

Test

Problem J4/S2: Fraction Action

Many advanced calculators have a fraction feature that will simplify fractions for you.

You are to write a program that will accept for input a non-negative integer as a numerator and a positive integer as a denominator, and output the fraction in simplest form. That is, the fraction cannot be reduced any further, and the numerator will be less than the denominator. You can assume that all input numerators and denominators will produce valid fractions.

Examples

Input 28 7	Input 13 5	Input 0 7	Input 55 10
Output 4	Output 2 3/5	Output 0	Output 5 1/2

- Greatest Common Divisor

Problem J4/S2: Fraction Action

Input 28 7 Output 4	Input 13 5 Output 2 3/5	Input 0 7 Output 0	Input 55 10 Output 5 1/2
--	--	---	---

- Greatest Common Divisor
- 13/5
- 1st: $13\%5 = 3 \rightarrow$ not divisible
- 2nd: whole = $(\text{int})13/5 = 2$
- 3rd: GCF = 1 $\rightarrow 13/5$
- 4th: $13\%5 = 3$
- 5th: whole (2) remainder(3)/denominator
- $N = 55 / D = 10$
- 1st: $55\%10 = 5 \rightarrow 55/10 = 5.\text{xyz} \rightarrow \text{whole} = 5$
- 2nd: GCF = 5 $\rightarrow N = 11 / D = 2$
- 3rd: $11\%2 = 1$
- 4th: 5 1/2

```
//determine if divisible  
If (ans == decimal){  
  //Find GCF  
  //Simplify  
  //Find remainder  
  //print  
}
```

Problem J4/S2: Fraction Action

Input 28 7	Input 13 5	Input 0 7	Input 55 10
Output 4	Output 2 3/5	Output 0	Output 5 1/2

- 0/7
- 1st: 0/7 = 0 (no decimal)
- 2nd: 0
- 28/7
- 1st: 28/7 = 4 (integer)
- 2nd: 4

```
If (ans == 0 || ans == integer){  
    print ans;  
}
```

```
void fraction(){
    //declaration and input
    int denominator = 0, numerator = 0, whole = 0, simplifiedN = 0, simplifiedD = 0, GCF = 1, remainder = 0;
    cin >> numerator >> denominator;
    /* IN JAVA
    Scanner input = new Scanner(system.in);
    numerator = input.nextInt();
    denominator = input.nextInt();
    */
}
```

```
void fraction(){
    //declaration and input
    int denominator = 0, numerator = 0, whole = 0, simplifiedN = 0, simplifiedD = 0, GCF = 1, remainder = 0;
    cin >> numerator >> denominator;

    //divisible?
    if (numerator%denominator == 0){
        //Case 0 or integer
        cout<<numerator/denominator<<endl;
    }else{
        //find whole and GCF
        //simplify
        //find remainder
        //print
    }
}
```

```

void fraction(){
    //declaration and input
    int denominator = 0, numerator = 0, whole = 0, simplifiedN = 0, simplifiedD = 0, GCF = 1, remainder = 0;
    cin >> numerator >> denominator;

    //divisible?
    if (numerator%denominator == 0){
        //Case 0 or integer
        cout<<numerator/denominator<<endl;
    }else{
        //find whole and GCF
        whole = (int)(numerator/denominator);
        //find greatest common factor
        for (int i = min(numerator, denominator); i > 0; i--){
            if (numerator % i == 0 && denominator % i == 0){
                GCF = i;
                break;
            }
        }
        //simplify
        //find remainder
        //print
    }
}

```

5 10
5 4 3 2 1

```
void fraction(){
    //find whole and GCF
    whole = (int)(numerator/denominator);
    //find greatest common factor
    for (int i = min(numerator, denominator); i > 0; i--){
        if (numerator % i == 0 && denominator % i == 0){
            GCF = i;
            break;
        }
    }
    //simplify
    simplifiedN = numerator/GCF;
    simplifiedD = denominator/GCF;

    //find remainder
    remainder = simplifiedN/simplifiedD;
    //print
    if (whole == 0){
        //print in one format
    }else{//print in the other format}
}
```


Problem S2: Multiple Choice

Your teacher likes to give multiple choice tests. One benefit of giving these tests is that they are easy to mark, given an answer key. The other benefit is that students believe they have a one-in-five chance of getting the correct answer, assuming the multiple choice possibilities are A, B, C, D or E. Write a program that your teacher can use to grade one multiple choice test.

Input Format

The input will contain the number N ($0 < N < 10000$) followed by $2N$ lines. The $2N$ lines are composed of N lines of student responses (with one of A, B, C, D or E on each line), followed by N lines of correct answers (with one of A, B, C, D or E on each line), in the same order as the student answered the questions (that is, if line i is the student response, then line $N + i$ contains the correct answer to that question).

Output Format

Output the number of questions the student answered correctly.

Sample Cases

Input

3 A B C A C B

Output

1

Input

3 A A A A B A

Output

2

```

void multipleChoice(){
    int numOfQ = 0, correctCount = 0;
    cin>>numOfQ;
    char student[numOfQ];
    char answer[numOfQ];

    for(int i = 0; i < numOfQ; i++){
        cin >> student[i];
    }

    for(int i = 0; i < numOfQ; i++){
        cin >> answer[i];
    }

    for(int i = 0; i < numOfQ; i++){
        if(student[i] == answer[i])
            correctCount++;
    }
    cout<<correctCount<<endl;
}

```

Input/output

C++:

cin >> int >> char;

Java:

Scanner input = new Scanner (system.in);

input.nextInt();

input.nextInt(); //take in next Integer

input.nextLine();//will take in a new line char
("\n")

Input.nextLine();//will take in next line

Problem C: Pattern Generator

Write a program that repeatedly reads two numbers n and k and prints all bit patterns of length n with k ones in **descending order** (when the bit patterns are considered as binary numbers). You may assume that $30 \geq n > 0$, $8 > k \geq 0$, and $n \geq k$. The first number in the input gives the number of pairs n and k . The numbers n and k are separated by a single space. Leading zeroes in a bit pattern should be included. See the example below.

Sample Input

```
3
2 1
2 0
4 2
```

Sample Output

The bit patterns are

```
10
01
```

The bit patterns are

```
00
```

The bit patterns are

```
1100
1010
1001
0110
0101
0011
```

```
void pattern(){
    cin >> numPair;
    int pair[numPair*2];

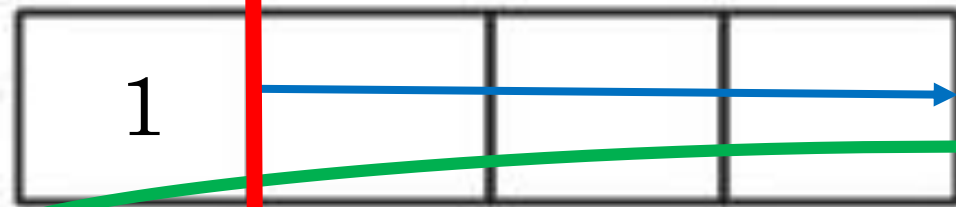
    //take in all pairs
    for(int i = 0; i < numPair*2; i = i + 2){
        cin >> pair[i] >> pair[i+1]; //pair[i] = n; pair[i+1] = k
    }

    //for each pair, print the array for them
    for (int i = 0; i < numPair*2; i = i + 2){
        cout<<endl;
        cout<<"The bit patterns are"<<endl;
        n = pair[i];
        k = pair[i+1];
        printarray(n,k);
    }

}
```

Understand Recursion → print(4,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,1); //print 3 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,2); //print 3 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

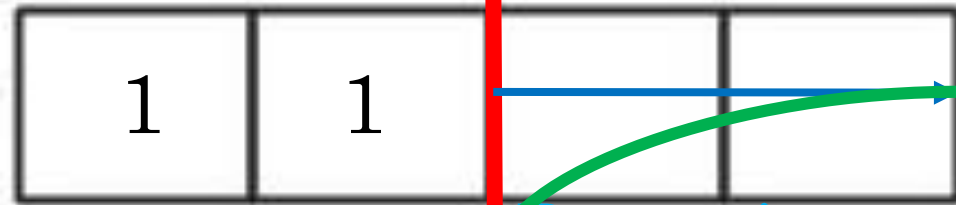
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

