Algolab (index.html#Chapters) Out[1]: **Chapter 3: Data**

Structures

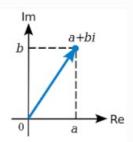
Chapter 3: Data Structures

class ComplexNumber

See theory here: http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/sp/s strutture.pdf) (First slides until class Fraction)

Let's try to define a complex number:

A complex number is a number that can be expressed in the form a + bi, where a and b are real numbers and i is the imaginary unit which satisfies the equation $i^2 = -1$. In this expression, a is the real part and b is the imaginary part of the complex number.



Complex number - Wikipedia https://en.wikipedia.org/wiki/Complex number

As the Fraction class, the ComplexNumber holds two values, in this case one for the real part and one for the imaginary one.

- Note each method takes as first import self argument. self will always be a reference to the object itself, and allows accessing its fields and methods
- self is not a keyword of Python, you could use any name you want for the first parameter, but it is much better to follow conventions and stick using self!
- Methods beginning and ending with double underscore '__' have often special meaning in Python: if you

In [2]:

```
see such a method around, it means it is overriding some default behaviour of Python
import unittest
import math
class ComplexNumber:
    def init (self, real, imaginary):
        self.real = real
        self.imaginary = imaginary
    def phase(self):
        """ Returns a float which is the phase (that is, the vector angle) of the co
mplex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        return math.atan2(self.imaginary, self.real)
    def log(self, base):
           Returns another ComplexNumber which is the logarithm of this complex num
ber
            This method is something we introduce by ourselves, according to the def
inition:
            (accomodated for generic base b)
```

```
https://en.wikipedia.org/wiki/Complex number#Natural logarithm
        11 11 11
        return ComplexNumber(math.log(self.real) / math.log(base), self.phase() / ma
th.log(base))
    def str (self):
        return str(self.real) + " + " + str(self.imaginary) + "i"
class ComplexNumberTest(unittest.TestCase):
    """ Test cases for ComplexNumber
         Note this is a *completely* separated class from ComplexNumber and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         ComplexNumber methods!
    11 11 11
    def test init(self):
        self.assertEqual(ComplexNumber(1,2).real, 1)
        self.assertEqual(ComplexNumber(1,2).imaginary, 2)
    def test phase(self):
            NOTE: we can't use assertEqual, as the result of phase() is a
            float number which may have floating point rounding errors. So it's
            necessary to use assertAlmostEqual
            As an option with the delta you can declare the precision you require.
            For more info see Python docs:
            https://docs.python.org/2/library/unittest.html#unittest.TestCase.assert
AlmostEqual
            NOTE: assertEqual might still work on your machine but just DO NOT use i
t
            for float numbers!!!
        .....
        self.assertAlmostEqual(ComplexNumber(0.0,1.0).phase(), math.pi / 2, delta=0.
001)
    def test str(self):
        self.assertEqual(str(ComplexNumber(1,2)), "1 + 2i")
        #self.assertEqual(str(ComplexNumber(1,0)), "1")
        #self.assertEqual(str(ComplexNumber(1.0,0)), "1.0")
        #self.assertEqual(str(ComplexNumber(0,1)), "i")
        #self.assertEqual(str(ComplexNumber(0,0)), "0")
    def test log(self):
        c = ComplexNumber(1.0, 1.0)
        l = c.log(math.e)
        self.assertAlmostEqual(l.real, 0.0, delta=0.001)
        self.assertAlmostEqual(l.imaginary, c.phase(), delta=0.001)
```

```
In [3]:
```

```
algolab.run(ComplexNumberTest)
```

Ran 4 tests in 0.009s

Once the init method is defined, we can create a ComplexNumber with a call like 'ComplexNumber(3,5)'

Notice in the constructor call we do not pass anything as self parameter (after all, we are creating the object)

In [4]:

```
my_complex = ComplexNumber(3,5)
```

We can now try to use one of the methods we defined:

In [5]:

```
phase = my_complex.phase()
print phase
```

1.03037682652

We can also pretty print the whole complex number. Internally, print function will look if the ComplexNumber has defined an __str__ method. If so, it will pass to the method the instance my_complex as the first argument, which in our methods will end up in the self parameter:

In [6]:

```
print my_complex
```

3 + 5i

We can also call methods that require a parameter like log(base). Notice that log function returns a ComplexNumber, and Python will automatically pretty print it for us.

In [7]:

```
logarithm = my_complex.log(math.e)
print logarithm
```

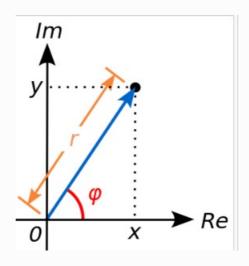
1.09861228867 + 1.03037682652i

Ok, now we are ready to define our own stuff.

Complex numbers magnitude

The absolute value (or modulus or magnitude) of a complex number z = x + yi is

$$r = |z| = \sqrt{x^2 + y^2}.$$



Implement the magnitude method, using this signature:

Complex numbers equality

Here we will try to give you a glimpse of some aspects related to Python equality, and trying to respect interfaces when overriding methods. Equality can be a nasty subject, here we will treat it in a simplified form.

