

Molecular Spectroscopy

David Lawton, TCD
Student No. 22337087
Lab Partner: Sami Lopez-Steffenson

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1 Abstract

The experiment described in this report regarded the use of two moderate resolution spectrometers to analyse the emission spectrum of N_2 . The spectrometers were calibrated using a mercury lamp, and the emission spectrum of N_2 was captured afterward. The wavenumbers of the peaks were calculated, and used to calculate the dissociation energy of the molecule, as well as the values of $\tilde{\nu}_B$, $\tilde{\nu}_B x_B$, $\tilde{\nu}_C$, and $\tilde{\nu}_C x_C$, parameters of the vibronic transition emissions.

While initially, there were further parts for which data was collected, involving the I_2 absorption spectrum, the data was not used in the final analysis due to time constraints, and so is not included in this report.

2 Introduction

This report details the experimental procedure and results of the Molecular Spectroscopy lab. The aim of the experiment was to learn about the principles of optical emission and absorption spectroscopy, and the molecules being analysed. The experiment was conducted using two computerised diffraction grating spectrometers, of crossed Czerny-Turner type, with a $50\mu m$ diameter optical fibre input. The output is displayed digitally using the software provided.

2.1 Theory & Background

Unlike the lines of atomic emission spectra, which are due to transitions between electronic energy level, molecular emission spectra are due to transitions between vibrational and rotational energy levels, as well as electronic. In this experiment we are concerned with only the **vibronic** transitions, which are transitions between vibrational and electronic energy levels, due to insufficiently high resolution to view rotational energy levels.

While the electronic levels are described similarly to that of an atom, we must use a different model for the vibrational levels.

2.1.1 Molecular Vibrations

It would seem natural to first consider the harmonic oscillator model for molecular vibrations, which is a decent approximation for small vibrations. The potential dictating this being

$$V(x) = \frac{1}{2}kx^2 \quad (1)$$

Which yields the energy levels:

$$E_\nu = \left(\nu + \frac{1}{2}\right)\hbar\omega \quad (2)$$

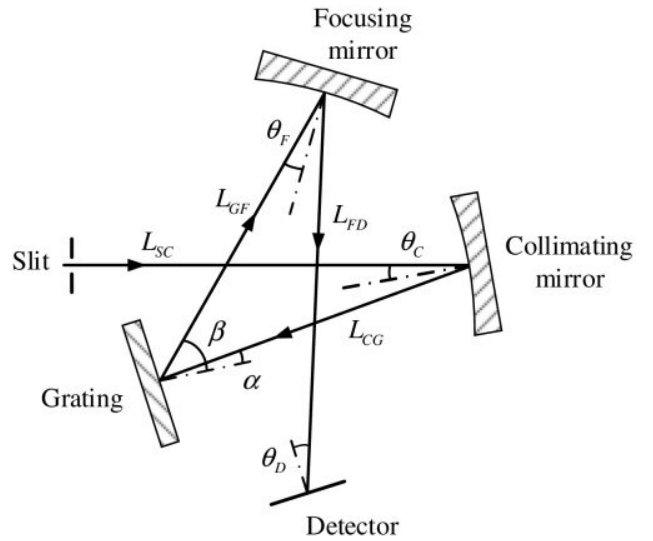


Figure 1: A diagram of a crossed Czerny-Turner Type Spectrometer's optical bench. [8]

Where ν is the vibrational quantum number, and $\omega = \sqrt{\frac{k}{\mu}}$ is the fundamental frequency of the oscillation. Here, k is the spring constant of the vibration, μ , the reduced mass, which is used when describing the system to reduce it from a two body problem to a one body problem.

Since rotational and vibrational energy levels are usually expressed in terms of wavenumber, we can convert the above to wavenumber by dividing by hc , where h is Planck's constant and c is the speed of light. This gives us the formula:

$$G(\nu) = \frac{E_\nu}{hc} = \left(\nu + \frac{1}{2} \right) \frac{\omega}{2\pi c} \quad (3)$$

Now consider the $\frac{\omega}{2\pi c}$ term.

$$\frac{\omega}{2\pi c} = \frac{2\pi f}{2\pi c} \quad (4)$$

$$= \frac{f}{c} \quad (5)$$

$$= \frac{1}{\lambda} = \tilde{\nu} \quad (6)$$

where $\tilde{\nu}$ is the wavenumber, expressed in m^{-1} .