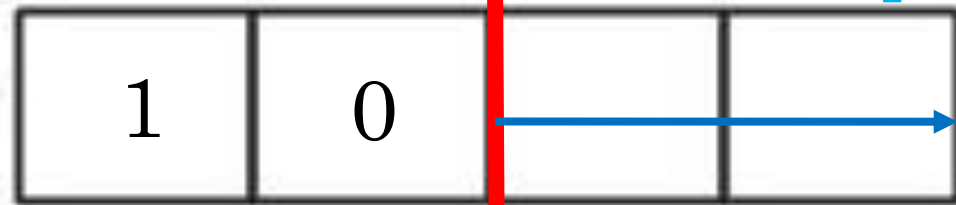
$$4 - 2 = 2$$

→ print(2,0); //print 2 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

→ print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

0101

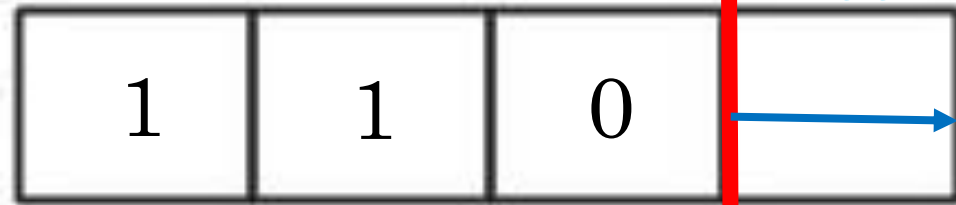
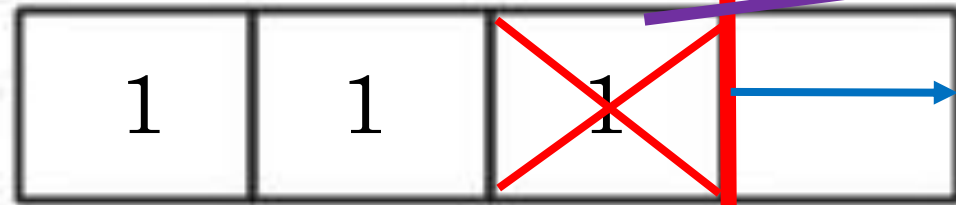
0011

After printing all the ones, print all the zeros

Understand Recursion \rightarrow print(2,0)

Example: 4 2 (4 digits, 2 ones)

Condition: if $k > 0$, then print 1



Recursion prints the rest for me

Digit Left(n)

$$4 - 3 = 1$$

\rightarrow print(1,0); //print 1 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(1,0)

Example: 4 2 (4 digits, 2 ones)



Condition not met: k needs to be > 0



Digit Left(n)

$$4 - 4 = 0$$

Ones left(k)

$$2 - 2 = 0$$

→ print(0,0); //print 0 digits with 0 one →

STOP → print this array

1100

1010

1001

0110

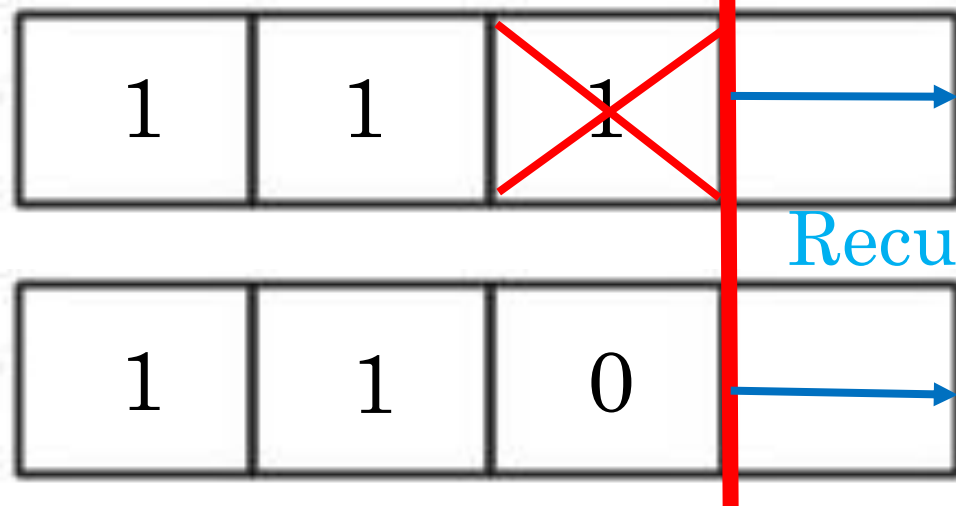
0101

0011

After printing all the ones, print all the zeros

Understand Recursion \rightarrow print(2,0)

Example: 4 2 (4 digits, 2 ones)



Recursion prints the rest for me

Digit Left(n)

$$4 - 3 = 1$$

\rightarrow print(1,0); //print 1 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

1100

1010

1001

0110

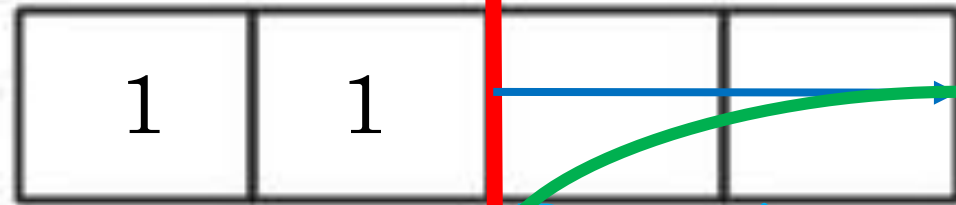
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

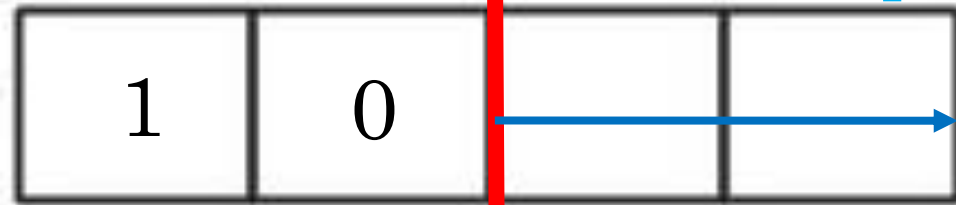
$$4 - 2 = 2$$

→ print(2,0); //print 2 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

→ print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

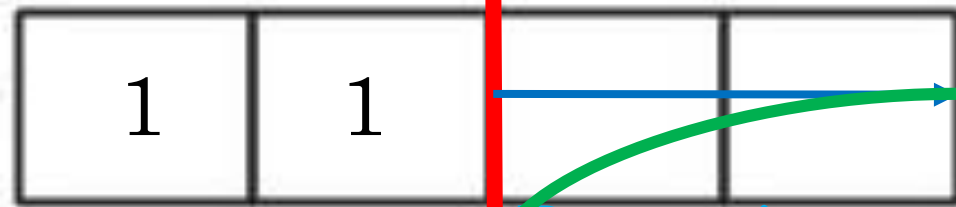
0101

0011

After printing all the ones, print all the zeros

Understand Recursion \rightarrow print(3,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 2 = 2$$

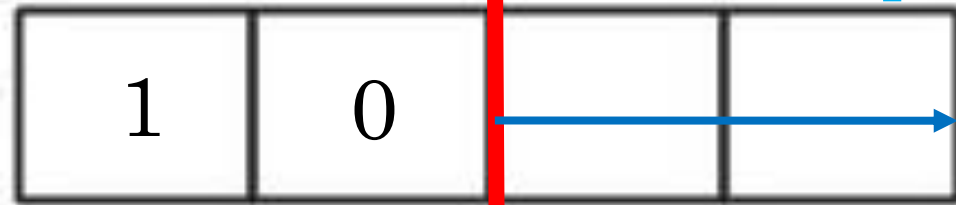
\rightarrow print(2,0); //print 2 digits with 0 ones