Equality [edit]

Two complex numbers are equal if and only if both their real and imaginary parts are equal. In symbols:

$$z_1=z_2 \ \leftrightarrow \ (\operatorname{Re}(z_1)=\operatorname{Re}(z_2) \ \wedge \ \operatorname{Im}(z_1)=\operatorname{Im}(z_2)).$$

• Implement equality for ComplexNumber more or less as it was done for Fraction

Use this method signature:

```
def eq (self, other):
```

and use this simple test case to check for equality:

- Beware 'equality' is tricky in Python for float numbers! Rule of thumb: when overriding __eq__, use 'dumb' equality, two things are the same only if their parts are literally equal
- If instead you need to determine if two objects are similar, define other 'closeness' functions.
- (Non mandatory read) if you are interested in the gory details of equality, see
 - How to Override comparison operators in Python (http://icalderone.livejournal.com/32837.html)
 - Messing with hashing (http://www.asmeurer.com/blog/posts/what-happens-when-you-mess-with-hashing-in-python/)

Complex numbers isclose

Complex numbers can be represented as vectors, so intuitively we can determine if a complex number is close to another by checking that the distance between its vector tip and the the other tip is less than a given delta. There are more precise ways to calculate it, but here we prefer keeping the example simple.

Given two complex numbers

$$z_1 = a + bi$$

and

$$z_2 = c + di$$

We can consider them as close if they satisfy this condition:

$$\sqrt{(a-c)^2 + (b-d)^2} < delta$$

• Implement the method, adding it to ComplexNumber class:

def isclose(self, c, delta):
 """ Returns True if the complex number is within a delta distance fro
m complex number c.

raise Exception("TODO Implement me!")

and add this test case to ComplexNumberTest class:

REMEMBER: Equality with __eq__ and closeness functions like isclose are very different things. Equality should check if two objects have the same memory address or, alternatively, if they contain the same things, while closeness functions should check if two objects are similar. You should never use functions like isclose inside __eq__ methods, unless you really know what you're doing.

Complex numbers addition

Complex numbers are added by separately adding the real and imaginary parts of the summands.

That is to say:

$$(a+bi) + (c+di) = (a+c) + (b+d)i.$$

Similarly, subtraction is defined by

$$(a+bi)-(c+di)=(a-c)+(b-d)i.$$

- a and c correspond to real, b and d correspond to imaginary
- implement addition for ComplexNumber more or less as it was done for Fraction in theory slides
- write some tests as well!

Use this definition:

```
def __add__(self, other):
    raise Exception("TODO implement me!")
```

And add this to the ComplexNumberTest class:

Adding a scalar

We defined addition among ComplexNumbers, but what about addition among a ComplexNumber and an int or a float?

Will this work?

ComplexNumber(3,4) + 5

What about this?

ComplexNumber(3,4) + 5.0

Try to add the following method to your class, and check if it does work with the scalar:

In [9]:

```
def __add__(self, other):
    # checks other object is instance of the class ComplexNumber
    if isinstance(other, ComplexNumber):
        return ComplexNumber(self.real + other.real, self.imaginary + other.imaginary)

# else checks the basic type of other is int or float
    elif type(other) is int or type(other) is float:
        return ComplexNumber(self.real + other, self.imaginary)

# other is of some type we don't know how to process.
# In this case the Python specs say we MUST return 'NotImplemented'
    else:
        return NotImplemented
```

Hopefully now you have a better add. But what about this? Will this work?

```
5 + ComplexNumber(3,4)
```

Answer: it won't, Python needs further instructions. Usually Python tries to see if the class of the object on left of the expression defines addition for operands to the right of it. In this case on the left we have a float number, and float numbers don't define any way to deal to the right with your very own ComplexNumber class. So as a last resort Python tries to see if your ComplexNumber class has defined also a way to deal with operands to the left of the ComplexNumber, by looking for the method __radd__, which means reverse addition. Here we implement it

```
def __radd__(self, other):
    """ Returns the result of expressions like other + self
    if (type(other) is int or type(other) is float):
        return ComplexNumber(self.real + other, self.imaginary)
    else:
        return NotImplemented
```

To check it is working and everything is in order for addition, add these test cases:

Multiplication and division [edit]

The multiplication of two complex numbers is defined by the following formula:

$$(a+bi)(c+di) = (ac-bd) + (bc+ad)i.$$

In particular, the square of the imaginary unit is -1:

$$i^2 = i \times i = -1$$
.

- Implement multiplication for ComplexNumber, usintaking inspiration from previous __add__ implementation
- Can you extend multiplication to work with scalars (both left and right) as well?

To implement mul , copy this definition into ComplexNumber class:

```
def __mul__(self, other):
    raise Exception("TODO Implement me!")
```

and add test cases to ComplexNumberTest class:

Stack

Stack theory

See theory here: http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (Slide 46)

See stack definition on the book

(http://interactivepython.org/runestone/static/pythonds/BasicDS/WhatisaStack.html)

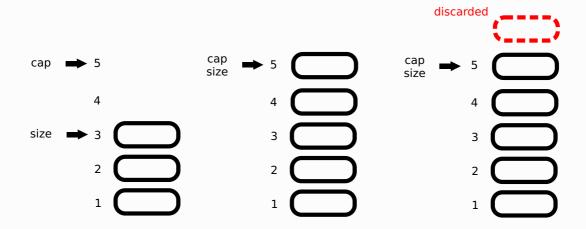
and following sections:

- Stack Abstract Data Type
 - (http://interactivepython.org/runestone/static/pythonds/BasicDS/TheStackAbstractDataType.html)
- Implementing a Stack in Python
 - (http://interactivepython.org/runestone/static/pythonds/BasicDS/ImplementingaStackinPython.html)
- Simple Balanced Parenthesis
 - (http://interactivepython.org/runestone/static/pythonds/BasicDS/SimpleBalancedParentheses.html)
- <u>Balanced Symbols a General Case</u>
 (http://interactivepython.org/runestone/static/pythonds/BasicDS/BalancedSymbols(AGeneralCase).html)

On slide 46 of theory (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf (Slide 46) there is the pseudo code for a version of stack we will call CappedStack:

```
STACK
ITEM[]A
                              % Elements
                                                ITEM peek()
int size
                           % Current size
                                                   if size > 0 then
                                                    | return A[size]
int cap
                        % Maximum size
STACK Stack(int \ dim)
                                                ITEM pop()
   Stack t \leftarrow \mathbf{new} Stack
                                                   if size > 0 then
   t.A \leftarrow \mathbf{new\ int}[1\dots dim]
                                                       ITEM t \leftarrow A[size]
   t.cap \leftarrow dim
                                                       size \leftarrow size - 1
   t.size \leftarrow 0
                                                       return t
   return t
                                                push(ITEM v)
boolean isEmpty()
                                                   if size < cap then
  return size = 0
                                                       size \leftarrow size + 1
                                                       A[size] \leftarrow v
int size()
   return size
```

A capped stack has a limit called *cap* over which elements are discarded:



- Copy the following skeleton and unit tests, and then implement the pseudo code
- Name internal variables that you don't want to expose to class users by prepending them with one
 underscore '_', like _elements or _cap.
 - The underscore is just a convention, class users will still be able to get internal variables by accessing them with field accessors like mystack._elements.
 - If users manipulate private fields and complain something is not working, you can tell them it's their fault!
- This time, we will try to write a little more robust code. In general, when implementing pseudocode you
 might need to think more about boundary cases. In this case, we add the additional constraint that if you
 pass to the stack a negative or zero cap, your class initalization is expected to fail and raise an
 AssertionError. Such error can be raised by commands like assert my_condition where
 my_condition is False
- For easier inspection of the stack, implement also an _str__ method so that calls to print show text like CappedStack: cap=4 elements=['a', 'b']

Notice that:

- We tried to use <u>more pythonic names (https://www.python.org/dev/peps/pep-0008/#id45)</u> for methods, so for example isEmpty was renamed to is empty
- In this case, when this stack reaches cap size, successive push requests silently exit without raising
 errors. Other implementations might raise an error and stop excecution when trying to push over on
 already filled stack.
- In this case, when this stack is required to pop or peek, if it is empty the functions will not return anything. During the Python translation, we might not return anything as well and relying on Python implicitly returning None.
- pop will both modify the stack and return a value

```
import unittest
class CappedStack:
          _init__(self, cap):
        """ Creates a CappedStack capped at cap. Cap must be > 0, otherwise an Asser
tionError is thrown
        raise Exception("TODO Implement me!")
    def size(self):
        raise Exception("TODO Implement me!")
    def is empty(self):
        raise Exception("TODO Implement me!")
    def pop(self):
        raise Exception("TODO Implement me!")
    def peek(self):
        raise Exception("TODO Implement me!")
    def push(self, item):
        raise Exception("TODO Implement me!")
    def cap(self):
        """ Returns the cap of the stack
        raise Exception("TODO Implement me!")
class CappedStackTest(unittest.TestCase):
    """ Test cases for CappedStackTest
         Note this is a *completely* separated class from CappedStack and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         CappedStack methods!
    .....
    def test init wrong cap(self):
            We use the special construct 'self.assertRaises(AssertionError)' to stat
е
            we are expecting the calls to CappedStack(0) and CappedStack(-1) to rais
e
            an AssertionError.
        with self.assertRaises(AssertionError):
            CappedStack(0)
        with self.assertRaises(AssertionError):
            CappedStack(-1)
    def test cap(self):
        self.assertEqual(CappedStack(1).cap(), 1)
        self.assertEqual(CappedStack(2).cap(), 2)
    def test size(self):
        s = CappedStack(5)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
```

```
s.pop()
    self.assertEqual(s.size(), 0)
def test is empty(self):
    s = CappedStack(5)
    self.assertTrue(s.is_empty())
    s.push("a")
    self.assertFalse(s.is_empty())
def test pop(self):
    s = CappedStack(5)
    self.assertEqual(s.pop(), None)
    s.push("a")
    self.assertEqual(s.pop(), "a")
    self.assertEqual(s.pop(), None)
def test peek(self):
    s = \overline{CappedStack(5)}
    self.assertEqual(s.peek(), None)
    s.push("a")
    self.assertEqual(s.peek(), "a")
    self.assertEqual(s.peek(), "a")
                                      # testing peek is not changing the stack
    self.assertEqual(s.size(), 1)
def test push(self):
    s = \overline{CappedStack(2)}
    self.assertEqual(s.size(), 0)
    s.push("a")
    self.assertEqual(s.size(), 1)
    s.push("b")
    self.assertEqual(s.size(), 2)
    self.assertEqual(s.peek(), "b")
    s.push("c") # capped, pushing should do nothing now!
    self.assertEqual(s.size(), 2)
    self.assertEqual(s.peek(), "b")
def test str(self):
    s = CappedStack(4)
    s.push("a")
    s.push("b")
    print s
```

UnorderedList

UnorderedList Theory

An UnorderedList for us is a linked list starting with a pointer called *head* that points to the first Node (if the list is empty the pointer points to None). Think of the list as a chain where each Node can contain some data retriavable with Node.get_data() method and you can access one Node at a time by calling the method Node.get next() on each node.

- See theory slides (http://disi.unitn.it/~montreso/sp/slides/04-strutture.pdf) from slide 25 (Monodirectional list)
- See <u>UnorderedList Abstract Data Type</u> (http://interactivepython.org/runestone/static/pythonds/BasicDS/TheUnorderedListAbstractDataType.html) on the book
- See <u>Implementing UnorderedListLinkedLists</u>
 (http://interactivepython.org/runestone/static/pythonds/BasicDS/ImplementinganUnorderedListLinkedLists.html)
 on the book

UnorderedList Exercises

Commandment: You shall also draw lists on paper, helps a lot avoiding mistakes

- 1. Copy the following skeleton and unit tests, and then implement the missing methods
 - This time there is no pseudo code, you should rely solely on theory from the slides and book, method definitions and your intuition
 - Pay close attention to the comments below each method definition, especially for boundary cases

Notice that there are a few differences with the book:

- We don't assume the list has all different values
- We used more pythonic names (https://www.python.org/dev/peps/pep-0008/#id45) for properties and methods, so for example private attribute Node.data was renamed to Node. data and accessor method Node.getData() was renamed to Node.get_data(). There are nicer ways to handle these kind of getters/setters pairs called 'properties' but we won't address them here.
- In boundary cases like removing a non-existing element we prefer to raise an exception with the command

```
raise Exception("Some error occurred!")
```

In general, this is the behaviour you also find in regular Python lists.

- 2. Once you're done implementing the methods, implement an append method that works in O(1), by using an additional pointer in the data structure
- 3. Once you're done with previous points, copy the file you have into a new file, and rename the class into BidirectionalList.
 - A. Add to Node backlinks by adding the attribute _prev and methods get_prev(self) and set_prev(self, pointer). Then update all BidirectionalList methods to take into account you now have backlinks. Take particular care for the boundary cases when the list is empty, has one element, or for nodes at the head and at the tail of the list.
 - B. Implement this method in O(n) by using the newly added backlinks:

Make sure this test pass:

```
def test_to_python_reversed(self):
        ul = UnorderedList()
        ul.add('c')
        ul.add('b')
        ul.add('a')
        pr = ul.to_python()
        pr.reverse() # we are reversing pr with Python's 'reverse()' method
        self.assertEquals(pr, ul.to python reversed())
```

UnorderedList Code Skeleton

```
In [12]:
```

```
class Node:
    def __init__(self,initdata):
        self._data = initdata
        self._next = None

def get_data(self):
    return self._data
```

```
def get next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set next(self,newnext):
        self. next = newnext
class UnorderedList:
        This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, rais
ing exceptions on
              boundary conditions like removing non exisiting elements.
    11 11 11
    def init (self):
        self. head = None
    def to python(self):
        "" Returns this UnorderedList as a regular Python list. This method is very
 handy for testing.
        python_list = []
        current = self. head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python list
        __str__(self):
        """ For potentially complex data structures like this one, having a __str__
method is essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        "" Returns True if the list has no nodes, True otherwise """
        raise Exception("TODO implement me!")
    def add(self,item):
        """ Adds item at the beginning of the list """
        raise Exception("TODO implement me!")
    def size(self):
        """ Returns the size of the list """
        raise Exception("TODO implement me!")
```

```
qet search(sett,item):
        """ Returns True if item is present in list, False otherwise
        raise Exception("TODO implement me!")
    def remove(self, item):
        """ Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        raise Exception("TODO implement me!")
    def append(self, e):
        """ Appends element e to the end of the list.
            For this exercise you can write the O(n) version
        11 11 11
        raise Exception("TODO implement me!")
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, s
o list.insert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equ
ivalent to list.append(e).
            When i > list.size(), raises an Exception (default Python list appends i
nstead to the end :-/ )
        11 11 11
        raise Exception("TODO implement me!")
    def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            It is an error if there is no such item.
        raise Exception("TODO implement me!")
    def pop(self):
        """ Remove the item at the given position in the list, and return it.
            If the list is empty, an exception is raised.
        raise Exception("TODO implement me!")
class UnorderedListTest(unittest.TestCase):
    """ Test cases for UnorderedList
         Note this is a *completely* separated class from UnorderedList and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         UnorderedList methods!
    11 11 11
    def test init(self):
        ul = UnorderedList()
    def test str(self):
        ul = UnorderedList()
        self.assertTrue('UnorderedList' in str(ul))
        ul.add('z')
        self.assertTrue('z' in str(ul))
```

```
ul.add('w')
    self.assertTrue('z' in str(ul))
    self.assertTrue('w' in str(ul))
def test is empty(self):
    ul = UnorderedList()
    self.assertTrue(ul.is empty())
    ul.add('a')
    self.assertFalse(ul.is empty())
def test add(self):
    """ Remember 'add' adds stuff at the beginning of the list ! """
    ul = UnorderedList()
    self.assertEquals(ul.to python(), [])
    ul.add('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.add('a')
    self.assertEquals(ul.to python(), ['a', 'b'])
def test size(self):
    ul = UnorderedList()
    self.assertEquals(ul.size(), 0)
    ul.add("a")
    self.assertEquals(ul.size(), 1)
    ul.add("b")
    self.assertEquals(ul.size(), 2)
def test search(self):
    ul = UnorderedList()
    self.assertFalse(ul.search("a"))
    ul.add("a")
    self.assertTrue(ul.search("a"))
    self.assertFalse(ul.search("b"))
    ul.add("b")
    self.assertTrue(ul.search("a"))
    self.assertTrue(ul.search("b"))
def test_remove_empty_list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.remove('a')
def test remove one element(self):
    ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
    ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test append(self):
    ul = UnorderedList()
    ul.append('a')
    self.assertTrue(ul.to python(),['a'])
    ul.append('b')
    self.assertTrue(ul.to python(),['a', 'b'])
def test insert empty list zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.assertEquals(ul.to_python(), ['a'])
def test_insert_empty_list_out_of_bounds(self):
```

```
ut = unoraerealist()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    ul.insert(2, 'c')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
    self.assertEquals(ul.index('b'),
    with self.assertRaises(Exception):
        ul.index('a')
    ul.add('a')
    self.assertEquals(ul.index('a'),
    self.assertEquals(ul.index('b'),
def test pop empty(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.pop()
def test pop one(self):
    ul = UnorderedList()
    ul.add('a')
    x = ul.pop()
```

```
def test_pop_two(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    x = ul.pop()
    self.assertEquals('a', x)
    self.assertEquals(ul.to_python(), ['b'])
    y = ul.pop()
    self.assertEquals('b', y)
    self.assertEquals(ul.to_python(), [])
```

Solutions

ComplexNumber Solution

```
In [13]:
import unittest
import math
class ComplexNumber:
    def init (self, real, imaginary):
        self.real = real
        self.imaginary = imaginary
   def str (self):
        return str(self.real) + " + " + str(self.imaginary) + "i"
    def phase(self):
        """ Returns a float which is the phase (that is, the vector angle) of the co
mplex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        return math.atan2(self.imaginary, self.real)
    def log(self, base):
        """ Returns another ComplexNumber which is the logarithm of this complex num
ber
            This method is something we introduce by ourselves, according to the def
inition:
            (accomodated for generic base b)
            https://en.wikipedia.org/wiki/Complex number#Natural logarithm
        return ComplexNumber(math.log(self.real) / math.log(base), self.phase() / ma
th.log(base))
    def magnitude(self):
        """ Returns a float which is the magnitude (that is, the absolute value) of
the complex number
            This method is something we introduce by ourselves, according to the def
inition:
            https://en.wikipedia.org/wiki/Complex number#Absolute value and argument
        11 11 11
```

```
return math.sqrt(self.real**2 + self.imaginary**2)
    def eq (self, other):
        return self.real == other.real and self.imaginary == other.imaginary
   def isclose(self, c, delta):
        """ Returns True if the complex number is within a delta distance from compl
ex number c.
        return math.sqrt((self.real-c.real)**2 + (self.imaginary-c.imaginary)**2) <</pre>
delta
   def add (self, other):
        if isinstance(other, ComplexNumber):
            return ComplexNumber(self.real + other.real, self.imaginary + other.imagi
nary)
        elif type(other) is int or type(other) is float:
            return ComplexNumber(self.real + other, self.imaginary)
        else:
            return NotImplemented
         radd (self, other):
        if (type(other) is int or type(other) is float):
            return ComplexNumber(self.real + other, self.imaginary)
            return NotImplemented
    def mul (self, other):
        if isinstance(other, ComplexNumber):
            return ComplexNumber(self.real * other.real - self.imaginary * other.ima
ginary,
                                 self.imaginary * other.real + self.real * other.ima
ginary)
        elif type(other) is int or type(other) is float:
            return ComplexNumber(self.real * other, self.imaginary * other)
        else:
            return NotImplemented
         rmul (self, other):
        if (type(other) is int or type(other) is float):
            return ComplexNumber(self.real * other, self.imaginary * other)
        else:
            return NotImplemented
class ComplexNumberTest(unittest.TestCase):
    """ Test cases for ComplexNumber
         Note this is a *completely* separated class from ComplexNumber and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         ComplexNumber methods!
    def test init(self):
        self.assertEqual(ComplexNumber(1,2).real, 1)
        self.assertEqual(ComplexNumber(1,2).imaginary, 2)
    def test_phase(self):
```

```
NOTE: we can't use assertEqual, as the result of phase() is a
            float number which may have floating point rounding errors. So it's
            necessary to use assertAlmostEqual
            As an option with the delta you can declare the precision you require.
            For more info see Python docs:
            https://docs.python.org/2/library/unittest.html#unittest.TestCase.assert
AlmostEqual
            NOTE: assertEqual might still work on your machine but just DO NOT use i
t
            for float numbers!!!
        self.assertAlmostEqual(ComplexNumber(0.0,1.0).phase(), math.pi / 2, delta=0.
001)
   def test str(self):
        self.assertEqual(str(ComplexNumber(1,2)), "1 + 2i")
        #self.assertEqual(str(ComplexNumber(1,0)), "1")
       #self.assertEqual(str(ComplexNumber(1.0,0)), "1.0")
       #self.assertEqual(str(ComplexNumber(0,1)), "i")
        #self.assertEqual(str(ComplexNumber(0,0)), "0")
    def test log(self):
        c = ComplexNumber(1.0, 1.0)
        l = c.log(math.e)
        self.assertAlmostEqual(l.real, 0.0, delta=0.001)
        self.assertAlmostEqual(l.imaginary, c.phase(), delta=0.001)
    def test magnitude(self):
        self.assertAlmostEqual(ComplexNumber(3.0,4.0).magnitude(),5, delta=0.001)
    def test integer equality(self):
            Note all other tests depend on this test!
            We want also to test the constructor, so in c we set stuff by hand
        c = ComplexNumber(0,0)
        c.real = 1
        c.imaginary = 2
        self.assertEquals(c, ComplexNumber(1,2))
    def test isclose(self):
        """ Notice we use `assertTrue` because we expect `isclose` to return a `boo
l` value, and
             we also test a case where we expect `False`
        self.assertTrue(ComplexNumber(1.0,1.0).isclose(ComplexNumber(1.0,1.1), 0.2))
        self.assertFalse(ComplexNumber(1.0,1.0).isclose(ComplexNumber(10.0,10.0), 0.
2))
   def test add zero(self):
        self.assertEquals(ComplexNumber(1,2) + ComplexNumber(0,0), ComplexNumber(1,2)
));
    def test add numbers(self):
        self.assertEquals(ComplexNumber(1,2) + ComplexNumber(3,4), ComplexNumber(4,6
));
    def test add scalar right(self):
```

```
Selt.assertEquals(ComplexNumber(1,2) + 3, ComplexNumber(4,2));
    def test add scalar left(self):
        self.assertEquals(3 + ComplexNumber(1,2), ComplexNumber(4,2));
    def test add negative(self):
        self.assertEquals(ComplexNumber(-1,0) + ComplexNumber(0,-1), ComplexNumber(-
1,-1));
    def test mul by zero(self):
        self.assertEquals(ComplexNumber(0,0) * ComplexNumber(1,2), ComplexNumber(0,0
));
    def test mul just real(self):
        self.assertEquals(ComplexNumber(1,0) * ComplexNumber(2,0), ComplexNumber(2,0)
));
    def test mul just imaginary(self):
        self.assertEquals(ComplexNumber(0,1) * ComplexNumber(0,2), ComplexNumber(-2,
0));
    def test mul scalar right(self):
        self.assertEquals(ComplexNumber(1,2) * 3, ComplexNumber(3,6));
    def test mul scalar left(self):
        self.assertEquals(3 * ComplexNumber(1,2), ComplexNumber(3,6));
```

In [14]:

```
algolab.run(ComplexNumberTest)
```

Ran 17 tests in 0.027s

0K

Stack Solution

In [15]:

```
import unittest
class CappedStack:
         init (self, cap):
    def
        """ Creates a CappedStack capped at cap.
            Cap must be > 0, otherwise an AssertionError is thrown
        assert cap > 0
        # notice we assign to variables with underscore to respect Python convention
S
        self. cap = cap
       # notice with use elements instead of the A in the pseudocode, because it i
S
       # clearer, starts with underscore, and capital letters are usual reserved
        # for classes or constants
        self. elements = []
    def size(self):
                  /colf olomon+cl
```

```
return ten(sett._etements)
    def is empty(self):
        return len(self. elements) == 0
    def pop(self):
        if (len(self. elements) > 0):
            return self._elements.pop()
        # else: implicitly, Python will return None
    def peek(self):
        if (len(self._elements) > 0):
            return self. elements[-1]
        # else: implicitly, Python will return None
    def push(self, item):
        if (len(self. elements) < self._cap):</pre>
            self. elements.append(item)
        # else fail silently
    def cap(self):
        """ Returns the cap of the stack
        return self. cap
    def str (self):
        return "CappedStack: cap=" + str(self. cap) + " elements=" + str(self. eleme
nts)
class CappedStackTest(unittest.TestCase):
    """ Test cases for CappedStackTest
         Note this is a *completely* separated class from CappedStack and
         we declare it here just for testing purposes!
         The 'self' you see here have nothing to do with the selfs from the
         CappedStack methods!
    def test init wrong cap(self):
            We use the special construct 'self.assertRaises(AssertionError)' to stat
е
            we are expecting the calls to CappedStack(0) and CappedStack(-1) to rais
e
            an AssertionError.
        with self.assertRaises(AssertionError):
            CappedStack(0)
        with self.assertRaises(AssertionError):
            CappedStack(-1)
    def test_cap(self):
        self.assertEqual(CappedStack(1).cap(), 1)
        self.assertEqual(CappedStack(2).cap(), 2)
    def test size(self):
        s = CappedStack(5)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.pop()
               contEqual(c circ() 0)
```

```
Sett.assertEquat(s.size(), 0)
    def test is empty(self):
        s = CappedStack(5)
        self.assertTrue(s.is empty())
        s.push("a")
        self.assertFalse(s.is empty())
    def test pop(self):
        s = CappedStack(5)
        self.assertEqual(s.pop(), None)
        s.push("a")
        self.assertEqual(s.pop(), "a")
        self.assertEqual(s.pop(), None)
    def test peek(self):
        s = CappedStack(5)
        self.assertEqual(s.peek(), None)
        s.push("a")
        self.assertEqual(s.peek(), "a")
        self.assertEqual(s.peek(), "a") # testing peek is not changing the stack
        self.assertEqual(s.size(), 1)
    def test push(self):
        s = CappedStack(2)
        self.assertEqual(s.size(), 0)
        s.push("a")
        self.assertEqual(s.size(), 1)
        s.push("b")
        self.assertEqual(s.size(), 2)
        self.assertEqual(s.peek(), "b")
        s.push("c") # capped, pushing should do nothing now!
        self.assertEqual(s.size(), 2)
        self.assertEqual(s.peek(), "b")
    def test str(self):
        s = CappedStack(4)
        s.push("a")
        s.push("b")
        print s
In [16]:
```

```
algolab.run(CappedStackTest)
.....
CappedStack: cap=4 elements=['a', 'b']
....
Ran 8 tests in 0.017s
OK
```

UnorderedList Solution

```
In [17]:
```

```
class Node:
    def __init__(self,initdata):
        self._data = initdata
        self._next = None

def get_data(self):
```

```
return self._data
    def get next(self):
        return self. next
    def set data(self,newdata):
        self. data = newdata
    def set next(self,newnext):
        self. next = newnext
class UnorderedList:
        This class is slightly different from the one present in the book:
            - has more pythonic names
            - tries to mimic more closely the behaviour of default Python list, rais
ing exceptions on
              boundary conditions like removing non exisiting elements.
    .....
    def
         init (self):
        self. head = None
    def to python(self):
        """ Returns this UnorderedList as a regular Python list. This method is very
 handy for testing.
        python list = []
        current = self. head
        while (current != None):
            python list.append(current.get data())
            current = current.get next()
        return python list
         str (self):
        """ For potentially complex data structures like this one, having a __str__
method is essential to
            quickly inspect the data by printing it.
        current = self. head
        strings = []
        while (current != None):
            strings.append(str(current.get data()))
            current = current.get next()
        return "UnorderedList: " + ",".join(strings)
    def is empty(self):
        return self._head == None
    def add(self,item):
        """ Adds item at the beginning of the list """
        new head = Node(item)
        new head.set next(self. head)
        self._head = new_head
    def size(self):
        """ Returns the size of the list """
        current = self. head
        count = 0
```

```
while (current != None):
            current = current.get next()
            count += 1
        return count
    def search(self,item):
        """ Returns True if item is present in list, False otherwise
        current = self. head
       while (current != None):
            if (current.get data() == item):
                return True
            else:
                current = current.get next()
        return False
    def remove(self, item):
        """ Removes first occurrence of item from the list
            If item is not found, raises an Exception.
        current = self. head
        prev = None
       while (current != None):
            if (current.get data() == item):
                if prev == None: # we need to remove the head
                    self._head = current.get_next()
                else:
                    prev.set_next(current.get next())
                    current = current.get next()
                return # Found, exits the function
            else:
                prev = current
                current = current.get next()
        raise Exception("Tried to remove a non existing item! Item was: " + str(item
))
    def append(self, e):
        """ Appends element e to the end of the list.
           For this exercise you can write the O(n) version
        if self. head == None:
            self.add(e)
        else:
            current = self. head
           while (current.get_next() != None):
                current = current.get next()
            current.set next(Node(e))
    def insert(self, i, e):
        """ Insert an item at a given position.
            The first argument is the index of the element before which to insert, s
o list.insert(0, e)
            inserts at the front of the list, and list.insert(list.size(), e) is equ
ivalent to list.append(e).
           When i > list.size(), raises an Exception (default Python list appends i
```

```
nstead to the end :-/ )
        11 11 11
        if (i < 0):
            raise Exception("Tried to insert at a negative index! Index was:" + str(
i))
        count = 0
        current = self. head
        prev = None
        while (count < i and current != None):</pre>
            prev = current
            current = current.get next()
            count += 1
        if (current == None):
            if (count == i):
                self.append(e)
            else:
                raise Exception("Tried to insert outside the list ! "
                                 + "List size=" + str(count) + " insert position=" +
 str(i))
        else:
            #0 1
            # i
            if (prev == None):
                self.add(e)
            else:
                new node = Node(e)
                prev.set next(new node)
                new node.set next(current)
    def index(self, e):
        """ Return the index in the list of the first item whose value is x.
            It is an error if there is no such item.
        current = self. head
        count = 0
        while (current != None):
            if (current.get data() == e):
                return count
            else:
                current = current.get next()
                count += 1
        raise Exception("Couldn't find element " + str(e) )
    def pop(self):
        """ Remove the item at the given position in the list, and return it.
            If the list is empty, an exception is raised.
        if (self. head == None):
            raise Exception("Tried to pop an empty list!")
            head_item = self._head.get_data()
            self. head = self. head.get next()
            return head item
class UnorderedListTest(unittest.TestCase):
```

```
Note this is a *completely* separated class from UnorderedList and
     we declare it here just for testing purposes!
     The 'self' you see here have nothing to do with the selfs from the
     UnorderedList methods!
def test init(self):
    ul = UnorderedList()
def test str(self):
    ul = UnorderedList()
    self.assertTrue('UnorderedList' in str(ul))
    ul.add('z')
    self.assertTrue('z' in str(ul))
    ul.add('w')
    self.assertTrue('z' in str(ul))
    self.assertTrue('w' in str(ul))
def test_is_empty(self):
    ul = UnorderedList()
    self.assertTrue(ul.is_empty())
    ul.add('a')
    self.assertFalse(ul.is empty())
def test add(self):
    """ Remember 'add' adds stuff at the beginning of the list! """
    ul = UnorderedList()
    self.assertEquals(ul.to python(), [])
    ul.add('b')
    self.assertEquals(ul.to python(), ['b'])
    ul.add('a')
    self.assertEquals(ul.to python(), ['a', 'b'])
def test size(self):
    ul = UnorderedList()
    self.assertEquals(ul.size(), 0)
    ul.add("a")
    self.assertEquals(ul.size(), 1)
    ul.add("b")
    self.assertEquals(ul.size(), 2)
def test search(self):
    ul = UnorderedList()
    self.assertFalse(ul.search("a"))
    ul.add("a")
    self.assertTrue(ul.search("a"))
    self.assertFalse(ul.search("b"))
    ul.add("b")
    self.assertTrue(ul.search("a"))
    self.assertTrue(ul.search("b"))
def test remove empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.remove('a')
def test_remove_one_element(self):
    ul = UnorderedList()
    ul.add('a')
    with self.assertRaises(Exception):
        ul.remove('b')
```