We can now write the energy levels in wavenumbers as:

$$G(\nu) = \left(\nu + \frac{1}{2} \right) \tilde{\nu} \quad (7)$$

Unfortunately, the harmonic oscillator model is not a good approximation for larger vibrations. This is because the potential does not account for the fact that there is a finite energy D_e which is the depth of the well. This is accounted for by the Morse potential [4], which is given by:

$$V(r) = D_e \left(1 - e^{-\beta(r-r_e)} \right)^2 \quad (8)$$

where r is the internuclear distance, r_e is the equilibrium internuclear distance and β is a constant defined by $\beta = \sqrt{\frac{k}{2D_e}}$. We can then write $\tilde{\nu}$ in terms of β and D_e as:

$$\tilde{\nu} = \frac{\beta}{c} \sqrt{\frac{D_e}{2\pi^2\mu}} \quad (9)$$

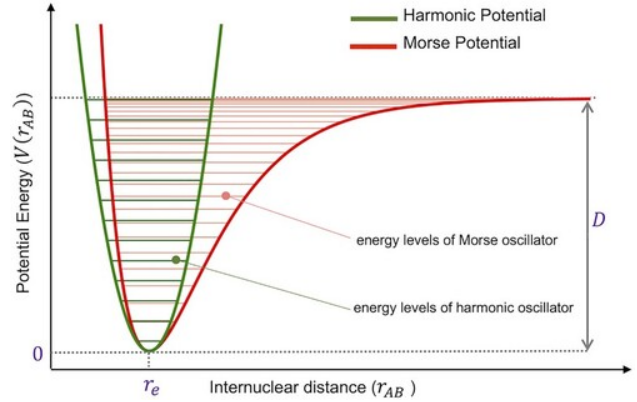


Figure 2: A diagram of the Morse Potential. [4]

Just as before, we solve the Schrodinger equation for the Morse potential [1] to find the energy levels, and convert to wavenumber.

$$G'(\nu) = \left(\nu + \frac{1}{2} \right) \tilde{\nu} - \left(\nu + \frac{1}{2} \right)^2 \tilde{\nu} x_e \quad (10)$$

where x_e is the anharmonicity constant.

$$x_e = \frac{\tilde{\nu}}{4D_e} \quad (11)$$

The Morse Potential also allows transitions of $\delta\nu = \pm p$ to occur, where p is an integer. These 'overtones' are not allowed in the harmonic oscillator model [2], and they occur because of the unequal spacing of energy levels in the anharmonic model.

2.1.2 Molecular Bonding

When molecules form, the atomic orbitals of the atoms involved combine to form molecular orbitals. These can be constructive or destructive, and the resulting molecular orbitals can be bonding or anti-bonding, respectively. The main difference between these is the fact that in anti-bonding orbitals, the electrons are less likely to be found in the region between the nuclei (exactly no likelihood at the nodal plane), and so the bond is weaker, as the electrons are more likely to be on opposite sides of the atoms, exerting a ‘pulling’ effect. This is not the case for bonding orbitals.

The bonding wavefunction is given by:

$$\psi_b = \frac{1}{\sqrt{2}}(\psi_1 + \psi_2) \quad (12)$$

and the anti-bonding wavefunction is given by:

$$\psi_{ab} = \frac{1}{\sqrt{2}}(\psi_1 - \psi_2) \quad (13)$$

where ψ_1 and ψ_2 are the atomic orbitals of the atoms involved (Identical for homonuclear diatomic molecules).

One section of this experiment concerns the emission spectrum of an N_2 molecule. The N_2 molecule has a triple bond, and so the molecular orbitals are formed from the $2s$ and $2p$ orbitals of the nitrogen atoms. As can be seen in figure 3, the $C^3\Pi_u$ and $B^3\Pi_g$ orbitals are the 3rd and 2nd energy orbitals, respectively (from 0th), where Π refers to the type of orbitals superimposed, and the u, g refer to ungerade and gerade. Molecular orbitals with the g subscript are bonding orbitals (symmetric), while those with the u subscript are anti-bonding orbitals (antisymmetric). The $C^3\Pi_u$ orbital corresponds to the anti-bonding orbitals of the $2p$ orbitals, while the $B^3\Pi_g$ corresponds to the bonding orbitals. It is clear then that the $C^3\Pi_u$ orbitals are higher in energy than the $B^3\Pi_g$ orbitals, due to their asymmetry. It also clearly portrays the instability of the anti-bonding orbitals, as the $C^3\Pi_u$ curve has a markedly shallower potential well than $B^3\Pi_g$.

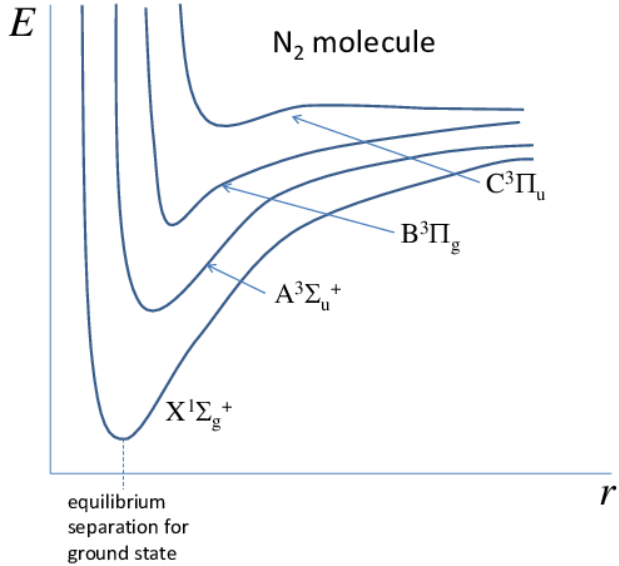


Figure 3: The molecular orbitals of an N_2 molecule. We are mainly concerned with $C^3\Pi_u$ and $B^3\Pi_g$ in this experiment. [6]

