 + s/3}$$

⇒ Sabemos:

$$\frac{\theta_L(s)}{\theta_m(s)} = \frac{N_1}{N_2}$$

$$\theta_m(s) = \frac{N_2}{N_1} \theta_L(s)$$

$$\frac{\theta_L(s)}{V_e(s)} = \frac{1/10 (s/12)}{s^2 + s/3} = \frac{1/24}{s^2 + s/3} = \frac{1}{24s^2 + 40s}$$