

14.1 Funciones Varias Variables (Homework)

Current Score

QUESTION	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
POINTS	2/2	1/1.5	1/1	1/1	1/1	1/1.0	1/1	1/1	1/1	1/1	1/1	1/0	1/1	1/1	1/1	1/1	1/1	1
	✓	✗	✓	✓	✓	★	✓	✓	✓	✓	✓	★	✓	✓	✓	✓	✓	✓
TOTAL SCORE	37.17/40		92.9%															

Due Date

Past Due

SUN, MAR 1, 2020
11:59 PM CST

Request Extension

Description

Assignment Submission & Scoring

Assignment Submission

For this assignment, you submit answers by question parts. The number of submissions remaining for each question part only changes if you submit or change the answer.

Assignment Scoring

Your last submission is used for your score.

The due date for this assignment has passed.

Your work can be viewed below, but no changes can be made.

Important! Before you view the answer key, decide whether or not you plan to request an extension. Your instructor may not grant you an extension if you have viewed the answer key. Automatic extensions are not granted if you have viewed the answer key.

https://www.webassign.net/web/Student/Assignment-Responses/last?dep=22834895

1/40

Request Extension

1. 2/2 points

Previous Answers

SCALCET8 14.1.003.

My Notes

Ask Your Teacher

A manufacturer has modeled its yearly production function P (the monetary value of its entire production in millions of dollars) as a Cobb-Douglas function

$$P(L, K) = 1.47L^{0.65}K^{0.35}$$

where L is the number of labor hours (in thousands) and K is the invested capital (in millions of dollars). Find $P(125, 45)$ and interpret it. (Round your answers to one decimal place.)

$P(125, 45) = 128.5$ ✓, so when the manufacturer invests \$45 million in capital and 125 thousand hours of labor are completed yearly, the monetary value of the production is about \$128.5 million.

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2. 1/1.5 points

Previous Answers

SCALCET8 14.1.009.

My Notes

Ask Your Teacher

Let $g(x, y) = \cos(x + 5y)$.

(a) Evaluate $g(5, -1)$.

$g(5, -1) = 1$ ✓

(b) Find the domain of g .

☐ $-5 \leq x \leq 5, -1 \leq y \leq 1$

☒ \mathbb{R}^2

☐ $\frac{x}{2} \leq x + 5y \leq \frac{\pi}{2}$

☐ $-1 \leq x + 5y \leq 1$

☐ $-1 \leq x \leq 1, \frac{1}{5} \leq y \leq \frac{1}{5}$ ✓

(c) Find the range of g . (Enter your answer using interval notation.)

(No Response)

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https://www.webassign.net/web/Student/Assignment-Responses/last?dep=22834895

2/40

3. 1/1 points

Previous Answers

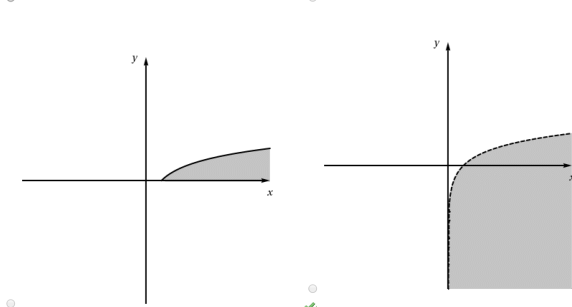
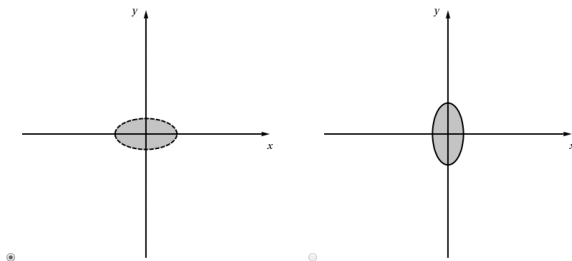
SCALCET8 14.1.015.

My Notes

Ask Your Teacher

Find and sketch the domain of the function.

$$f(x, y) = \ln(4 - x^2 - 4y^2)$$



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https://www.webassign.net/web/Student/Assignment-Responses/last?dep=22834895

3/40

4. 1/1 points

Previous Answers

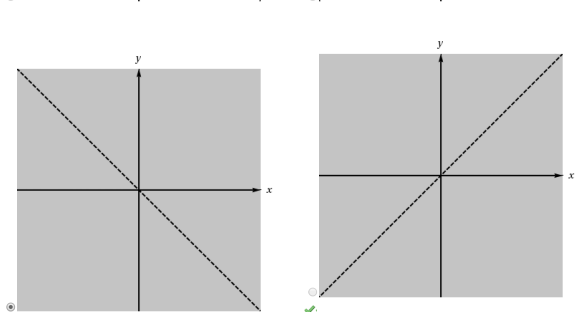
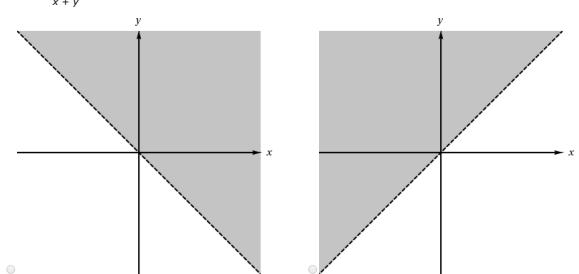
SCALCET8 14.1.017.

My Notes

Ask Your Teacher

Find and sketch the domain of the function.

$$g(x, y) = \frac{x - y}{x + y}$$



Need Help?

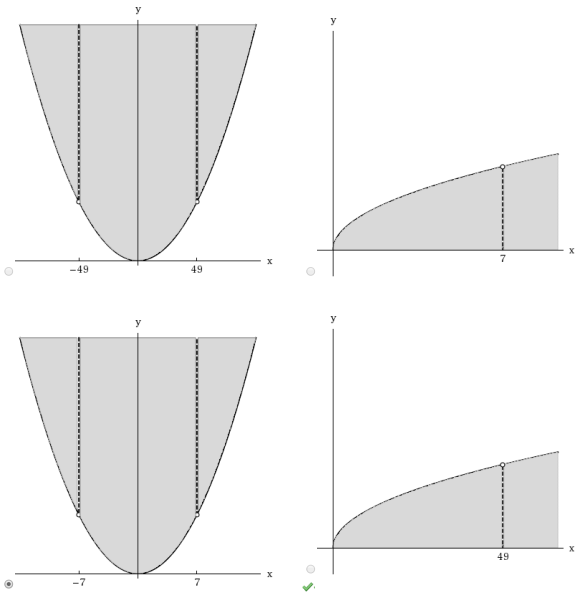
Talk to a Tutor

https://www.webassign.net/web/Student/Assignment-Responses/last?dep=22834895

4/40

Find and sketch the domain of the function.

$f(x,y) = \frac{\sqrt{y-x^2}}{49-x^2}$



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This question has several parts that must be completed sequentially. If you skip a part of the question, you will not receive any points for the skipped part, and you will not be able to come back to the skipped part.

Tutorial Exercise
Find and sketch the domain of the function.

$f(x,y) = \frac{\sqrt{y-x^2}}{16-x^2}$

Step 1
When finding the domain of a function, we must rule out points where the denominator equals zero and where there are negative values in the square root.

Step 2
For $f(x,y) = \frac{\sqrt{y-x^2}}{16-x^2}$, the denominator equals 0 when $x^2 = 16$.

Therefore, we must have $x \neq \pm 4$.

Step 3
The numerator $\sqrt{y-x^2}$ is defined only when $y-x^2 \geq 0$.

Therefore, we must have $y \geq x^2$.

$y \geq x^2$

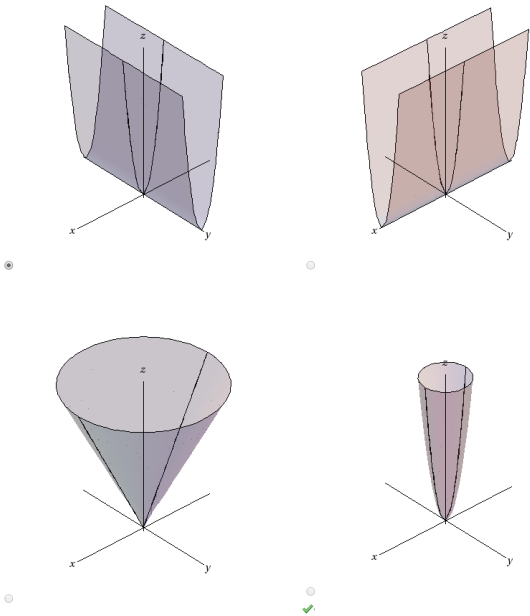
Step 4
Combining the above, we determine that the domain of the given function is as follows.

$y \geq x^2$
 $y \neq x^2$
 $y \geq x^2, x \neq \pm 4$

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Sketch the graph of the function.

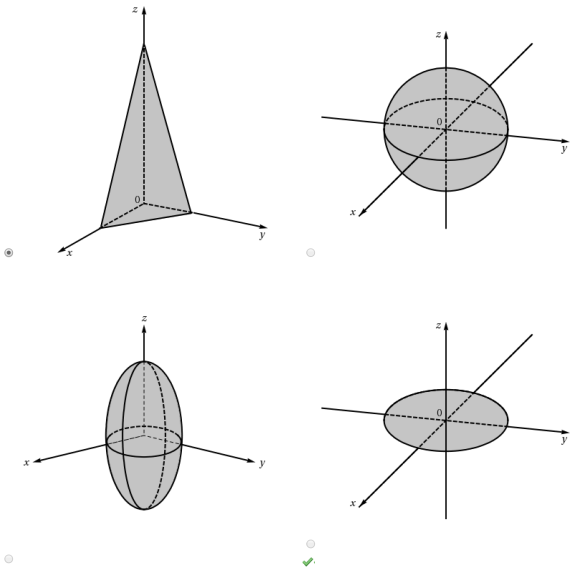
$f(x,y) = x^2$



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Sketch the graph of the function.

$f(x,y) = 12 - 4x - 5y$

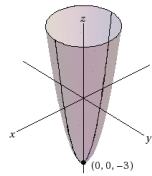
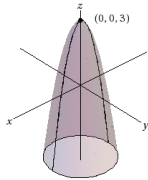
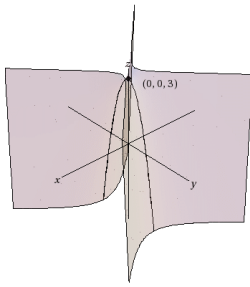
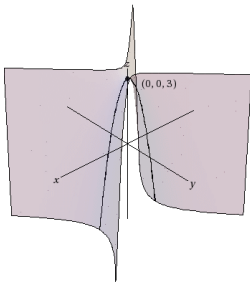


Need Help? Watch It Talk to a Tutor

9. 1/1 points Previous Answers SCALCET8 14.1.028.

Sketch the graph of the function.

$$f(x, y) = 3 - x^2 - y^2$$

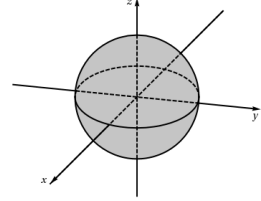
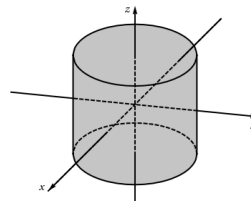
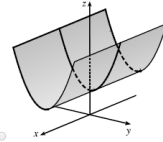
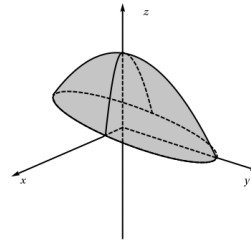


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10. 1/1 points Previous Answers SCALCET8 14.1.031.

Sketch the graph of the function.

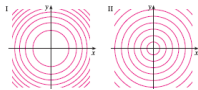
$$f(x, y) = \sqrt{9 - 9x^2 - y^2}$$



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11. 1/1 points Previous Answers SCALCET8 14.1.036.MI.

Two contour maps are shown. One is for a function f whose graph is a cone. The other is for a function g whose graph is a paraboloid. Which is which, and why?

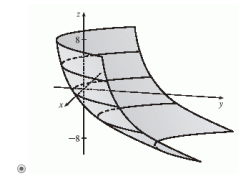
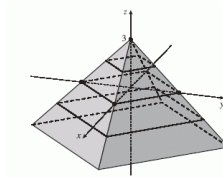
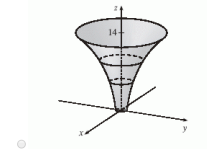
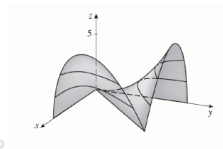
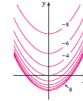


- ☐ Map II is the paraboloid. Map I is the cone. The cone's z -values change at a constant rate.
- ☐ Map I is the paraboloid. Map II is the cone. The paraboloid's z -values change at a constant rate.
- ☐ Map II is the paraboloid. Map I is the cone. The paraboloid's z -values change at a constant rate.
- ☒ Map I is the paraboloid. Map II is the cone. The cone's z -values change at a constant rate.

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12. 1/0 points Previous Answers SCALCET8 14.1.042.

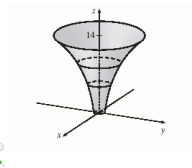
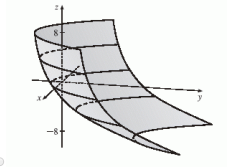
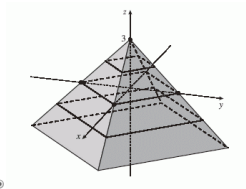
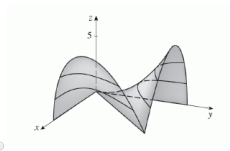
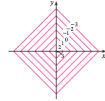
A contour map of a function is shown. Use it to make a rough sketch of the graph of f .



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13. 1/1 points Previous Answers SCALCET8 14.1.044. My Notes Ask Your Teacher

A contour map of a function is shown. Use it to make a rough sketch of the graph of f .

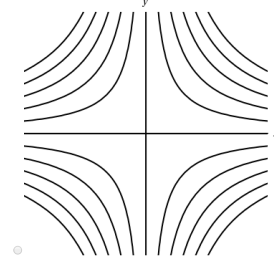
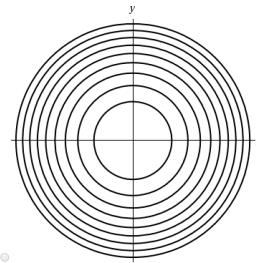
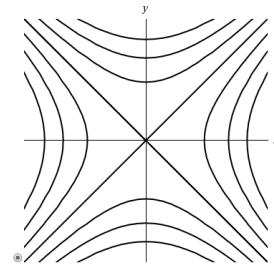
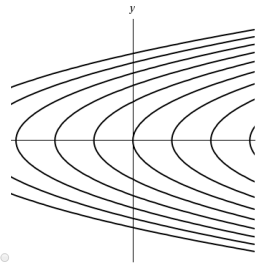


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14. 1/1 points Previous Answers SCALCET8 14.1.045. My Notes Ask Your Teacher

Draw a contour map of the function showing several level curves.

$$f(x, y) = x^2 - y^2$$

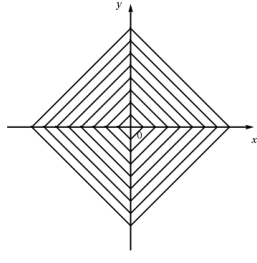
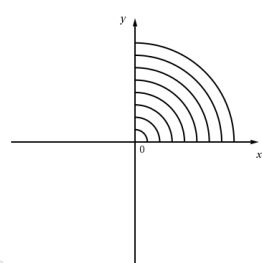
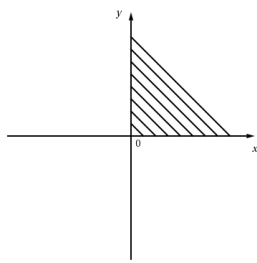
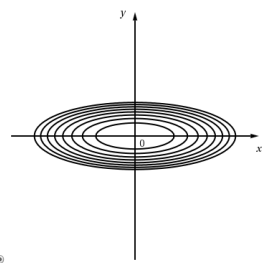


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15. 1/1 points Previous Answers SCALCET8 14.1.053. My Notes Ask Your Teacher

Sketch a contour map of the function.

$$f(x, y) = x^2 + 9y^2$$

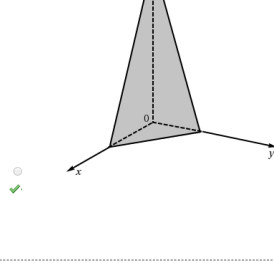
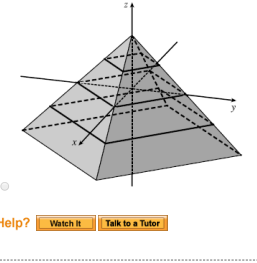
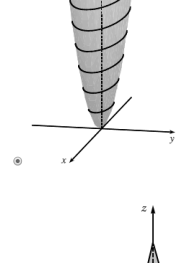
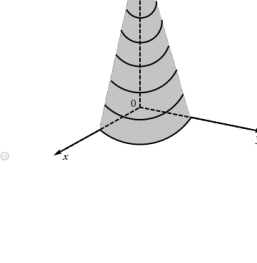


Sketch a graph of the function and compare it to the contour map.

16. 1/1 points Previous Answers SCALCET8 14.1.067. My Notes Ask Your Teacher

Describe the level surfaces of the function.

$$f(x, y, z) = x + 4y + 2z$$



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16. 1/1 points Previous Answers SCALCET8 14.1.067. My Notes Ask Your Teacher

Describe the level surfaces of the function.

$$f(x, y, z) = x + 4y + 2z$$

- ☒ The level surfaces are a family of parallel planes.
- ☐ The level surfaces are a family of ellipsoids.
- ☐ The level surfaces are a family of hyperboloids.
- ☐ The level surfaces are a family of hyperbolic cylinders.

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17. 1/1 points Previous Answers SCALCET8 14.1.068. My Notes Ask Your Teacher

Describe the level surfaces of the function.

$f(x, y, z) = x^2 + 4y^2 + 5z^2$

☐ The level surfaces are a family of parallel planes.

☒ The level surfaces are a family of ellipsoids.

☐ The level surfaces are a family of hyperboloids.

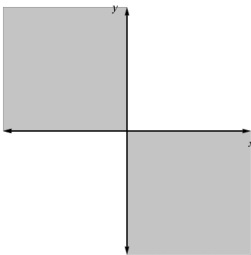
☐ The level surfaces are a family of hyperbolic cylinders.

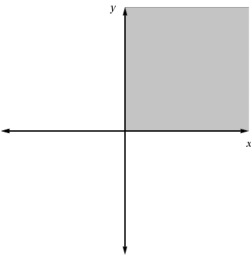
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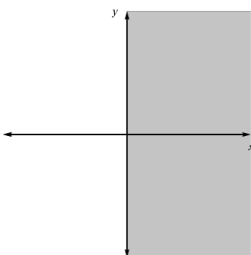
18. 1/1 points Previous Answers SCALCET8 14.1.502.XP. My Notes Ask Your Teacher

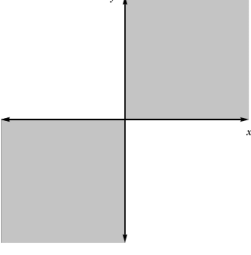
Find and sketch the domain of the function.

$f(x, y) = \sqrt{3xy}$

☐

☐

☐

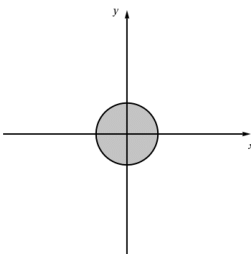
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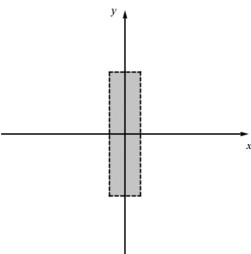
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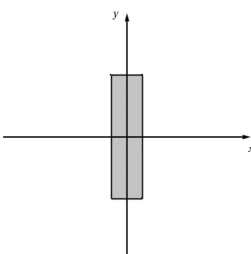
19. 1/1 points Previous Answers SCALCET8 14.1.503.XP. My Notes Ask Your Teacher

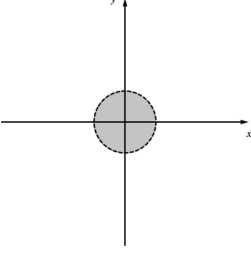
Find and sketch the domain of the function.

$f(x, y) = \sqrt{1 - x^2} - \sqrt{16 - y^2}$

☐

☐

☒

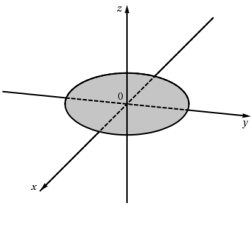
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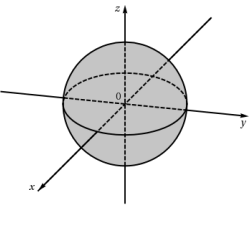
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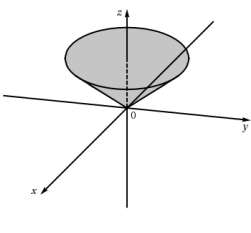
20. 1/1 points Previous Answers SCALCET8 14.1.506.XP. My Notes Ask Your Teacher

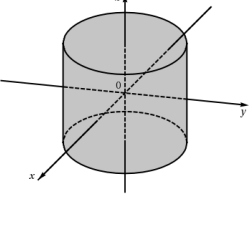
Find and sketch the domain of the function.

$f(x, y, z) = \sqrt{4 - x^2 - y^2 - z^2}$

☐

☒

☐

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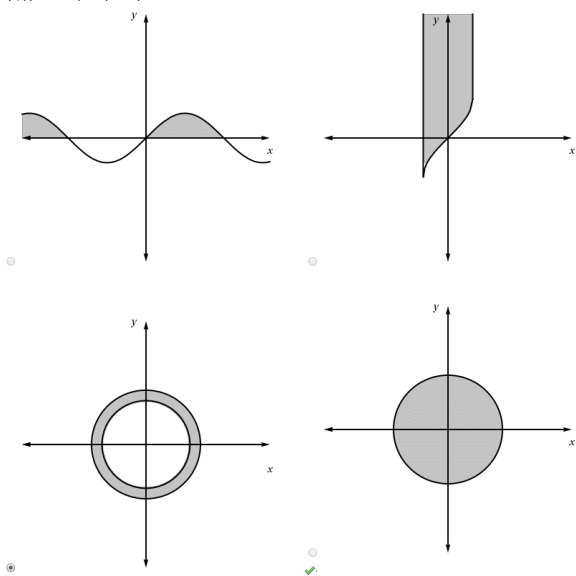
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21. 1/0 points Previous Answers SCALCET8 14.1.505.XP.

My Notes Ask Your Teacher

Find and sketch the domain of the function.

$$f(x, y) = \arcsin(x^2 + y^2 - 4)$$



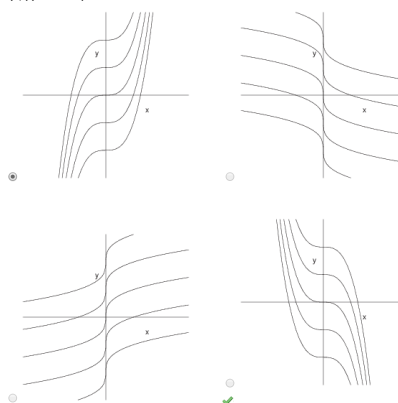
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22. 1/1 points Previous Answers SCALCET8 14.1.510.XP.

My Notes Ask Your Teacher

Draw a contour map of the function showing several level curves.

$$f(x, y) = x^3 - 4y$$



Need Help? Talk to a Tutor

23. 1/1 points Previous Answers SCALCET8 14.1.513.XP.

My Notes Ask Your Teacher

Consider the function below.

$$f(x, y) = \ln(x + y - 3)$$

(a) Evaluate $f(1, 3)$.

0

(b) Evaluate $f(e, 3)$.

1

(c) Find the domain of f .

- ☐ $x > 3$
☐ $y > 3$
☒ $x + y > 3$
☐ $x + y - 3 > 1$
☐ $x > 3, y > 3$

(d) Find the range of f . (Enter your answer using interval notation.)
$$(-\infty, \infty)$$

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24. 1/1.5 points Previous Answers SCALCET8 14.1.514.XP.

My Notes Ask Your Teacher

Consider the function below.

$$f(x, y) = x^2 e^{3xy}$$

(a) Evaluate $f(6, 0)$.

36

(b) Find the domain of f .

- ☐ $(0, \infty) \times (0, \infty)$
☐ $\mathbb{R} \times (0, \infty)$
☐ $(0, \infty) \times \mathbb{R}$
☐ $(0, \infty) \times (1/3, \infty)$
☒ $\mathbb{R} \times \mathbb{R}$

(c) Find the range of f . (Enter your answer using interval notation.)

(No Response)

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25. 0.5/1 points Previous Answers SCALCET8 14.1.515.XP.

My Notes Ask Your Teacher

Consider the function below.

$$f(x, y) = \sqrt{5 + x - y^2}$$

(a) Find the domain of f .

- ☐ $y^2 \geq x$
☒ $x \geq y^2 - 5$
☐ $x + 5 \leq y^2$
☐ $|x - y^2| \geq 0$
☐ $x \geq y^2$

(b) Find the range of f . (Enter your answer using interval notation.)

(No Response)

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26. 1.5/1.5 points Previous Answers SCALCET8 12.6.001.

My Notes

Ask Your Teacher

(a) What does the equation $y = x^2$ represent as a curve in \mathbb{R}^2 ?

- ☐ hyperbola
☐ circle
☒ parabola
☐ ellipse
☐ line

(b) What does it represent as a surface in \mathbb{R}^3 ?

- ☒ parabolic cylinder
☐ ellipsoid
☐ cone
☐ elliptic paraboloid
☐ hyperboloid

(c) What does the equation $z = y^2$ represent?

- ☐ cone
☐ ellipsoid
☐ elliptic paraboloid
☐ hyperboloid
☒ parabolic cylinder

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27. 1/1 points Previous Answers SCALCET8 12.6.003.

My Notes

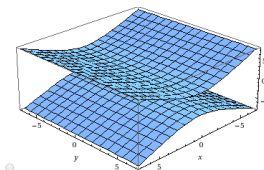
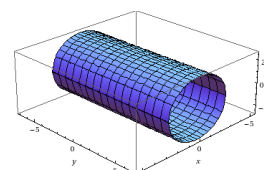
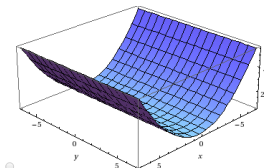
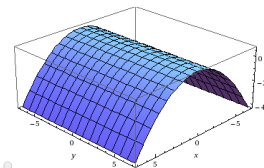
Ask Your Teacher

Describe the surface.

$$x^2 + z^2 = 7$$

- ☐ sphere
☐ ellipsoid
☐ hyperboloid
☒ circular cylinder
☐ elliptic cylinder
☐ hyperbolic cylinder
☐ parabolic cylinder
☐ elliptic paraboloid

Sketch the surface.



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28. 1/1 points Previous Answers SCALCET8 12.6.005.

My Notes

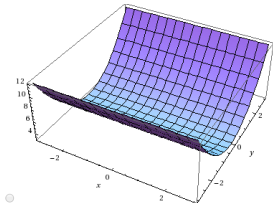
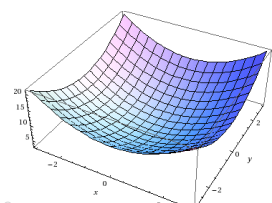
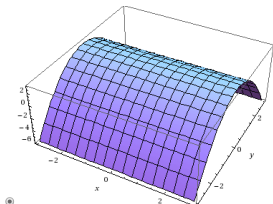
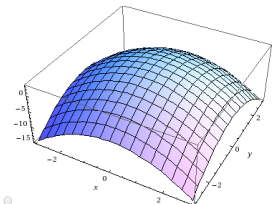
Ask Your Teacher

Describe the surface.

$$z = 3 - y^2$$

- ☐ cone
☐ ellipsoid
☐ hyperboloid
☐ elliptic cylinder
☐ hyperbolic cylinder
☒ parabolic cylinder
☐ elliptic paraboloid
☐ hyperbolic paraboloid

Sketch the surface.



Need Help?

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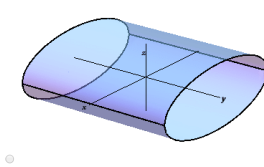
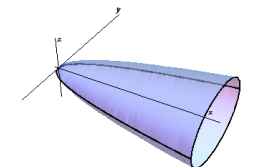
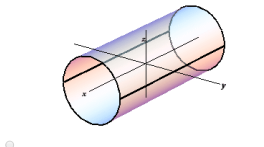
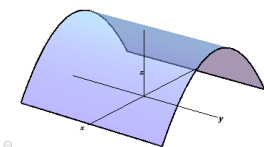
29. 1/1 points Previous Answers SCALCET8 12.6.011.

My Notes

Ask Your Teacher

Use traces to sketch the surface.

$$x = y^2 + 3z^2$$



Identify the surface.

- ☐ elliptic cylinder
☐ parabolic cylinder
☐ elliptic cone
☐ hyperboloid of one sheet
☐ ellipsoid
☒ elliptic paraboloid
☐ hyperboloid of two sheets
☐ hyperbolic paraboloid

Need Help?

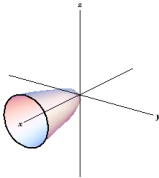
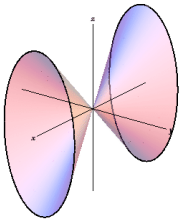
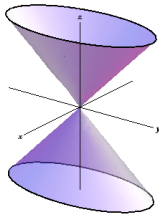
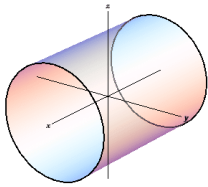
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30. [1/1 points](#) [Previous Answers](#) SCALCET8 12.6.013. [My Notes](#) [Ask Your Teacher](#)

Use traces to sketch the surface.

$$x^2 = 4y^2 + z^2$$



Identify the surface.

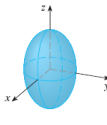
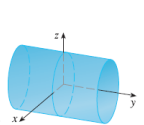
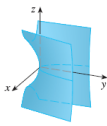
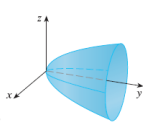
- ☐ hyperbolic paraboloid
- ☐ ellipsoid
- ☐ hyperboloid of two sheets
- ☐ parabolic cylinder
- ☒ elliptic cone
- ☐ elliptic cylinder
- ☐ hyperboloid of one sheet
- ☐ elliptic paraboloid

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33. [1/1 points](#) [Previous Answers](#) SCALCET8 12.6.025. [My Notes](#) [Ask Your Teacher](#)

Match the equation with its graph.

$$y = 2x^2 + z^2$$

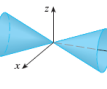
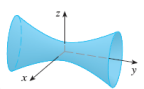
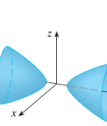
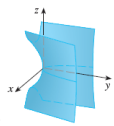


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34. [1/1 points](#) [Previous Answers](#) SCALCET8 12.6.026. [My Notes](#) [Ask Your Teacher](#)

Match the equation with its graph.

$$y^2 = x^2 + 2z^2$$

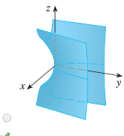
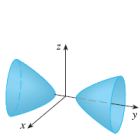
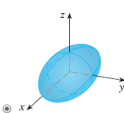
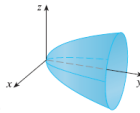


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31. [1/1 points](#) [Previous Answers](#) SCALCET8 12.6.021. [My Notes](#) [Ask Your Teacher](#)

Match the equation with its graph.

$$x^2 + 4y^2 + 9z^2 = 1$$

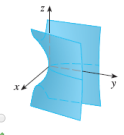
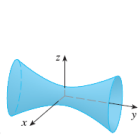
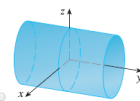
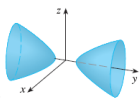


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32. [1/1 points](#) [Previous Answers](#) SCALCET8 12.6.023. [My Notes](#) [Ask Your Teacher](#)

Match the equation with its graph.

$$x^2 - y^2 + z^2 = 1$$

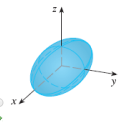
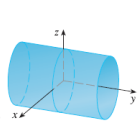
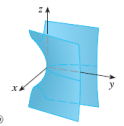
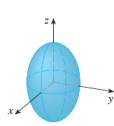


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35. [1/1 points](#) [Previous Answers](#) SCALCET8 12.6.028. [My Notes](#) [Ask Your Teacher](#)

Match the equation with its graph.

$$y = x^2 - z^2$$



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36. 0/0 points Previous Answers SCALCET8 12.6.034. My Notes Ask Your Teacher

Consider the equation below.

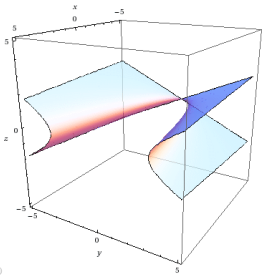
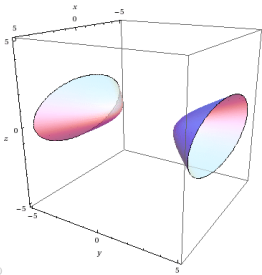
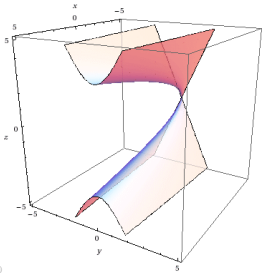
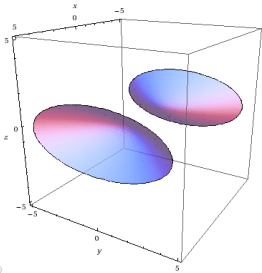
$y^2 = x^2 + 5z^2 + 5$
Reduce the equation to one of the standard forms.
 $5x^2 - y^2 + 5z^2 = -5$

✖

Classify the surface.

- ☐ ellipsoid
- ☐ elliptic paraboloid
- ☐ hyperbolic paraboloid
- ☐ cone
- ☐ hyperboloid of one sheet
- ☐ hyperboloid of two sheets

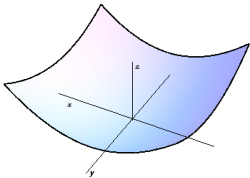
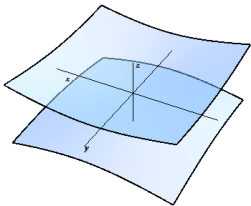
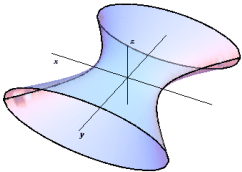
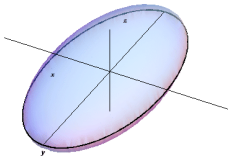
Sketch the surface.



37. 0.75/1.5 points Previous Answers SCALCET8 12.6.507.XP. My Notes Ask Your Teacher

Use traces to sketch the surface.

$6x^2 - 24y^2 + z^2 = 24$



Identify the surface.

- ☐ ellipsoid
- ☒ elliptic paraboloid
- ☐ hyperboloid of two sheets
- ☐ hyperbolic paraboloid
- ☐ elliptic cylinder
- ☐ elliptic cone
- ☐ hyperboloid of one sheet
- ☐ parabolic cylinder

✖

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38. -1 points SCALCET8 12.6.508.XP. My Notes Ask Your Teacher

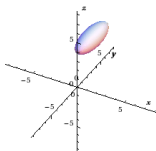
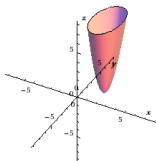
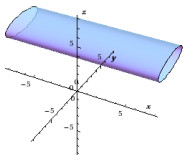
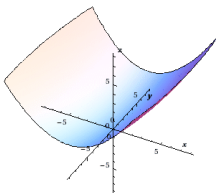
Consider the equation below.

$9x^2 + y^2 + 9z^2 - 6y - 72z + 144 = 0$
Reduce the equation to one of the standard forms.
[No Response]

Classify the surface.

- ☐ parabolic cylinder
- ☐ circular cone
- ☐ elliptic cylinder
- ☐ ellipsoid
- ☐ hyperboloid of two sheets
- ☐ hyperbolic paraboloid
- ☐ hyperboloid of one sheet
- ☐ elliptic paraboloid

Sketch the surface.



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40. -/1.5 points SCALCET8 12.6.AE.005.

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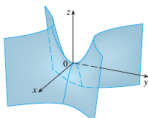


Figure 1
[Video Example](#)

EXAMPLE 5 Sketch the surface $z = 5y^2 - 6x^2$.

SOLUTION The traces in the vertical planes $x = k$ are the parabolas $z = \text{[No Response]}$, which open upward. The traces in $y = k$ are the parabolas $z = \text{[No Response]}$, which open downward. The horizontal traces are $\text{[No Response]} = k$, a family of hyperbolas. We draw the family of traces in Figure 2, and we show how the traces appear when placed in their correct planes in Figure 3. In Figure 1 we fit together the terms to form the surface $z = 5y^2 - 6x^2$, a **hyperbolic paraboloid**. Notice that the shape of the surface near the origin resembles that of a saddle. This surface will be investigated further in a later section when we discuss saddle points.

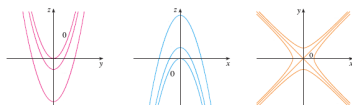


Figure 2

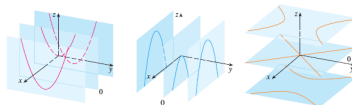


Figure 3

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39. -/0 points SCALCET8 12.6.509.XP.

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Consider the equation below.

$$3y^2 + z^2 - x - 13y - 4z + 16 = 0$$

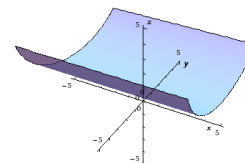
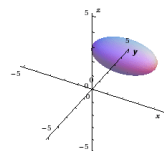
Reduce the equation to one of the standard forms.

[\[No Response\]](#)

Classify the surface.

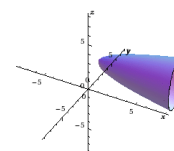
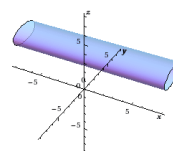
- ☐ ellipsoid
- ☐ elliptic paraboloid
- ☐ circular cone
- ☐ hyperboloid of two sheets
- ☐ hyperbolic paraboloid
- ☐ hyperboloid of one sheet
- ☐ parabolic cylinder
- ☐ elliptic cylinder

Sketch the surface.



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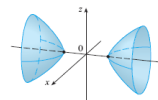
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41. 0.32/1.5 points SCALCET8 12.6.AE.007.

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[Video Example](#)

EXAMPLE 7 Identify and sketch the surface $4x^2 - y^2 + 2z^2 + 4 = 0$.

SOLUTION Dividing by -4 , we first put the equation into standard form:

$$-x^2 + \frac{y^2}{4} - \frac{z^2}{2} = 1$$

Comparing this equation with equations of quadratic surfaces, we see that it represents a [\[No Response\]](#), the only difference being that in this case the axis of the hyperboloid is the [\[No Response\]](#). The traces in the xy - and yz -planes are the hyperbolas

$$-x^2 + \frac{y^2}{4} = 1 \quad z = 0$$

and

$$\frac{y^2}{4} - \frac{z^2}{2} = 1 \quad x = 0.$$

The surface has no trace in the xz -plane, but traces in the vertical planes $y = k$ for $|k| > 2$ are the ellipses

$$x^2 + \frac{z^2}{2} = \text{[No Response]} - 1 \quad y = k$$

which can be written as

$$\frac{x^2}{\text{[No Response]} - 1} + \frac{z^2}{2(\text{[No Response]} - 1)} = 1 \quad y = k.$$

Thus the traces are used to make the sketch in the figure.

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