Ones left(k)

$$2 - 2 = 0$$

Done

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

\rightarrow print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

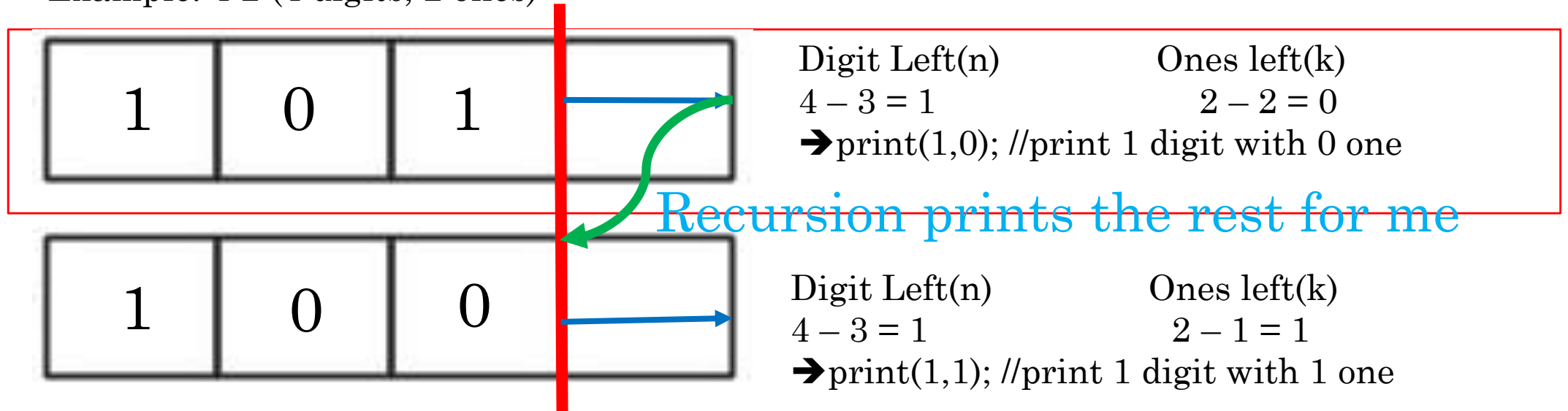
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)

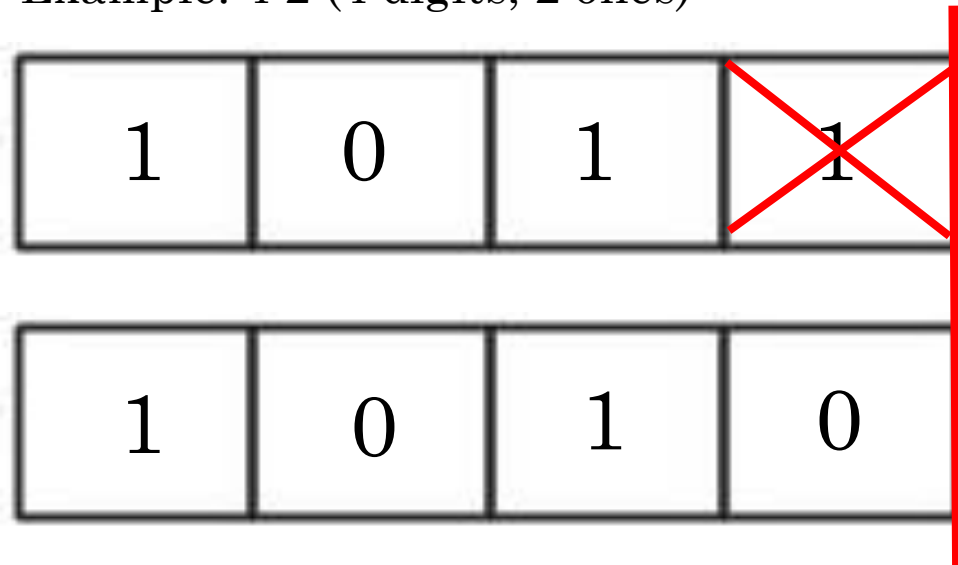


1100
1010
1001
0110
0101
0011

After printing all the ones, print all the zeros

Understand Recursion \rightarrow print(1,0)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 4 = 0$$

\rightarrow print(0,0); //print 0 digits with 0 one \rightarrow

STOP \rightarrow print this array

Ones left(k)

$$2 - 2 = 0$$

1100

1010

1001

0110

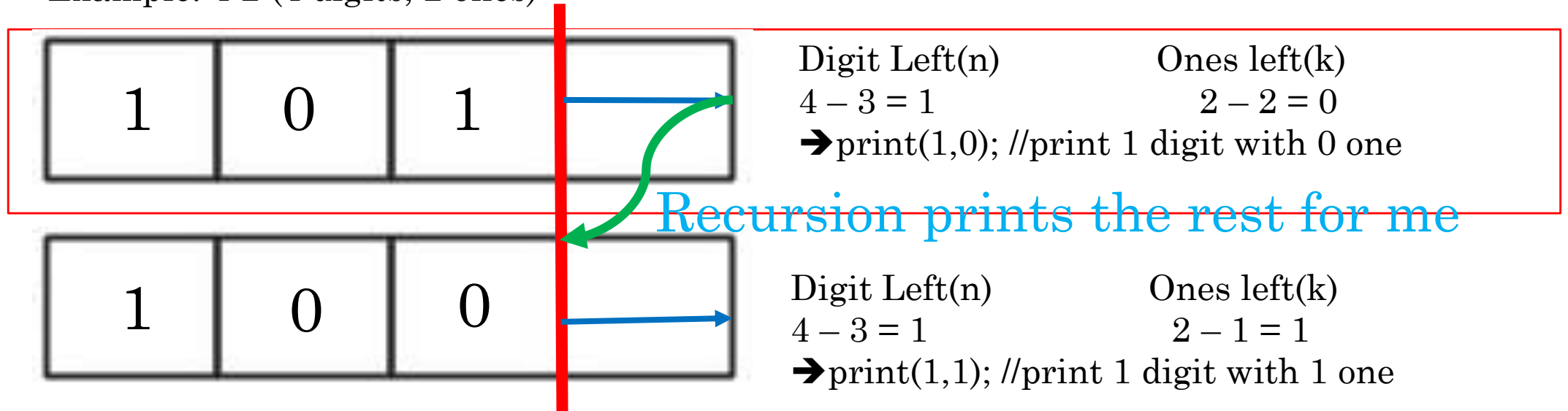
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)

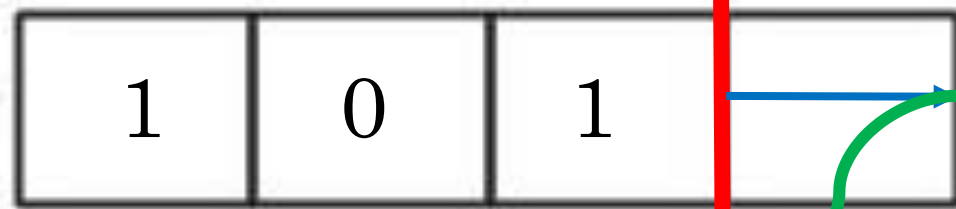


1100
1010
1001
0110
0101
0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,0); //print 1 digit with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

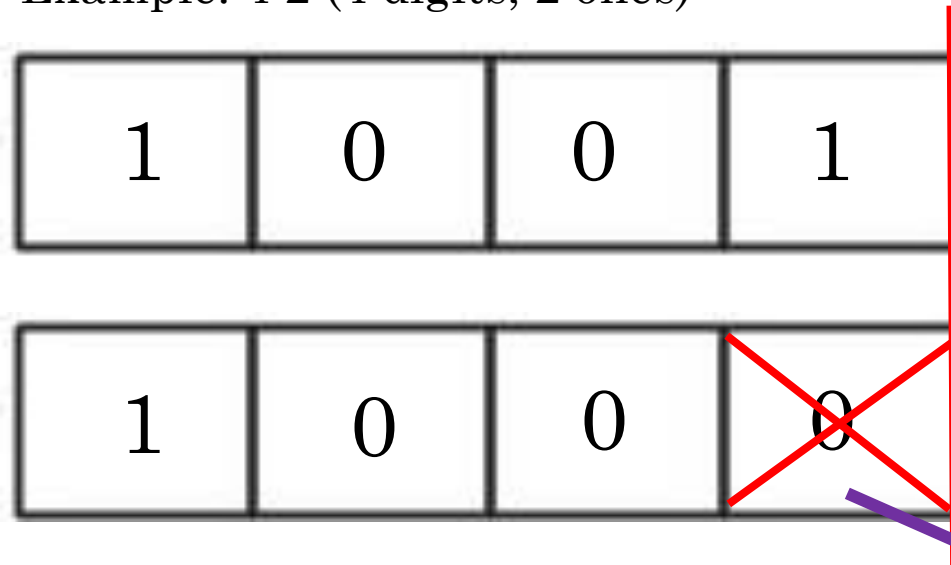
0101

0011

After printing all the ones, print all the zeros

Understand Recursion \rightarrow print(1,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 4 = 0$$

\rightarrow print(0,0); //print 0 digits with 0 one \rightarrow

STOP \rightarrow print this array

Ones left(k)

$$2 - 2 = 0$$

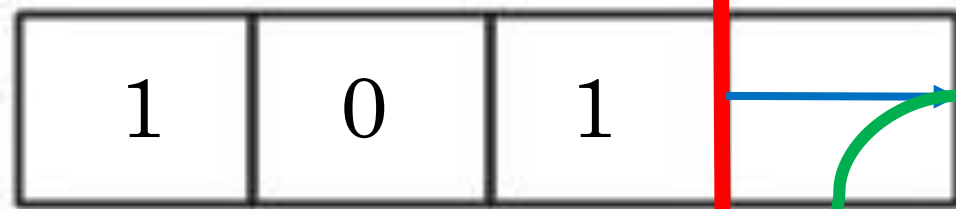
Condition: if $n > k$ (i.e. after we print zero here, if we still have enough space for ones, then print zero)

After printing all the ones, print all the zeros

1100
1010
1001
0110
0101
0011

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

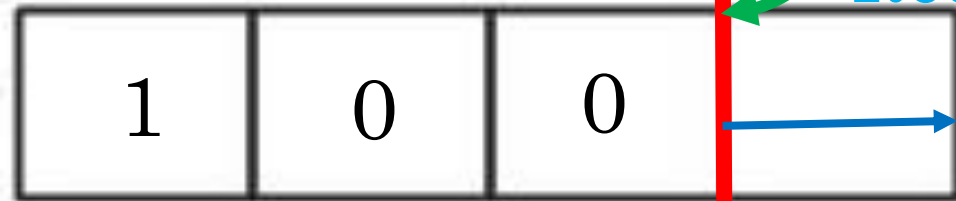
$$4 - 3 = 1$$

→ print(1,0); //print 1 digit with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

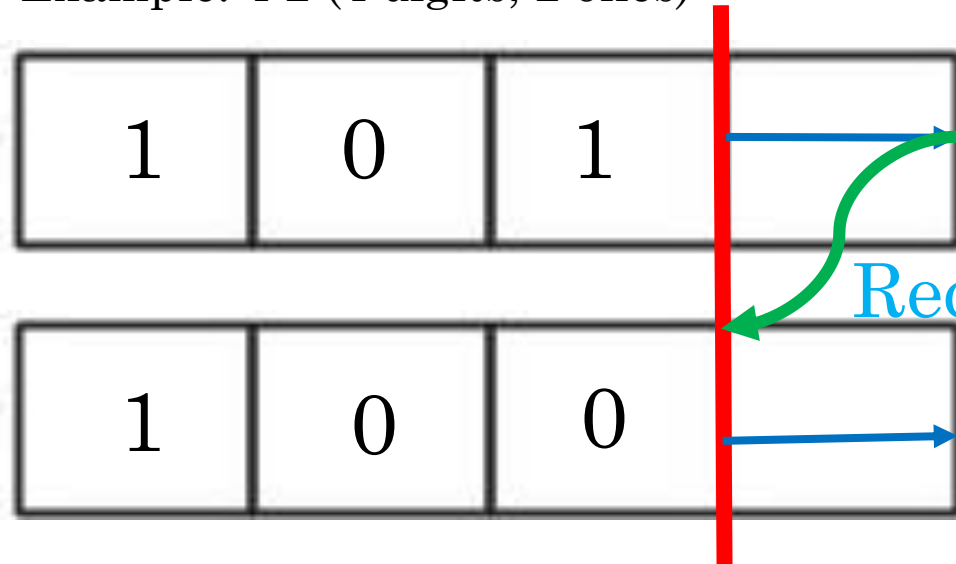
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,0); //print 1 digit with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me

Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

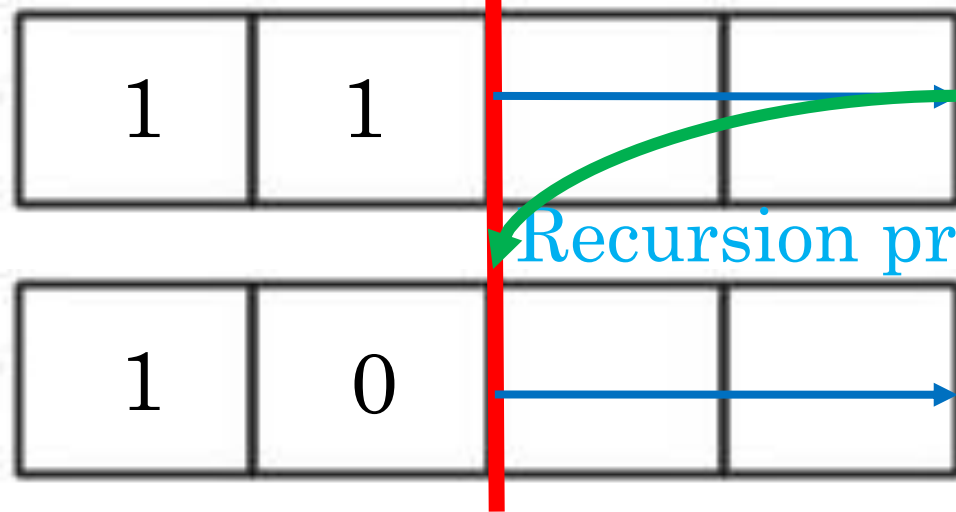
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)	Ones left(k)
$4 - 2 = 2$	$2 - 2 = 0$
→ print(2,0); //print 2 digits with 0 ones	

Done

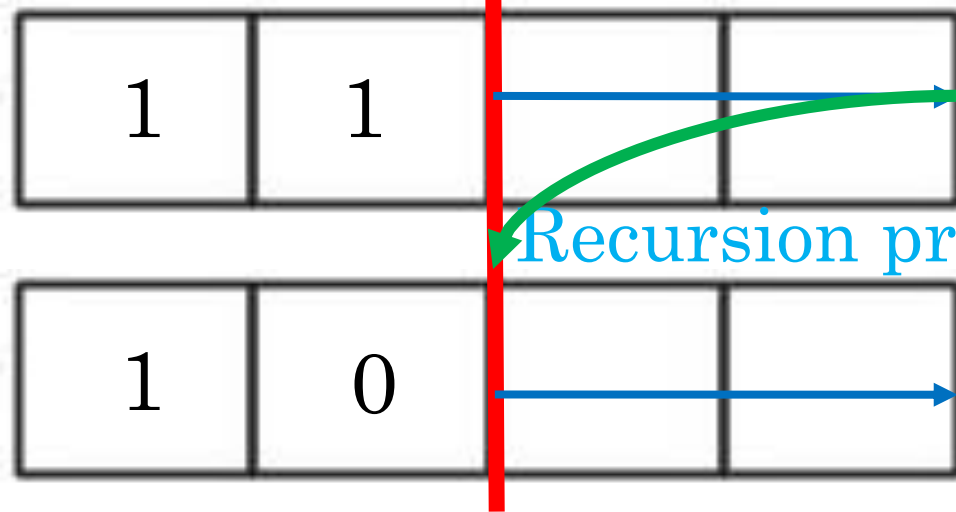
Digit Left(n)	Ones left(k)
$4 - 2 = 2$	$2 - 1 = 1$
→ print(2,1); //print 2 digits with 1 one	

1100
1010
1001
0110
0101
0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)	Ones left(k)
$4 - 2 = 2$	$2 - 2 = 0$
→ print(2,0); //print 2 digits with 0 ones	

Done

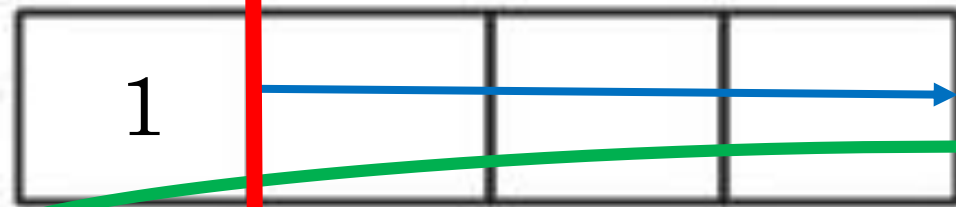
Digit Left(n)	Ones left(k)
$4 - 2 = 2$	$2 - 1 = 1$
→ print(2,1); //print 2 digits with 1 one	

1100
1010
1001
0110
0101
0011

After printing all the ones, print all the zeros

Understand Recursion → print(4,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,1); //print 3 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,2); //print 3 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

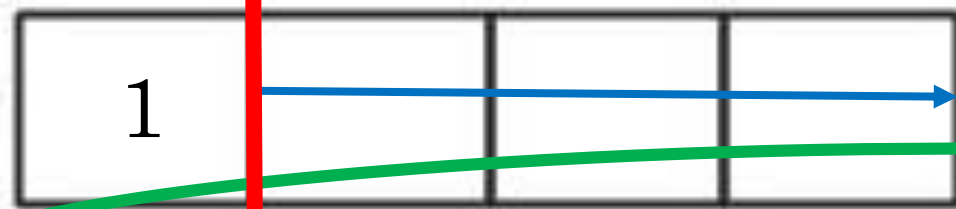
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(4,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,1); //print 3 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,2); //print 3 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

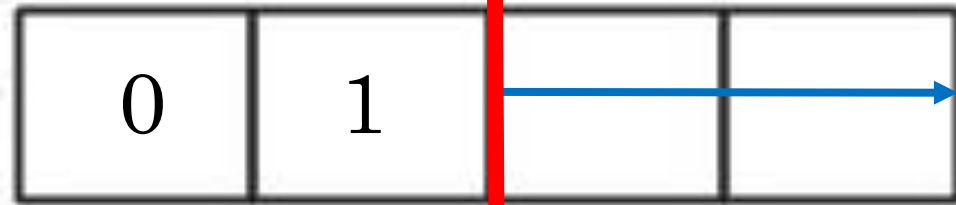
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

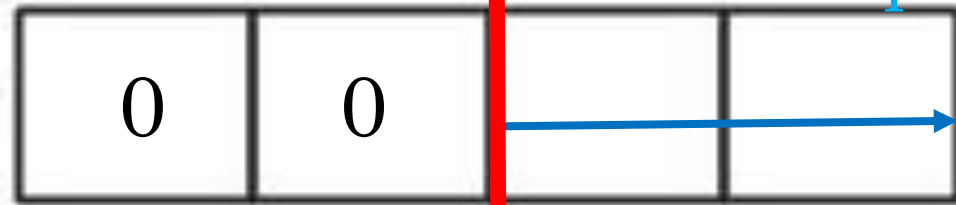
$$4 - 2 = 2$$

→ print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

→ print(2,2); //print 2 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

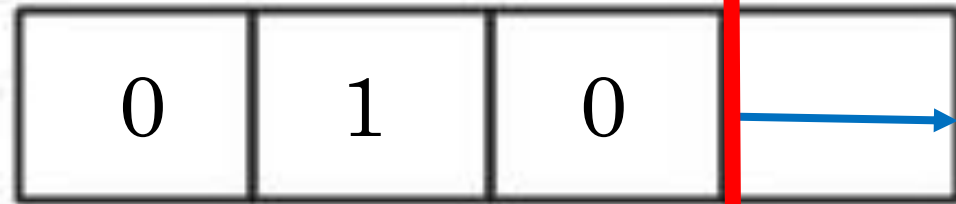
$$4 - 3 = 1$$

→ print(1,0); //print 1 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

0101

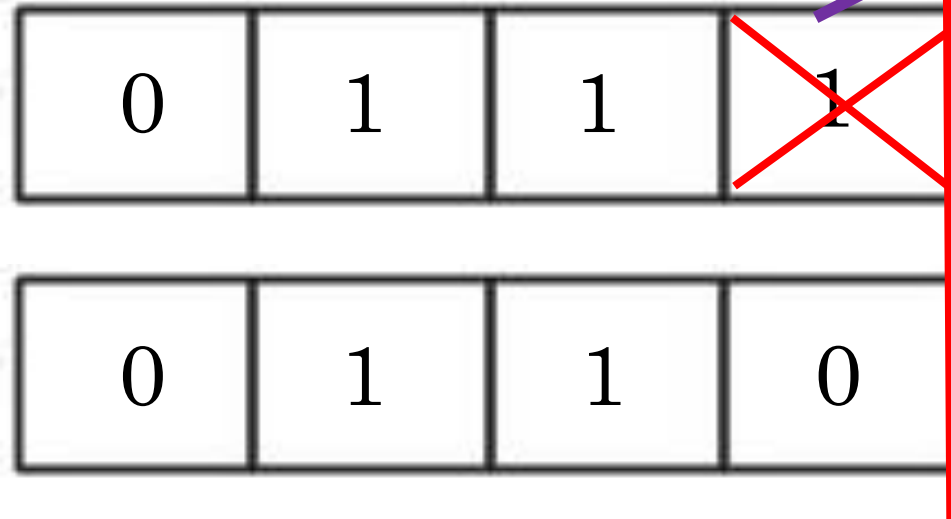
0011

After printing all the ones, print all the zeros

Understand Recursion → print(1,0)

Example: 4 2 (4 digits, 2 ones)

Condition: if $k > 0$ not met



Digit Left(n)

$$4 - 4 = 0$$

→ print(0,0); //print 0 digits with 0 one

→ STOP → print

Ones left(k)

$$2 - 2 = 0$$

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

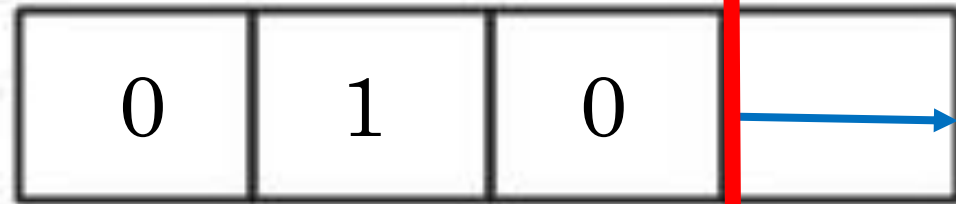
$$4 - 3 = 1$$

→ print(1,0); //print 1 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,0); //print 1 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(1,1)

Example: 4 2 (4 digits, 2 ones)

0	1	0	1
---	---	---	---

0	1	0	0
---	---	---	--------------

Digit Left(n)

$$4 - 4 = 0$$

→ print(0,0); //print 0 digits with 0 one

→ Stop → print

Ones left(k)

$$2 - 2 = 0$$

Condition: if $n > k$ not met

1100

1010

1001

0110

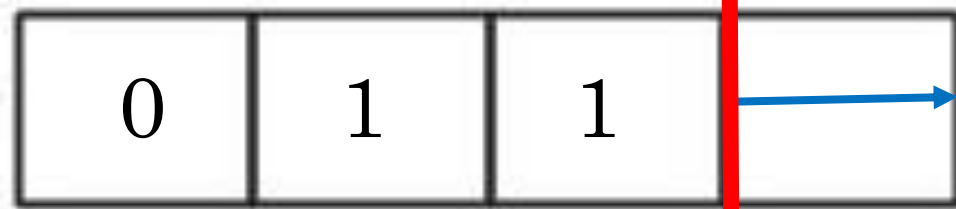
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 1 digits with 0 one

Ones left(k)

$$2 - 2 = 0$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

1100

1010

1001

0110

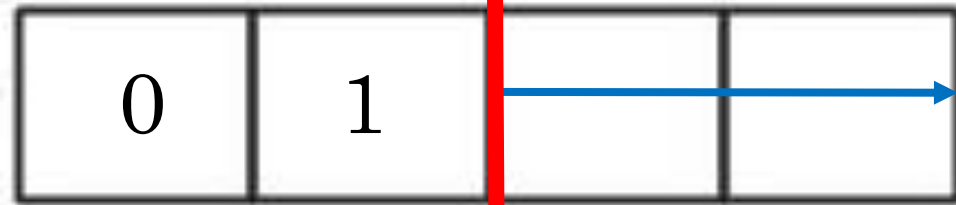
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

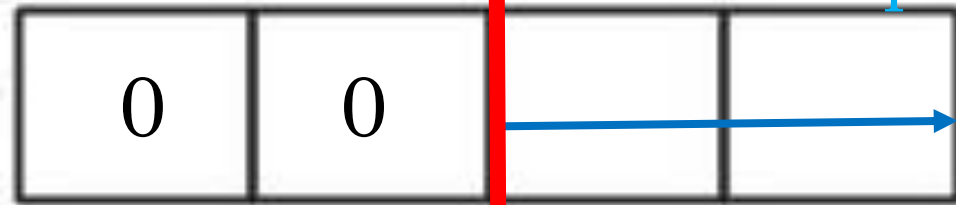
$$4 - 2 = 2$$

→ print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

→ print(2,2); //print 2 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

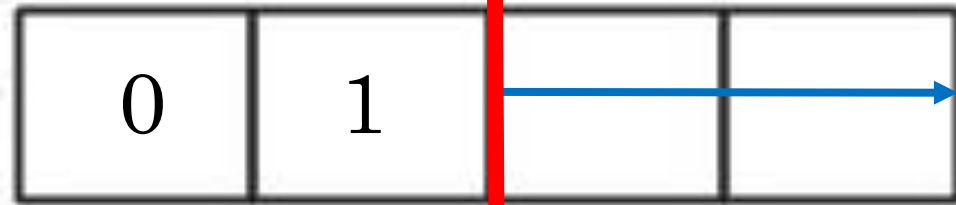
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

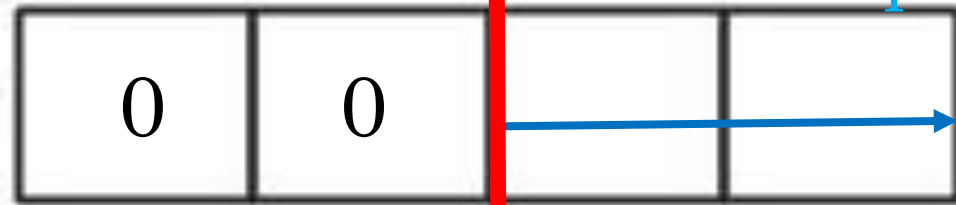
$$4 - 2 = 2$$

→ print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

→ print(2,2); //print 2 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

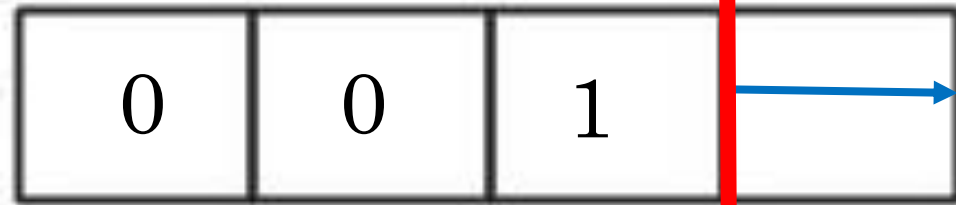
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

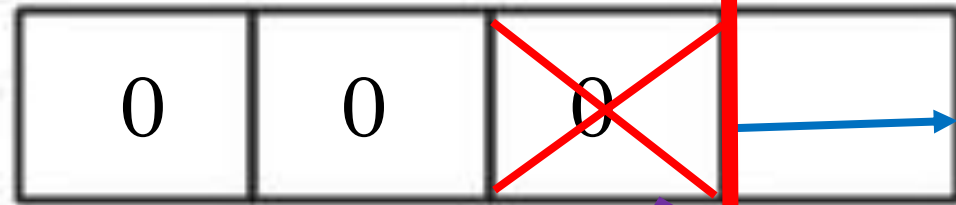
$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,2); //print 1 digit with 2 ones

Ones left(k)

$$2 - 0 = 2$$

Condition: if $n > k$ not met

1100

1010

1001

0110

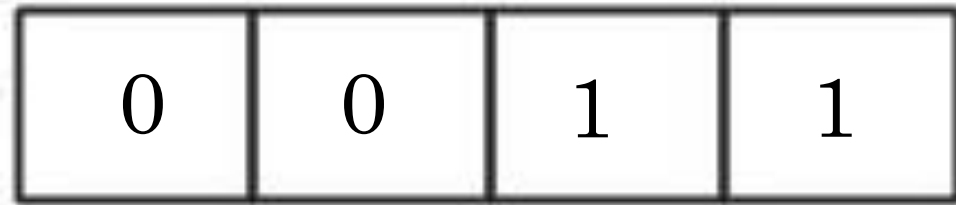
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(1,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

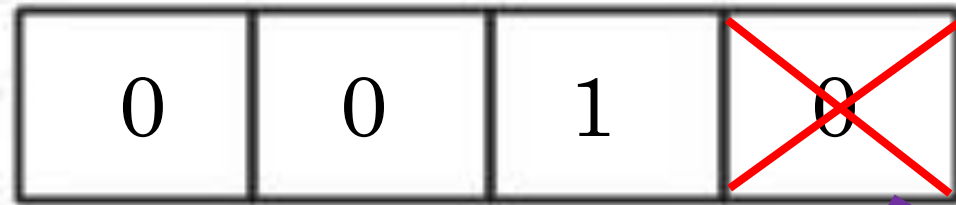
$$4 - 3 = 0$$

→ print(0,0); //print 0 digit with 0 one

→ stop → print

Ones left(k)

$$2 - 1 = 0$$



Condition: if $n > k$ not met

1100

1010

1001

0110

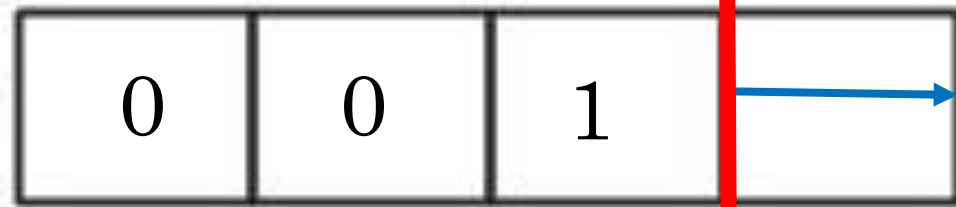
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

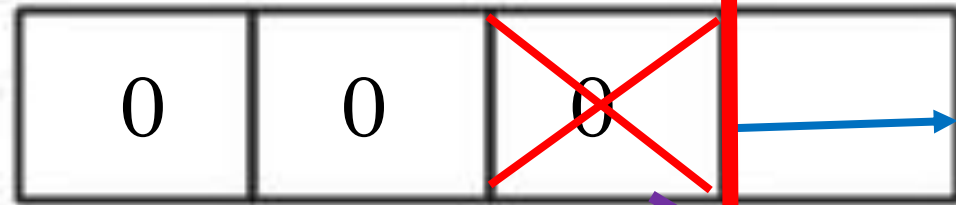
$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,2); //print 1 digit with 2 ones

Ones left(k)

$$2 - 0 = 2$$

Condition: if $n > k$ not met

1100

1010

1001

0110

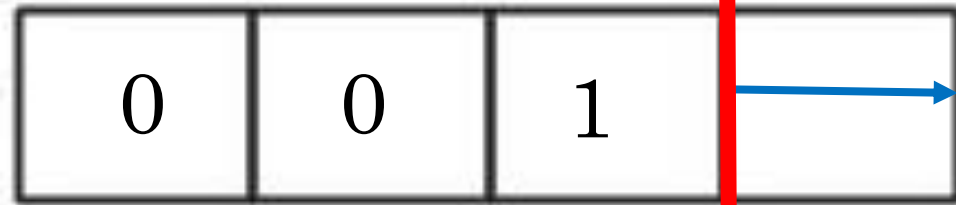
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(2,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

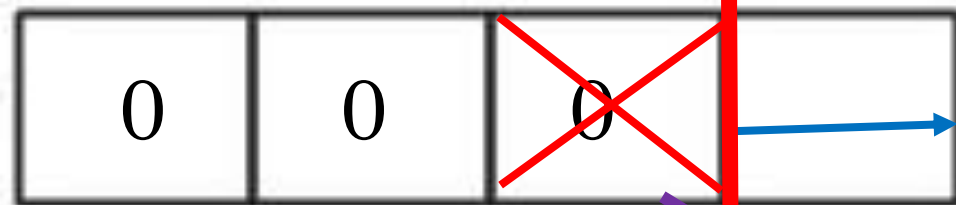
$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,2); //print 1 digit with 2 ones

Ones left(k)

$$2 - 0 = 2$$

Condition: if $n > k$ not met

1100

1010

1001

0110

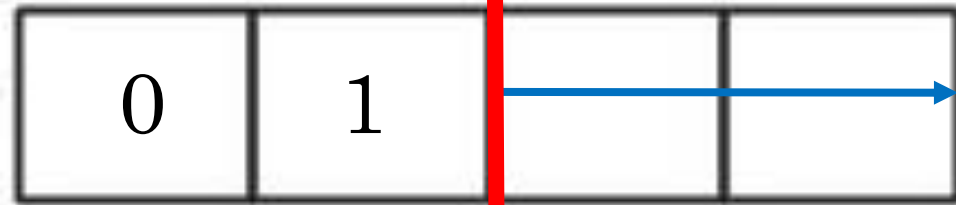
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(3,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

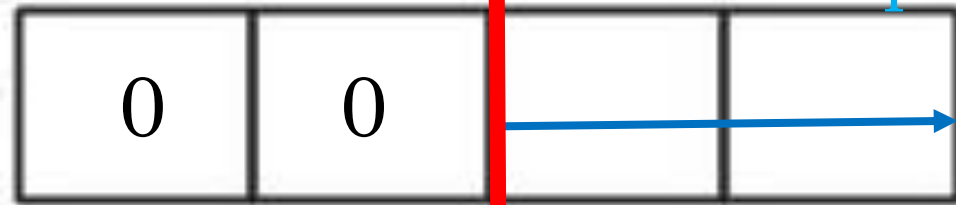
$$4 - 2 = 2$$

→ print(2,1); //print 2 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 2 = 2$$

→ print(2,2); //print 2 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

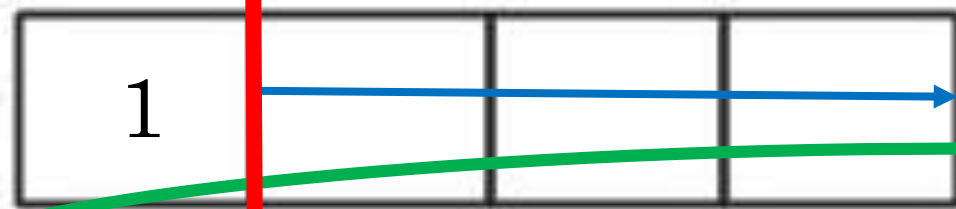
0101

0011

After printing all the ones, print all the zeros

Understand Recursion → print(4,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,1); //print 3 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,2); //print 3 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

0101

0011

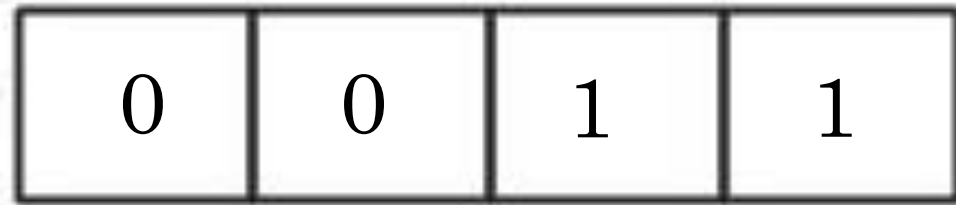
Nothing more to choose → End of recursion

After printing all the ones, print all the zeros

```
void printarray(int i, int j){  
    if(i == 0 && j == 0){  
        for(int a = 0; a < n; a++){  
            cout<<array[a];  
        }  
        cout<<endl;  
    }else{  
        if (j > 0){  
            array[n - i] = 1;  
            printarray(i - 1, j - 1);  
        }  
        if (i > j){  
            array[n - i] = 0;  
            printarray(i-1,j);  
        }  
    }  
}
```

Understand Recursion → print(1,1)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

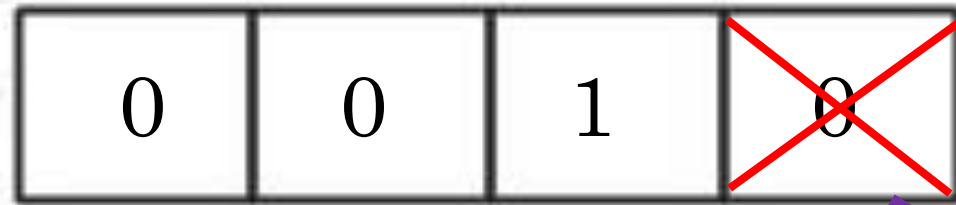
$$4 - 3 = 0$$

→ print(0,0); //print 0 digit with 0 one

→ stop → print

Ones left(k)

$$2 - 1 = 0$$



Condition: if $n > k$ not met

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

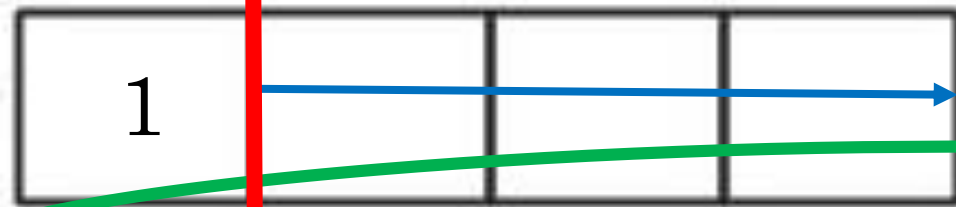
```

void printarray(int i, int j){
    if(i == 0 && j == 0){
        for(int a = 0; a < n; a++){
            cout<<array[a];
        }
        cout<<endl;
    }else{
        //if has one left = print one series first
        if (j > 0){
            //n - i = current position
            array[n - i] = 1;
            printarray(i - 1, j - 1);
        }
        //then print zero series, print zero if and only if
        //the number of spots left > number of one left
        if (i > j){
            array[n - i] = 0;
            printarray(i-1,j);
        }
    }
}

```


Understand Recursion → print(4,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,1); //print 3 digits with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 1 = 3$$

→ print(3,2); //print 3 digits with 2 ones

Ones left(k)

$$2 - 0 = 2$$

1100

1010

1001

0110

0101

0011

After printing all the ones, print all the zeros

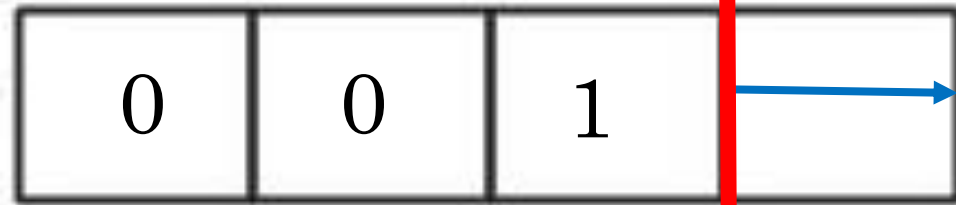
```

void printarray(int i, int j){
    if(i == 0 && j == 0){
        for(int a = 0; a < n; a++){
            cout<<array[a];
        }
        cout<<endl;
    }else{
        //if has one left = print one series first
        if (j > 0){
            //n - i = current position
            array[n - i] = 1;
            printarray(i - 1, j - 1);
        }
        //then print zero series, print zero if and only if
        //the number of spots left > number of one left
        if (i > j){
            array[n - i] = 0;
            printarray(i-1,j);
        }
    }
}

```

Understand Recursion → print(2,2)

Example: 4 2 (4 digits, 2 ones)



Digit Left(n)

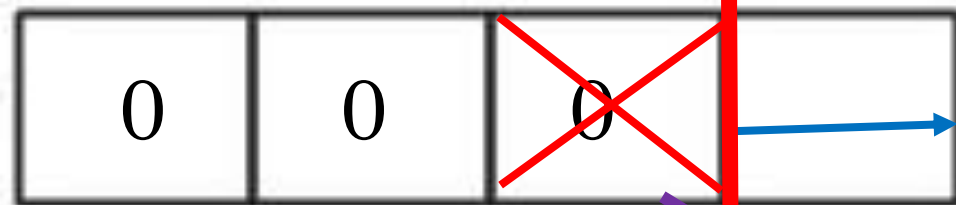
$$4 - 3 = 1$$

→ print(1,1); //print 1 digit with 1 one

Ones left(k)

$$2 - 1 = 1$$

Recursion prints the rest for me



Digit Left(n)

$$4 - 3 = 1$$

→ print(1,2); //print 1 digit with 2 ones

Ones left(k)

$$2 - 0 = 2$$

Condition: if $n > k$ not met

1100

1010

1001

0110

0101

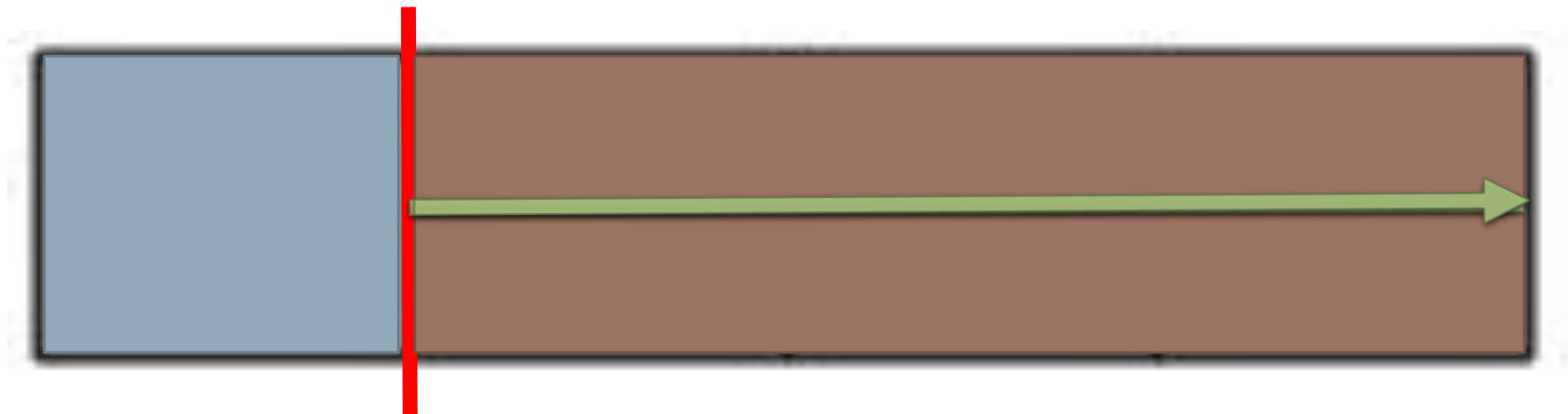
0011

After printing all the ones, print all the zeros

```

void printarray(int i, int j){
    if(i == 0 && j == 0){
        for(int a = 0; a < n; a++){
            cout<<array[a];
        }
        cout<<endl;
    }else{
        //if has one left = print one series first
        if (j > 0){
            //n - i = current position
            array[n - i] = 1;
            printarray(i - 1, j - 1);
        }
        //then print zero series, print zero if and only if
        //the number of spots left > number of one left
        if (i > j){
            array[n - i] = 0;
            printarray(i-1,j);
        }
    }
}

```



Problem S3: Absolutely Acidic

You are gathering readings of acidity level in a very long river in order to determine the health of the river. You have placed N sensors in the river, and each sensor gives an integer reading R . For the purposes of your research, you would like to know the frequency of each reading, and find **the absolute difference between the two most frequent readings**.

If there are more than two readings that have the highest frequency, the difference computed should be the *largest* such absolute difference between two readings with this frequency.

If there is only one reading with the largest frequency, but more than one reading with the second largest frequency, the difference computed should be the *largest* absolute difference between the most frequently occurring reading and any of the readings which occur with second-highest frequency.

Input Format

The first line of input will be the integer N ($2 \leq N \leq 2 \times 10^6$), the number of sensors. The next N lines each contain the reading for that sensor, which is an integer R ($1 \leq R \leq 1000$). You should assume that there are at least two different readings in the input.

Output Format

Output the positive integer value representing the absolute difference between the two most frequently occurring readings, subject to the tie-breaking rules outlined above.

Sample

Sample Input 1

5 1 1 1 4 3

Sample Output 1

3

Sample Input 2

4 10 6 1 8

Sample Output 2

9

Input: 2 1 1 1 3 4 3 10 12 3

Using array

[illegible]

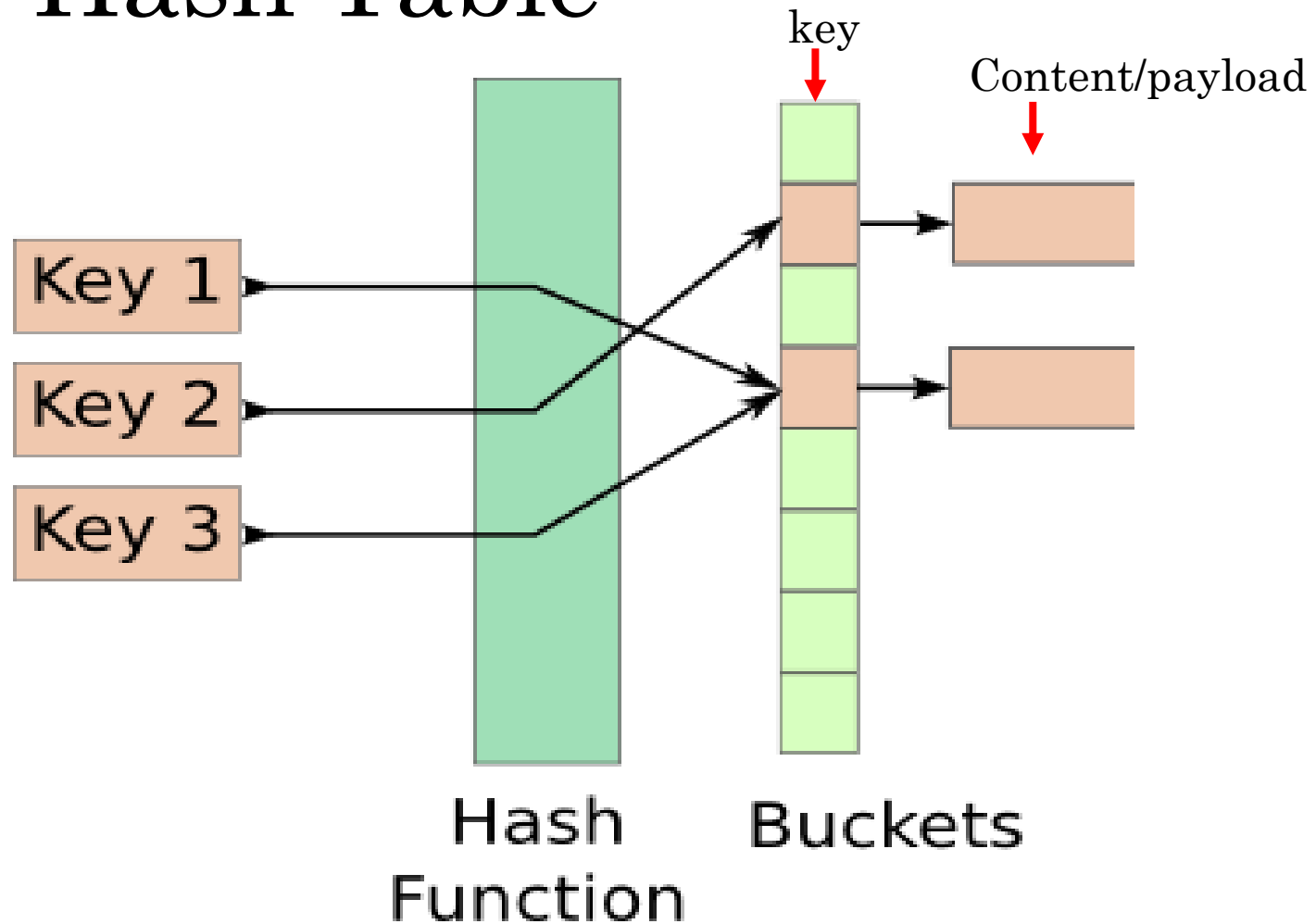
Input: 2 1 1 1 3 4 3 10 12 3

Using array

	0	1	2	3	4	5	6	7	8	9
Sensor value	1	1	1	2	3	3	3	4	10	12
Frequency	3	3	3	1	3	3	3	1	1	1
HighestIndex	0	4								
SecondIndex										

```
if (highestIndex.length() > 1){ //loop through highestIndex, find largest abs}
else{
    find largest abs of difference between
    sensorvalue[highestIndex[0]] and sensorvalue[secondIndex[i]]
}
```

Hash Table



Practice

- <http://wcipeg.com/problem/ccc10j2>
- <http://wcipeg.com/problem/ccc14s1>
- <http://wcipeg.com/problem/ccc10j3>