

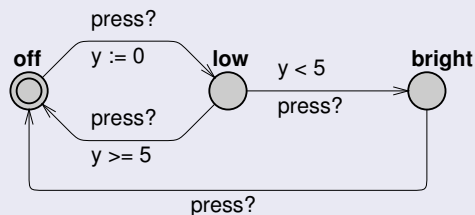
Embedded Systems Specification and Design

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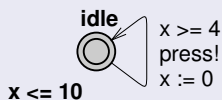
- Modelling a system as a *network* of timed automata
- Semantics of parallel composition
- Specifying real-time properties
 - Test automata
 - Uppaal's property specification language

Network of Timed Automata

Lamp



User



What behaviours is the **system** capable of?

Parallel Composition: Preliminaries

- Timed automata composed into a **network of timed automata** consisting of n TA's $A_i = (L_i, l_i^0, C, A, E_i, \mathcal{I}_i)$, $1 \leq i \leq n$.
- Assume a common set of clocks and actions
- A location vector is a vector $\bar{l} = (l_1, \dots, l_n)$.
- We compose the invariant functions into a common function over location vectors $\mathcal{I}(\bar{l}) \triangleq \bigwedge_i \mathcal{I}_i(l_i)$.
- We write $\bar{l}[l'_i/l_i]$ to denote the vector where the i th element l_i of \bar{l} is replaced by l'_i .

Parallel Composition

Gives the meaning of a system comprising several components.

Definition (Network of TA Semantics)

Let $A_i = (L_i, l_i^0, C, A, E_i, \mathcal{I}_i)$ be a network of n timed automata. Let $\bar{l}_0 = (l_1^0, \dots, l_n^0)$ be the initial location vector. The semantics is defined as a transition system (S, s_0, \rightarrow) , where $S = (L_1 \times \dots \times L_n) \times \mathbb{R}^C$ is the set of states, $s_0 = (\bar{l}_0, u_0)$ is the initial state, and $\rightarrow \subseteq S \times S$ is the transition relation defined by the rules for

- Time Progress (TP)
- Independent Action (IA), and
- Synchronising Action (SA)

as follows.

Transition Rules for Parallel Composition

$$\text{TP } (\bar{l}, u) \xrightarrow{d} (\bar{l}, u + d), \text{ if } \forall d' : 0 \leq d' \leq d \Rightarrow u + d' \in \mathcal{I}(\bar{l})$$

Transition Rules for Parallel Composition

- TP** $(\bar{l}, u) \xrightarrow{d} (\bar{l}, u + d)$, if $\forall d' : 0 \leq d' \leq d \Rightarrow u + d' \in \mathcal{I}(\bar{l})$
- IA** $(\bar{l}, u) \xrightarrow{\tau} (\bar{l}[l'_i/l_i], u')$ if there exists $(l_i, \tau, g, r, l'_i) \in E_i$ such that $u \in g$, $u' = [r \mapsto 0]u$, and $u' \in \mathcal{I}(\bar{l}[l'_i/l_i])$

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- SA** $(\bar{l}, u) \xrightarrow{c} (\bar{l}[l'_i/l_i, l'_j/l_j], u')$ if there exists $(l_i, c?, g_i, r_i, l'_i) \in E_i$ and $(l_j, c!, g_j, r_j, l'_j) \in E_j$ such that $u \in (g_i \wedge g_j)$, $u' = [r_i \cup r_j \mapsto 0]u$, and $u' \in \mathcal{I}(\bar{l}[l'_i/l_i, l'_j/l_j])$

- Want to check formal model to see if it has specified properties.
- Interested in both safety and liveness properties
- Safety property
 - Nothing bad ever happens
E.g. the train is never in the crossing when the gate is open
- Liveness property
 - Something good eventually happens
E.g. whenever the gate is closed, it is eventually opened again

How to specify properties of a TA

- **State properties**

Simple boolean formulas that can be checked with respect to a single state

- **Test automata**

- **Real-time temporal logic**

- Allow the expression of properties that concern executions (paths), i.e. sequences of states

- Construct a TA A_s that acts as an observer of the model A_m
- Usually the observer TA includes one special error location
- The property is tested by checking that the observer can never reach its error location in the composition $A_m \mid A_s$
- Good:
 - Can use simple reachability analysis to test complex properties
- Not so good:
 - May need to modify model in order to allow observation
 - Ad hoc specification may not be correct

Test Automaton Example

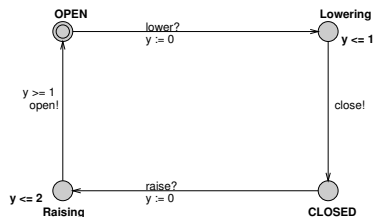


Figure: GATE Automaton

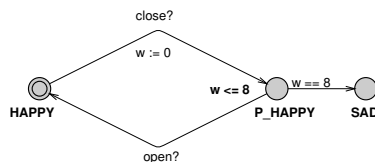


Figure: OBSERVER Automaton

- Check that observer is never **SAD**
- Requires change to GATE model to allow observation

Uppaal's Specification Language

- A simple real-time temporal logic
- Like LTL but with real-time values and path quantifiers
- No nested temporal operators
- Kept simple deliberately so that properties can be decided by reachability testing
- Simple, efficient implementation of verification procedure

Definition of the Specification Language

- Simple state properties
 - Location assertions
 $P.I$
 - Process P is in location I
E.g. Gate.CLOSED, Train.IN, etc.
 - deadlock
 - Clock constraints
 $ID \text{ REL } NAT \mid ID \text{ REL } ID \mid ID \text{ REL } ID + NAT$
 $\mid ID \text{ REL } ID - NAT$
E.g. $x \geq 3$, $x > y$, $x \leq y + 4$, $x == y - 2$

Definition of the Specification Language ctd

- Assume AP is the set of simple state properties
- The set SP of state properties can be expressed as

$SP ::= AP \mid \text{not } SP \mid (SP) \mid SP \text{ or } SP \mid SP \text{ and } SP$
 $\mid SP \text{ imply } SP$

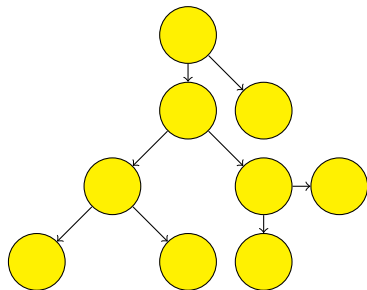
E.g. not Train.IN, Gate.CLOSED or Gate.OPEN, Train.OUT and $x \leq 5$, Gate.OPEN imply not TRAIN.IN, deadlock

Definition of the Specification Language ctd

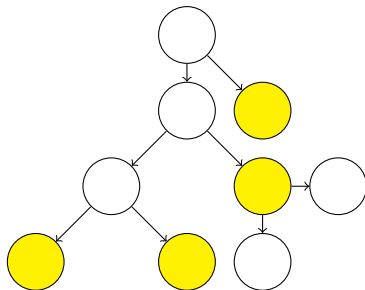
- Path properties
- $\text{Prop} ::= A[] \text{ SP} \quad - \text{ all paths always}$
 - $| E<> \text{ SP} \quad - \text{ some path eventually}$
 - $| E[] \text{ SP} \quad - \text{ some path always}$
 - $| A<> \text{ SP} \quad - \text{ all paths eventually}$
 - $| \text{ SP } \rightarrow \text{ SP} \quad - \text{ leads to}$
- E.g. $A[]$ not deadlock, $E<> \text{ Gate.OPEN}$
- Each property in UPPAAL must be expressed as a path property
- N.B. $P \rightarrow Q$ is equivalent to $A[] (P \text{ imply } A<> Q)$
But UPPAAL doesn't allow nested path quantifiers in general

All paths

$A[]\phi$

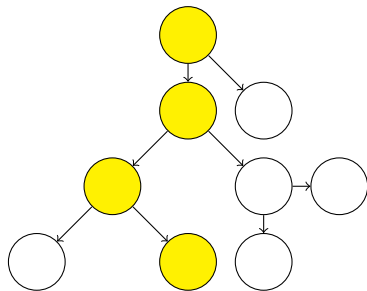


$A<>\phi$

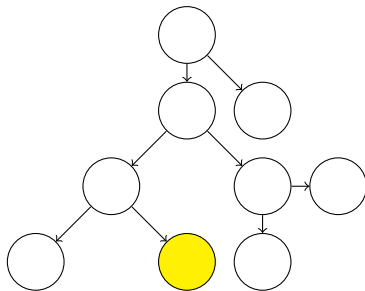


Some path

$E[]\phi$

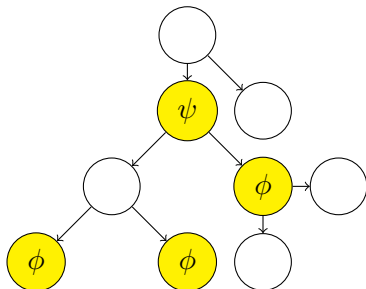


$E<>\phi$



Leads to

$$\psi \leadsto \phi$$



Example properties

- $A[]$ not deadlock
 - On all executions, in every state, the property not deadlock is true
- $E \leftrightarrow \text{Train.In}$
 - On some execution, in some state, the train is in the crossing
- $A[] (\text{Train.In} \implies \text{Gate.Closed})$
 - On all executions, in every state, if the train is in the crossing, the gate is closed
- $\text{Gate.Closed} \rightarrow \text{Gate.Open} \text{ and } (g \leq 30)$
 - Whenever the gate is closed, it is eventually opened within 30 time units (assumes g is global clock which is reset on entry to Gate.Closed)