Algolab (lildex html#Chapters)

Chapter 2: Data Structures

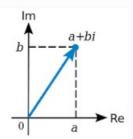
Chapter 2: Data Structures

class ComplexNumber

See theory here: http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/) strutture.pdf) (First slides until class Fraction)

Let's try to define a complex number:

A complex number is a number that can be expressed in the form a + bi, where a and b are real numbers and i is the imaginary unit which satisfies the equation $i^2 = -1$. In this expression, a is the real part and b is the imaginary part of the complex number.



Complex number - Wikipedia https://en.wikipedia.org/wiki/Complex number

As the Fraction class, the ComplexNumber holds two values, in this case one for the real part and one for the imaginary one.

- Note each method takes as first import self argument. self will always be a reference to the object itself, and allows accessing its fields and methods
- self is not a keyword of Python, you could use any name you want for the first parameter, but it is much better to follow conventions and stick using self!
- Methods beginning and ending with double underscore '__' have often special meaning in Python: if you see such a method around, it means it is overriding some default behaviour of Python

```
In [2]:
import unittest
import math
class ComplexNumber:
    def init (self, real, imaginary):
        self.real = real
        self.imaginary = imaginary
    def phase(self):
        """ Returns a float which is the phase (that is, the vector angle) of the co
mplex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        return math.atan2(self.imaginary, self.real)
    def log(self, base):
           Returns another ComplexNumber which is the logarithm of this complex num
ber
            This method is something we introduce by ourselves, according to the def
inition:
            (accomodated for generic base b)
            https://en.wikipedia.org/wiki/Complex number#Natural logarithm
```

```
return ComplexNumber(math.log(self.real) / math.log(base), self.phase() / ma
th.log(base))
    def str (self):
        return str(self.real) + " + " + str(self.imaginary) + "i"
class ComplexNumberTest(unittest.TestCase):
    """ Test cases for ComplexNumber
         Note this is a *completely* separated class from ComplexNumber and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         ComplexNumber methods!
    .....
    def test init(self):
        self.assertEqual(ComplexNumber(1,2).real, 1)
        self.assertEqual(ComplexNumber(1,2).imaginary, 2)
    def test phase(self):
            NOTE: we can't use assertEqual, as the result of phase() is a
            float number which may have floating point rounding errors. So it's
            necessary to use assertAlmostEqual
            As an option with the delta you can declare the precision you require.
            For more info see Pvthon docs:
            https://docs.python.org/2/library/unittest.html#unittest.TestCase.assert
AlmostEqual
            NOTE: assertEqual might still work on your machine but just DO NOT use i
t
            for float numbers!!!
        self.assertAlmostEqual(ComplexNumber(0.0,1.0).phase(), math.pi / 2, delta=0.
001)
    def test str(self):
        self.assertEqual(str(ComplexNumber(1,2)), "1 + 2i")
        #self.assertEqual(str(ComplexNumber(1,0)), "1")
        #self.assertEqual(str(ComplexNumber(1.0,0)), "1.0")
        #self.assertEqual(str(ComplexNumber(0,1)), "i")
        #self.assertEqual(str(ComplexNumber(0,0)), "0")
    def test log(self):
        c = \overline{ComplexNumber(1.0, 1.0)}
        l = c.log(math.e)
        self.assertAlmostEqual(l.real, 0.0, delta=0.001)
        self.assertAlmostEqual(l.imaginary, c.phase(), delta=0.001)
In [3]:
```

```
algolab.run(ComplexNumberTest)
```

```
....
Ran 4 tests in 0.030s
```

Once the init method is defined, we can create a ComplexNumber with a call like 'ComplexNumber(3,5)'

Notice in the constructor call we do not pass anything as self parameter (after all, we are creating the object)

In [4]:

```
my_complex = ComplexNumber(3,5)
```

We can now try to use one of the methods we defined:

In [5]:

```
phase = my_complex.phase()
print phase
```

1.03037682652

We can also pretty print the whole complex number. Internally, print function will look if the ComplexNumber has defined an __str__ method. If so, it will pass to the method the instance my_complex as the first argument, which in our methods will end up in the self parameter:

In [6]:

```
print my_complex
```

3 + 5i

We can also call methods that require a parameter like log(base). Notice that log function returns a ComplexNumber, and Python will automatically pretty print it for us.

In [7]:

```
logarithm = my_complex.log(math.e)
print logarithm
```

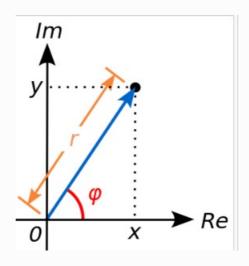
1.09861228867 + 1.03037682652i

Ok, now we are ready to define our own stuff.

Complex numbers magnitude

The absolute value (or modulus or magnitude) of a complex number z = x + yi is

$$r = |z| = \sqrt{x^2 + y^2}.$$



Implement the magnitude method, using this signature:

Complex numbers equality

Here we will try to give you a glimpse of some aspects related to Python equality, and trying to respect interfaces when overriding methods. Equality can be a nasty subject, here we will treat it in a simplified form.

Equality [edit]

Two complex numbers are equal if and only if both their real and imaginary parts are equal. In symbols:

$$z_1=z_2 \ \leftrightarrow \ (\operatorname{Re}(z_1)=\operatorname{Re}(z_2) \ \wedge \ \operatorname{Im}(z_1)=\operatorname{Im}(z_2)).$$

• Implement equality for ComplexNumber more or less as it was done for Fraction

Use this method signature:

```
def eq (self, other):
```

and use this simple test case to check for equality:

- Beware 'equality' is tricky in Python for float numbers! Rule of thumb: when overriding __eq__, use 'dumb' equality, two things are the same only if their parts are literally equal
- If instead you need to determine if two objects are similar, define other 'closeness' functions.
- (Non mandatory read) if you are interested in the gory details of equality, see
 - How to Override comparison operators in Python (http://icalderone.livejournal.com/32837.html)
 - Messing with hashing (http://www.asmeurer.com/blog/posts/what-happens-when-you-mess-with-hashing-in-python/)

Complex numbers isclose

Complex numbers can be represented as vectors, so intuitively we can determine if a complex number is close to another by checking that the distance between its vector tip and the the other tip is less than a given delta. There are more precise ways to calculate it, but here we prefer keeping the example simple.

Given two complex numbers

$$z_1 = a + bi$$

and

$$z_2 = c + di$$

We can consider them as close if they satisfy this condition:

$$\sqrt{(a-c)^2 + (b-d)^2} < delta$$

• Implement the method, adding it to ComplexNumber class:

def isclose(self, c, delta):
 """ Returns True if the complex number is within a delta distance fro
m complex number c.

raise Exception("TODO Implement me!")

and add this test case to ComplexNumberTest class:

REMEMBER: Equality with __eq__ and closeness functions like isclose are very different things. Equality should check if two objects have the same memory address or, alternatively, if they contain the same things, while closeness functions should check if two objects are similar. You should never use functions like isclose inside __eq__ methods, unless you really know what you're doing.

Complex numbers addition

Complex numbers are added by separately adding the real and imaginary parts of the summands.

That is to say:

$$(a+bi) + (c+di) = (a+c) + (b+d)i.$$

Similarly, subtraction is defined by

$$(a+bi)-(c+di)=(a-c)+(b-d)i.$$

- a and c correspond to real, b and d correspond to imaginary
- implement addition for ComplexNumber more or less as it was done for Fraction in theory slides
- write some tests as well!

Use this definition:

```
def __add__(self, other):
    raise Exception("TODO implement me!")
```

And add this to the ComplexNumberTest class:

Adding a scalar

We defined addition among ComplexNumbers, but what about addition among a ComplexNumber and an int or a float?

Will this work?

ComplexNumber(3,4) + 5

What about this?

ComplexNumber(3,4) + 5.0

Try to add the following method to your class, and check if it does work with the scalar:

In [9]:

```
def __add__(self, other):
    # checks other object is instance of the class ComplexNumber
    if isinstance(other, ComplexNumber):
        return ComplexNumber(self.real + other.real, self.imaginary + other.imaginary)

# else checks the basic type of other is int or float
    elif type(other) is int or type(other) is float:
        return ComplexNumber(self.real + other, self.imaginary)

# other is of some type we don't know how to process.
# In this case the Python specs say we MUST return 'NotImplemented'
    else:
        return NotImplemented
```

Hopefully now you have a better add. But what about this? Will this work?

```
5 + ComplexNumber(3,4)
```

Answer: it won't, Python needs further instructions. Usually Python tries to see if the class of the object on left of the expression defines addition for operands to the right of it. In this case on the left we have a float number, and float numbers don't define any way to deal to the right with your very own ComplexNumber class. So as a last resort Python tries to see if your ComplexNumber class has defined also a way to deal with operands to the left of the ComplexNumber, by looking for the method __radd__, which means reverse addition. Here we implement it

```
def __radd__(self, other):
    """ Returns the result of expressions like other + self
    if (type(other) is int or type(other) is float):
        return ComplexNumber(self.real + other, self.imaginary)
    else:
        return NotImplemented
```

To check it is working and everything is in order for addition, add these test cases:

Multiplication and division [edit]

The multiplication of two complex numbers is defined by the following formula:

$$(a+bi)(c+di) = (ac-bd) + (bc+ad)i.$$

In particular, the square of the imaginary unit is -1:

$$i^2 = i \times i = -1$$
.

- Implement multiplication for ComplexNumber, taking inspiration from previous add implementation
- Can you extend multiplication to work with scalars (both left and right) as well?

To implement mul , copy this definition into ComplexNumber class:

```
def __mul__(self, other):
    raise Exception("TODO Implement me!")
```

and add test cases to ComplexNumberTest class:

```
def test_mul_by_zero(self):
        self.assertEquals(ComplexNumber(0,0) * ComplexNumber(1,2), ComplexNum
ber(0,0));

    def test_mul_just_real(self):
        self.assertEquals(ComplexNumber(1,0) * ComplexNumber(2,0), ComplexNum
ber(2,0));

    def test_mul_just_imaginary(self):
        self.assertEquals(ComplexNumber(0,1) * ComplexNumber(0,2), ComplexNum
ber(-2,0));

    def test_mul_scalar_right(self):
        self.assertEquals(ComplexNumber(1,2) * 3, ComplexNumber(3,6));

    def test_mul_scalar_left(self):
        self.assertEquals(3 * ComplexNumber(1,2), ComplexNumber(3,6));
```

Stack

Stack theory

See theory here: http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (Slide 46)

See stack definition on the book

(http://interactivepython.org/runestone/static/pythonds/BasicDS/WhatisaStack.html)

and following sections:

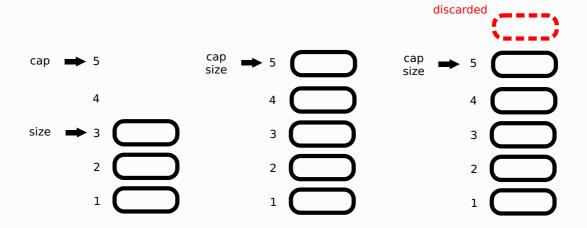
- Stack Abstract Data Type
 - (http://interactivepython.org/runestone/static/pythonds/BasicDS/TheStackAbstractDataType.html)
- Implementing a Stack in Python (http://interactivepython.org/runestone/static/pythonds/BasicDS/ImplementingaStackinPython.html)
- <u>Simple Balanced Parenthesis</u> (http://interactivepython.org/runestone/static/pythonds/BasicDS/SimpleBalancedParentheses.html)
- <u>Balanced Symbols a General Case</u> (http://interactivepython.org/runestone/static/pythonds/BasicDS/BalancedSymbols(AGeneralCase).html)

Stack exercises

On slide 46 of theory (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (Slide 46) there is the pseudo code for a version of stack we will call CappedStack:

```
STACK
ITEM[] A
                               % Elements
                                                 ITEM peek()
int size
                           % Current size
                                                    if size > 0 then
                         % Maximum size
                                                     | return A[size]
int cap
STACK Stack(int dim)
                                                 ITEM pop()
    Stack t \leftarrow \mathbf{new} Stack
                                                    if size > 0 then
    t.A \leftarrow \mathbf{new} \ \mathbf{int}[1 \dots dim]
                                                         ITEM t \leftarrow A[size]
    t.cap \leftarrow dim
                                                         size \leftarrow size - 1
    t.size \leftarrow 0
                                                        return t
   return t
                                                 push(ITEM v)
boolean isEmpty()
                                                    if size < cap then
  return size = 0
                                                         size \leftarrow size + 1
                                                         A[size] \leftarrow v
 int size()
   return size
```

A capped stack has a limit called *cap* over which elements are discarded:



- Copy the following skeleton and unit tests, and then implement the pseudo code
- Name internal variables that you don't want to expose to class users by prepending them with one
 underscore '_', like _elements or _cap.
 - The underscore is just a convention, class users will still be able to get internal variables by accessing them with field accessors like mystack._elements.
 - If users manipulate private fields and complain something is not working, you can tell them it's their fault!
- This time, we will try to write a little more robust code. In general, when implementing pseudocode you
 might need to think more about boundary cases. In this case, we add the additional constraint that if you
 pass to the stack a negative or zero cap, your class initalization is expected to fail and raise an
 AssertionError. Such error can be raised by commands like assert my_condition where
 my_condition is False
- For easier inspection of the stack, implement also an str_ method so that calls to print show text like CappedStack: cap=4 elements=['a', 'b']

IMPORTANT: The psudo code uses indexes to keep track the stack size. Since you are providing an actual implementation in Python, you can exploit any Python feature you deem correct to implement the data structure, and even depart a bit from the literal pseudo code. For example, internally you could represent the data as a list, and use its own methods to grow it.