""" rest cases for unorgerealist

```
ul.remove('a')
    self.assertEquals(ul.to python(), [])
def test append(self):
    ul = UnorderedList()
    ul.append('a')
    self.assertTrue(ul.to python(),['a'])
    ul.append('b')
    self.assertTrue(ul.to python(),['a', 'b'])
def test insert empty list zero(self):
    ul = UnorderedList()
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a'])
def test insert empty list out of bounds(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.insert(1, 'a')
    with self.assertRaises(Exception):
        ul.insert(-1, 'a')
def test insert one element list before(self):
    ul = UnorderedList()
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert one element list after(self):
    ul = UnorderedList()
    ul.add('a')
    ul.insert(1,
                 'b')
    self.assertEquals(ul.to python(), ['a','b'])
def test insert two element list insert before(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('b')
    ul.insert(0, 'a')
    self.assertEquals(ul.to python(), ['a','b','c'])
def test insert two element list insert middle(self):
    ul = UnorderedList()
    ul.add('c')
    ul.add('a')
    ul.insert(1, 'b')
    self.assertEquals(ul.to python(), ['a','b', 'c'])
def test insert two element list insert after(self):
    ul = UnorderedList()
    ul.add('b')
    ul.add('a')
    ul.insert(2, 'c')
    self.assertEquals(ul.to_python(), ['a','b', 'c'])
def test index empty list(self):
    ul = UnorderedList()
    with self.assertRaises(Exception):
        ul.index('a')
def test index(self):
    ul = UnorderedList()
    ul.add('b')
              +Equalatul inday(tht) 0)
```

```
sett.assertEquals(ut.index('p'), 0)
        with self.assertRaises(Exception):
            ul.index('a')
        ul.add('a')
        self.assertEquals(ul.index('a'),
        self.assertEquals(ul.index('b'),
                                           1)
    def test_pop_empty(self):
        ul = UnorderedList()
        with self.assertRaises(Exception):
            ul.pop()
    def test pop one(self):
        ul = UnorderedList()
        ul.add('a')
        x = ul.pop()
        self.assertEquals('a', x)
    def test pop two(self):
        ul = UnorderedList()
        ul.add('b')
        ul.add('a')
        x = ul.pop()
        self.assertEquals('a', x)
        self.assertEquals(ul.to python(), ['b'])
        y = ul.pop()
        self.assertEquals('b', y)
        self.assertEquals(ul.to_python(), [])
In [18]:
algolab.run(UnorderedListTest)
Ran 21 tests in 0.036s
0K
```

In [19]: