

WebAssign  
1.5 Inversas (Homework)

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Diferencial, section B, Spring 2019  
Instructor: Christiaan Ketelaar

Current Score : 15 / 15 Due : Sunday, February 10, 2019 11:59 PM CST Last Saved : n/a Saving... ()

The due date for this assignment is past. Your work can be viewed below, but no changes can be made.

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1. 1/1 points | [Previous Answers](#)SCalc8 6.1.003.

A function is given by a table of values. Determine whether it is one-to-one.

$x$	1	2	3	4	5	6
$f(x)$	12	12.6	13.7	15.6	13.2	12.6

- ☐ Yes, it is one-to-one.  
☒ No, it is not one-to-one.

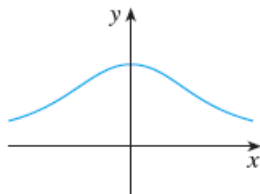


Solution or Explanation

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2. 1/1 points | [Previous Answers](#)SCalc8 6.1.005.

A function is given by a graph. Determine whether it is one-to-one.



- ☐ Yes  
☒ No

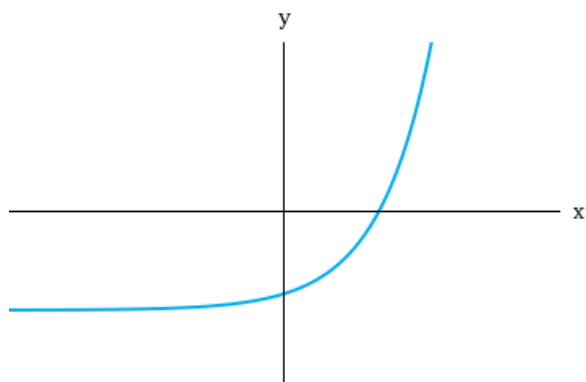


Solution or Explanation

We could draw a horizontal line that intersects the graph in more than one point. Thus, by the [Horizontal Line Test](#), the function is not one-to-one.

3. 1/1 points | [Previous Answers](#)SCalc8 6.1.006.

A function is given by a graph. Determine whether it is one-to-one.



- ☒ Yes, it is one-to-one.
- ☐ No, it is not one-to-one.



Solution or Explanation

[Click to View Solution](#)

4. 1/1 points | [Previous Answers](#)SCalc8 6.1.010.

A function is given by a formula. Determine whether it is one-to-one.

$$f(x) = x^6 - 12$$

- ☐ Yes, it is one-to-one.
- ☒ No, it is not one-to-one.



Solution or Explanation

The graph of  $f(x) = x^6 - 12$  is symmetric with respect to the  $y$ -axis. Pick any  $x$ -values equidistant from 0 to find two equal function values. For example,  $f(-1) = -11$  and  $f(1) = -11$ , so  $f$  is not one-to-one.

5. 1/1 points | [Previous Answers](#)SCalc8 6.1.016.

A function is given by a verbal description. Determine whether it is one-to-one.

The function  $f(t)$  is your height at age  $t$

- ☐ Yes, it is one-to-one.
- ☒ No, it is not one-to-one.

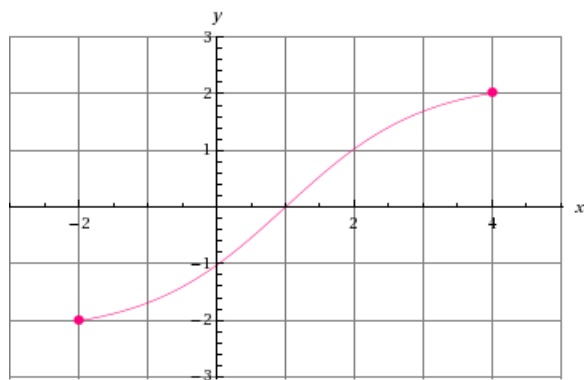


Solution or Explanation

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6. 2/2 points | [Previous Answers](#)SCalc8 6.1.020.

The graph of  $f$  is given.



(a) Why is  $f$  one-to-one?

$f$  is one-to-one because it passes the  .

(b) What are the domain and range of  $f^{-1}$ ? (Enter your answers in interval notation.)

domain

range

(c) What is the value of  $f^{-1}(0)$ ?

(d) Estimate the value of  $f^{-1}(-1)$  to the nearest tenth.

Solution or Explanation

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7. 1/1 points | [Previous Answers](#)SCalc8 6.1.024.MI.

Find a formula for the inverse of the function.

$$f(x) = \frac{2x - 1}{2x + 9}$$

$f^{-1}(x) =$

Solution or Explanation

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8. 1/1 points | [Previous Answers](#)SCalc8 6.1.025.

Find a formula for the inverse of the function.

$$f(x) = 2 + \sqrt{3 + 5x}$$

$$f^{-1}(x) =$$

✓  $\frac{1}{5}(x-2)^2 - \frac{3}{5}$

Solution or Explanation

$$y = f(x) = 2 + \sqrt{3 + 5x} \quad (y \geq 2) \Rightarrow y - 2 = \sqrt{3 + 5x} \Rightarrow (y - 2)^2 = 3 + 5x \Rightarrow (y - 2)^2 - 3 = 5x \Rightarrow x = \frac{1}{5}(y - 2)^2 - \frac{3}{5}.$$

Interchange  $x$  and  $y$ :  $y = \frac{1}{5}(x - 2)^2 - \frac{3}{5}$ . So  $f^{-1}(x) = \frac{1}{5}(x - 2)^2 - \frac{3}{5}$ . Note that the domain of  $f^{-1}$  is  $x \geq 2$ .

9. 2/2 points | [Previous Answers](#)SCalc8 6.1.504.XP.

Consider the following function.

$$f(x) = x^4 + 5, \quad x \geq 0$$

Find an explicit formula for  $f^{-1}$ .

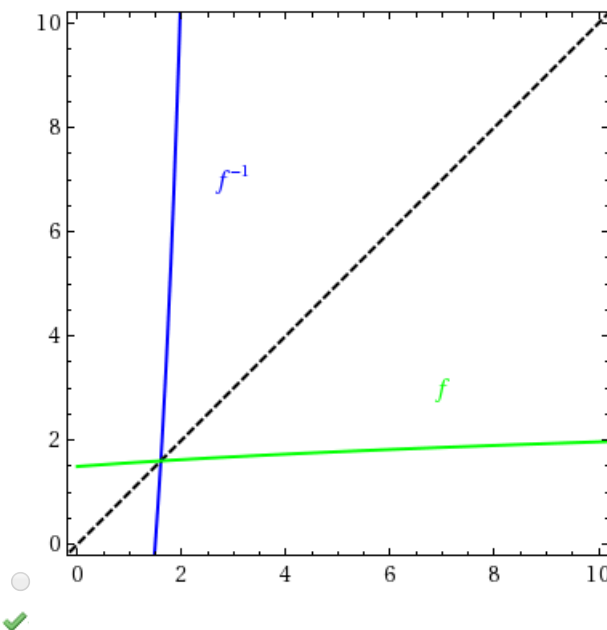
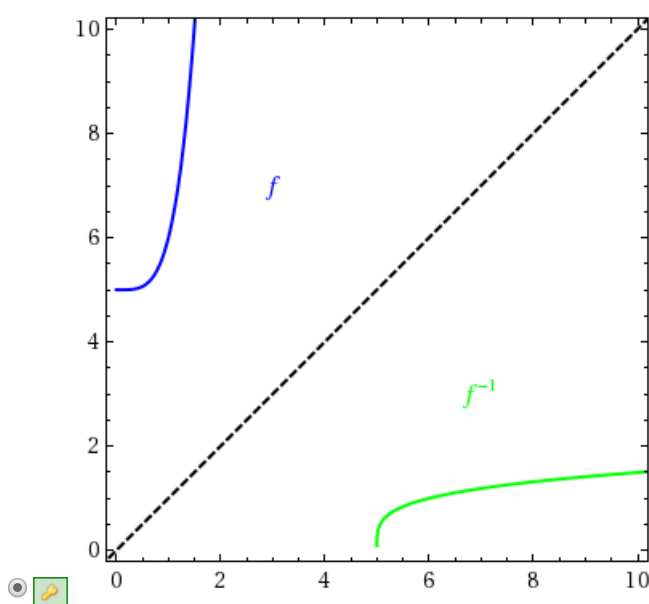
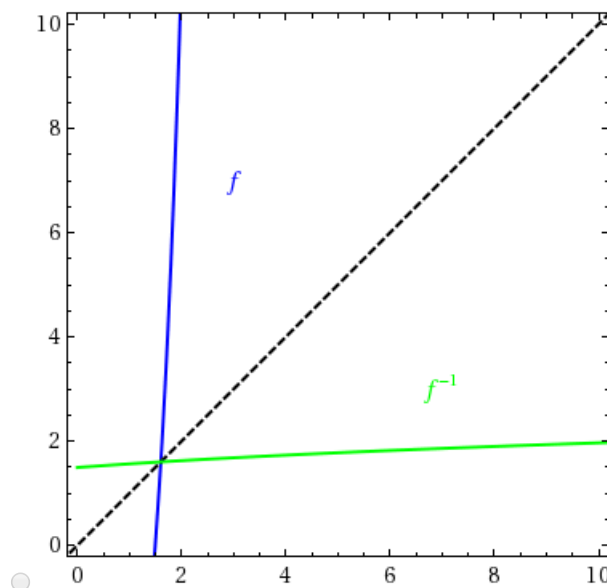
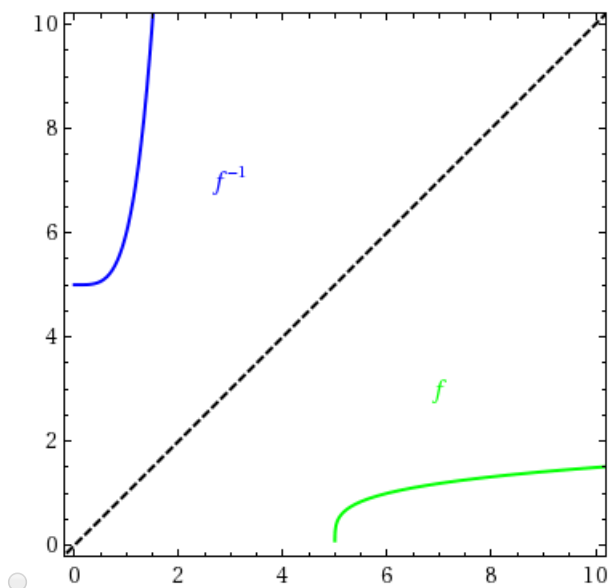
$$f^{-1}(x) =$$

$$\sqrt[4]{x-5}$$



$$\sqrt[4]{x-5}$$

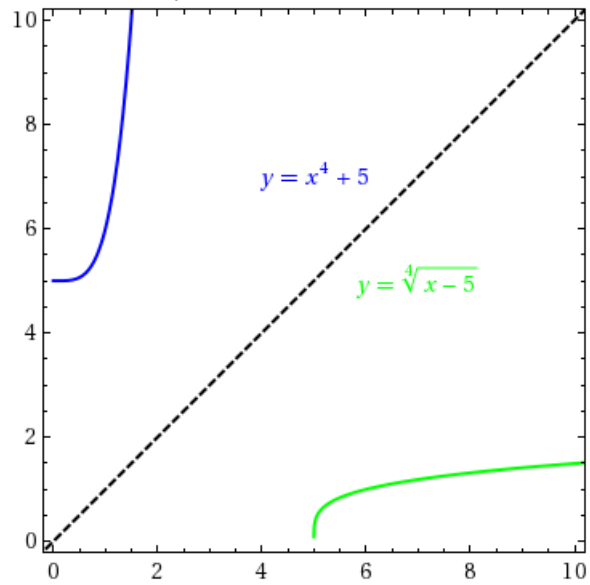
Graph  $f^{-1}$ ,  $f$ , and the line  $y = x$  on the same screen. To check your work, see whether the graphs of  $f$  and  $f^{-1}$  are reflections about the line.



Solution or Explanation

$y = f(x) = x^4 + 5 \Rightarrow y - 5 = x^4 \Rightarrow x = \sqrt[4]{y-5}$  [not  $\pm$  since  $x \geq 0$ ]. Interchange  $x$  and  $y$ :  $y = \sqrt[4]{x-5}$ . So  $f^{-1}(x) = \sqrt[4]{x-5}$ . The graph of  $y = \sqrt[4]{x-5}$  is just the graph of  $y = \sqrt[4]{x}$  shifted right five units. From the graph, we see that  $f$  and  $f^{-1}$  are reflections

about the line  $y = x$ .



10.2/2 points | [Previous Answers](#)SCalc8 6.1.JIT.004.MI.Use the Inverse Function Property to see if  $f$  and  $g$  are inverses of each other.

$$f(x) = \frac{9-x}{10}, \quad g(x) = -10x + 9$$

$$f(g(x)) = \frac{-10x+9}{10}$$

$$= \frac{9 - (-10x+9)}{10}$$

$$= \frac{9 - (-10x+9)}{10}$$

$$= \frac{10x}{10}$$

$$= x \text{ for all } x.$$


$$g(f(x)) = \frac{9-x}{10}$$

$$= -10 \cdot \frac{9-x}{10} + 9$$

$$= -90 + 10x + 90$$

$$= x - 9 + 9$$

$$= x \text{ for all } x.$$

Thus,  $f$  and  $g$  are  are inverses of each other.

11.2/2 points | [Previous Answers](#)SCalc8 6.1.AE.004.[Video Example](#) **EXAMPLE 4** Find the inverse function of

$$f(x) = x^3 + 3, \quad 0 \leq x < \infty$$

**SOLUTION** According to [this outline](#) We first write

$$y = x^3 + 3.$$

Then we solve this equation for  $x$ .

$$x^3 = \boxed{y - 3}$$

$$x = \sqrt[3]{\boxed{y - 3}}$$

Finally, we interchange  $x$  and  $y$ .

$$y = \sqrt[3]{x - 3}$$

Therefore the inverse function is

$$f^{-1}(x) = \sqrt[3]{x - 3}.$$