Algolab (index.html#Chapters)

Out [2]: Chapter 3: Data Structures

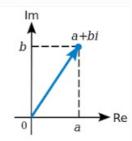
Chapter 3: Data Structures

class ComplexNumber

See theory here: http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (First slides until class Fraction)

Let's try to define a complex number:

A **complex number** is a **number** that can be expressed in the form a + bi, where a and b are real **numbers** and i is the imaginary unit which satisfies the equation $i^2 = -1$. In this expression, a is the real part and b is the imaginary part of the **complex number**.



Complex number - Wikipedia https://en.wikipedia.org/wiki/Complex number

As the Fraction class, the ComplexNumber holds two values, in this case one for the *real* part and one for the *imaginary* one.

- Note each method takes as first import self argument. self will always be a reference to the object itself, and allows accessing its fields and methods
- self is not a keyword of Python, you could use any name you want for the first parameter, but it is much better to follow conventions and stick using self!
- Methods beginning and ending with double underscore '__' have often special meaning in Python: if you see such a method around, it means it is overriding some default behaviour of Python

In [3]:

```
import unittest
import math
class ComplexNumber:
          init (self, real, imaginary):
        """ In\overline{\text{it}} ializes the complex number with real and imaginary part """
        self.real = real
        self.imaginary = imaginary
    def magnitude(self):
        """ Returns a float which is the magnitude (that is, the absolute value) of
the complex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        return math.sqrt(self.real**2 + self.imaginary**2)
          str (self):
        """ Returns a string representation of the object, overriding default Python
behaviour. """
        return str(self.real) + " + " + str(self.imaginary) + "i"
```

```
class ComplexNumberTest(unittest.TestCase):
    """ Test cases for ComplexNumber
         Note this is a *completely* separated class from ComplexNumber and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         ComplexNumber methods!
    11 11 11
    def test init(self):
        self.assertEqual(ComplexNumber(1,2).real, 1)
        self.assertEqual(ComplexNumber(1,2).imaginary, 2)
    def test magnitude(self):
             Notice we can't use assertEqual, as the result of magnitude() is a
             float number which may have floating point rounding errors. So it's
             necessary to use assertAlmostEqual
             As an option with the delta you can declare the precision you require.
             For more info see Python docs:
             https://docs.python.org/2/library/unittest.html#unittest.TestCase.assert
AlmostEqual
             NOTE: assertEqual might still work on your machine but just DO NOT use i
t
             for float numbers!!!
        11 11 11
        # self.assertEqual(ComplexNumber(3.0.4.0).magnitude().5)
        self.assertAlmostEqual(ComplexNumber(3.0,4.0).magnitude(),5, delta=0.001)
    def test str(self):
        self.assertEqual(str(ComplexNumber(1,2)), "1 + 2i")
        #self.assertEqual(str(ComplexNumber(1,0)), "1")
        #self.assertEqual(str(ComplexNumber(1.0,0)), "1.0")
        #self.assertEqual(str(ComplexNumber(0,1)), "i")
#self.assertEqual(str(ComplexNumber(0,0)), "0")
In [4]:
algolab.run(ComplexNumberTest)
. . .
Ran 3 tests in 0.007s
0K
Once the init method is defined, we can create a ComplexNumber with a call like 'ComplexNumber(3,5)'
Notice in the constructor call we do not pass anything as self parameter (after all, we are creating the object)
In [5]:
my complex = ComplexNumber(3,5)
```

We can now try to use one of the methods we defined:

```
In [6]:
```

```
mag = my_complex.magnitude()
print mag
```

5.83095189485

We can also pretty print the whole complex number. Internally, print function will look if the ComplexNumber has defined an $_str_$ method. If so, it will pass to the method the instance my_complex as the first argument, which in our methods will end up in the self parameter:

In [7]:

```
print my_complex
```

3 + 5i

Ok, now we are ready to define our own stuff.

Complex numbers equality

Equality [edit]

Two complex numbers are equal if and only if both their real and imaginary parts are equal. In symbols:

$$z_1=z_2 \; \leftrightarrow \; (\operatorname{Re}(z_1)=\operatorname{Re}(z_2) \, \wedge \, \operatorname{Im}(z_1)=\operatorname{Im}(z_2)).$$

Here we will try to give you a glimpse of some aspectes related to Python equality, and trying to respect interfaces when overriding methods. Equality can be a nasty subject, here we will treat it in a simplified form.

 Can you try to implement equality for ComplexNumber more or less as it was done for Fraction in theory slides?

use

```
def __eq__(self, other):
```

and write some tests as well!

- Beware 'equality' is tricky in Python for float numbers! Rule of thumb: when overriding __eq__, use 'dumb' equality, two things are the same only if their parts are literally equal
- If instead you need to determine if two objects are similar, define other 'closeness' functions.
- (Non mandatory read) if you are interested in the gory details of equality, see
 - How to Override comparison operators in Python (http://jcalderone.livejournal.com/32837.html)
 - Messing with hashing (http://www.asmeurer.com/blog/posts/what-happens-when-you-mess-with-hashing-in-python/)

Use this simple test case to check for equality:

Complex numbers addition

Complex numbers are added by separately adding the real and imaginary parts of the summands.

That is to say:

$$(a+bi) + (c+di) = (a+c) + (b+d)i.$$

Similarly, subtraction is defined by

$$(a+bi) - (c+di) = (a-c) + (b-d)i.$$

- Can you try to implement addition for ComplexNumber more or less as it was done for Fraction in theory slides? Write some tests as well!
- a and c correspond to real, b and d correspond to imaginary

use

```
def add (self, other):
```

In [8]:

```
import unittest

class ComplexNumberTest(unittest.TestCase):
    def test_add(self):
        assertEquals(ComplexNumber(1,2) + ComplexNumber(3,4), ComplexNumber(3,6));
```

Adding a scalar

We defined addition among ComplexNumbers, but what about addition among a ComplexNumber and an int or a float?

Will this work?

ComplexNumber(3,4) + 5

What about this?

ComplexNumber(3,4) + 5.0

Try to add the following method to your class, and check if it does work with the scalar:

In [9]:

```
def __add__(self, other):
    # checks other object is instance of the class ComplexNumber
    if isinstance(other, ComplexNumber):
        return ComplexNumber(self.real + other.real,self.imaginary + other.imaginary)

# else checks the basic type of other is int or float
    elif type(other) is int or type(other) is float:
        return ComplexNumber(self.real + other, self.imaginary)

# other is of some type we don't know how to process.
# In this case the Python specs say we MUST return 'NotImplemented'
    else:
        return NotImplemented
```

Hopefully now you have a better add. But what about this? Will this work?

```
5 + ComplexNumber(3,4)
```

Answer: it won't, Python needs further instructions. Usually Python tries to see if the class of the object on left of the expression defines addition for operands to the right of it. In this case on the left we have a float number, and float numbers don't define any way to deal to the right with your very own ComplexNumber class. So as a last resort Python tries to see if your ComplexNumber class has defined also a way to deal with operands to the left of the ComplexNumber, by looking for the method __radd__, which means reverse addition. Here we implement it

```
def __radd__(self, other):
    """ Returns the result of expressions like other + self
    if (type(other) is int or type(other) is float):
        return ComplexNumber(self.real + other, self.imaginary)
    else:
        return NotImplemented
```

To check it is working and everything is in order for addition, add these test cases:

Multiplication and division [edit]

The multiplication of two complex numbers is defined by the following formula:

$$(a+bi)(c+di) = (ac-bd) + (bc+ad)i.$$

In particular, the square of the imaginary unit is -1:

$$i^2 = i \times i = -1$$
.

- Can you try to implement multiplication for ComplexNumber more or less as it was done for Fraction in theory slides?
- Can you extend multiplication to wor with scalars (both left and right) as well?

```
use
```

Solutions

ComplexNumber Solution

```
In [10]:
```

```
import unittest

class ComplexNumber:

def __init__(self, real, imaginary):
    self.real = real
    self.imaginary = imaginary

def __str__(self):
    return str(self.real) + " + " + str(self.imaginary) + "i"

def __eq__(self, other):
    return self.real == other.real and self.imaginary == other.imaginary

def __add__(self, other):
    if isinstance(other, ComplexNumber):
        return ComplexNumber(self real + other real self imaginary + other imaginary)
```

```
TELUTH COMPLEXIVATION (SELT. LEGI + OTHER LEGIC, SELT. LINGYLIGITY + OTHER LINGYL
nary)
        elif type(other) is int or type(other) is float:
            return ComplexNumber(self.real + other, self.imaginary)
        else:
            return NotImplemented
         radd (self, other):
        if (type(other) is int or type(other) is float):
            return ComplexNumber(self.real + other, self.imaginary)
        else:
            return NotImplemented
    def mul (self, other):
        if isinstance(other, ComplexNumber):
            return ComplexNumber(self.real * other.real - self.imaginary * other.ima
ginary,
                                  self.imaginary * other.real + self.real * other.ima
ginary)
        elif type(other) is int or type(other) is float:
            return ComplexNumber(self.real * other, self.imaginary * other)
        else:
            return NotImplemented
    def __rmul__(self, other):
        \overline{if} (type(other) is int or type(other) is float):
            return ComplexNumber(self.real * other, self.imaginary * other)
        else:
            return NotImplemented
class ComplexNumberTest(unittest.TestCase):
    def test integer equality(self):
            Note all other tests depend on this test!
            We want also to test the constructor, so in c we set stuff by hand
        c = ComplexNumber(0,0)
        c.real = 1
        c.imaginary = 2
        self.assertEquals(c, ComplexNumber(1,2))
    def test add zero(self):
        self.assertEquals(ComplexNumber(1,2) + ComplexNumber(0,0), ComplexNumber(1,2)
));
    def test add numbers(self):
        self.assertEquals(ComplexNumber(1,2) + ComplexNumber(3,4), ComplexNumber(4,6
));
    def test add scalar right(self):
        self.assertEquals(ComplexNumber(1,2) + 3, ComplexNumber(4,2));
    def test add scalar left(self):
        self.assertEquals(3 + ComplexNumber(1,2), ComplexNumber(4,2));
    def test add negative(self):
        self.assertEquals(ComplexNumber(-1,0) + ComplexNumber(0,-1), ComplexNumber(-
1,-1));
```

```
def test mul by zero(self):
        self.assertEquals(ComplexNumber(0,0) * ComplexNumber(1,2), ComplexNumber(0,0)
));
   def test mul just real(self):
        self.assertEquals(ComplexNumber(1,0) * ComplexNumber(2,0), ComplexNumber(2,0)
));
    def test mul just imaginary(self):
        self.assertEquals(ComplexNumber(0,1) * ComplexNumber(0,2), ComplexNumber(-2,
0));
   def test mul scalar right(self):
        self.assertEquals(ComplexNumber(1,2) * 3, ComplexNumber(3,6));
    def test mul scalar left(self):
        self.assertEquals(3 * ComplexNumber(1,2), ComplexNumber(3,6));
```

In [11]:

```
algolab.run(ComplexNumberTest)
Ran 11 tests in 0.022s
```

0K