

$$\frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \dots + \frac{1}{(3n-2)(3n+1)} = \frac{n}{3n+1}$$

$$\sum_{i=1}^{n} \left(\frac{1}{(3n-2)(3n+1)} \right) = \frac{n}{3n+1}$$

Prueba por inducción

Paso base:
$$n = 1$$

$$\frac{1}{(3(1)-2)(3(1)+1)} = \frac{1}{3(1)+1}$$

$$\frac{1}{(3-2)(3+1)} = \frac{1}{3+1}$$

$$\frac{1}{(4)(4)} = \frac{1}{4}$$

$$\frac{1}{(1)(4)} = \frac{1}{4}$$

$$\frac{1}{4} = \frac{1}{4} \checkmark$$

Paso inductive:

$$P(n) \rightarrow P(n+1)$$
 $n=k$

$$\frac{1}{1\cdot 4} + \frac{1}{4\cdot 7} + ... + \frac{1}{(3n-2)(3n+1)} = \frac{n}{3n+1}$$

$$\frac{1}{1.4} + \frac{1}{4.7} + \dots + \frac{1}{(3n-2)(3n+1)} + \frac{1}{(3(n+1)-2)(3(n+1)+1)} = \frac{n}{(3n+1)} + \frac{1}{(3(n+1)-2)(3(n+1)+1)}$$

$$= \frac{1}{(3n+1)} + \frac{1}{(3n+3-2)(3n+3+1)}$$

$$= \frac{n}{(3n+1)} + \frac{1}{(3n+1)(3n+4)}$$

$$= \frac{1}{(3n+1)} \left(n + \frac{1}{3n+4} \right)$$

$$= \frac{1}{(3n+1)} \left(\frac{n(3n+4)}{(3n+4)} + \frac{1}{3n+4} \right)$$

$$= \frac{1}{(3n+1)} \left(\frac{3n^2 + 4n + 1}{(3n+4)} \right)$$

$$= \frac{3n^2 + 4n + 1}{(3n+1)(3n+4)} = \frac{3n^2 + 4n + 1}{9n^2 + 12n + 3n + 4}$$

$$= \frac{3n^2 + 4n + 1}{9n^2 + 15n + 4} = \frac{(3n+1)(n+1)}{(3n+4)(3n+4)}$$

$$= \frac{n+1}{3n+3+1} = \frac{n+1}{3(n+1)+1}$$

2) Forma recursiva Pm(n). Producto entero de m

nxm es n svmado a sí mismo m veces

5x3 5 sumado a si mismo 3 veces

5+5+5

Coso base: cuando el que usemos como contador se vuelva O devolvemos 1

def mult
$$(n, m)$$
:

if $(m = 0)$:

return $n + mult(n, m-1)$

mult $(5,3)$
 $5 + mult(5,2)$
 $5 + mult(5,1)$
 $5 + mult(5,0) = 0$