Implementation of dilution rate-dependent glycolytic enzyme activity

The growth rate dependent change in protein activity was considered in this work. We used the experimental gly-colytic enzymes activity quantification between dilution rates of 0.025-0.4 h⁻¹ (van Hoek *et al*, 2000). The experimental setup was also chemostats as in the experimental steady sate data used in this work (Canelas *et al*, 2011), making this comparison more reliable. The experimental data from (van Hoek *et al*, 2000) is plotted in Fig. 1:

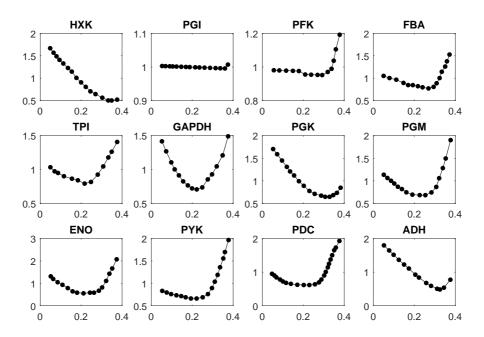


FIGURE 1 Experimental protein activity in the (van Hoek *et al*, 2000) dataset. Activity is plotted in the Y-axis (unitless) and dilution rate in the X-axis (in h⁻¹).

For all the glycolytic enzymes for which the experimental data was available, enzymatic activity was interpolated at a given dilution rate. A ratio was then calculated between this interpolated value and the experimental value at $0.1 \, h^{-1}$ accounting for a relative change in activity. The value at $0.1 \, h^{-1}$ was taken as a reference, since the kinetic parameters in the model and the single glucose perturbation simulations were performed in this dilution rate. This ratio was then use to alter the V_{max} for each glycolytic enzyme. The example below shows the case for HXK reaction rate:

$$HXK_{cor,d} = \frac{activity_{HXK,d}}{activity_{HXK,0.1}}$$
 (1)

$$v_{\text{HXK}} = \frac{\text{HXK}_{\text{cor,d}} \, V_m \, \left(\text{ATP GLCi} - \frac{\text{ADP G6P}}{K_{\text{eq}}} \right)}{K_{m,\text{glc}} \, K_{m,\text{atp}} \, \left(\frac{\text{ADP}}{K_{m,\text{adp}}} + \frac{\text{ATP}}{K_{m,\text{atp}}} + 1 \right) \left(\frac{\text{G6P}}{K_{m,\text{gfc}}} + \frac{\text{GLCi}}{K_{m,\text{glc}}} + \frac{\text{T6P}}{K_{i,\text{t6p}}} + 1 \right)}$$
(2)

References

Canelas AB, Ras C, ten Pierick A, van Gulik WM, Heijnen JJ (2011) An in vivo data-driven framework for classification and quantification of enzyme kinetics and determination of apparent thermodynamic data. *Metabolic engineering* **13**: 294–306

van Hoek P, van Dijken JP, Pronk JT (2000) Regulation of fermentative capacity and levels of glycolytic enzymes in chemostat cultures of Saccharomyces cerevisiae. *Enzyme and microbial technology* **26**: 724–736