2.1.3 Vibronic Transitions, Franck-Condon Factors

We know already that $\Delta n = \pm 1$ for electronic transitions, where n is the electronic quantum number. For vibrational transitions, this is not the case. The Franck-Condon principle states that an electronic transition is most likely to occur without changes in the positions of the nuclei in the molecular entity and its environment (vibrational, external motion)(Figure 4). The quantum mechanical formulation of this principle is that the intensity of a vibronic transition is proportional to the square of the overlap integral between the vibrational wavefunctions of the two states that are involved in the transition.

$$P_{mn} = |\langle \psi_{xm} | \mu | \psi_{yn} \rangle|^2 \propto \left| \int \psi_{xm}^*(r) \psi_{yn}(r) dr \right|^2 \quad (14)$$

Where P_{mn} , the Franck-Condon factor, is the probability of a transition from the m th vibrational state of the initial electronic state to the n th vibrational state of the adjacent final electronic state, ψ_{xm} is the wavefunction of the m th vibrational level in the x th electronic level, ψ_{yn} is the wavefunction of the n th vibrational level in the y th electronic level, and μ is the transition dipole moment operator.

The assumption we make that the transitions are vertical is a good one, as the timescale of the electronic transition is at a maximum, a few femtoseconds, while the timescale of the nuclear motion is at a minimum, 10s to hundreds of femtoseconds, while molecular motion is in the timescale of nanoseconds or larger. This means that the nuclei are essentially stationary during the electronic transition.

A similar way to think about this is that electronic, atomic, and molecular frequencies of motion are to Gamma rays, X-rays, and visible light, respectively.

It is also important to describe our notation for each transition. For the N_2 molecule, we are working with transitions between the $B^3\Pi_g$ and $C^3\Pi_u$ orbitals. We denote each transition as $i - j$, where i is the initial vibrational level in the $C^3\Pi_u$ orbital, and j is the final vibrational level in the $B^3\Pi_g$ orbital.

2.2 Energy of Vibronic Transitions

To predict the wavenumber of emitted spectral lines in vibronic transition, we must consider both the difference of energy between the two electronic states, and the difference in vibrational energy between the two states. By recognising, $\frac{\Delta E_{el}}{hc} = \tilde{\nu}_{el}$, where $\tilde{\nu}_{el}$ is the wavenumber of the emission due solely to the change in energy level, and subbing Eq. 7, we can write the energy of a vibronic transition as:

$$\tilde{\nu}_{\nu'\nu''} = \frac{\Delta E_{el}}{hc} + \left(\frac{E_{\nu'}}{hc} - \frac{E_{\nu''}}{hc} \right) \quad (15)$$

$$= \tilde{\nu}_{el} + \tilde{\nu}_C \left[\left(\nu' + \frac{1}{2} \right) - x_C \left(\nu' + \frac{1}{2} \right)^2 \right] - \tilde{\nu}_B \left[\left(\nu'' + \frac{1}{2} \right) - x_B \left(\nu'' + \frac{1}{2} \right)^2 \right] \quad (16)$$

where the subscript C refers to the initial electronic state, E_3 , and the subscript B refers to the final electronic state, E_2 .

We can then rearrange the equation to remove constant $\tilde{\nu}_{el}$, and write the equation in terms of the wavenumber of the 0 - 0 transition:

$$\tilde{\nu}_{\nu'\nu''} = \tilde{\nu}_{00} + \tilde{\nu}_C \nu' - \tilde{\nu}_B \nu'' - \tilde{\nu}_C x_C (\nu' + 1) \nu' + \tilde{\nu}_B x_B (\nu'' + 1) \nu'' \quad (17)$$

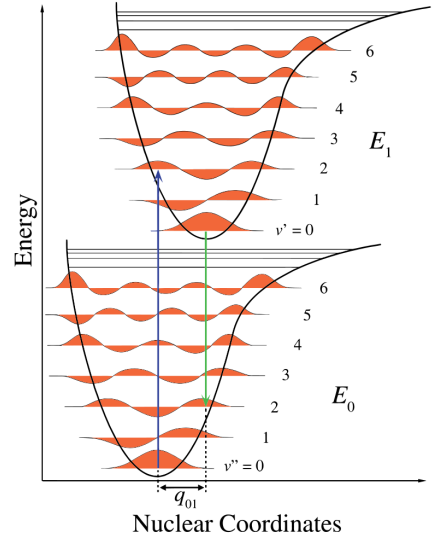


Figure 4: A diagram illustrating the Franck-Condon Principle. Since the transitions are assumed to be vertical, vibrational levels with minimal change in r are more likely to be involved in the transition. [10]

We then, after measuring sufficiently many wavenumbers of peaks, are left with a solvable system of equations, with 4 unknowns, $\tilde{\nu}_C$, $\tilde{\nu}_B$, x_C , and x_B .