QUESTION: If we already have Python lists that can more or less do the job of the stack, why do we need to wrap them inside a Stack? Can't we just give our users a Python list?

QUESTION: When would you not use a Python list to hold the data in the stack?

Notice that:

- We tried to use <u>more pythonic names (https://www.python.org/dev/peps/pep-0008/#id45)</u> for methods, so for example is Empty was renamed to is empty
- In this case, when this stack reaches cap size, successive push requests silently exit without raising
 errors. Other implementations might raise an error and stop excecution when trying to push over on
 already filled stack.
- In this case, when this stack is required to pop or peek, if it is empty the functions will not return anything. During the Python translation, we might not return anything as well and relying on Python implicitly returning None.
- pop will both modify the stack and return a value

CappedStack Code Skeleton

In [11]:

```
import unittest
class CappedStack:
          init (self, cap):
        """ Creates a CappedStack capped at cap. Cap must be > 0, otherwise an Asser
tionError is thrown
        raise Exception("TODO Implement me!")
    def size(self):
        raise Exception("TODO Implement me!")
    def is empty(self):
        raise Exception("TODO Implement me!")
    def pop(self):
        raise Exception("TODO Implement me!")
    def peek(self):
        raise Exception("TODO Implement me!")
    def push(self, item):
        raise Exception("TODO Implement me!")
    def cap(self):
        """ Returns the cap of the stack
```

```
raise Exception("TODO Implement me!")
class CappedStackTest(unittest.TestCase):
    """ Test cases for CappedStackTest
         Note this is a *completely* separated class from CappedStack and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         CappedStack methods!
    .....
    def test init wrong cap(self):
            We use the special construct 'self.assertRaises(AssertionError)' to stat
е
            we are expecting the calls to CappedStack(0) and CappedStack(-1) to rais
е
            an AssertionError.
        .....
        with self.assertRaises(AssertionError):
            CappedStack(0)
        with self.assertRaises(AssertionError):
            CappedStack(-1)
    def test_cap(self):
        self.assertEqual(CappedStack(1).cap(), 1)
        self.assertEqual(CappedStack(2).cap(), 2)
    def test_size(self):
        s = CappedStack(5)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.pop()
        self.assertEqual(s.size(), 0)
    def test is empty(self):
        s = CappedStack(5)
        self.assertTrue(s.is empty())
        s.push("a")
        self.assertFalse(s.is empty())
    def test pop(self):
        s = CappedStack(5)
        self.assertEqual(s.pop(), None)
        s.push("a")
        self.assertEqual(s.pop(), "a")
        self.assertEqual(s.pop(), None)
    def test_peek(self):
        s = CappedStack(5)
        self.assertEqual(s.peek(), None)
        s.push("a")
        self.assertEqual(s.peek(), "a")
        self.assertEqual(s.peek(), "a") # testing peek is not changing the stack
        self.assertEqual(s.size(), 1)
    def test push(self):
        s = CappedStack(2)
        self.assertEqual(s.size(), 0)
        c puch ( " a " )
```

```
s.pusn("a")
self.assertEqual(s.size(), 1)
s.push("b")
self.assertEqual(s.size(), 2)
self.assertEqual(s.peek(), "b")
s.push("c") # capped, pushing should do nothing now!
self.assertEqual(s.size(), 2)
self.assertEqual(s.peek(), "b")

def test_str(self):
    s = CappedStack(4)
    s.push("a")
    s.push("b")
    print s
```

UnorderedList

UnorderedList Theory

An UnorderedList for us is a linked list starting with a pointer called *head* that points to the first Node (if the list is empty the pointer points to None). Think of the list as a chain where each Node can contain some data retriavable with Node.get_data() method and you can access one Node at a time by calling the method Node.get next() on each node.

- See theory slides (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf) from slide 25 (Monodirectional list)
- See <u>UnorderedList Abstract Data Type</u>
 (http://interactivepython.org/runestone/static/pythonds/BasicDS/TheUnorderedListAbstractDataType.html)
 on the book
- See <u>Implementing UnorderedListLinkedLists</u>
 (http://interactivepython.org/runestone/static/pythonds/BasicDS/ImplementinganUnorderedListLinkedLists.html)
 on the book

UnorderedList Exercises

1) Understand the problem

Copy the following skeleton and unit tests, and then implement the missing methods, in the order they are presented in the skeleton.

- This time there is not much pseudo or Python code to find around, you should rely solely on theory from the slides and book, method definitions and your intuition
- Pay close attention to the comments below each method definition, especially for boundary cases

WARNING: Do *not* use a Python list to hold data inside the data structure. Differently from the CappedStack exercise, here you can only use Node class. Each Node in the _data field can hold only one element which is provided by the user of the class, and we don't care about the type of the value the user gives us (so it can be an int, a float, a string, or even a Python list!)

WARNING: NEVER EVER WRITE code like this: self = something
Instead, assign values to *fields* of self, like self._head = something

WARNING: if there isn't the word "Return" in a method comment, then most probably that method does not return anything!

WARNING: Methods of the class UnorderedList are supposed to *never* return instances of Node. If you see them returned in the tests, then you are making some mistake. Users of UnorderedList are should only be able to get access to items inside the Node data fields.

Notice that there are a few differences with the book:

- · We don't assume the list has all different values
- We used <u>more pythonic names (https://www.python.org/dev/peps/pep-0008/#id45)</u> for properties and methods, so for example private attribute Node.data was renamed to Node._data and accessor method Node.getData() was renamed to Node.get_data(). There are nicer ways to handle these kind of getters/setters pairs called 'properties' but we won't address them here.
- In boundary cases like removing a non-existing element we prefer to raise an exception with the command

```
raise Exception("Some error occurred!")
```

In general, this is the behaviour you also find in regular Python lists.

2) Save a copy of your work

You already wrote a lot of code, and you don't want to lose it, right? Since we are going to make many modifications, when you reach a point when the code does something useful, it is good practice to save a copy of what you have done somewhere, so if you later screw up something, you can always restore the copy of the work

- Add also somewhere in the copy (in a comment at the top of the .py file or in a separate README.txt file) the version (like 1.0), the date, and a description of the main features (for example "Simple linked list, not particularly performant").
- Backing up the work is a form of the so-called *versioning*: there are much better ways to do it (like using <u>ait (https://git-scm.com)</u>) but we don't address them here.

3) Faster size()

Implement a size() method that works in O(1). To make this work without going through the whole list each time, we will need a new _size field that keeps track of the size. When the list is mutated with methods like add, append, etc you will also need to update the _size field accordingly. Proceed like this:

- 3.1) add a new field size in the class constructor and initialize it to zero
- 3.2) modify the size() method to just return the size field.
- 3.3) The data structure starts to be complex, and we need better testing. If you look at the tests, very often there are lines of code like self.assertEquals(ul.to python(), ['a', 'b']) in the test add method:

```
def test_add(self):
    ul = UnorderedList()
    self.myAssert(ul, [])
    ul.add('b')
    self.assertEquals(ul.to_python(), ['b'])
    ul.add('a')
    self.assertEquals(ul.to_python(), ['a', 'b'])
```

Last line checks our unordered list ul contains a sequence of linked nodes that once transformed to a python list actually equals ['a', 'b']. Since in the new implementation we are going to mutate _size field a lot, it could be smart to also check that ul.size() equals len(["a", "b"]). Repeating this check in every test method could be quite verbose. Instead, we can do a smarter thing, and develop in the UnorderedListTest class a new assertion method on our own:

3.3.1) Add this method to UnorderedListTest class:

```
def myAssert(self, unordered_list, python_list):
    """ Checks provided unordered_list can be represented as the given py
thon_list. Since v2.
    self.assertEquals(unordered_list.to_python(), python_list)
    # check this new invariant about the size
    self.assertEquals(unordered_list.size(), len(python_list))
```

WARNING: method myAssert must *not* being with test_, otherwise unittest will run it as a test!

3.3.2) Now, how to use this powerful new myAssert method? In the test class, just replace every occurence of

```
self.assertEquals(ul.to python(), ['a', 'b'])
```

into calls like this:

```
self.myAssert(ul, ['a', 'b'])
```

WARNING: Notice the `.to python()` after `ul` is gone.

- 3.4) Actually update size in the various methods where data is mutated, like add, insert, etc.
- 3.5) Run the tests and hope for the best ;-)

4) Faster append()

We are now better equipped to make further improvements. Once you're done implementing the above and made sure everything works, you can implement an append method that works in O(1) by adding an additional pointer in the data structure that always point at the last node. To further exploit the pointer, you can also add a fast last(self) method that returns the last value in the list. Proceed like this:

- 4.1) Save a copy of your work somewhere, putting version (2.0), date, and comments on the improvements.
- 4.2) Add an additional pointer called last in the constructor.
- 4.3) Copy this method into the class. Just copy it, don't implement it for now.

```
def last(self):
    """ Returns the last element in the list, in O(1).
    If list is empty, raises an Exception. Since v2.
    raise Exception("TODO implement me!")
```

4.4) Let's do some so-called *test driven development*, that is, first we write the tests, then we write the implementation.

WARNING: During the exam you will be asked to write tests, so don't skip writing them now!!

4.4.1) Implement a test for last() method, by adding this to UnorderedListTest class:

```
def test_last(self):
          raise Exception("TODO IMPLEMENT ME !")
```

In the method, create a list and add elements using only calls to add method and checks using the myAssert method. When done, ask your instructor if the test is correct (or look at the proposed solution at the bottom of the worksheet), it is important you get it right otherwise you won't be able to properly test your code.

4.4.2) You already have a test for the append() method, but, how can you be sure the _last pointer is updated correctly throughout the code? When you implemented the fast size() method you wrote some invariant in the myAssert method. We can do the same this time, too. Find the invariant and add the corresponding check to the

myAssert method. When done, ask your instructor if the invariant is correct (or look at the proposed solution at the bottom of the worksheet): it is important you get it right otherwise you won't be able to properly test your code.

- 4.5) Update the methods that mutate the data structure (add, insert, remove ...) so they keep _last pointed to last element. If the list is empty, _last will point to None. Taking particular care of corner cases such as empty list and one element list.
- 4.6) Cross your fingers and run the tests!

5) Go bidirectional

Our list so far has links that allow us to traverse it fast in one direction. But what if we want fast traversal in the reverse direction, from last to first element? What if we want a pop() that works in O(1)? To speed up these operations we could add backward links to each Node. Proceed in the following way:

5.1) Save your work

Once you're done with previous points, save the version you have somewhere adding comments about the improvements done so far, the version number (like 2.0) and the date. Then start working on a new copy.

5.2) Node backlinks

In Node class, add backlinks by adding the attribute _prev and methods get_prev(self) and set_prev(self, pointer).

5.3) Better __str__

Improve __str__ method so it shows presence or absence of links, along with the size of the list. next pointers presence must be represented with > character, absence with * character. They must be put after the item representation. prev pointers presence must be represented with < character, absence with * character. They must be put befor the item representation.

For example, for the list ['a','b','c'], you would have the following representation:

```
UnorderedList(size=3):*a><b><c*
```

As a special case for empty list you should print the following:

```
UnorderedList(size=0):[]
```

Other examples of proper lists, with 3, 2, and 1 element can be:

```
UnorderedList(size=3):*a><b><c*
UnorderedList(size=2):*a><b*
UnorderedList(size=1):*a*</pre>
```

This new __str__ method should help you to spot broken lists like the following, were some pointers are not correct:

```
Broken list, all prev pointers are missing:
UnorderedList(size=3):*a>*b>*c*

Broken list, size = 3 but shows only one element with next pointer set to Non e:
UnorderedList(size=3):*a*

Broken list, first backward pointer points to something other than None
UnorderedList(size=3):<a><b><c*</pre>
```

5.4) Modify add()

Update the UnorderedList add method to take into account you now have backlinks. Take particular care for the boundary cases when the list is empty, has one element, or for nodes at the head and at the tail of the list.

5.5) Add to_python_reversed()

Implement to python reversed method with a linear scan by using the newly added backlinks:

```
def to_python_reversed(self):
        """ Returns a regular Python list with the elements in reverse order,
            from last to first. Since v3. """
        raise Exception("TODO implement me")
```

Add also this test, and make sure it pass:

```
def test to python_reversed(self):
        ul = UnorderedList()
        ul.add('c')
ul.add('b')
        ul.add('a')
        pr = ul.to python()
        pr.reverse() # we are reversing pr with Python's 'reverse()' method
        self.assertEquals(pr, ul.to python reversed())
```

5.6) Add invariant

By using the method to python reversed(), add a new invariant to the myAssert method. If implemented correctly, this will surely spot a lot of possible errors in the code.

5.7) Modify other methods

Modify all other methods that mutate the data structure (insert, remove, etc) so that they update the backward links properly.

5.8) Run the tests

If you wrote meaningful tests and all pass, congrats!

