Perivadas de donciones para nétricas

laugen tos hovizantales.

$$y^{\mathfrak{I}}(t) = \emptyset \qquad k$$

x 2 (t) 7 6

tungentes verticales.

$$y^{3}(t) \neq 0$$

6) Legender derivadas de y(x):

$$\frac{dy}{dx} = \frac{y^{3}(t)}{x^{3}(t)}; \quad \frac{dy}{d^{2}x} = \frac{d}{dx}(y^{3}(x))$$

$$\frac{d^2y}{d^2x} = \frac{d}{dt}(y^3(x))$$

$$x^3(t)$$

Ejercicio: encontrav 1era & segunda divivada:

a)
$$x = 1.5 t^2$$
 ; $y = t^3 + 1.5 t^6$

$$\frac{dy}{dx} = \frac{y^{3}(t)}{x^{3}(t)} = \frac{3t^{2} + 9t^{5}}{3t} = \underbrace{t + 3t^{4}}_{\frac{dy}{dx}}$$

$$\frac{d^{2}y}{d^{2}x} = \frac{\frac{d}{dt}(y^{3}(x))}{x^{3}(t)} = \underbrace{1 + 12t^{3}}_{3t} = \underbrace{\frac{1}{3t} + 4t^{2}}_{\frac{d^{2}y}{d^{2}x}}$$

$$y''' = \frac{\frac{d}{dt} \left(y''(x) \right)}{x''(x)} = \frac{1}{3t} \left(\frac{-4}{3t^2} + 8t \right)$$

$$\frac{\frac{d^3y}{d^3x}}{t^3}$$

b)
$$y = e^t$$
 j $y = te^{-t} \Rightarrow 1 \cdot e^{-t} - te^{-t}$

$$\frac{dy}{dx} = \frac{y_1(t)}{x_2(t)} = \frac{1 \cdot e^{-t} - e^{-t}}{e^{t}} = \frac{e^{-2t}}{e^{-2t}}$$

$$\frac{d^{2}y}{d^{2}x} = \frac{\frac{d}{dt}(\frac{dy}{dx})}{x^{2}(t)} = \frac{1}{e^{t}}(-2e^{-2t} - e^{-2t} + 2te^{-2t})$$

$$= -3e^{-3t} - 2e^{-3t}t$$

c)
$$X = \cos \theta$$
; $y = \cos 2\theta$
 $\sin (2\theta) = 2\sin \theta \cos \theta$

$$\frac{dy}{dx} = \frac{y^{2}(\theta)}{x^{2}(\theta)} = \frac{-2 \sin(2\theta)}{-\sin \theta} = \frac{2 \cdot 2 \cdot \sin \theta \cdot \cos \theta}{-\sin \theta} = \frac{2 \cdot 2 \cos \theta}{dx}$$

$$\frac{d\dot{y}}{d^2x} = \frac{d}{d\theta} \left(\frac{4\cos\theta}{\cos\theta} \right) = \frac{-4\sin\theta}{-\sin\theta} = -4$$

Pado a que la deux es una constante asumine, que es una constante

$$y = cas(2\theta) = sin^2\theta - cos^2\theta$$

= 1-cos^2-cos^2\theta = -1 + 2(cqs\theta)^2

60. Lurva paramétrica:

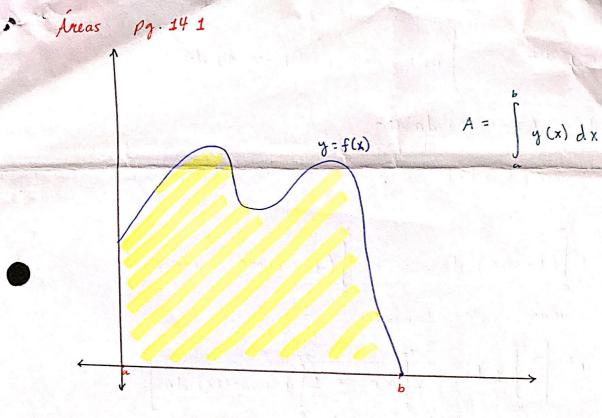
$$y = -1 + 2x^{2}$$

$$\frac{dy}{dx} = 4x$$

$$\frac{d^{2}y}{dx} = 4$$

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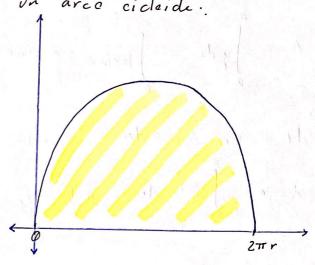


$$dx = f'(t)dt$$
 $y = g(t)$ integra en t $t_1 \leq t \leq t_2$

Par lo tanfo
$$A = \int_{a}^{b} y \, dx = \int_{b}^{c} g(t) \, g^{2}(t) \, dt$$

Ejercicio 6: encuentra el área de la región dada.

a. La región de baje de un arco cicleide.
$$x = r(\theta - \sin \theta)$$



$$A = \int_{\alpha}^{b} y \, dx = \int_{0}^{2\pi} f(1 - \omega s \theta) r \quad (1 - cer \theta) \, d\theta$$

$$dx = r(1 - cos \theta) \, d\theta$$

$$A = r^2 \int_0^2 (1 - \cos \theta)^2 d\theta = r^2 \int_0^2 (1 - 2\cos \theta + \cos^2 \theta) d\theta$$

$$vear \cos^2 \theta = \frac{1}{2} + \frac{\cos(2\theta)}{2}$$

$$= r^2 \int_0^{2\pi} \int_0^{2\pi} d\theta = r^2 \int$$

$$= r^{2} \left[\int_{0}^{2\pi} 1 \, d\theta - 2 \int_{0}^{2\pi} \cos \theta + \frac{1}{2} \int_{0}^{2\pi} 1 + \cos(2\theta) \, d\theta \right]$$

$$= r^2 \left[\frac{3}{2}\theta - 2\sin\theta + \frac{1}{4}\sin(2\theta) \right]^{2\pi} =$$

$$= r^2 \left[\frac{3}{2} 2\pi - 2 \sin^2 \pi + \frac{1}{4} \sin(4\pi) \right] = r^2 \frac{6\pi}{2}$$

b) Medin elipse
$$X = -a \cos \theta$$

$$y = b \cdot \sin \theta$$

$$X = -a\cos\theta$$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

$$y = b \cdot \sin\theta$$

$$A = \int_{0}^{\pi} y dx = \int_{0}^{\pi} b \sin \theta \cdot a \sin \theta d\theta$$

$$A = ab \int_{0}^{\pi} \sin^{2}\theta \, d\theta = \frac{a \cdot b}{2} \int_{0}^{\pi} (1 - \cos 2\theta) \, d\theta$$

$$A = \frac{a \cdot b}{2} \left[\Theta - \frac{1}{2} \sin(2\theta) \right] = \frac{a \cdot b}{2} \left[\left(\pi - \frac{1}{2} \sin(2\pi) \right) - \left(0 - \frac{1}{2} \sin(2\pi) \right) \right]$$

$$A = \frac{a \cdot b}{2} \cdot \pi$$

Por le tanto ... La media alijse er 0.5 a. b TI