$$\begin{pmatrix} 1 & 2 \\ 2 & 6 \end{pmatrix} \cdot \begin{pmatrix} \tilde{\nu}_B \\ -\tilde{\nu}_B x_B \end{pmatrix} = \begin{pmatrix} 1 & 1/\tilde{\nu}_{02} \\ 1 & 1/\tilde{\nu}_{01} \end{pmatrix} \cdot \begin{pmatrix} \tilde{\nu}_{00} \\ -\tilde{\nu}_{01}\tilde{\nu}_{02} \end{pmatrix} \quad (18)$$

$$\begin{pmatrix} 2 & 1 \\ 6 & 2 \end{pmatrix} \cdot \begin{pmatrix} \tilde{\nu}_C x_C \\ -\tilde{\nu}_C \end{pmatrix} = \begin{pmatrix} 1 & 1/\tilde{\nu}_{20} \\ 1 & 1/\tilde{\nu}_{10} \end{pmatrix} \cdot \begin{pmatrix} \tilde{\nu}_{00} \\ -\tilde{\nu}_{10}\tilde{\nu}_{20} \end{pmatrix} \quad (19)$$

This allows us to calculate one (or more) values of $\tilde{\nu}_C$, $\tilde{\nu}_B$, x_B , and x_C . It is easier for us to calculate the values of $\tilde{\nu}_C x_C$ and $\tilde{\nu}_B x_B$ instead of x_C and x_B separately, as we can then calculate the dissociation energy of the molecule, D_0 , using the formula:

$$\frac{D_0}{hc} = \sum \frac{E_{\nu''}}{hc} \quad (20)$$

Where $E_{\nu''}$ is the increase in energy of the vibrational level ν'' , and the sum is over all vibrational levels.

Since

$$E_{\nu''} = \tilde{\nu}_{0\nu''} - \tilde{\nu}_{0(\nu''+1)} \quad (21)$$

we can estimate all the values of $E_{\nu''}$ and sum them to find D_0 .

3 Methodology

The general steps we took to setup for the procedure were first to ensure the spectrometer was connected to the computer, before turning on the computer and opening the software. We then carefully put the fibre optic cable corresponding to the spectrometer of lower threshold into the higher clamp, used for observation.

3.1 Calibration

The first section of the procedure was the calibration of the spectrometers, which involved placing the calibration lamp (Mercury) directly facing the optical fibre (and wall).

We varied the parameters of the sample, which were the integration time, the scans to average, the bin width, and correction for dark current, and noted the affects of varying each. We then tried to optimise our parameters for a low error, low noise sample. This involved keeping our integration time so that the maximum lied under the saturation point, since increasing the sample size reduces the effect of the noise, relative to the size of the sample. We also tried to do this while keeping a large number of scans to average, keeping bin widths small, and keeping electrical dark correction on.

It followed only to capture the emission spectrum of mercury using the Flame-T spectrometer (lower threshold, 300 – 510nm), swapped the optical fibres, and then captured the emission spectrum using the Flame-S spectrometer (higher threshold, 350 – 850nm).

We then use these spectrums to calibrate the spectrometers, by finding the peaks of the mercury spectrums using the code specified, and comparing them to the literature values. The optical resolution, resolving power of the spectrometers are found, and compared to expected values.

3.2 Emission Spectrum of N_2

The second part of the experiment was to capture the emission spectrum of N_2 using the Flame-T spectrometer. This involved the use of an N_2 lamp, which was placed facing the wall, with the fibre optic cable mounted in the front panel of the lamp, due to the UV light emitted by the lamp.

The spectrum is optimised, and captured two spectra, one for observing the large peak behaviour, and one for observing the smaller peaks. The peaks are then fitted with Lorentzian functions, and the wavenumbers of the peaks are calculated.

The wavenumbers are then used to calculate the values of $\tilde{\nu}_B$, $\tilde{\nu}_B x_B$, $\tilde{\nu}_C$, and $\tilde{\nu}_C x_C$, and the transition wavenumbers, and their differences for a fixed ν' , are put into a DesLandres table.

These differences are fitted for a linear function, and the by calculating the x -intercept, we can find the dissociation energy of the molecule.

4 Results

4.1 Calibration

The results of the first part of the procedure, section 3.1, were threefold. First we observed the effect of changing the collection parameters on the emission spectrum, and noted the value of saturation of the spectrometer. Secondly, after capturing the mercury emission spectrum, we estimated the optical resolution as the average of the full-width half-maximums of the Gaussian fits of our single peaks. Finally, we compared the centres of the Gaussian fits to the literature values of the strong lines of the mercury spectrum.

We begin with the first results, the effect of changing the collection parameters on the emission spectrum.

Integration Time (ms)	Scans to Average	Bin Width (nm)	Dark Correction
Increase: Larger count, reducing sample error of count, relative effect of noise.	Increase: Reduced fluctuation, which is due to standard error of the mean, and so reduced count error.	Increase: Smoother spectrum, potential loss of data, and increase of error.	On Shifts counts down by value caused by electric dark current(11).
Decrease: Smaller count and increased error of count, significantly affects appearance of smaller peaks.	Decrease: Increases fluctuation, and thus count error, but reduces time of collection.	Decrease: More detailed spectrum, but increased effects of noise.	Off No correction for electric dark current, causing upward shift of counts.
Definitions: Keyword 8	Keyword 9	Keyword 10	Keyword 11

These results were then used in the optimisation of each spectrum collected.

The value at which the count data saturated (with electric dark off) was exactly 65,535 counts as can be seen in figure 5. This value allows us to deduce the amount of bits the ADC (Keyword 14) has, since the total number of counts it can encode per wavelength is expected to be 2^s , where s is the number of bits. Since we expect the ADC to have 12, 14 or 16 bits, we evaluated the saturation value for these, and found $2^{16} = 65536$, which, including 0 is the total number of possible values of counts (since electric dark off, no negative, non-integer values per scan).

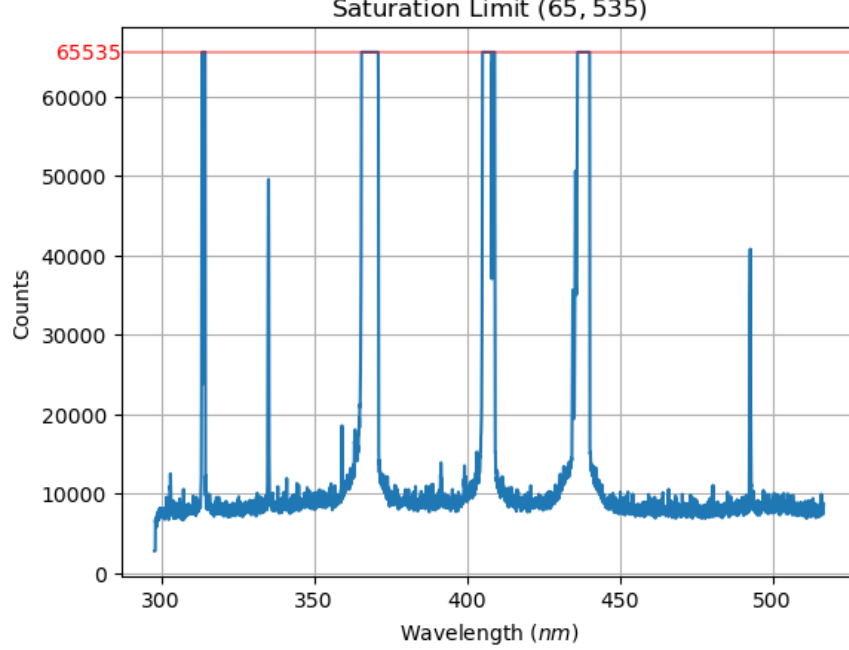


Figure 5: The saturation limit of the spectrometer at 65535 counts, as read from the data, visualised.

After capturing the mercury emission spectrum, we found the peaks of the spectrum using the code provided in section 6.2, and compared the centres of the Gaussian fits to the literature values. The error takes into account both the spread of the peaks and the accuracy of the fit.

Expected [7] (nm)	Measured FLM-T (nm)	Expected-Measured FLMT (nm)	Measured FLM-S (nm)	Expected-Measured FLMS (nm)
312.567	314.043 ± 0.147	1.476 ± 0.147	-	-
334.148	335.073 ± 0.144	0.925 ± 0.144	-	-
365.015	365.949 ± 0.185	0.935 ± 0.185	-	-
366.328	367.228 ± 0.174	0.900 ± 0.174	370.264 ± 0.617	3.936 ± 0.617
404.656	405.456 ± 0.166	0.800 ± 0.166	409.766 ± 0.474	5.110 ± 0.474
407.750	408.571 ± 0.174	0.821 ± 0.174	412.831 ± 0.828	5.081 ± 0.828
435.833	436.549 ± 0.160	0.716 ± 0.160	440.884 ± 0.589	5.051 ± 0.589
546.075	-	-	550.526 ± 0.882	4.451 ± 0.882
576.961	-	-	581.127 ± 0.746	4.166 ± 0.746
579.067	-	-	582.873 ± 0.965	3.806 ± 0.965

If we assume that the offset is constant, we can take the average of the differences, and add this to any measured spectrum to get the corrected spectrum. These offsets are $(0.939 \pm 0.0623)nm$ and $(4.514 \pm 0.282)nm$ for the Flame-T and Flame-S spectrometers, where the error is propagated through the averaging by adding in quadrature, and dividing by sample size.

The optical resolution we found using the same fits, since it is related to the standard deviation of the Gaussian fits by

$$FWHM = 2\sqrt{2\ln(2)}\sigma \quad (22)$$

This then allows to find a value for each peak.

Expected	FWHM (nm) - Optical Resolution		Resolving Power	
	FLAME-T	FLAME-S	FLAME-T	FLAME-S
312.155	0.335 ± 0.016	-	931.806 ± 44.504	-
334.148	0.328 ± 0.017	-	1018.744 ± 52.801	-
365.015	0.391 ± 0.018	-	933.542 ± 42.98	-
366.328	0.391 ± 0.012	1.432 ± 0.122	936.900 ± 28.75	255.815 ± 21.794
404.656	0.387 ± 0.012	1.116 ± 0.027	1045.622 ± 32.422	362.595 ± 8.772
407.750	0.421 ± 0.015	1.592 ± 0.134	968.527 ± 34.5	256.124 ± 21.56
435.833	0.372 ± 0.015	1.384 ± 0.036	1171.594 ± 47.242	314.908 ± 8.19
546.075	-	2.013 ± 0.235	-	271.274 ± 31.669
576.961	-	1.741 ± 0.249	-	331.396 ± 47.397
579.067	-	2.258 ± 0.317	-	256.451 ± 36.003

This resolution data gives us two plot, against which we fit linear functions.

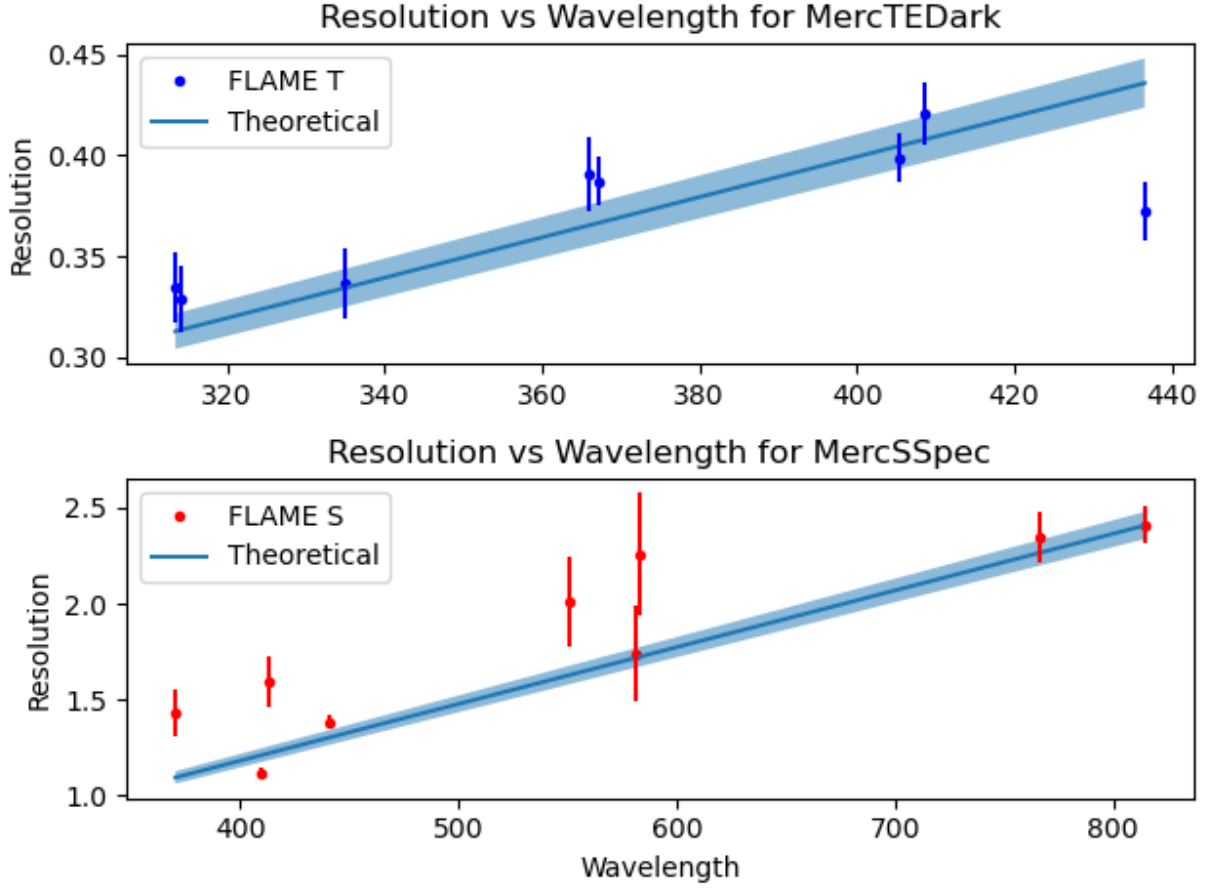


Figure 6: The optical resolution of the Flame-T and Flame-S spectrometers, with a linear fit and 95% confidence intervals.

This fit gives us a value of $(9.9811 \pm 0.1395)10^{-4}$ for the slope of the FLAME-T spectrometer fit, and 2.9554 ± 0.0436 for the FLAME-S spectrometer, which are $\frac{1}{R_T}$, $\frac{1}{R_S}$, where $R_T = 1001.894 \pm 14.007$, $R_S =$

338.359 ± 4.993 . This are both well within reasonable proximity of our estimated values above.

4.2 Emission Spectrum of N_2

The results of the second part of the procedure, the emission spectrum of N_2 , beginning first with the fitting and labelling of the peaks of the spectrum, with the use of some literature values [3].

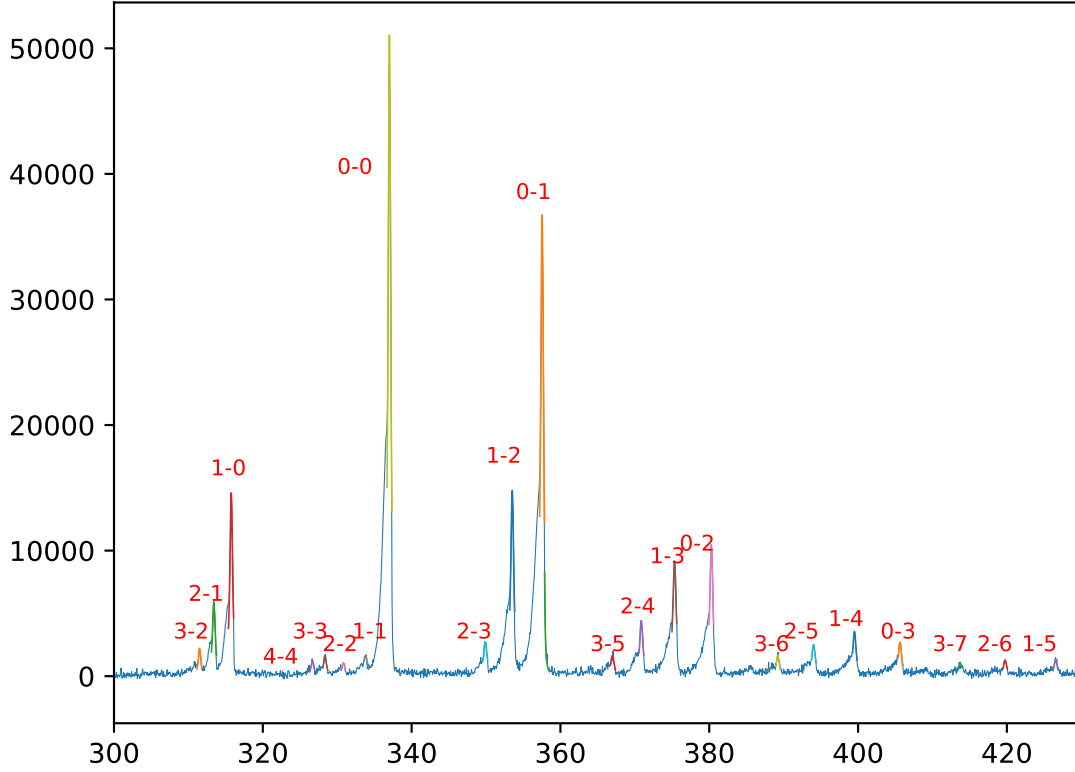


Figure 7: The emission spectrum of N_2 with Lorentzian fits on each peak.

we then used the data to calculate the wavenumbers of the peaks which we then used to calculate the values of $\tilde{\nu}_B = (1.73 \pm 0.05) \cdot 10^{-7} m^{-1}$ and $\tilde{\nu}_B x_B = (1.5 \pm 0.8) \cdot 10^{-9} m^{-1}$, however since the $2-0$ transition (and all $n-0, n \geq 2$) is too high energy, the values of $\tilde{\nu}_C, \tilde{\nu}_C x_C$ cannot be calculated in the same fashion. Instead we fill some values we know into Eq. 17. This gives us values $\tilde{\nu}_C = (2.03 \pm 0.12) \cdot 10^{-7} m^{-1}, \tilde{\nu}_C x_C = (4 \pm 3) \cdot 10^{-9} m^{-1}$

We then put the transition wavenumbers into a DesLandres table.

ν'/ν''	0 ± 0.002	$\Delta\tilde{\nu}_1$ ± 0.003	1 ± 0.002	$\Delta\tilde{\nu}_2$ ± 0.003	2 ± 0.002	$\Delta\tilde{\nu}_3$ ± 0.003	3 ± 0.002	$\Delta\tilde{\nu}_4$ ± 0.003	4 ± 0.002	$\Delta\tilde{\nu}_5$ ± 0.003	5 ± 0.002	$\Delta\tilde{\nu}_6$ ± 0.003	6 ± 0.002
0	2.967	0.170	2.797	0.167	2.630	0.165	2.465	-	-	-	-	-	-
1	3.167	0.171	2.996	0.167	2.829	0.165	2.664	0.165	2.503	0.159	2.344	-	-
2	-	-	3.191	0.168	3.023	0.165	2.858	0.162	2.696	0.158	2.538	0.156	2.382
etc.													

We then graph our $\Delta\tilde{\nu}_n$, the values against the corresponding values of ν'' , and fit a linear function to the data.

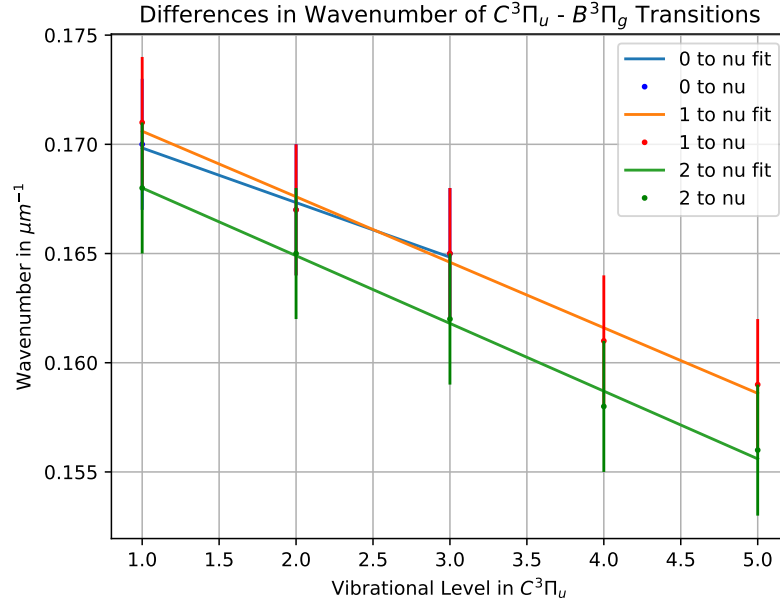


Figure 8: The difference in the wavenumber of successive transitions, equaling the energy increases of rotational levels of $B^3\Pi_g$ orbital (Eq. 21).

since the x -intercept ($x = 69$ for $\nu' = 0$) is the 'maximum' value of ν'' , we can find the dissociation energy of the molecule by summing over as in Eq. 20, and dividing by hc . This gives us a value of $D_0 = (7.264 \pm 0.899)eV$.

While the data for a procedure regarding the absorption spectrum of I_2 was collected, it was not analysed in this report due to time constraints.

5 Discussion

While much of the topics of interest in this experiment were in the uncompleted section, we can still discuss the results of the completed sections.

The calibration of the spectrometers was successful, with the FLAME-T spectrometer found to have an offset of 0.939 ± 0.0623 nm, and the FLAME-S spectrometer found to have an offset of 4.514 ± 0.282 nm. The chromatic resolving power of the spectrometers was found to be $R_T = 1001.894 \pm 14.007$, $R_S = 338.359 \pm 4.993$. These values could be useful in the event of another experiment, as they are not something

that changes much with time.

The emission spectrum of N_2 yielded some solid results, in the values of wavenumbers of relevant vibronic transitions, and the dissociation energy, D_0 of the molecule. However if the experiment was to be repeated, the use of a spectrometer able to catch lower wavelengths would be useful, as many of the transitions were too high energy to be measured.

6 Appendix

6.1 Keywords, Mathematical Preliminaries

6.1.1 Keywords

1. **Vibronic Transition:** A transition between vibrational and electronic energy levels.
2. **Franck-Condon Principle:** The principle that states that an electronic transition is most likely to occur without changes in the positions of the nuclei in the molecular entity and its environment (vibrational, external motion) [5].
3. **Morse Potential:** A potential used to describe the energy levels of a molecule, which accounts for the finite energy D_e which is the depth of the well.
4. **Molecular Orbital:** An orbital formed from the combination of atomic orbitals of the atoms involved in the molecule.
5. **Optical Resolution:** Defined as the ability of an optical instrument to distinguish between two objects that are close together. In spectroscopy, we take it to be the full width at half maximum of the peaks.
6. **Resolving Power:** Defined as the ability of an optical instrument to distinguish between two wavelengths that are close together. In spectroscopy, we take it to be the ratio of the wavelength of the peak to the smallest resolvable difference in wavelengths.
7. **Wavenumber:** The reciprocal of the wavelength of a wave, expressed in m^{-1} .
8. **Integration Time:** The time taken to measure the sample.
9. **Scans to Average:** The number of scans taken to average the sample.
10. **Bin Width:** The width of the bins used to measure the sample.
11. **Dark Current:** The current that flows through the spectrometer when no light is incident on the detector.
12. **Dissociation Energy:** The energy required to break a bond in a molecule.
13. **Anharmonicity Constant:** A constant that describes the deviation of a potential from the harmonic oscillator model.
14. **ADC:** Analogue to Digital converter, which converts continuous-time, continuous amplitude, voltage input to discrete-time, discrete-amplitude digital output [9].

6.1.2 Mathematical Preliminaries

1. **Gaussian Distribution:** A continuous probability distribution described by the formula:

$$g(x) = Ae^{-\frac{(x-x_0)^2}{2\sigma^2}} \quad (23)$$

where A is the amplitude, x_0 is the mean, and σ is the standard deviation.

6.2 Code

All code used in this experiment can be found at <https://github.com/DavidLawton04/MuchStuff/tree/a66c3f8d47b7b2ac18273ab8eca6349f52667f22/Junior%20Sophister/JS%20Labs/Molecular%20Spectroscopy>

References

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