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Corto #5 Cálculo Multivariable (20 min)

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1. Analice si la función $r = \langle 3e^{-t}, \ln(2t^2 - 1), \tan(2\pi) \rangle$ es continua en $t = 1$.

$$\lim_{t \rightarrow 1} (r) = \left\langle \underbrace{\lim_{t \rightarrow 1} (3e^{-t})}_{f(t)}, \underbrace{\lim_{t \rightarrow 1} (\ln(2t^2 - 1))}_{g(t)}, \underbrace{\lim_{t \rightarrow 1} (\tan(2\pi))}_{h(t)} \right\rangle$$

$$\lim_{t \rightarrow 1} (f(t)) = \frac{3}{e} \quad \text{---} \times$$

$$\begin{aligned} \lim_{t \rightarrow 1} (g(t)) &= \ln(2(1)^2 - 1) \\ &= \ln(2 - 1) \\ &= \ln(1) \\ &= 0 \quad \text{---} \times \end{aligned}$$

$$\begin{aligned} \lim_{t \rightarrow 1} (h(t)) &= \tan(2\pi) \\ &= \frac{\sin(2\pi)}{\cos(2\pi)} \leftarrow 0 \quad r(1) \end{aligned}$$

$$= 0 \quad \text{---} \times$$

Si es continua en $t=1$ $\langle \frac{3}{e}, 0, 0 \rangle$

2. Encuentre la ec. de la recta tangente a $r(t) = \langle te^{t-1}, \frac{8}{\pi} \arctan(t), 2 \ln(t) \rangle$ en $t = 1$.

$$\vec{r}_T = \vec{r}(a) + t \vec{r}'(a)$$

$$\begin{aligned} \vec{r}(1) &= \left\langle 1 \cdot e^{(1-1)}, \frac{8}{\pi} \underbrace{\arctan(1)}_{\frac{\pi}{4}}, \underbrace{2 \ln(1)}_0 \right\rangle \\ &= \left\langle 1, \frac{8}{\pi} \cdot \frac{\pi}{4}, 0 \right\rangle \\ &= \langle 1, 2, 0 \rangle \end{aligned}$$

$$\frac{\sin(\pi/4)}{\cos(\pi/4)} = \frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = 1$$

$$\boxed{\vec{r}_T(1) = \langle 1, 2, 0 \rangle + t \langle 2, \frac{4}{\pi}, 2 \rangle}$$

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$$\vec{r}'(t) = \left\langle (e^{t-1} + t e^{t-1} \cdot 1), \left(\frac{8}{\pi} \cdot \frac{1}{t^2+1} \right), \left(\frac{2}{t} \right) \right\rangle$$

$$\vec{r}'(t) = \left\langle e^{t-1} + t e^{t-1}, \frac{8}{\pi(t^2+1)}, \frac{2}{t} \right\rangle$$

$$\begin{aligned} \vec{r}'(1) &= \left\langle e^0 + 1 \cdot e^0, \frac{8}{\pi(1+1)}, \frac{2}{1} \right\rangle = \left\langle 1 + 1, \frac{8}{2\pi}, 2 \right\rangle \\ &= \left\langle 2, \frac{4}{\pi}, 2 \right\rangle \end{aligned}$$