UnorderedList Code Skeleton

```
In [16]:
import unittest
class Node:
    """ A Node of an UnorderedList. Holds data provided by the user. """
    def init (self,initdata):
        self. data = initdata
        self. next = None
    def get data(self):
        return self. data
    def get next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set next(self,newnext):
        self. next = newnext
class UnorderedList:
        This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, rais
ina exceptions on
```

```
boundary conditions like removing non exisiting elements.
    11 11 11
        init (self):
    def
        self. head = None
    def to python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very
 handy for testing.
        python list = []
        current = self. head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python list
          str (self):
        """ For potentially complex data structures like this one, having a __str__
method is essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        """ Returns True if the list has no nodes, True otherwise """
        raise Exception("TODO implement me!")
    def add(self,item):
        """ Adds item at the beginning of the list """
        raise Exception("TODO implement me!")
    def size(self):
        """ Returns the size of the list """
        raise Exception("TODO implement me!")
    def search(self,item):
        """ Returns True if item is present in list, False otherwise
        raise Exception("TODO implement me!")
    def remove(self, item):
        """ Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        raise Exception("TODO implement me!")
    def append(self, e):
        """ Appends element e to the end of the list.
            For this exercise you can write the O(n) version
```

```
raise Exception("TODO implement me!")
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, s
o list.insert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equ
ivalent to list.append(e).
            When i > list.size(), raises an Exception (default Python list appends i
nstead to the end :-/ )
        ......
        raise Exception("TODO implement me!")
    def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            If there is no such item, an exception is raised.
        raise Exception("TODO implement me!")
    def pop(self):
        """ Remove the last item of the list, and return it.
            If the list is empty, an exception is raised.
        raise Exception("TODO implement me!")
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
    .....
    def test init(self):
        ul = UnorderedList()
    def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
        ul.add('z')
        self.assertTrue('z' in str(ul))
        ul.add('w')
        self.assertTrue('z' in str(ul))
        self.assertTrue('w' in str(ul))
    def test is empty(self):
        ul = UnorderedList()
        self.assertTrue(ul.is empty())
        ul.add('a')
        self.assertFalse(ul.is empty())
    def test add(self):
        """ \overline{\mathsf{R}}emember 'add' adds stuff at the beginning of the list ! """
        ul = UnorderedList()
        self.assertEquals(ul.to python(), [])
```

```
ur.add('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.add('a')
    self.assertEquals(ul.to python(), ['a', 'b'])
def test size(self):
    ul = UnorderedList()
    self.assertEquals(ul.size(), 0)
    ul.add("a")
    self.assertEquals(ul.size(), 1)
    ul.add("b")
    self.assertEquals(ul.size(), 2)
def test search(self):
    ul = UnorderedList()
    self.assertFalse(ul.search("a"))
    ul.add("a")
    self.assertTrue(ul.search("a"))
    self.assertFalse(ul.search("b"))
    ul.add("b")
    self.assertTrue(ul.search("a"))
    self.assertTrue(ul.search("b"))
def test remove empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.remove('a')
def test remove one element(self):
    ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove two element(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['a'])
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test_remove first occurrence(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('b')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.remove('b')
    self.assertEquals(ul.to python(), [])
def test_append(self):
    ul = UnorderedList()
    ul.append('a')
    self.assertEquals(ul.to python(),['a'])
    ul.append('b')
    self.assertEquals(ul.to python(),['a', 'b'])
```

```
def test insert empty list zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a'])
def test_insert_empty_list_out_of_bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1,
                 'b')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    ul.insert(2, 'c')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
    self.assertEquals(ul.index('b'),
    with self.assertRaises(Exception):
        ul.index('a')
    ul.add('a')
    self.assertEquals(ul.index('a'),
                                       0)
    self.assertEquals(ul.index('b'),
def test pop empty(self):
    ul = UnorderedList()
```

```
witn selt.assertkalses(Exception):
        ul.pop()
def test pop one(self):
    ul = UnorderedList()
    ul.add('a')
    x = ul.pop()
    self.assertEquals('a', x)
def test pop two(self):
    ul = UnorderedList()
    ul.add('b')
   ul.add('a')
    x = ul.pop()
    self.assertEquals('b', x)
    self.assertEquals(ul.to python(), ['a'])
    y = ul.pop()
    self.assertEquals('a', y)
    self.assertEquals(ul.to python(), [])
```

Solutions

ComplexNumber Solution

```
In [17]:
```

```
import unittest
import math
class ComplexNumber:
    def init (self, real, imaginary):
        self.real = real
        self.imaginary = imaginary
    def str (self):
        return str(self.real) + " + " + str(self.imaginary) + "i"
    def phase(self):
        """ Returns a float which is the phase (that is, the vector angle) of the co
mplex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        return math.atan2(self.imaginary, self.real)
    def log(self, base):
        """ Returns another ComplexNumber which is the logarithm of this complex num
ber
            This method is something we introduce by ourselves, according to the def
inition:
            (accomodated for generic base b)
            https://en.wikipedia.org/wiki/Complex number#Natural logarithm
        return ComplexNumber(math.log(self.real) / math.log(base), self.phase() / ma
th.log(base))
    def magnitude(self):
```

```
""" Returns a float which is the magnitude (that is, the absolute value) of
the complex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        return math.sqrt(self.real**2 + self.imaginary**2)
    def __eq__(self, other):
        return self.real == other.real and self.imaginary == other.imaginary
    def isclose(self, c, delta):
        """ Returns True if the complex number is within a delta distance from compl
ex number c.
        return math.sqrt((self.real-c.real)**2 + (self.imaginary-c.imaginary)**2) <</pre>
delta
    def add (self, other):
        \overline{\mathbf{if}} is \overline{\mathbf{in}} stance (other, Complex Number):
            return ComplexNumber(self.real + other.real,self.imaginary + other.imagi
nary)
        elif type(other) is int or type(other) is float:
            return ComplexNumber(self.real + other, self.imaginary)
            return NotImplemented
         radd (self, other):
        if (type(other) is int or type(other) is float):
            return ComplexNumber(self.real + other, self.imaginary)
        else:
            return NotImplemented
    def mul (self, other):
        if isinstance(other, ComplexNumber):
            return ComplexNumber(self.real * other.real - self.imaginary * other.ima
ginary,
                                  self.imaginary * other.real + self.real * other.ima
ginary)
        elif type(other) is int or type(other) is float:
            return ComplexNumber(self.real * other, self.imaginary * other)
        else:
            return NotImplemented
         rmul (self, other):
        if (type(other) is int or type(other) is float):
            return ComplexNumber(self.real * other, self.imaginary * other)
        else:
            return NotImplemented
class ComplexNumberTest(unittest.TestCase):
    """ Test cases for ComplexNumber
         Note this is a *completely* separated class from ComplexNumber and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         ComplexNumber methods!
    11 11 11
```

```
def test init(self):
        self.assertEqual(ComplexNumber(1,2).real, 1)
        self.assertEqual(ComplexNumber(1,2).imaginary, 2)
    def test phase(self):
            NOTE: we can't use assertEqual, as the result of phase() is a
            float number which may have floating point rounding errors. So it's
            necessary to use assertAlmostEqual
            As an option with the delta you can declare the precision you require.
            For more info see Python docs:
            https://docs.python.org/2/library/unittest.html#unittest.TestCase.assert
AlmostEqual
            NOTE: assertEqual might still work on your machine but just DO NOT use i
t
            for float numbers!!!
        self.assertAlmostEqual(ComplexNumber(0.0,1.0).phase(), math.pi / 2, delta=0.
001)
    def test str(self):
        self.assertEqual(str(ComplexNumber(1,2)), "1 + 2i")
        #self.assertEqual(str(ComplexNumber(1,0)), "1")
       #self.assertEqual(str(ComplexNumber(1.0,0)), "1.0")
       #self.assertEqual(str(ComplexNumber(0,1)), "i")
        #self.assertEqual(str(ComplexNumber(0,0)), "0")
    def test_log(self):
        c = ComplexNumber(1.0, 1.0)
        l = c.log(math.e)
        self.assertAlmostEqual(l.real, 0.0, delta=0.001)
        self.assertAlmostEqual(l.imaginary, c.phase(), delta=0.001)
    def test magnitude(self):
        self.assertAlmostEqual(ComplexNumber(3.0,4.0).magnitude(),5, delta=0.001)
    def test integer equality(self):
            Note all other tests depend on this test!
            We want also to test the constructor, so in c we set stuff by hand
        c = ComplexNumber(0,0)
        c.real = 1
        c.imaginary = 2
        self.assertEquals(c, ComplexNumber(1,2))
    def test isclose(self):
        """ Notice we use `assertTrue` because we expect `isclose` to return a `boo
l` value, and
             we also test a case where we expect `False`
        self.assertTrue(ComplexNumber(1.0,1.0).isclose(ComplexNumber(1.0,1.1), 0.2))
        self.assertFalse(ComplexNumber(1.0,1.0).isclose(ComplexNumber(10.0,10.0), 0.
2))
   def test add zero(self):
        self.assertEquals(ComplexNumber(1,2) + ComplexNumber(0,0), ComplexNumber(1,2)
```

```
));
   def test add numbers(self):
       self.assertEquals(ComplexNumber(1,2) + ComplexNumber(3,4), ComplexNumber(4,6)
));
   def test_add scalar right(self):
       self.assertEquals(ComplexNumber(1,2) + 3, ComplexNumber(4,2));
   def test add scalar left(self):
       self.assertEquals(3 + ComplexNumber(1,2), ComplexNumber(4,2));
   def test add negative(self):
       self.assertEquals(ComplexNumber(-1,0) + ComplexNumber(0,-1), ComplexNumber(-
1,-1));
   def test_mul by zero(self):
       self.assertEquals(ComplexNumber(0,0) * ComplexNumber(1,2), ComplexNumber(0,0)
));
   def test mul just real(self):
       self.assertEquals(ComplexNumber(1,0) * ComplexNumber(2,0), ComplexNumber(2,0)
));
   def test mul just imaginary(self):
       0));
   def test mul scalar right(self):
       self.assertEquals(ComplexNumber(1,2) * 3, ComplexNumber(3,6));
   def test mul scalar left(self):
       self.assertEquals(3 * ComplexNumber(1,2), ComplexNumber(3,6));
```

```
In [18]:
```

```
algolab.run(ComplexNumberTest)
```

Ran 17 tests in 0.034s

0K

CappedStack Solution

In [19]:

```
import unittest

class CappedStack:

    def __init__(self, cap):
        """ Creates a CappedStack capped at cap.

        Cap must be > 0, otherwise an AssertionError is thrown

        assert cap > 0
        # notice we assign to variables with underscore to respect Python convention

self._cap = cap
        # notice with use of ements instead of the A in the recordered absence it is
```

```
# notice with use _elements instead of the A in the pseudocode, because it i
S
        # clearer, starts with underscore, and capital letters are usual reserved
        # for classes or constants
        self. elements = []
    def size(self):
        return len(self._elements)
    def is empty(self):
        return len(self. elements) == 0
    def pop(self):
        if (len(self. elements) > 0):
            return self. elements.pop()
        # else: implicitly, Python will return None
    def peek(self):
        if (len(self. elements) > 0):
            return self._elements[-1]
        # else: implicitly, Python will return None
    def push(self, item):
        if (len(self. elements) < self. cap):</pre>
            self. elements.append(item)
        # else fail silently
    def cap(self):
        """ Returns the cap of the stack
        return self. cap
    def str (self):
        return "CappedStack: cap=" + str(self. cap) + " elements=" + str(self. eleme
nts)
class CappedStackTest(unittest.TestCase):
    """ Test cases for CappedStackTest
         Note this is a *completely* separated class from CappedStack and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         CappedStack methods!
    11 11 11
    def test init wrong cap(self):
            We use the special construct 'self.assertRaises(AssertionError)' to stat
e
            we are expecting the calls to CappedStack(0) and CappedStack(-1) to rais
P
            an AssertionError.
        with self.assertRaises(AssertionError):
            CappedStack(0)
        with self.assertRaises(AssertionError):
            CappedStack(-1)
    def test cap(self):
        self.assertEqual(CappedStack(1).cap(), 1)
        self.assertEqual(CappedStack(2).cap(), 2)
```

```
def test size(self):
        s = CappedStack(5)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.pop()
        self.assertEqual(s.size(), 0)
    def test is empty(self):
        s = CappedStack(5)
        self.assertTrue(s.is empty())
        s.push("a")
        self.assertFalse(s.is empty())
    def test pop(self):
        s = CappedStack(5)
        self.assertEqual(s.pop(), None)
        s.push("a")
        self.assertEqual(s.pop(), "a")
        self.assertEqual(s.pop(), None)
    def test_peek(self):
        s = CappedStack(5)
        self.assertEqual(s.peek(), None)
        s.push("a")
        self.assertEqual(s.peek(), "a")
        self.assertEqual(s.peek(), "a") # testing peek is not changing the stack
        self.assertEqual(s.size(), 1)
    def test push(self):
        s = CappedStack(2)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.push("b")
        self.assertEqual(s.size(), 2)
        self.assertEqual(s.peek(), "b")
        s.push("c") # capped, pushing should do nothing now!
        self.assertEqual(s.size(), 2)
        self.assertEqual(s.peek(), "b")
    def test str(self):
        s = CappedStack(4)
        s.push("a")
        s.push("b")
        print s
In [20]:
```

```
algolab.run(CappedStackTest)
. . . . . . . .
CappedStack: cap=4 elements=['a', 'b']
Ran 8 tests in 0.015s
0K
```

UnorderedList v1 Solution

In [21]:

```
import unittest
class Node:
    """ A Node of an UnorderedList. Holds data provided by the user. """
    def init (self,initdata):
        self. data = initdata
        self. next = None
    def get data(self):
        return self._data
    def get next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set next(self,newnext):
        self. next = newnext
class UnorderedList:
        UnorderedList v1
        This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, rais
ing exceptions on
              boundary conditions like removing non exisiting elements.
    11 11 11
    def init (self):
        self. head = None
    def to python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very
 handy for testing.
        python list = []
        current = self. head
        while (current != None):
            python_list.append(current.get_data())
            current = current.get next()
        return python list
        __str__(self):
        """ For potentially complex data structures like this one, having a __str__
method is essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is_empty(self):
```

```
return self._head == None
def add(self,item):
    """ Adds item at the beginning of the list """
    new head = Node(item)
    new head.set next(self. head)
    self._head = new_head
def size(self):
    """ Returns the size of the list """
    current = self. head
    count = 0
   while (current != None):
        current = current.get next()
        count += 1
    return count
def search(self,item):
    """ Returns True if item is present in list, False otherwise
    current = self. head
   while (current != None):
        if (current.get data() == item):
            return True
        else:
            current = current.get next()
    return False
def remove(self, item):
    """ Removes first occurrence of item from the list
        If item is not found, raises an Exception.
    current = self. head
    prev = None
   while (current != None):
        if (current.get data() == item):
            if prev == None: # we need to remove the head
                self. head = current.get next()
                prev.set next(current.get next())
                current = current.get next()
            return # Found, exits the function
        else:
            prev = current
            current = current.get next()
    raise Exception("Tried to remove a non existing item! Item was: " + str(item
def append(self, e):
    """ Appends element e to the end of the list.
        For this exercise you can write the O(n) version
    if self. head == None:
        self.add(e)
    else:
         surrent - colf bood
```

))

```
while (current.get next() != None):
                current = current.get next()
            current.set next(Node(e))
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, s
o list.insert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equ
ivalent to list.append(e).
            When i > list.size(), raises an Exception (default Python list appends i
nstead to the end :-/ )
        11 11 11
        if (i < 0):
            raise Exception("Tried to insert at a negative index! Index was:" + str(
i))
        count = 0
        current = self._head
        prev = None
        while (count < i and current != None):</pre>
            prev = current
            current = current.get next()
            count += 1
        if (current == None):
            if (count == i):
                self.append(e)
            else:
                raise Exception("Tried to insert outside the list ! "
                                 + "List size=" + str(count) + " insert position=" +
 str(i))
        else:
            #0 1
            if (prev == None):
                self.add(e)
            else:
                new node = Node(e)
                prev.set next(new node)
                new node.set next(current)
    def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            If item is not found, raises an Exception.
        current = self. head
        count = 0
        while (current != None):
            if (current.get data() == e):
                return count
            else:
                current = current.get next()
                count += 1
        raise Exception("Couldn't find element " + str(e) )
```

current = sett._nead

```
def pop(self):
        """ Remove the last item of the list, and return it.
            If the list is empty, an exception is raised.
        if (self. head == None):
            raise Exception("Tried to pop an empty list!")
        else:
            current = self. head
            if (current.get next() == None): # one element list
                last item = self. head.get data()
                self. head = None
                    # we have more than one element
                prev = None
                while current.get next() != None: # current will reach last element
                    prev = current
                    current = current.get next()
                last item = current.get data()
                prev.set next(None)
            return last item
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
    11 11 11
    def test init(self):
        ul = UnorderedList()
   def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
        ul.add('z')
        self.assertTrue('z' in str(ul))
        ul.add('w')
        self.assertTrue('z' in str(ul))
        self.assertTrue('w' in str(ul))
   def test is empty(self):
        ul = UnorderedList()
        self.assertTrue(ul.is empty())
        ul.add('a')
        self.assertFalse(ul.is empty())
    def test add(self):
        """ Remember 'add' adds stuff at the beginning of the list! """
        ul = UnorderedList()
        self.assertEquals(ul.to python(), [])
        ul.add('b')
        self.assertEquals(ul.to_python(), ['b'])
        ul.add('a')
        self.assertEquals(ul.to python(), ['a', 'b'])
    def test_size(self):
```

```
ut = unoraerealist()
    self.assertEquals(ul.size(), 0)
    ul.add("a")
    self.assertEquals(ul.size(), 1)
    ul.add("b")
    self.assertEquals(ul.size(), 2)
def test_search(self):
    ul = UnorderedList()
    self.assertFalse(ul.search("a"))
    ul.add("a")
    self.assertTrue(ul.search("a"))
    self.assertFalse(ul.search("b"))
    ul.add("b")
    self.assertTrue(ul.search("a"))
    self.assertTrue(ul.search("b"))
def test remove empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.remove('a')
def test remove one element(self):
    ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove two element(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['a'])
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove first occurrence(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('b')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.remove('b')
    self.assertEquals(ul.to python(), [])
def test append(self):
    ul = UnorderedList()
    ul.append('a')
    self.assertEquals(ul.to python(),['a'])
    ul.append('b')
    self.assertEquals(ul.to_python(),['a', 'b'])
def test insert empty list zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a'])
```

```
def test_insert_empty_list_out of bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to_python(), ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    ul.insert(2, 'c')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
    self.assertEquals(ul.index('b'),
    with self.assertRaises(Exception):
        ul.index('a')
    ul.add('a')
    self.assertEquals(ul.index('a'),
                                       0)
    self.assertEquals(ul.index('b'),
def test pop empty(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.pop()
def test pop one(self):
    ul = UnorderedList()
    11 244/1211
```

```
ut.add('a')
x = ul.pop()
self.assertEquals('a', x)

def test_pop_two(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
x = ul.pop()
self.assertEquals('b', x)
self.assertEquals(ul.to_python(), ['a'])
y = ul.pop()
self.assertEquals('a', y)
self.assertEquals(ul.to_python(), [])
```

```
In [22]:
```

```
algolab.run(UnorderedListTest)
......
Ran 23 tests in 0.040s
0K
```

UnorderedList v2 Solution

In [23]:

```
import unittest
class Node:
    """ A Node of an UnorderedList. Holds data provided by the user.
        Node v2 remains the same as Node v1
         init (self,initdata):
    def
        self. data = initdata
        self. next = None
    def get data(self):
        return self._data
    def get next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set next(self,newnext):
        self. next = newnext
class UnorderedList:
        a linked list implementation, v2.
        Improvements upon UnorderedList v1:
        * calculates size() in O(1)
        * calculates append() in O(1)
        * adds last() method to retrieve last element in O(1)
```

```
This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, rais
ing exceptions on
              boundary conditions like removing non exisiting elements.
    def init (self):
        self. head = None
        self. size = 0 # NEW attribute ' size'
        self. last = None # NEW attribute ' last'
    def to python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very
 handy for testing.
        python list = []
        current = self. head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python list
         str (self):
        """ For potentially complex data structures like this one, having a __str__
method is essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        return self. head == None
    def add(self,item):
        """ Adds item at the beginning of the list """
        new head = Node(item)
        new head.set next(self. head)
        if self. head == None: # NEW
            self. last = new head # NEW
        self. head = new_head
        self. size += 1 # NEW, we just return the field value. This is fast!
    def size(self):
        """ Returns the size of the list in O(1) """
        return self. size # NEW, we just return the field value. This is fast!
    def search(self,item):
        """ Returns True if item is present in list, False otherwise
        current = self. head
        while (current != None):
            if (current.get data() == item):
```

```
return irue
            else:
                current = current.get next()
        return False
    def remove(self, item):
        """ Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        current = self. head
        prev = None
       while (current != None):
            if (current.get data() == item):
                if (self. last == current): # NEW
                    self. last = prev
                                             # NEW
                if prev == None: # we need to remove the head
                    self. head = current.get next()
                else:
                    prev.set next(current.get next())
                    current = current.get next()
                self. size -= 1 # NEW, need to update size
                return # Found, exits the function
                prev = current
                current = current.get next()
        raise Exception("Tried to remove a non existing item! Item was: " + str(item
))
    def append(self, e):
        """ Appends element e to the end of the list, in O(1)
        0.00
        if self. head == None:
            self.add(e)
        else:
            new node = Node(e)
            self. last.set next(new node) # NEW, we directly exploit last pointer
            self. last = new node # NEW, need to update last
            self. size += 1 # NEW, need to update size
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, s
o list.insert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equ
ivalent to list.append(e).
            When i > list.size(), raises an Exception (default Python list appends i
nstead to the end :-/ )
        0.00
        if (i < 0):
            raise Exception("Tried to insert at a negative index! Index was:" + str(
i))
        count = 0
        current = self. head
        prev = None
```

```
while (count < i and current != None):</pre>
           prev = current
           current = current.get next()
           count += 1
       if (current == None):
           if (count == i):
               self.append(e)
           else:
               raise Exception("Tried to insert outside the list ! "
                               + "List size=" + str(count) + " insert position=" +
str(i))
       else:
           #0 1
             i
           if (prev == None):
               self.add(e)
           else:
               new node = Node(e)
               prev.set next(new node)
               new node.set next(current)
               self. size += 1 # NEW, need to update size
  def index(self, e):
       """ Return the index in the list of the first item whose value is x.
           If item is not found, raises an Exception.
       current = self. head
       count = 0
      while (current != None):
           if (current.get data() == e):
               return count
           else:
               current = current.get next()
               count += 1
       raise Exception("Couldn't find element " + str(e) )
  def pop(self):
       """ Remove the last item of the list, and return it.
           If the list is empty, an exception is raised.
       if (self. head == None):
           raise Exception("Tried to pop an empty list!")
       else:
           current = self. head
           if (current.get_next() == None): # one element list
               popped = self. head
               self.\_head = None
               self. last = None # NEW
                    # we have more than one element
               prev = None
               while current.get_next() != None: # current will reach last element
                   prev = current
                   current = current.get next()
               popped = current
               -- 1 f 1--+ - -- -- # NEW
```

```
selt._last = prev
                                   # NEW
                prev.set next(None)
            self. size -= 1 # NEW
            return popped.get data()
    def last(self):
        """ Returns the last element in the list, in O(1).
            If list is empty, raises an Exception. Since v2.
        11 11 11
        if (self. head == None):
            raise Exception("Tried to get the last element of an empty list!")
        else:
            return self. last.get data()
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList v2
        Test cases are improved by adding a new method myAssert(self, unordered list
, python list)
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
    11 11 11
    def myAssert(self, unordered_list, python_list):
        """ Checks provided unordered list can be represented as the given python li
st. Since v2
        self.assertEquals(unordered list.to python(), python list)
        # we check this new invariant about the size
        self.assertEquals(unordered list.size(), len(python list))
        # we check this new invariant about the last element
        if len(python list) != 0:
            self.assertEquals(unordered list.last(), python list[-1])
    def test init(self):
        ul = UnorderedList()
    def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
        ul.add('z')
        self.assertTrue('z' in str(ul))
        ul.add('w')
        self.assertTrue('z' in str(ul))
        self.assertTrue('w' in str(ul))
    def test_is_empty(self):
        ul = UnorderedList()
        self.assertTrue(ul.is empty())
        ul.add('a')
        self.assertFalse(ul.is empty())
    def test add(self):
        """ Remember 'add' adds stuff at the beginning of the list! """
        ul = UnorderedList()
        self.myAssert(ul, [])
        "1 ~44/1h1)
```

```
ur.add( b )
    self.myAssert(ul, ['b'])
    ul.add('a')
    self.myAssert(ul, ['a', 'b'])
def test size(self):
    ul = UnorderedList()
    self.assertEquals(ul.size(), 0)
    ul.add("a")
    self.assertEquals(ul.size(), 1)
    ul.add("b")
    self.assertEquals(ul.size(), 2)
def test search(self):
    ul = UnorderedList()
    self.assertFalse(ul.search("a"))
    ul.add("a")
    self.assertTrue(ul.search("a"))
    self.assertFalse(ul.search("b"))
    ul.add("b")
    self.assertTrue(ul.search("a"))
    self.assertTrue(ul.search("b"))
def test_remove_empty_list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.remove('a')
def test remove one element(self):
    ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
    ul.remove('a')
    self.assertEquals(ul.to_python(), [])
def test remove two element(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['a'])
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove first occurrence(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('b')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.remove('b')
    self.assertEquals(ul.to python(), [])
def test append(self):
    ul = UnorderedList()
    ul.append('a')
    self.myAssert(ul,['a'])
    ul.append('b')
    self.myAssert(ul,['a', 'b'])
```

```
def test insert empty list zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.myAssert(ul, ['a'])
def test insert empty list out of bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.myAssert(ul, ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1, 'b')
    self.myAssert(ul, ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.myAssert(ul, ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.myAssert(ul, ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    ul.insert(2, 'c')
    self.myAssert(ul, ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
    self.assertEquals(ul.index('b'),
    with self.assertRaises(Exception):
        ul.index('a')
    ul.add('a')
    self.assertEquals(ul.index('a'),
    self.assertEquals(ul.index('b'), 1)
def test pop empty(self):
    ul = UnorderedList()
    with colf accortDaicac/Evention).
```

```
witn self.assertkaises(Exception):
            ul.pop()
    def test_pop_one(self):
        ul = UnorderedList()
        ul.add('a')
        x = ul.pop()
        self.assertEquals('a', x)
    def test pop two(self):
        ul = UnorderedList()
        ul.add('b')
        ul.add('a')
        x = ul.pop()
        self.assertEquals('b', x)
        self.myAssert(ul, ['a'])
        y = ul.pop()
        self.assertEquals('a', y)
        self.myAssert(ul, [])
    def test last(self):
        """ \overline{T}his tests only simple cases. More in-depth testing will be provided by
calls to myAssert """
        ul = UnorderedList()
        with self.assertRaises(Exception):
            ul.last()
        ul.add('b')
        self.assertEquals(ul.last(), 'b')
        ul.add('a')
        self.assertEquals(ul.last(), 'b')
In [24]:
algolab.run(UnorderedListTest)
Ran 24 tests in 0.028s
0K
```

In [25]: