Structures - Stacks and linked lists

Stack

Stack theory

See theory here: http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf) (Slide 46)

See stack definition on the book (http://interactivepython.org/runestone/static/pythonds/BasicDS/WhatisaStack.html)

and following sections:

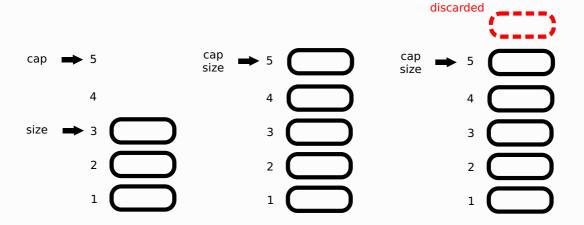
- <u>Stack Abstract Data Type</u>
 (http://interactivepython.org/runestone/static/pythonds/BasicDS/TheStackAbstractDataType.html)
- Implementing a Stack in Python (http://interactivepython.org/runestone/static/pythonds/BasicDS/ImplementingaStackinPython.html)
- <u>Simple Balanced Parenthesis</u> (http://interactivepython.org/runestone/static/pythonds/BasicDS/SimpleBalancedParentheses.html)
- <u>Balanced Symbols a General Case</u> (http://interactivepython.org/runestone/static/pythonds/BasicDS/BalancedSymbols(AGeneralCase).html)

Stack exercises

On slide 46 of theory (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (Slide 46) there is the pseudo code for a version of stack we will call CappedStack:

```
STACK
ITEM[]A
                              % Elements ITEM peek()
int size
                           % Current size
                                                if size > 0 then
int cap
                        % Maximum size
                                                    return A[size]
 STACK Stack(int dim)
                                                ITEM pop()
    Stack t \leftarrow \mathbf{new} Stack
                                                   if size > 0 then
    t.A \leftarrow \mathbf{new} \ \mathbf{int}[1 \dots dim]
                                                       ITEM t \leftarrow A[size]
   t.cap \leftarrow dim
                                                       size \leftarrow size - 1
    t.size \leftarrow 0
                                                       return t
   return t
                                                push(ITEM v)
 boolean isEmpty()
                                                   if size < cap then
   return size = 0
                                                       size \leftarrow size + 1
                                                       A[size] \leftarrow v
 int size()
   return size
```

A capped stack has a limit called *cap* over which elements are discarded:



- Copy the following skeleton and unit tests, and then implement the pseudo code
- Name internal variables that you don't want to expose to class users by prepending them with one underscore '_', like _elements or _cap.
 - The underscore is just a convention, class users will still be able to get internal variables by accessing them with field accessors like mystack. elements.
 - If users manipulate private fields and complain something is not working, you can tell them it's their fault!
- This time, we will try to write a little more robust code. In general, when implementing pseudocode you might need to think more about boundary cases. In this case, we add the additional constraint that if you pass to the stack a negative or zero cap, your class initalization is expected to fail and raise an AssertionError. Such error can be raised by commands like assert my condition where my condition is False
- For easier inspection of the stack, implement also an __str__ method so that calls to print show text like CappedStack: cap=4 elements=['a', 'b']

IMPORTANT: The psudo code uses indexes to keep track the stack size. Since you are providing an actual implementation in Python, you can exploit any Python feature you deem correct to implement the data structure, and even depart a bit from the literal pseudo code. For example, internally you could represent the data as a list, and use its own methods to grow it.

QUESTION: If we already have Python lists that can more or less do the job of the stack, why do we need to wrap them inside a Stack? Can't we just give our users a Python list?

QUESTION: When would you not use a Python list to hold the data in the stack?

Notice that:

- We tried to use <u>more pythonic names (https://www.python.org/dev/peps/pep-0008/#id45)</u> for methods, so for example isEmpty was renamed to is empty
- In this case, when this stack reaches cap size, successive push requests silently exit without raising errors. Other implementations might raise an error and stop excecution when trying to push over on already filled stack.
- In this case, when this stack is required to pop or peek, if it is empty the functions will not return anything. During the Python translation, we might not return anything as well and relying on Python implicitly returning None.
- pop will both modify the stack and return a value

CappedStack Code Skeleton

In [3]:

import unittest

class CappedStack:
 def init (self, cap):

```
""" Creates a CappedStack capped at cap. Cap must be > 0, otherwise an AssertionError
is thrown
        raise Exception("TODO Implement me!")
    def size(self):
        raise Exception("TODO Implement me!")
    def is empty(self):
        raise Exception("TODO Implement me!")
    def pop(self):
        raise Exception("TODO Implement me!")
    def peek(self):
        raise Exception("TODO Implement me!")
    def push(self, item):
        raise Exception("TODO Implement me!")
    def cap(self):
        """ Returns the cap of the stack
        raise Exception("TODO Implement me!")
class CappedStackTest(unittest.TestCase):
    """ Test cases for CappedStackTest
         Note this is a *completely* separated class from CappedStack and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         CappedStack methods!
    def test init wrong cap(self):
            We use the special construct 'self.assertRaises(AssertionError)' to state
            we are expecting the calls to CappedStack(0) and CappedStack(-1) to raise
            an AssertionError.
        with self.assertRaises(AssertionError):
            CappedStack(0)
        with self.assertRaises(AssertionError):
            CappedStack(-1)
    def test cap(self):
        self.assertEqual(CappedStack(1).cap(), 1)
        self.assertEqual(CappedStack(2).cap(), 2)
    def test size(self):
        s = CappedStack(5)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.pop()
        self.assertEqual(s.size(), 0)
    def test is_empty(self):
        s = CappedStack(5)
        self.assertTrue(s.is empty())
        s.push("a")
        self.assertFalse(s.is empty())
    def test pop(self):
        s = CappedStack(5)
        self.assertEqual(s.pop(), None)
        s.push("a")
```

```
self.assertEqual(s.pop(), "a")
    self.assertEqual(s.pop(), None)
def test peek(self):
    s = CappedStack(5)
    self.assertEqual(s.peek(), None)
    s.push("a")
    self.assertEqual(s.peek(), "a")
    self.assertEqual(s.peek(), "a") # testing peek is not changing the stack
    self.assertEqual(s.size(), 1)
def test push(self):
    s = CappedStack(2)
    self.assertEqual(s.size(), 0)
    s.push("a")
    self.assertEqual(s.size(), 1)
    s.push("b")
    self.assertEqual(s.size(), 2)
    self.assertEqual(s.peek(), "b")
    s.push("c") # capped, pushing should do nothing now!
    self.assertEqual(s.size(), 2)
    self.assertEqual(s.peek(), "b")
def test str(self):
    s = CappedStack(4)
    s.push("a")
    s.push("b")
   print s
```

UnorderedList

UnorderedList Theory

An UnorderedList for us is a linked list starting with a pointer called *head* that points to the first Node (if the list is empty the pointer points to None). Think of the list as a chain where each Node can contain some data retriavable with Node.get_data() method and you can access one Node at a time by calling the method Node.get next() on each node.

- See theory slides (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf) from slide 25 (Monodirectional list)
- See <u>UnorderedList Abstract Data Type</u> (http://interactivepython.org/runestone/static/pythonds/BasicDS/TheUnorderedListAbstractDataType.html) on the book
- See <u>Implementing UnorderedListLinkedLists</u>
 (http://interactivepython.org/runestone/static/pythonds/BasicDS/ImplementinganUnorderedListLinkedLists.html) on the book

UnorderedList Exercises

1) Understand the problem

Copy the following skeleton and unit tests, and then implement the missing methods, in the order they are presented in the skeleton.

- This time there is not much pseudo or Python code to find around, you should rely solely on theory from the slides and book, method definitions and your intuition
- Pay close attention to the comments below each method definition, especially for boundary cases

COMMANDMENT: You shall also draw lists on paper, helps a lot avoiding mistakes

WARNING: Do *not* use a Python list to hold data inside the data structure. Differently from the CappedStack exercise, here you can only use Node class. Each Node in the _data field can hold only one element which is provided by the user of the class, and we don't care about the type of the value the user gives us (so it can be an int, a float, a string, or even a Python list!)

WARNING: NEVER EVER WRITE code like this: self = something

Instead, assign values to fields of self, like self._head = something

WARNING: if there isn't the word "Return" in a method comment, then most probably that method does not return anything!

WARNING: Methods of the class UnorderedList are supposed to *never* return instances of Node. If you see them returned in the tests, then you are making some mistake. Users of UnorderedList are should only be able to get access to items inside the Node data fields.

Notice that there are a few differences with the book:

- · We don't assume the list has all different values
- We used <u>more pythonic names (https://www.python.org/dev/peps/pep-0008/#id45)</u> for properties and methods, so for example private attribute Node.data was renamed to Node._data and accessor method Node.getData() was renamed to Node.get_data(). There are nicer ways to handle these kind of getters/setters pairs called 'properties' but we won't address them here.
- In boundary cases like removing a non-existing element we prefer to raise an exception with the command

```
raise Exception("Some error occurred!")
```

In general, this is the behaviour you also find in regular Python lists.

2) Save a copy of your work

You already wrote a lot of code, and you don't want to lose it, right? Since we are going to make many modifications, when you reach a point when the code does something useful, it is good practice to save a copy of what you have done somewhere, so if you later screw up something, you can always restore the copy.

- Add also somewhere in the copy (in a comment at the top of the .py file or in a separate README.txt file) the version (like 1.0), the date, and a description of the main features (for example "Simple linked list, not particularly performant").
- Backing up the work is a form of the so-called *versioning*: there are much better ways to do it (like using <u>git (https://gitscm.com)</u>) but we don't address them here.

3) Faster size()

Implement a size() method that works in 0(1). To make this work without going through the whole list each time, we will need a new _size field that keeps track of the size. When the list is mutated with methods like add, append, etc you will also need to update the _size field accordingly. Proceed like this:

- 3.1) add a new field size in the class constructor and initialize it to zero
- 3.2) modify the size() method to just return the size field.
- 3.3) The data structure starts to be complex, and we need better testing. If you look at the tests, very often there are lines of code like self.assertEquals(ul.to python(), ['a', 'b']) in the test add method:

```
def test_add(self):
    ul = UnorderedList()
    self.myAssert(ul, [])
    ul.add('b')
    self.assertEquals(ul.to_python(), ['b'])
    ul.add('a')
    self.assertEquals(ul.to_python(), ['a', 'b'])
```

Last line checks our unordered list ul contains a sequence of linked nodes that once transformed to a python list actually equals ['a', 'b']. Since in the new implementation we are going to mutate _size field a lot, it could be smart to also check that ul.size() equals len(["a", "b"]). Repeating this check in every test method could be quite verbose. Instead, we can do a smarter thing, and develop in the UnorderedListTest class a new assertion method on our own:

3.3.1) Add this method to UnorderedListTest class:

```
def myAssert(self, unordered_list, python_list):
        """ Checks provided unordered_list can be represented as the given python_list.
Since v2.
        """
        self.assertEquals(unordered_list.to_python(), python_list)
        # check this new invariant about the size
        self.assertEquals(unordered_list.size(), len(python_list))
```

WARNING: method myAssert must *not* being with test_, otherwise unittest will run it as a test!

3.3.2) Now, how to use this powerful new myAssert method? In the test class, just replace every occurence of

```
self.assertEquals(ul.to_python(), ['a', 'b'])
into calls like this:
```

WARNING: Notice the `.to python()` after `ul` is gone.

- 3.4) Actually update size in the various methods where data is mutated, like add, insert, etc.
- 3.5) Run the tests and hope for the best ;-)

self.myAssert(ul, ['a', 'b'])

4) Faster append()

We are now better equipped to make further improvements. Once you're done implementing the above and made sure everything works, you can implement an append method that works in O(1) by adding an additional pointer in the data structure that always point at the last node. To further exploit the pointer, you can also add a fast last(self) method that returns the last value in the list. Proceed like this:

- 4.1) Save a copy of your work somewhere, putting version (2.0), date, and comments on the improvements.
- 4.2) Add an additional pointer called last in the constructor.
- 4.3) Copy this method into the class. Just copy it, don't implement it for now.

```
def last(self):
    """ Returns the last element in the list, in O(1).
    If list is empty, raises an Exception. Since v2.
    raise Exception("TODO implement me!")
```

4.4) Let's do some so-called test driven development, that is, first we write the tests, then we write the implementation.

WARNING: During the exam you will be asked to write tests, so don't skip writing them now !!

4.4.1) Implement a test for last() method, by adding this to UnorderedListTest class:

```
def test_last(self):
          raise Exception("TODO IMPLEMENT ME !")
```

In the method, create a list and add elements using only calls to add method and checks using the myAssert method. When done, ask your instructor if the test is correct (or look at the proposed solution at the bottom of the worksheet), it is important you get it right otherwise you won't be able to properly test your code.

- 4.4.2) You already have a test for the append() method, but, how can you be sure the _last pointer is updated correctly throughout the code? When you implemented the fast size() method you wrote some invariant in the myAssert method. We can do the same this time, too. Find the invariant and add the corresponding check to the myAssert method. When done, ask your instructor if the invariant is correct (or look at the proposed solution at the bottom of the worksheet): it is important you get it right otherwise you won't be able to properly test your code.
- 4.5) Update the methods that mutate the data structure (add, insert, remove ...) so they keep _last pointed to last element. If the list is empty, last will point to None. Taking particular care of corner cases such as empty list and one element list.
- 4.6) Cross your fingers and run the tests!

5) Go bidirectional

Our list so far has links that allow us to traverse it fast in one direction. But what if we want fast traversal in the reverse direction, from last to first element? What if we want a pop() that works in O(1)? To speed up these operations we could add backward links to each Node. Proceed in the following way:

5.1) Save your work

Once you're done with previous points, save the version you have somewhere adding comments about the improvements done so far, the version number (like 2.0) and the date. Then start working on a new copy.

5.2) Node backlinks

In Node class, add backlinks by adding the attribute _prev and methods get_prev(self) and set_prev(self, pointer).

5.3) Better str

Improve __str__ method so it shows presence or absence of links, along with the size of the list. next pointers presence must be represented with > character, absence with * character. They must be put after the item representation. prev pointers presence must be represented with < character, absence with * character. They must be put befor the item representation.

For example, for the list ['a','b','c'], you would have the following representation:

```
UnorderedList(size=3):*a><b><c*
```

As a special case for empty list you should print the following:

```
UnorderedList(size=0):[]
```

Other examples of proper lists, with 3, 2, and 1 element can be:

```
UnorderedList(size=3):*a><b><c*
UnorderedList(size=2):*a><b*
UnorderedList(size=1):*a*</pre>
```

This new str method should help you to spot broken lists like the following, were some pointers are not correct:

```
Broken list, all prev pointers are missing:
UnorderedList(size=3):*a>*b>*c*

Broken list, size = 3 but shows only one element with next pointer set to None:
UnorderedList(size=3):*a*

Broken list, first backward pointer points to something other than None
UnorderedList(size=3):<a><b><c*</pre>
```

5.4) Modify add()

Update the UnorderedList add method to take into account you now have backlinks. Take particular care for the boundary cases when the list is empty, has one element, or for nodes at the head and at the tail of the list.

5.5) Add to_python_reversed()

Implement to python reversed method with a linear scan by using the newly added backlinks:

Add also this test, and make sure it pass:

```
def test_to_python_reversed(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.add('a')
    pr = ul.to_python()
    pr.reverse() # we are reversing pr with Python's 'reverse()' method
    self.assertEquals(pr, ul.to python reversed())
```

5.6) Add invariant

By using the method to_python_reversed(), add a new invariant to the myAssert method. If implemented correctly, this will surely spot a lot of possible errors in the code.

5.7) Modify other methods

Modify all other methods that mutate the data structure (insert, remove, etc) so that they update the backward links properly.

5.8) Run the tests

If you wrote meaningful tests and all pass, congrats!

UnorderedList Code Skeleton

```
In [8]:
import unittest
class Node:
    """ A Node of an UnorderedList. Holds data provided by the user. """
        init (self,initdata):
        self._data = initdata
        self. next = None
    def get_data(self):
        return self. data
    def get next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set next(self,newnext):
        self. next = newnext
class UnorderedList:
        This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, raising except
ions on
              boundary conditions like removing non exisiting elements.
    .....
    def init (self):
        self. head = None
    def to_python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very handy for
testing.
        python_list = []
        current = self._head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python_list
          str (self):
        """ For potentially complex data structures like this one, having a __str__ method is
essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
```

```
while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        """ Returns True if the list has no nodes, True otherwise """
        raise Exception("TODO implement me!")
    def add(self,item):
        """ Adds item at the beginning of the list """
        raise Exception("TODO implement me!")
    def size(self):
        """ Returns the size of the list """
        raise Exception("TODO implement me!")
    def search(self,item):
        """ Returns True if item is present in list, False otherwise
        raise Exception("TODO implement me!")
    def remove(self, item):
        """ Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        raise Exception("TODO implement me!")
    def append(self, e):
        """ Appends element e to the end of the list.
           For this exercise you can write the O(n) version
        raise Exception("TODO implement me!")
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, so list.ins
ert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equivalent to
 list.append(e).
            When i > list.size(), raises an Exception (default Python list appends instead to
the end :-/ )
        raise Exception("TODO implement me!")
    def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            If there is no such item, an exception is raised.
        raise Exception("TODO implement me!")
    def pop(self):
        """ Remove the last item of the list, and return it.
            If the list is empty, an exception is raised.
        raise Exception("TODO implement me!")
```

```
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
    def test init(self):
        ul = UnorderedList()
    def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
        ul.add('z')
        self.assertTrue('z' in str(ul))
        ul.add('w')
        self.assertTrue('z' in str(ul))
        self.assertTrue('w' in str(ul))
    def test_is_empty(self):
        ul = UnorderedList()
        self.assertTrue(ul.is empty())
        ul.add('a')
        self.assertFalse(ul.is_empty())
    def test add(self):
        """ \overline{\mathsf{R}}emember 'add' adds stuff at the beginning of the list ! """
        ul = UnorderedList()
        self.assertEquals(ul.to python(), [])
        ul.add('b')
        self.assertEquals(ul.to python(), ['b'])
        ul.add('a')
        self.assertEquals(ul.to python(), ['a', 'b'])
    def test size(self):
        ul = UnorderedList()
        self.assertEquals(ul.size(), 0)
        ul.add("a")
        self.assertEquals(ul.size(), 1)
        ul.add("b")
        self.assertEquals(ul.size(), 2)
    def test search(self):
        ul = UnorderedList()
        self.assertFalse(ul.search("a"))
        ul.add("a")
        self.assertTrue(ul.search("a"))
        self.assertFalse(ul.search("b"))
        ul.add("b")
        self.assertTrue(ul.search("a"))
        self.assertTrue(ul.search("b"))
    def test remove empty list(self):
        ul = UnorderedList()
        with self.assertRaises(Exception):
            ul.remove('a')
    def test remove one element(self):
        ul = UnorderedList()
        ul.add('a')
        with self.assertRaises(Exception):
            ul.remove('b')
        ul.remove('a')
        self.assertEquals(ul.to python(), [])
    def test remove two element(self):
        ul = UnorderedList()
```

```
ul.add('b')
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['a'])
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove first occurrence(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('b')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.remove('b')
    self.assertEquals(ul.to python(), [])
def test_append(self):
    ul = UnorderedList()
    ul.append('a')
    self.assertEquals(ul.to python(),['a'])
    ul.append('b')
    self.assertEquals(ul.to_python(),['a', 'b'])
def test_insert_empty_list_zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a'])
def test insert empty list out of bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to_python(), ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1,
                 'b')
    self.assertEquals(ul.to python(), ['a','b'])
def test_insert_two_element_list_insert_before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
```

```
ul.insert(2, 'c')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
    self.assertEquals(ul.index('b'), 0)
    with self.assertRaises(Exception):
        ul.index('a')
    ul.add('a')
    self.assertEquals(ul.index('a'),
    self.assertEquals(ul.index('b'), 1)
def test_pop_empty(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.pop()
def test_pop_one(self):
    ul = UnorderedList()
    ul.add('a')
    x = ul.pop()
    self.assertEquals('a', x)
def test pop two(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    x = ul.pop()
    self.assertEquals('b', x)
    self.assertEquals(ul.to python(), ['a'])
    y = ul.pop()
    self.assertEquals('a', y)
    self.assertEquals(ul.to python(), [])
```

Solutions

CappedStack Solution

```
In [9]:
```

```
def is empty(self):
        return len(self. elements) == 0
    def pop(self):
        if (len(self. elements) > 0):
            return self. elements.pop()
        # else: implicitly, Python will return None
    def peek(self):
        if (len(self. elements) > 0):
            return self. elements[-1]
        # else: implicitly, Python will return None
    def push(self, item):
        if (len(self. elements) < self. cap):</pre>
            self. elements.append(item)
        # else fail silently
    def cap(self):
        """ Returns the cap of the stack
        return self. cap
    def __str__(self):
        return "CappedStack: cap=" + str(self._cap) + " elements=" + str(self._elements)
class CappedStackTest(unittest.TestCase):
    """ Test cases for CappedStackTest
         Note this is a *completely* separated class from CappedStack and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         CappedStack methods!
    def test init wrong cap(self):
            We use the special construct 'self.assertRaises(AssertionError)' to state
            we are expecting the calls to CappedStack(0) and CappedStack(-1) to raise
            an AssertionError.
        with self.assertRaises(AssertionError):
            CappedStack(0)
        with self.assertRaises(AssertionError):
            CappedStack(-1)
    def test cap(self):
        self.assertEqual(CappedStack(1).cap(), 1)
        self.assertEqual(CappedStack(2).cap(), 2)
    def test size(self):
        s = CappedStack(5)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.pop()
        self.assertEqual(s.size(), 0)
    def test is empty(self):
        s = CappedStack(5)
        self.assertTrue(s.is_empty())
        s.push("a")
        self.assertFalse(s.is empty())
    def test pop(self):
        s = CappedStack(5)
```

```
selt.assertEqual(s.pop(), None)
    s.push("a")
    self.assertEqual(s.pop(), "a")
    self.assertEqual(s.pop(), None)
def test peek(self):
    s = CappedStack(5)
    self.assertEqual(s.peek(), None)
    s.push("a")
    self.assertEqual(s.peek(), "a")
    self.assertEqual(s.peek(), "a") # testing peek is not changing the stack
    self.assertEqual(s.size(), 1)
def test push(self):
    s = CappedStack(2)
    self.assertEqual(s.size(), 0)
    s.push("a")
    self.assertEqual(s.size(), 1)
    s.push("b")
    self.assertEqual(s.size(), 2)
    self.assertEqual(s.peek(), "b")
    s.push("c") # capped, pushing should do nothing now!
    self.assertEqual(s.size(), 2)
    self.assertEqual(s.peek(), "b")
def test str(self):
    s = CappedStack(4)
    s.push("a")
    s.push("b")
    print s
```

```
In [10]:
```

```
algolab.run(CappedStackTest)
......
CappedStack: cap=4 elements=['a', 'b']
.....
Ran 8 tests in 0.018s
OK
```

UnorderedList v1 Solution

In [11]:

```
import unittest

class Node:
    """ A Node of an UnorderedList. Holds data provided by the user. """

def __init__ (self,initdata):
    self._data = initdata
    self._next = None

def get_data(self):
    return self._data

def get_next(self):
    return self._next

def set_data(self,newdata):
    self._data = newdata

def set_next(self,newnext):
    self._next = newnext

class UnorderedList:
    """
```

```
UnorderedList v1
        This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, raising except
ions on
              boundary conditions like removing non exisiting elements.
    def
        init (self):
        self. head = None
    def to python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very handy for
 testing.
        python list = []
        current = self. head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python_list
          _str___(self):
        For potentially complex data structures like this one, having a __str__ method is
essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        return self._head == None
    def add(self,item):
        """ Adds item at the beginning of the list """
        new head = Node(item)
        new_head.set_next(self._head)
        self. head = new head
    def size(self):
        """ Returns the size of the list """
        current = self. head
        count = 0
        while (current != None):
            current = current.get next()
            count += 1
        return count
    def search(self,item):
        """ Returns True if item is present in list, False otherwise
        current = self. head
        while (current != None):
            if (current.get data() == item):
                return True
            else:
                current = current.get next()
        return False
```

```
def remove(self, item):
        """ Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        current = self. head
        prev = None
        while (current != None):
            if (current.get data() == item):
                if prev == None: # we need to remove the head
                    self. head = current.get next()
                else:
                    prev.set_next(current.get next())
                    current = current.get next()
                return # Found, exits the function
            else:
                prev = current
                current = current.get next()
        raise Exception("Tried to remove a non existing item! Item was: " + str(item))
    def append(self, e):
        """ Appends element e to the end of the list.
            For this exercise you can write the O(n) version
        if self. head == None:
            self.add(e)
        else:
            current = self. head
            while (current.get next() != None):
                current = current.get next()
            current.set next(Node(e))
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, so list.ins
ert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equivalent to
 list.append(e).
            When i > list.size(), raises an Exception (default Python list appends instead to
the end :-/ )
        .....
        if (i < 0):
            raise Exception("Tried to insert at a negative index! Index was:" + str(i))
        count = 0
        current = self. head
        prev = None
        while (count < i and current != None):</pre>
            prev = current
            current = current.get next()
            count += 1
        if (current == None):
            if (count == i):
                self.append(e)
            else:
                raise Exception("Tried to insert outside the list ! "
                                 + "List size=" + str(count) + " insert position=" + str(i))
        else:
            #0 1
            # i
            if (prev == None):
                self.add(e)
            else:
```

```
new node = Node(e)
                prev.set next(new node)
                new node.set next(current)
   def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            If item is not found, raises an Exception.
        current = self. head
        count = 0
       while (current != None):
            if (current.get data() == e):
                return count
            else:
                current = current.get next()
                count += 1
        raise Exception("Couldn't find element " + str(e) )
    def pop(self):
        """ Remove the last item of the list, and return it.
            If the list is empty, an exception is raised.
        if (self. head == None):
            raise Exception("Tried to pop an empty list!")
       else:
            current = self. head
            if (current.get next() == None): # one element list
                last item = self. head.get data()
                self. head = None
                     # we have more than one element
            else:
                prev = None
                while current.get next() != None: # current will reach last element
                    prev = current
                    current = current.get next()
                last item = current.get data()
                prev.set next(None)
            return last item
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
   def test_init(self):
       ul = UnorderedList()
   def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
       ul.add('z')
        self.assertTrue('z' in str(ul))
        ul.add('w')
        self.assertTrue('z' in str(ul))
        self.assertTrue('w' in str(ul))
```

```
def test is empty(self):
    ul = UnorderedList()
    self.assertTrue(ul.is empty())
    ul.add('a')
    self.assertFalse(ul.is empty())
def test add(self):
    """ Remember 'add' adds stuff at the beginning of the list ! """
    ul = UnorderedList()
    self.assertEquals(ul.to python(), [])
    ul.add('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.add('a')
    self.assertEquals(ul.to python(), ['a', 'b'])
def test size(self):
    ul = UnorderedList()
    self.assertEquals(ul.size(), 0)
    ul.add("a")
    self.assertEquals(ul.size(), 1)
    ul.add("b")
    self.assertEquals(ul.size(), 2)
def test_search(self):
    ul = UnorderedList()
    self.assertFalse(ul.search("a"))
    ul.add("a")
    self.assertTrue(ul.search("a"))
    self.assertFalse(ul.search("b"))
    ul.add("b")
    self.assertTrue(ul.search("a"))
    self.assertTrue(ul.search("b"))
def test remove empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.remove('a')
def test remove one element(self):
    ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
    ul.remove('a')
    self.assertEquals(ul.to_python(), [])
def test remove two element(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['a'])
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove first occurrence(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('b')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.remove('b')
    self.assertEquals(ul.to_python(), [])
```

```
def test append(self):
    ul = UnorderedList()
    ul.append('a')
    self.assertEquals(ul.to_python(),['a'])
    ul.append('b')
    self.assertEquals(ul.to python(),['a', 'b'])
def test insert empty list zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a'])
def test insert empty list out of bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to_python(), ['a','b'])
def test_insert_one_element_list_after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to_python(), ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to_python(), ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    ul.insert(2,
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
    self.assertEquals(ul.index('b'), 0)
    with self.assertRaises(Exception):
        ul.index('a')
    ul.add('a')
    self.assertEquals(ul.index('a'),
    self.assertEquals(ul.index('b'),
def test pop empty(self):
    ul = UnorderedList()
```

```
with self.assertRaises(Exception):
        ul.pop()
def test pop one(self):
    ul = UnorderedList()
    ul.add('a')
    x = ul.pop()
    self.assertEquals('a', x)
def test pop two(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    x = ul.pop()
    self.assertEquals('b', x)
    self.assertEquals(ul.to python(), ['a'])
    y = ul.pop()
    self.assertEquals('a', y)
    self.assertEquals(ul.to python(), [])
```

```
In [12]:

algolab.run(UnorderedListTest)

......
Ran 23 tests in 0.039s

OK
```

UnorderedList v2 Solution

In [13]:

```
import unittest
class Node:
    """ A Node of an UnorderedList. Holds data provided by the user.
       Node v2 remains the same as Node v1
    def init (self,initdata):
        self. data = initdata
        self. next = None
    def get data(self):
        return self. data
    def get_next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set_next(self,newnext):
        self. next = newnext
class UnorderedList:
        a linked list implementation, v2.
        Improvements upon UnorderedList v1:
        * calculates size() in O(1)
        * calculates append() in O(1)
        * adds last() method to retrieve last element in O(1)
```

```
This class is slightly different from the one present in the book:

    has more pythonic names

            - tries to mimic more closely the behaviour of default Python list, raising except
ions on
              boundary conditions like removing non exisiting elements.
    def init (self):
        self. head = None
        self. size = 0 # NEW attribute ' size'
        self. last = None # NEW attribute ' last'
    def to python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very handy for
 testing.
        python list = []
        current = self. head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python list
    def
         _str__(self):
        For potentially complex data structures like this one, having a __str__ method is
essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        return self. head == None
    def add(self,item):
        """ Adds item at the beginning of the list """
        new head = Node(item)
        new head.set next(self. head)
        if self. head == None: # NEW
            self. last = new head # NEW
        self. head = new head
        self. size += 1 # NEW, we just return the field value. This is fast!
    def size(self):
        """ Returns the size of the list in O(1) """
        return self. size # NEW, we just return the field value. This is fast!
    def search(self,item):
        """ Returns True if item is present in list, False otherwise
        current = self. head
        while (current != None):
            if (current.get data() == item):
                return True
            else:
                current = current.get next()
        return False
    def remove(self, item):
```

```
""" Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        current = self. head
        prev = None
        while (current != None):
            if (current.get data() == item):
                if (self._last == current): # NEW
                     self. last = prev
                                              # NEW
                if prev == None: # we need to remove the head
                     self. head = current.get next()
                else:
                     prev.set next(current.get next())
                     current = current.get next()
                self._size -= 1 # NEW, need to update _size
return # Found, exits the function
            else:
                prev = current
                current = current.get next()
        raise Exception("Tried to remove a non existing item! Item was: " + str(item))
    def append(self, e):
        """ Appends element e to the end of the list, in O(1)
        if self. head == None:
            self.add(e)
        else:
            new node = Node(e)
            self. last.set next(new node) # NEW, we directly exploit last pointer
            self. last = new node # NEW, need to update last
            self. size += 1 # NEW, need to update size
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, so list.ins
ert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equivalent to
 list.append(e).
            When i > list.size(), raises an Exception (default Python list appends instead to
the end :-/)
        .....
        if (i < 0):
            raise Exception("Tried to insert at a negative index! Index was:" + str(i))
        count = 0
        current = self. head
        prev = None
        while (count < i and current != None):</pre>
            prev = current
            current = current.get next()
            count += 1
        if (current == None):
            if (count == i):
                self.append(e)
            else:
                raise Exception("Tried to insert outside the list ! "
                                 + "List size=" + str(count) + " insert position=" + str(i))
        else:
            #0 1
            # i
            if (prev == None):
```

```
self.add(e)
            else:
                new node = Node(e)
                prev.set next(new node)
                new node.set next(current)
                self. size += 1 # NEW, need to update size
    def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            If item is not found, raises an Exception.
        current = self. head
        count = 0
        while (current != None):
            if (current.get data() == e):
                return count
            else:
                current = current.get next()
                count += 1
        raise Exception("Couldn't find element " + str(e) )
    def pop(self):
        """ Remove the last item of the list, and return it.
            If the list is empty, an exception is raised.
        if (self. head == None):
            raise Exception("Tried to pop an empty list!")
        else:
            current = self. head
            if (current.get next() == None): # one element list
                popped = self. head
                self. head = None
                self._last = None # NEW
                    # we have more than one element
            else:
                prev = None
                while current.get next() != None: # current will reach last element
                    prev = current
                    current = current.get_next()
                popped = current
                self. last = prev
                                    # NEW
                prev.set next(None)
            self. size -= 1 # NEW
            return popped.get data()
    def last(self):
        """ Returns the last element in the list, in O(1).
            If list is empty, raises an Exception. Since v2.
        if (self._head == None):
            raise Exception("Tried to get the last element of an empty list!")
        else:
            return self. last.get data()
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList v2
       Test cases are improved by adding a new method myAssert(self, unordered list, python l
```

```
ist)
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
   def myAssert(self, unordered list, python list):
        """ Checks provided unordered list can be represented as the given python list. Since
v2
        self.assertEquals(unordered list.to python(), python list)
       # we check this new invariant about the size
        self.assertEquals(unordered list.size(), len(python list))
        # we check this new invariant about the last element
       if len(python list) != 0:
            self.assertEquals(unordered list.last(), python list[-1])
    def test init(self):
        ul = UnorderedList()
    def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
        ul.add('z')
        self.assertTrue('z' in str(ul))
        ul.add('w')
        self.assertTrue('z' in str(ul))
        self.assertTrue('w' in str(ul))
    def test is empty(self):
        ul = UnorderedList()
        self.assertTrue(ul.is empty())
        ul.add('a')
        self.assertFalse(ul.is empty())
    def test add(self):
        """ Remember 'add' adds stuff at the beginning of the list ! """
        ul = UnorderedList()
        self.myAssert(ul, [])
        ul.add('b')
        self.myAssert(ul, ['b'])
        ul.add('a')
        self.myAssert(ul, ['a', 'b'])
   def test size(self):
        ul = UnorderedList()
        self.assertEquals(ul.size(), 0)
       ul.add("a")
        self.assertEquals(ul.size(), 1)
        ul.add("b")
        self.assertEquals(ul.size(), 2)
   def test search(self):
        ul = UnorderedList()
        self.assertFalse(ul.search("a"))
        ul.add("a")
        self.assertTrue(ul.search("a"))
        self.assertFalse(ul.search("b"))
        ul.add("b")
        self.assertTrue(ul.search("a"))
        self.assertTrue(ul.search("b"))
    def test remove empty list(self):
        ul = UnorderedList()
       with self.assertRaises(Exception):
            ul.remove('a')
    def test_remove_one_element(self):
```

```
ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove two element(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to python(), ['a'])
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test remove first occurrence(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('b')
    with self.assertRaises(Exception):
        ul.remove('c')
    ul.remove('b')
    self.assertEquals(ul.to_python(), ['b'])
    ul.remove('b')
    self.assertEquals(ul.to python(), [])
def test append(self):
    ul = UnorderedList()
    ul.append('a')
    self.myAssert(ul,['a'])
    ul.append('b')
    self.myAssert(ul,['a', 'b'])
def test insert_empty_list_zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.myAssert(ul, ['a'])
def test insert empty list out of bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0,
    self.myAssert(ul, ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1, 'b')
    self.myAssert(ul, ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.myAssert(ul, ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
```

```
ul.add('c')
        ul.add('a')
        ul.insert(1, 'b')
        self.myAssert(ul, ['a','b', 'c'])
    def test insert two element list insert after(self):
        ul = UnorderedList()
        ul.add('b')
        ul.add('a')
        ul.insert(2, 'c')
        self.myAssert(ul, ['a','b', 'c'])
    def test index empty list(self):
        ul = UnorderedList()
        with self.assertRaises(Exception):
            ul.index('a')
    def test_index(self):
        ul = UnorderedList()
        ul.add('b')
        self.assertEquals(ul.index('b'), 0)
        with self.assertRaises(Exception):
            ul.index('a')
        ul.add('a')
        self.assertEquals(ul.index('a'), 0)
        self.assertEquals(ul.index('b'), 1)
    def test pop empty(self):
        ul = UnorderedList()
        with self.assertRaises(Exception):
            ul.pop()
    def test pop one(self):
        ul = UnorderedList()
        ul.add('a')
        x = ul.pop()
        self.assertEquals('a', x)
    def test pop two(self):
        ul = UnorderedList()
        ul.add('b')
        ul.add('a')
        x = ul.pop()
        self.assertEquals('b', x)
        self.myAssert(ul, ['a'])
        y = ul.pop()
        self.assertEquals('a', y)
        self.myAssert(ul, [])
    def test last(self):
        """ This tests only simple cases. More in-depth testing will be provided by calls to m
yAssert """
        ul = UnorderedList()
        with self.assertRaises(Exception):
            ul.last()
        ul.add('b')
        self.assertEquals(ul.last(), 'b')
        ul.add('a')
        self.assertEquals(ul.last(), 'b')
```

[n [14]:
algolab.run(UnorderedListTest)
Ran 24 tests in 0.030s
DK
[n [15]: