Preprint of article about an open hardware RTU device.

# Multiple Sensor Interface by the same hardware to USB and serial connection

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#### Abstract

The Multiple Sensor Interface is a simple sensor interface that works with USB, RS485 and GPIO. It allows one to make measurements using a variety of sensors based on the change of inductance, resistance, capacitance, and frequency using the same connector and same electronic interface circuit between the sensor and the microcontroller. The same device also provides some additional connectors for small voltage measurement. Any sensors used for the measurement of distinct phenomena can be used if the sensor output is based on inductance, resistance, capacitance or frequency within the measurement range of the device, obtaining a variable precision depending on the used sensor. The device presented is not meant for precise or accurate measurements. It is meant to be a reusable hardware that can be adapted/configured to a varied number of distinct situations, providing, to the user, more freedom in sensor selection as well as more options for device/system maintenance or reuse.

**Keywords:** Sensor systems and applications; Oscillators; Design aiming for reuse, repurpose, repair, customization.

#### 1 Introduction

The electronic waste (e-waste) is a modern problem under increasing concern and awareness, there are various possible approaches to reduce and mitigate it, the most obvious is the collection and recycling of discarded devices, however the most ideal is just to make technology that lasts because not only is physically fit by quality design, production, and components; but because its design was intended to be most versatile ensuring the same device can be used and reused in various applications/contexts just by changing connections, jumpers, and firmware configurations. Some design aspects for making a device more reusable are: the use of standard connectors and protocols, think of it as a module to be part of a larger system, minimize barriers for connecting/interfacing components and devices from distinct manufacturers.

## 1.1 Project objectives and trade-offs

This article is focused on the design of a sensor interface device with USB and serial(UART,RS-485), aimed to allow the interface to many distinct 2-wire sensors based on the change of inductance, resistance, capacitance, frequency, and also small voltage; sensors that can be interchanged using the same hardware and same port of the device, thus meaning the electronics designed must also be versatile.

Obviously providing a versatile device to the users will have its negative trade-offs, like:

- 1- probably significant lower precision/accuracy;
- 2- some sensor calibration must be provided/done by the end user after replacing a sensor;
- 3- the calibration function will not be linear or 'easy' as desired for sensors and its interfaces.

However, for some applications the mentioned trade-offs are not necessarily a deal-breaker, like when the user is

\*Lisboa, Portugal; E-mail: david.n.quelhas@gmail.com https://pt.linkedin.com/in/dquelhas ORCID: 0000-0002-0282-0972 https://multiple-sensor-interface.blogspot.com technical and is ok with using a device that requires more setup/configuration, some users like devices that are more customizable or repairable. Also is possibly valued a device that if no longer useful for a user, it might still be useful for another user on a different application/context.

### 1.2 License and context

The hardware design here disclosed is distributed under "CERN Open Hardware Licence Version 2 - Weakly Reciprocal" (CERN-OHL-W), its associated software/firmware under GNU licenses (GPL, LGPL).

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This article is about a 'hobby' project done by the author (David Nuno Quelhas, MSc Electronics Eng, alumni of Instituto Superior Tecnico, Portugal) with occasional 'work' between the years 2012 and 2022 on his 'free time'.

#### 1.3 Prior art review

The topic and devices commonly described in literature as 'Multiple Sensor Interface' and also as 'Universal Sensor Interface', commonly fall under 3 distinct categories: a) Device that has a more versatile interface or signal conditioning circuit capable of interfacing various sensor types; b) Device that includes various specialized interfaces or signal conditioning circuits for each sensor type, typically built using various PCB boards for the sensors, to connect or stack into a PCB board with a microcontroller that will register and/or transmit the measurements, or alternatively have all these different circuits integrated inside a single integrated circuit (micro-chip); c) Hardware and/or software systems that collect or register sensor data from various distinct sensing devices/circuits, that may apply some processing to the raw data for obtaining measurements, then to be transmitted to other systems or to a data storage, and so these hardware/software systems may also be called/named 'interface'.

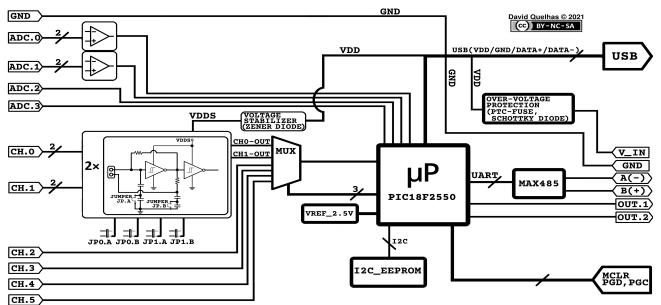


Figure 1: Diagram of the Multiple Sensor Interface device.

The article review presented here will be about 'more versatile interface or signal conditioning circuit' that is the category most similar to this article. Types of versatile sensor interface found on prior art:

- 1- Interfacing resistive or capacitive sensors by measuring the charge-discharge time of an RC circuit, or measuring the frequency or PWM from an oscillator whose pace is controlled by the speed of a capacitor charge-discharge trough a resistor; for example: [6], [7], [8].
- 2- Interfacing sensors based on the variation of impedance (includes sensor based on variation of resistance, capacitance or inductance) by an LCR meter, impedance meter, or potentiostat circuit; for example: [9], [10], [11], [12].
- 3 Interfacing a sensor as part of a bridge circuit (example: resistive sensor on a resistance bridge, capacitive sensor on a capacitance bridge) [13].

The Multiple Sensor Interface presented on this article has a working principle more similar to the circuits mentioned as type 1 (RC time or frequency or PWM of oscillator), however in comparison with the mentioned references/articles, the interface circuit of this article can interface more distinct sensor types, namely besides interfacing resistive and capacitive sensors it also interfaces inductive sensors and sensors by frequency measurement using exactly the same circuit and connector/port, also it is a simple circuit with a reduced number of components.

The Multiple Sensor Interface presented on this article in comparison to the circuits mentioned as type 2 (LCR or impedance meters), has the advantage of not requiring an AC voltage/signal generator for exciting the measurement circuit, and not requiring the complex hardware and/or complex post processing for digitizing voltage signal waveforms, that is typically required for the calculation of amplitude and phase difference of voltage signals, on the measurement of impedance by LCR or impedance meters.

The Multiple Sensor Interface presented on this article in comparison to the circuits mentioned as type 3 (measuring a sensor as part of a bridge), has the advantage of using the

same circuit for all sensor types (resistive, capacitive, inductive, frequency), instead of requiring a different circuit (the bridge circuit) for each sensor type; thus the interface circuit of this article is a simple circuit with a reduced number of components probably much simpler than any circuitry required for obtaining a single output signal usable for measuring various sensor types on multiple bridge circuits.

A comparison regarding the accuracy or precision of this sensor interface and other interfaces/devices was not made, since the stated focus of the article is how to achieve a most versatile sensor interface, and also considering that such comparison may be easier when considering specific type(s) of sensor/application.

### 2 Design, Materials and Methods

### 2.1 Sensor Interface Device

Here is presented the Multiple Sensor Interface (Fig.1), the interface main components / sub-circuits are: The connectors and sensor interface circuits (oscillators) for inductance, resistance, capacitance, and frequency (CH.0, CH.1); the connectors and over-voltage protection(zener diode) for frequency measurement (CH.2, CH.3, CH.4, CH.5); the connectors and interface circuit for voltage measurement (ADC.0, ADC.1, ADC.2, ADC.3); analog multiplexer for the sensor channels, the microcontroller (PIC18F2550); I2C EEPROM for storing calibration tables; USB connector; connector and circuit for RS-485 and UART; digital outputs connector (OUT.1, OUT.2).

The digital outputs have the value of a boolean function defined by the user, boolean functions with logic variables that are the result of a comparison ('bigger' or 'smaller' than), between the value/measurement of a sensor channel and a configurable threshold value. The connectors used for frequency measurement may be connected to external single sensor interface circuits (oscillators).

### 2.2 The sensor interface circuit (oscillator)

The sensor interface (Fig.2) is an oscillator with a circuit design based on the Pierce oscillator with some modifica-

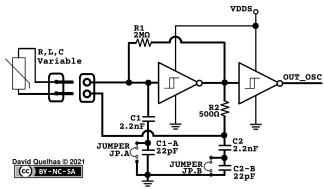


Figure 2: Schematic of the sensor interface circuit (oscillator).

tions. The 1st difference is that there is no quartz crystal, and on the location of the crystal will be connected the sensor to be measured (variable inductance or resistance or capacitance), the 2nd difference is that instead of simple inverters ('NOT' gates) will be used Schmitt-trigger inverters(high-speed Si-gate CMOS, 74HC14), this is a very relevant difference that will allow the oscillator to work even with a resistive or capacitive sensor, in fact the interface circuit works with sensors mostly as a Schmmit-Trigger oscillator. Also the Schmitt-Trigger inverters may minimize signal jitter of the oscillator output.

The sensor interface circuit has 2 pairs of series capacitors (C1 2.2nF,C1-A 22pF and C2 2.2nF,C2-B 22pF) instead of just 2 capacitors(C1,C2) so the value of C1 and C2 can be adjusted just by placing/removing a jumper; placing a jumper removes C1-A or C1-B from the circuit making 2.2nF the value of C1 or C2; removing the jumper lets the capacitors in series making 21.78pF the total value of (C1, C1-A) or (C2, C2-B). So on the rest of the article, whenever is mentioned C1 or C2 is meant the resulting capacitor value that can be 2.2nF(jumper on) or 21.78pF(jumper off), accordingly with mentioned jumper configuration.

The sensors can be connected directly on the Multiple-Sensor Interface(on the screw terminals/connectors), or by using a cable; for a cable longer than 20cm is recommended the use of shielded twisted-pair(STP) cable to prevent crosstalk between sensor channels or external EMI.

#### 2.3 Measurement process

The Multiple-Sensor device has a microcontroller (PIC18F2550) that is able to make frequency and voltage measurements, so the device makes frequency measurements for sensor channels CH.0 to CH.5; and makes voltage measurements for sensor channels ADC.0 to ADC.3; these frequency and voltage measurements made by the device are designated as the RAW\_value of a sensor channel. To obtain the measurement of a sensor channel, the device uses a 2 column calibration table, that is a long list of points (RAW\_value; measurement) relating the measurement value (obtained during calibration by an external reference device) to the corresponding RAW\_value obtained on the Multiple-Sensor device, these calibration tables are stored on an I2C EEPROM memory on the Multiple-Sensor device.

The Multiple-Sensor device can work in two modes: single-channel or multiple-channel, the CH.0 to CH.5 RAW\_value(frequency) are calculated through a counter/timer of the PIC18F2550 by periodically reading its value and calculating the frequency f=count/period

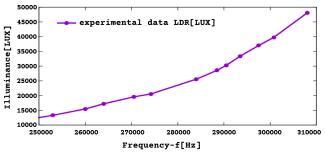


Figure 3: Plot experimental data with line, LDR light(brightness) sensor connected on Multiple-Sensor Interface; example of a calibration table exclusively from experimental data.

([Hz]=[cycles]/[s]). So in single-channel mode the frequency is always calculated on the selected/enabled sensor channel, in multiple-channel mode the frequency is calculated for each sensor channel sequentially (time-division multiplexing), since there are 6 channels to measure but only on counter/timer of the microcontroller for that job. Thus in multiple-ch mode a measurement takes 6x more time to be updated/refreshed than in single-ch mode.

For the sensor channels ADC.0 to ADC.3 the RAW\_value is the voltage of those channels measured by using the ADC (Analog to Digital Converter) of the microcontroller and also reading a 2.5V voltage reference.

The sensor measurements are calculated by searching the RAW\_value on the correspondent calibration table, and by using from the table 2 points (RAW\_value,measurement) referenced here as points P and Q such that the measured RAW\_value is bigger than RAW\_value of P and is lower than RAW\_value of Q; then is calculated a linear equation:  $measurement = a \cdot (RAW_value) + b, \text{ defined by the points} P \text{ and Q. So every-time the device calculates a sensor measurement, it will calculate the correspondent linear equation for the current RAW_value and use it to obtain the current measurement (Fig.3) .$ 

# 2.4 Device calibration for a sensor

Device calibration is about obtaining calibration tables for each sensor channel, here are 2 ways to obtain it:

- 1- Do a full manual calibration using an external meter as reference where both the reference meter and the Multiple-Sensor device(with a sensor connected) are exposed to same stimulus/environment that is controllable by the user to produce all adequate variations/intensities necessary to record an extensive calibration table, with all experimental pairs of (RAW\_value,measurement).
- 2- Using a known function that relates the measured phenomena to the obtained RAW\_value on the Multiple-Sensor device (obtained by theoretical or experimental study), although a purely theoretical calibration could be used, prob-

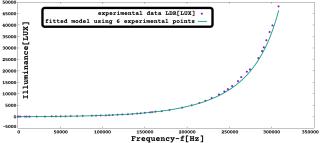


Figure 4: Plot experimental data and fitted model(by using 6 points), LDR light(brightness) sensor connected on Multiple-Sensor Interface.

ably is better or easier to obtain a calibration table by using a known function and have its constants/parameters calculated by a data fitting to some few experimental data points (RAW\_value, measurement) obtained for the device calibration. So for example if the known function had 6 constants/parameters, you would require at least 6 different experimental measurements to obtain the function for that sensor channel, then having the function is just a question calculating a longer list of pairs (RAW\_value,measurement) on the desired measurement range. Fig.4 is the result of fitting the model function  $Illuminance(f) = (a + (b/(c + d \cdot f))) \cdot ((n \cdot f^2) + m)$ , to the points (229Hz, 0LUX; 8500Hz, 10LUX; 14000Hz, 30LUX; 76500Hz, 300LUX; 130000Hz, 1072LUX; 194000Hz, 3950LUX).

#### 3 Results and Analysis

### 3.1 Device testing

The author developed and built prototypes of the described device, made of the components described on the previous section and on Fig.1 diagram. Then the device was experimented with various different sensors; including various common sensor components, namely: LDR (Light Dependent Resistor or also designated as photo-resistor), RTD(Resistance Temperature Detector), FSR(Force Sensitive Resistor), Relative-Humidity sensor (RH to impedance); as well some handmade sensors done by the author for the purpose of exploring the device usability, namely: a water level sensor (by variation of capacitance based on water height), a proximity sensor (based on the variation of inductance of a flat coil, caused by the vicinity of a metallic object, or the vicinity of a non-metallic object covered with aluminum or copper adhesive tape), a force sensor (based on resistance variation when pressed) made using 'carbon impregnated foam' (also known as ESD/antistatic foam), aluminum foil and adhesive tape.

The tests done with the device connected on the various mentioned sensors, were made with the purpose of verifying that the device is indeed usable with various types of sensors, but those tests are not the most appropriate for studying how the device works, or for characterizing the device itself by determining its usability range, or for gathering quantitative data about the device to be used along with the data from a sensor datasheet for determining its compatibility.



Figure 5: Equipment used for testing; R, C, L test components (top); and the Multiple-Sensor Interface (center bottom).

So the tests chosen for characterizing the device were records (on 2 column tables) of the measured values of inductance, resistance, capacitance paired with measured frequency on the Multiple Sensor Interface device. For these tests (Fig.5) were used arrays(PCBs) of inductors, resistors, capacitors that allow to obtain various different values just by changing a jumper/switch, also were used single components (including in series or parallel association); these fixed value components were connected as the sensor on the device. The various figures with plots/graphs on this article will show both the experimental data obtained on the mentioned tests, as well the theoretical graphs obtained from circuit analysis of the device, for comparison purposes; also at the end of the article on Appendix B are tables with the experimental data obtained on the mentioned tests.

### 3.2 Sensor Interface Circuit Analysis

#### 3.2.1 Multiple-Sensor Interface for Inductive sensors

When is connected an inductor or inductive sensor the Multiple-Sensor Interface (Fig.2) may work as a Pierce Oscillator(where the sensor is connected instead of a quartz crystal). The theoretical analysis used here for the oscillator was based on a model of 2 circuit blocks named 'A' and ' $\beta$ ' connected for feedback by connecting the output of one to the input other. The 'A' is an electronic amplifier providing voltage gain, the ' $\beta$ ' is an electronic filter providing frequency selection (resonance), so whatever voltage signal amplified by 'A' is frequency selected by ' $\beta$ ' and feed back to the input of A for further amplification. As known, this oscillator is start-up by whatever noise ( $\nu_s$ ) available at the input of 'A', Fig.6 is a diagram depicting this concept.

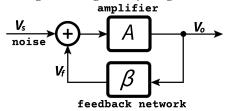


Figure 6: Diagram of model for the oscillator with an inductive sensor (Pierce Osc., model of feedback linear oscillator).

The analysis of the circuit as Pierce oscillator was made using the Barkhausen stability criterion, that says  $A\beta=1$  to be possible to occur sustained oscillations (oscillations on steady state analysis). The purpose/focus is to obtain the inductance(of sensor) as function of oscillation frequency, the Multiple-Sensor Int. circuit analysis when operating as Pierce Oscillator is available on Appendix A, and most of it is similar to typical Pierce Oscillator with piezoelectric crystal, as available on the bibliography list "Crystal Oscillators for Digital Electronics" class notes by Peter McLean [2].

The conclusion of that circuit analysis is that the equation relating the oscillation frequency with the inductance and capacitance can be written as a typical equation of LC oscillator circuits, by using the definition of a "load capacitance"  $C_L$  as  $(1/C_L) = (1/C_1) + (1/C_2)$ .

The frequency of oscillation on the Pierce oscillator (using  $C_1, C_2, L_s$ ) is:

$$\omega_0 = \frac{1}{\sqrt{L_s C_L}} \quad \Leftrightarrow \quad f_0 = \frac{1}{2\pi \sqrt{L_s C_L}}$$
 (1)

So the expression (theoretical) of measured inductance

 $L_{sensor}$  as a function of frequency(f) is:

$$L_{sensor} = L_s = \frac{1}{4\pi^2 C_L f^2} = \frac{C_1 + C_2}{4\pi^2 C_1 C_2 f^2}$$
 (2)

On experimental tests done was observed that when using  $C_1$ = $C_2$ =2.2nF (JP.A and JP.B closed) or when using  $C_1$ =21.78pF (JP.A open),  $C_2$ =2.2nF (JP.B closed), with decreasing values of  $L_s$  connected, the oscillation frequency exhibited a sudden change, at some small value of L(around  $10\mu H$  for  $C_1$ = $C_2$ =2.2nF), not coherent with theoretical model of Pierce oscillator. This may be related to the fact that the same circuit also implements a Schmitt-Trigger oscillator(next section), that oscillates under different criteria, so the author opinion is when  $L_s$  approaches some small value it may change from Pierce oscillator to Schmitt-Trigger oscillator. Fig.7 and Fig.8 shows the experimental data for various inductance values connected as the sensor and the plot  $L_s(f)$  using (2) with  $C_1$ = $C_2$ =2.2nF and  $C_1$ =21.78pF,  $C_2$ =2.2nF.

Since the mentioned sudden change of oscillator mode and frequency is not adequate on a  $L_s(f)$  function usable for sensor interfacing; then on experimental tests with jumper configuration: JP.A on and JP.B off ( $C_1$ =2.2nF,  $C_2$ =21.78pF), it was observed a continuous and progressive  $f(L_s)$  function. With  $C_1$ =2.2nF,  $C_2$ =21.78pF, the experimental  $L_{s,expr}(f)$  followed a straight line for  $L_s$  in  $[0\mu H; 100\mu H]$ , then for  $L_s$ >100 $\mu H$  the experimental  $L_{s,expr}(f)$  continued with a shape that has some visual similarity to theoretical (as Pierce oscillator), but with significantly different  $L_s$  values. It was noticed that for larger values of  $L_s$  the theoretical (Pierce oscillator, JP.A on, JP.B off) could be approximated to the experimental data by a constant multiplicative factor ( $L_{s,expr}(f) \approx 0.03 \cdot L_{s,theo}(f)$ , for  $L_s$ >1mH), as visible in Fig.9.

For modeling(data fitting) purposes, the author knows that a function  $L_s(f)=(a+(b/(c+d\cdot f)))\cdot (n\cdot f+m)$ , where 'a,b,c,d,m,n' are constants to fit, can be fitted to experimental data on both low and high values of  $L_s$ .

On following section 3.3 was used an approximated model (for Schmitt-Trigger oscillator) applied to Multiple-

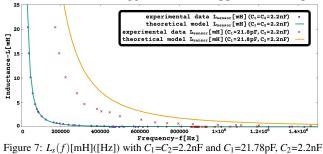


Figure 7:  $L_s(f)$ [mH]([Hz]) with  $C_1$ = $C_2$ =2.2nF and  $C_1$ =21.78pF,  $C_2$ =2.2nF (Pierce Osc., Multi-Sensor Int. with inductive sensor)

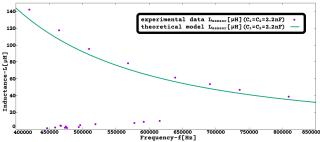


Figure 8: Frequency jump of  $L_s(f)[\mu H]([Hz])$  with  $C_1=C_2=2.2$ nF (Pierce Osc., Multi-Sensor Int. with inductive sensor).

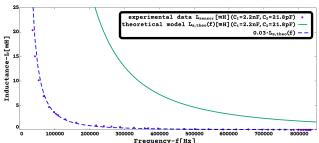


Figure 9:  $L_s(f)$ [mH]([Hz]) with  $\hat{C}_1$ =2.2nF,  $\hat{C}_2$ =21.78pF (theoretical  $L_s(f)$  as a Pierce Osc.).

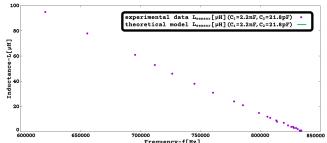


Figure 10: Experimental data of  $L_s$  in  $[0\mu H; 100\mu H]$ , with  $C_1$ =2.2nF,  $C_2$ =21.78pF (theoretical  $L_s(f)$  as a Pierce Osc.).

Sensor Interface with inductive sensor (JP.A on, JP.B off), that exhibited a theoretical  $L_s(f)$  plot much closer to the experimental data, corroborating the hypothesis that with jumper configuration JP.A on, JP.B off ( $C_1$ =2.2nF,  $C_2$ =21.78pF), it operates as a Schmitt-Trigger oscillator, where  $L_s$  acts as an impedance influencing  $C_1$  charge and discharge speed.

On following section 3.4, also about inductive sensor (JP.A on, JP.B off), was used a theoretical model(for Schmitt-Trigger oscillator) with some rude/obscene approximations; that model was successful in predicting the correct shape of  $L_s(f)$  although with a somewhat considerable displacement to the experimental data.

### 3.2.2 Multiple-Sensor Interface for Resistive sensors

In case you connect a resistive sensor (or capacitive) to the Multiple-Sensor Interface it will not be able to satisfy the conditions for oscillation of equations (35) and (36), consequent of the Barkhausen criterion applied to the circuit, as it was explained on the previous section that on the  $\pi$ (shaped)-network of Fig.37 if  $Z_1$  and  $Z_2$  are capacitive (corresponding to  $C_1$  and  $C_2$ ) then  $Z_s$  must be inductive so that  $A(\omega_0)\beta(\omega_0)=1$ . So the conclusion is when you connect a resistive sensor (or capacitive) you no longer have a Pierce Oscillator. The Multiple-Sensor Interface is made using Schmitt-trigger inverters(high-speed Si-gate CMOS, 74HC14), and the Schmitt trigger is a bistable multivibrator that can be used to implement another type of multivibrator, the relaxation oscillator. So in the case of a resistive sensor the circuit to analyze is a Schmitt-trigger inverter connected to a network of resistors and capacitors.

To analyze this circuit the Schmitt-Trigger inverter was replaced by a theoretical switch that changes the voltage of node  $v_o$  to VDDS (power supply stabilized voltage for the sensor interface) when voltage  $v_i$  is lower than  $V_T^+$ , and changes  $v_o$  to GND when voltage  $v_i$  is higher than  $V_T^+$ .

So the circuit of Fig.11 is here analyzed to obtain  $f(R_s)$ , and then its inverse function  $R_s(f)=R_{sensor}$  that may be useful for using/configuring the Multiple-Sensor Interface. Notice that  $i_i\approx 0$  since  $v_i$  is the input of a Schmitt-trigger in-

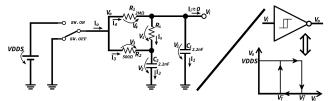


Figure 11: Multi-Sensor Int., resistive sensor(Schmitt-trigger osc.)

verter (high-speed Si-gate CMOS) that has a very high input impedance and so  $i_i \approx 0$  is an appropriate approximation simplifying the circuit. So from the circuit are obtained the Nodes and loops:  $i_4 = i_s + i_1$ , equations:

$$i_3 + i_s = i_2$$
,  $i_o = i_3 + i_4$ ,  $i_1 + i_2 = i_o$ ,  $i_1 + i_2 = i_3 + i_4$ ,  $v_1 - v_2 - v_s = 0$ ,  $v_4 + v_s + v_2 - v_o = 0$ ,  $v_4 + v_s - v_3 = 0$ ,  $v_3 = v_o - v_2$ ,  $v_4 = v_o - v_i$ ,  $v_2 = v_i - v_s$ .

Components:  $i_1=C_1(dv_1/dt),$  $i_2=C_2(dv_2/dt),$  $v_3 = R_2 i_3, \quad v_4 = R_1 i_4, \quad v_s = R_s i_s$ 

Solving:

$$\frac{v_o - v_i}{R_1} = \frac{v_s}{R_s} + C_1 \frac{dv_i}{dt} \tag{3}$$

$$\frac{v_o - v_i + v_s}{R_2} + \frac{v_s}{R_s} = C_2 \frac{dv_2}{dt} \tag{4}$$

Solving:  $v_2 = v_i - v_s \Rightarrow dv_2/dt = d(v_i - v_s)/dt \Rightarrow$  $dv_2/dt = (dv_i/dt) - (dv_s/dt)$ 

So using the previous result the (4) can be changed to:

$$\frac{v_o - v_i}{R_2} + \left(\frac{1}{R_2} + \frac{1}{R_s}\right)v_s = C_2\left(\frac{dv_i}{dt} - \frac{v_s}{dt}\right) \tag{5}$$

Solving (3) for  $v_s$  is obtained:

$$v_s = \frac{R_s(v_o - v_i)}{R_1} - R_s C_1 \frac{dv_i}{dt}$$
 (6)

Calculating the derivative on both sides of (6) is obtained (remember  $v_o$  is a constant equal to VDDS or GND depending on the position of the switch 'SW'):

$$\frac{dv_s}{dt} = \frac{-R_s}{R_1} \frac{dv_i}{dt} - R_s C_1 \frac{d^2 v_i}{dt^2} \tag{7}$$

Now using (6) and (7) to remove the variables  $v_s$  and  $dv_s/dt$ from equation (5) is obtained an equation solvable for determining  $v_i(t)$ :

$$\left(\frac{1}{R_2} + \frac{R_s}{R_2 R_1} + \frac{1}{R_1}\right) (v_o - v_i) = \\
\left(C_1 \left(1 + \frac{R_s}{R_2}\right) + C_2 \left(1 + \frac{R_s}{R_1}\right)\right) \frac{dv_i}{dt} + R_s C_1 C_2 \frac{d^2 v_i}{dt^2} \tag{8}$$

The equation (8) is of the type:  $c(v_o - v_i) = b(dv_i/dt) +$  $a(d^2v_i/dt^2)$  that has the general solution:  $v_i(t) = v_o +$  $k_1e^{\lambda_1t} + k_2e^{\lambda_2t}$ , where  $k_1,k_2$  are integration constants to be defined by 'initial conditions' and  $\lambda_1$ ,  $\lambda_2$  are defined by:  $a\lambda^2 + b\lambda + c = 0 \Leftrightarrow \lambda = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  and e is the Euler-Napier constant  $e = \sum_{n=0}^{\infty} (1/(n!))$ .

So defining here  $a_r$ ,  $b_r$ ,  $c_r$  as the values of a, b, c for obtaining  $v_i(t)$  when using a resistive sensor, has:  $a_r = R_s C_1 C_2$ ,  $b_r = (C_1(1 + (R_s/R_2))) + (C_2(1 + (R_s/R_1))),$ 

$$c_r = (1/R_2) + (R_s/(R_2R_1)) + (1/R_1)$$
.

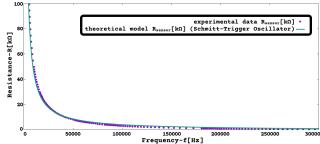


Figure 12:  $R_s[k\Omega]$  versus frequency[0Hz, 300kHz] (Schmitt-Trigger Oscillator, Multiple-Sensor Interface with resistive sensor).

In order to obtain  $v_i(t)$  for this circuit is required to calculate  $k_1$  and  $k_2$ , that are constants to be defined by 'initial conditions', the value of these constants is related to the voltage (or electrical charge) on capacitors  $C_1$  and  $C_2$  at the moment the inverter gate changes its output voltage (high to low, or low to high), on the model used for analyzing the circuit that is when the 'theoretical switch'  $v_o$  changes state. Also, is only known the value of  $v_i$  (to be  $V_T^-$  or  $V_T^+$ ) when the inverter gate  $v_o$  changes value, so is very difficult to calculate both  $k_1$  and  $k_2$  by algebraic manipulation. Admitting that  $R_1 \gg R_2$  and that  $C_1 \geq C_2$  (that is the case of the circuit that was studied and tested where  $R_1=2M\Omega$  and  $R_2=500\Omega$ ), then is known that the capacitor  $C_2$  will charge faster than  $C_1$  for all values of  $R_s$ , and in case  $R_s$  has an impedance comparable to  $R_2$  then  $C_2$  will charge much faster than  $C_1$ . So the voltage (and electrical charge) of  $C_2$  follows closely the values of  $v_o$ and so will be of small relevance to the initial conditions of the circuit, thus  $v_i(t) = v_o + k_1 e^{\lambda_1 t} + k_2 e^{\lambda_2 t}$  can be approximated as single exponential function  $v_i(t) \approx v_o + ke^{\lambda t}$ , this approximation is implied on the following calculations.

Is selected the solution  $\lambda_2 = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$  by setting  $k_1 = 0$ , because is the one that provides an adequate value for  $v_i(t)$ ,  $f(R_s)$ , consistent with experimental data, however for obtaining the function  $R_s(f)$  you may use any.

For convenience of making  $v_i(t)$  more similar to typical RC circuits is defined  $\tau = -1/\lambda$ ,  $v_i(t) = v_o + k_2 e^{-t/\tau_2}$ .

Charging time of 
$$C_1$$
:  $v_o = VDDS$   
 $v_i(t=0)=V_T^- \rightarrow V_T^- = VDDS + k_2e^0 \rightarrow k_2 = V_T^- - VDDS$   
 $v_i(t=T_C)=V_T^+ \rightarrow V_T^+ = VDDS + k_2e^{-T_C/\tau_2} \rightarrow$   
 $\rightarrow T_C = -\tau_2 ln((V_T^+ - VDDS)/(V_T^- - VDDS))$ 

Discharging time of 
$$C_1$$
:  $v_o = 0$ 

$$v_i(t=0) = V_T^+ \to V_T^+ = 0 + k_2 e^0 \to k_2 = V_T^+$$

$$v_i(t=T_D) = V_T^- \to V_T^- = 0 + k_2 e^{-T_D/\tau_2} \to T_D = -\tau_2 ln(V_T^-/V_T^+)$$

The time for a complete cycle of charge and discharge of  $C_1$  is:  $T = T_C + T_D$ ; the frequency of  $v_i(t)$  is f = 1/T.

Solving: 
$$T = -\tau_2 \left( ln \left( \frac{V_T^+ - VDDS}{V_T^- - VDDS} \right) + ln \left( \frac{V_T^-}{V_T^+} \right) \right) \iff T = \tau_2 ln \left( \frac{(V_T^- - VDDS)V_T^+}{(V_T^+ - VDDS)V_T^-} \right)$$

For convenience defining the constant 'H' by: 
$$H = ln\left(\frac{(V_T^- - VDDS)V_T^+}{(V_T^+ - VDDS)V_T^-}\right),$$
 then  $f = 1/T \Leftrightarrow f = 1/(\tau_2 H) \Leftrightarrow f = -\lambda_2/H$ .

then 
$$f = 1/T \Leftrightarrow f = 1/(\tau_2 H) \Leftrightarrow f = -\lambda_2/H$$
.

So the expression (theoretical) of measured resistance  $R_{sensor}$  as a function of frequency(f) is:

$$R_{sensor} = R_s = \frac{(C_1 + C_2)R_2R_1Hf - R_2 - R_1}{(C_2R_2Hf - 1)(C_1R_1Hf - 1)}$$
 (9)

Using the values  $C_1=C_2=2.2nF$ ,  $R_2=500\Omega$ ,  $R_1=2M\Omega$ ,  $V_T^-=1.2V$ ,  $V_T^+=2.2V$ , VDDS=4.18V, is obtained H=1.01496, Fig.12 shows experimental data for Multiple-Sensor Interface with various resistance values connected as the sensor and also shows the plot of  $R_{sensor}(f)$  using (9) with the mentioned values of  $C_1$ ,  $C_2$ ,  $R_2$ ,  $R_1$ , H.

### 3.2.3 Multiple-Sensor Interface for capacitive sensors

In case you connect a capacitive sensor (or resistive) to the Multiple-Sensor Interface it will not be able to satisfy the conditions for oscillation of the Pierce oscillator, equations (35) and (36), by  $A(\omega_0)\beta(\omega_0)=1$ , and so it is again a Schmitt-Trigger relaxation oscillator. So to analyze this circuit the Schmitt-trigger inverter was replaced by a theoretical switch (Schmitt-Trigger), just like previously with resistive sensors.

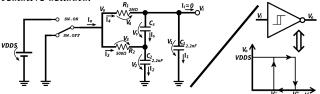


Figure 13: Multi-Sensor Int., capacitive sensor (Schmitt-trigger osc.)

So the circuit of Fig.13 is here analyzed to obtain  $f(C_s)$ , and then its inverse function  $C_s(f) = C_{sensor}$  that is useful for using/configuring the Multiple-Sensor Interface. Notice that  $i_i \approx 0$  since  $v_i$  is the input of the Schmitt-trigger inverter(high-speed Si-gate CMOS) that has a very high input impedance and so  $i_i \approx 0$  is an appropriate approximation simplifying the circuit. So from the circuit are obtained the equations:

Nodes and loops:  $i_4 = i_s + i_1$ ,  $i_3 + i_s = i_2$ ,  $i_0 = i_3 + i_4$ ,  $i_1 + i_2 = i_0$ ,  $i_1 + i_2 = i_3 + i_4$ ,  $v_1 - v_2 - v_s = 0$ ,  $v_4 + v_s + v_2 - v_0 = 0$ ,  $v_4 + v_s - v_3 = 0$ ,  $v_3 = v_0 - v_2$ ,  $v_4 = v_0 - v_i$ ,  $v_2 = v_i - v_s$ .

Components:  $i_1=C_1(dv_1/dt)$ ,  $i_2=C_2(dv_2/dt)$ ,  $v_3=R_2i_3$ ,  $v_4=R_1i_4$ ,  $i_s=C_s(dv_s/dt)$ .

Solving:

$$\frac{v_o - v_i}{R_1} = C_s \frac{dv_s}{dt} + C_1 \frac{dv_i}{dt} \tag{10}$$

$$\frac{v_o - v_2}{R_2} + C_s \frac{dv_s}{dt} = C_2 \frac{dv_2}{dt} \tag{11}$$

$$\frac{v_o - v_2}{R_2} + \frac{v_o - v_i}{R_1} = C_1 \frac{dv_i}{dt} + C_2 \frac{dv_2}{dt}$$
 (12)

Since  $v_s = v_i - v_2$  then  $dv_s/dt = (dv_i/dt) - (dv_2/dt)$ , and so using it on equation (10), is obtained:

$$\frac{dv_2}{dt} = \left(1 + \frac{C_1}{C_s}\right) \frac{dv_i}{dt} - \frac{v_o - v_i}{C_s R_1} \tag{13}$$

Using  $dv_s/dt = (dv_i/dt) - (dv_2/dt)$  and (13) on equation (11), is obtained:

$$v_{2} = v_{o} + \frac{R_{2}(C_{2} + C_{s})(v_{o} - v_{i})}{C_{s}R_{1}} + R_{2}C_{s} \left(1 - \left(1 + \frac{C_{2}}{C_{s}}\right)\left(1 + \frac{C_{1}}{C_{s}}\right)\right) \frac{dv_{i}}{dt}$$
(14)

Calculating the derivative of (14) is obtained:

$$\frac{d(v_2)}{dt} = -\frac{R_2(C_2 + C_s)}{C_s R_1} \frac{dv_i}{dt} + R_2 C_s \left( 1 - \left( 1 + \frac{C_2}{C_s} \right) \left( 1 + \frac{C_1}{C_s} \right) \right) \frac{d^2 v_i}{dt^2}$$
(15)

Now using (14) and (15) to remove the variables  $v_2$  and  $dv_2/dt$  from the equation (12), is obtained an equation solvable for determining  $v_i(t)$ :

$$v_o - v_i = (R_2(C_2 + C_s) + R_1(C_1 + C_s))\frac{dv_i}{dt} + R_2R_1(C_1C_2 + C_s(C_1 + C_2))\frac{d^2v_i}{dt^2}$$
(16)

The equation (16) is of the type:  $c(v_o-v_i)=b(dv_i/dt)+a(d^2v_i/dt^2)$ , that has the general solution:  $v_i(t)=v_o+k_1e^{\lambda_1t}+k_2e^{\lambda_2t}$ , where  $k_1,k_2$  are integration constants to be defined by 'initial conditions' and  $\lambda_1$ ,  $\lambda_2$  are defined by:  $a\lambda^2+b\lambda+c=0 \Leftrightarrow \lambda=\frac{-b\pm\sqrt{b^2-4ac}}{2a}$  and e is the Euler-Napier constant  $e=\sum_{n=0}^{\infty}(1/(n!))$ .

So defining here  $a_c$ ,  $b_c$ ,  $c_c$  as the values of a, b, c for obtaining  $v_i(t)$  when using a capacitive sensor, has:  $c_c = 1$ ,

$$b_c = (R_2(C_2 + C_s) + R_1(C_1 + C_s)),$$
  

$$a_c = R_2R_1(C_1C_2 + C_s(C_1 + C_2)).$$

In order to obtain  $v_i(t)$  for this circuit is required to calculate  $k_1$  and  $k_2$ , to be defined by 'initial conditions'; notice that this circuit has 3 capacitors that store electrical charge defining 'initial conditions', but the location of  $C_s$  connected between  $C_1$  and  $C_2$  implies that the voltage of  $C_s$  (or its electrical charge) is completely defined/known by the voltages (or electrical charges) on  $C_1$  and  $C_2$ .

Will be made the same approximation/simplification of  $v_i(t) \approx v_o + ke^{\lambda t}$ , as explained and done on the case of resistive sensor.

Is selected the solution  $\lambda_2 = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$  by setting  $k_1 = 0$ , because is the one that provides an adequate value for  $v_i(t)$ ,  $f(C_s)$ , consistent with experimental data, however for obtaining the function  $C_s(f)$  you may use any.

For convenience of making  $v_i(t)$  more similar to typical RC circuits is defined  $\tau = -1/\lambda$ , and so  $v_i(t) = v_o + k_2 e^{-t/\tau_2}$ .

So when is connected a capacitive sensor  $(C_s)$  the differential equation and solution  $v_i(t)$  are the same as when is connected a resistive sensor  $(R_s)$ , the only differences are on the values of a, b, c; and as such the equations of f(frequency) and T(period) are also the same and are reused from the previous section.

The constant 'H' defined by:

$$H = ln\left(\frac{(V_T^- - VDDS)V_T^+}{(V_T^+ - VDDS)V_T^-}\right),$$
 and  $f = 1/T \Leftrightarrow f = 1/(\tau_2 H) \Leftrightarrow f = -\lambda_2/H$ .

So the expression (theoretical) of measured capacitance  $C_{sensor}$  as a function of frequency(f) is:

$$C_{sensor} = C_s = \frac{(C_1R_1 + C_2R_2)Hf - 1 - C_1C_2R_1R_2H^2f^2}{Hf((C_1 + C_2)R_1R_2Hf - R_1 - R_2)}$$
(17)

Using the values  $C_1=C_2=2.2nF$ ,  $R_2=500\Omega$ ,  $R_1=2M\Omega$ ,  $V_T^-=1.2V$ ,  $V_T^+=2.2V$ , VDDS=4.18V, is obtained H=1.01496, Fig.14 shows the plot of  $C_s(f)$  using (17) with the mentioned values of  $C_1$ ,  $C_2$ ,  $R_2$ ,  $R_1$ , H.

Analyzing the plot on Fig.14 by firstly looking at plot regions with  $C_s>0$ , its visible that the  $C_s(f)$  plot is over the vertical axis (f=0) and this would mean that for all values of  $C_s$  the frequency would be zero (f=0), but visible to the right is another curve that is also placed on the area of  $C_s>0$  (for frequency [447957Hz, 895689Hz]) and at a first view this curve would seem appropriate. But strangely on  $C_s>0$ ,

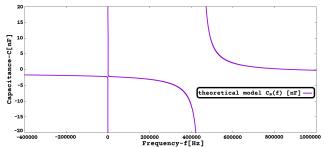


Figure 14:  $C_s(f)$  [nF] versus frequency[-400kHz, 1MHz] (Schmitt-Trigger Oscillator, Multiple-Sensor Interface with capacitive sensor).

f>0 for each value of  $C_s$  are 2 values of frequency, while for  $C_s$ <0, f>0 each value of  $C_s$  has only one possible value of frequency (f<0 is considered meaningless/ignored).

The experimental data shows that the way the oscillator works using a capacitive sensor is different from what some would expect on a first view of the plot  $C_s(f)$ , in order to compare the experimental data with the theoretical model is shown on Fig.15 and Fig.16 the experimental data for Multiple-Sensor Interface with various capacitance values connected as the sensor and also the plot of  $abs(C_s(f))$  (=  $|C_s(f)|$ ) using (17) with the mentioned values of  $C_1$ ,  $C_2$ ,  $R_1$ ,  $R_2$ , H.

So it seems that the obtained function of  $C_s(f)$  although strangely indicates negative values for the sensor capacitance it can provide a theoretical curve/plot similar to what was obtained on the experimental data for  $C_{sensor}$ . On the following sections is given a better insight on why  $C_s(f)$  has a negative value.

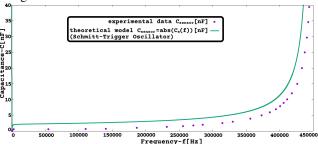


Figure 15:  $C_s[nF]$  versus frequency[0Hz, 450kHz] by  $|C_s(f)|$  (Schmitt-Trigger osc., Multi-Sensor with capacitive sensor)

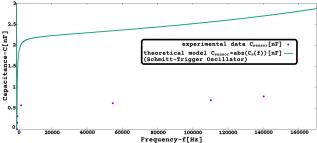


Figure 16:  $C_s[nF]$  versus frequency[0Hz, 170kHz] by  $|C_s(f)|$  (Schmitt-Trigger osc., Multi-Sensor with capacitive sensor)

#### 3.2.4 Multiple-Sensor Int. for measuring frequency

For measuring frequency of an external voltage signal (between 0V and VDDS, so preferentially a digital signal or in case of analog signal it should be limited/trimmed before) is possible to use the mentioned Multiple-Sensor Interface and so using the same port/connector of the device. For this the user should remove/open the jumpers "JP.A", "JP.B" making the capacitors C1-A, C2-B active on the circuit, this will make  $C_1 = C_2 = 21.8pF$  that is a quite low capacitance that

will have an insignificant effect on the external voltage signal. The external voltage signal should be connected to the 1st pin of the sensor channel that is the one connected directly to input of the Schmitt-Trigger Inverter, so making the inverter directly driven by the external voltage signal, then the Multiple-Sensor Interface is just a converter of the voltage signal to a square wave signal where its frequency will be measured through the counter/timer of the PIC18F2550.

The external voltage signal would preferentially be from a sensor with a square wave output, and the sensor have its power supplied by one of the VDDS,GND ports/connectors of the sensor interface device or by an external connection to the same power supply used to power the device.

### 3.3 Alternative Approximate Circuit Analysis

### 3.3.1 Sensor interface circuit simplified

The Multiple-Sensor Interface circuit when working as Schmitt-Trigger oscillator (using  $R_s$ ,  $C_s$ , or  $L_s$  with specific  $C_1$ , $C_2$  values) can be studied and understood in a more intuitive way by making some simplification/approximation that may be inaccurate for quantitative purposes but still captures its essence, with the benefit of exposing how it works and resulting in much simpler differential equations. So the interface circuit is a more complex Schmitt-Trigger oscillator, but its essence is the same, it is just some capacitors being charged by currents that pass trough some resistors, and the voltage on a capacitor( $v_i$ ) will trigger(at  $V_T^-$  or  $V_T^+$ ) a switch(electronic inverter) to change the voltage( $v_o$ ) [3].

So the sensor and interface circuit can be described approximately as a basic Schmitt-Trigger oscillator that only has one capacitor and one resistor (that determine the frequency of oscillation), and so was used the simplified circuit on Fig.17 where  $C_{approx}$  is a capacitor and  $R_{approx}$  is a resistor that approximate in overall the capacitance and resistance of the sensor interface oscillator.

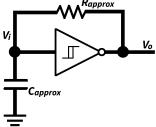


Figure 17: Schematic of a basic Schmitt-Trigger Oscillator to be used as an approximation of the circuit of Multiple-Sensor Interface

To build expressions of  $C_{approx}$  and  $R_{approx}$  that include  $R_1$ ,  $R_2$ ,  $C_1$ ,  $C_2$  are considered initially 2 extreme cases of the sensor impedance( $Z_s$ ): 1st  $|Z_s|$ =0 the sensor can be replaced by a wire, and 2nd  $|Z_s|$ = $\infty$  the sensor can be removed(open circuit), these 2 extreme cases possible for the sensor impedance are represented on Fig.18.

Now the sensor can be described as an electric connection that can be weakened or intensified depending on the sensor impedance, so when  $|Z_s|$  changes progressively from 0 to  $+\infty$  the circuit behavior changes progressively and smoothly from the behavior of the left circuit to the behavior of right circuit of Fig.18. So to obtain equations for  $R_{approx}$  and  $C_{approx}$  was selected an expression that allows to change smoothly the resistance and capacitance of the left side circuit to the resistance and capacitance of the right side circuit of Fig.18.

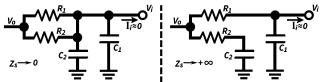


Figure 18: Schematic of the RC network of the Schmitt-Trigger Oscillator for the 2 extreme cases of sensor impedance ( $Z_s$ ).

So as on Fig.18, here are the values of  $C_{approx}$  and  $R_{approx}$  for the 2 extreme values of  $|Z_s|$ =0 and  $|Z_s|$ =+ $\infty$ :

$$C_{approx}(Z_s=0)=C_1+C_2;$$
  $C_{approx}(Z_s=\infty)=C_1;$   $R_{approx}(Z_s=0)=(R_1R_2)/(R_1+R_2);$   $R_{approx}(Z_s=\infty)=R_1;$ 

# 3.3.2 $R_{approx}$ and $C_{approx}$ for a resisitve sensor $(R_s)$

Here are functions modeled to describe  $C_{approx}$  and  $R_{approx}$  (with resistive sensor) with a smooth transition from its values at  $|Z_s|=0$  and  $|Z_s|=+\infty$ , where  $|Z_s|=R_s$ :

$$C_{approx} = (C_1 + C_2) \frac{R_1}{|Z_s| + R_1} + C_1 \frac{|Z_s|}{|Z_s| + R_1}$$
 (18)

$$R_{approx} = \frac{R_1 R_2}{(R_1 + R_2)} \frac{2R_1}{(|Z_s| + 2R_1)} + R_1 \frac{|Z_s|}{|Z_s| + 2R_1}$$
(19)

Using the equations:  $f=1/T \Leftrightarrow f=1/(\tau H) \Leftrightarrow f=-\lambda/H$ , and using  $\tau=R_{approx}C_{approx}$ , where  $|Z_s|$  was removed using  $|Z_s|=R_s$ , it can be obtained  $R_s(f)$ .

Using values  $V_T^-$ =1.2V,  $V_T^+$ =2.2V, VDDS=4.18V, is obtained H=1.01496 (valid for any type of sensor).

Using the values  $C_1=C_2=2.2nF$ ,  $R_2=500\Omega$ ,  $R_1=2M\Omega$ , H=1.01496 with the approximate model ( $C_{approx}$ ,  $R_{approx}$ ), is obtained the plot of  $R_s(f)$  on Fig.19.

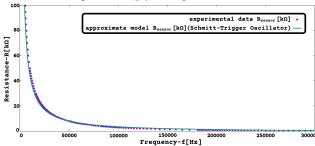


Figure 19:  $R_s(f)[k\Omega]$  by approximate model ( $C_{approx}$ ,  $R_{approx}$ ; Multi-Sensor Int. with resistive sensor).

### 3.3.3 $R_{approx}$ and $C_{approx}$ for an inductive sensor $(L_s)$

This approximate model for the interface circuit with inductive sensor is only valid for jumper configuration(capacitor values) that make it work as Schmitt-Trigger oscillator, as is expected for JP.A closed, JP.B open  $(C_1=2.2\text{nF}, C_2=21.78\text{pF})$ . Here are functions modeled to describe  $C_{approx}$  and  $R_{approx}$  (with inductive sensor) with a smooth transition from its values at  $|Z_s|=0$  and  $|Z_s|=+\infty$ , where  $|Z_s|=2\pi f L_s$ :

$$C_{approx} = (C_1 + C_2) \frac{R_1}{|Z_s| + R_1} + C_1 \frac{|Z_s|}{|Z_s| + R_1}$$
 (20)

$$R_{approx} = \frac{R_1 R_2}{(R_1 + R_2)} \frac{R_1}{(|Z_s| + R_1)} + R_1 \frac{|Z_s|}{|Z_s| + R_1}$$
(21)

Using the values  $C_1$ =2.2nF,  $C_2$ =21.78pF,  $R_2$ =500 $\Omega$ ,  $R_1$ =2 $M\Omega$ , H=1.01496 with the approximate model ( $C_{approx}$ ,  $R_{approx}$ ), is obtained the plot of  $L_s(f)$  on Fig.20 and Fig.21.

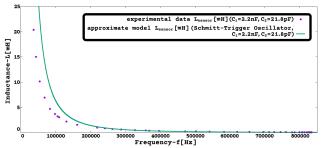


Figure 20:  $L_s$ [mH] versus frequency[0Hz, 850kHz] by approximate model ( $C_{approx}$ ,  $R_{approx}$ ; Multi-Sensor Int. with inductive sensor)

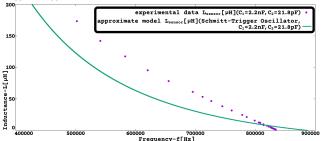


Figure 21:  $L_s[\mu H]$  versus frequency=f[Hz] by approximate model ( $C_{approx}$ ,  $R_{approx}$ ; Multi-Sensor Int. with inductive sensor)

### 3.3.4 $R_{approx}$ and $C_{approx}$ for a capacitive sensor $(C_s)$

Here are functions modeled to describe  $C_{approx}$  and  $R_{approx}$  (with capacitive sensor) with a smooth transition from its values at  $|Z_s|$ =0 and  $|Z_s|$ = +  $\infty$ , where  $|Z_s|$ =1/(2 $\pi f C_s$ ):

$$C_{approx} = (C_1 + C_2) \frac{R_1}{|Z_s| + R_1} + C_1 \frac{|Z_s|}{|Z_s| + R_1}$$
 (22)

$$R_{approx} = \frac{R_1 R_2}{(R_1 + R_2)} \frac{R_1}{(|Z_s| + R_1)} + R_1 \frac{|Z_s|}{|Z_s| + R_1}$$
(23)

Using the values  $C_1=C_2=2.2nF$ ,  $R_2=500\Omega$ ,  $R_1=2M\Omega$ , H=1.01496, with the approximate model ( $C_{approx}$ ,  $R_{approx}$ ), is obtained the plot  $C_s(f)$  on Fig.22 and Fig.23.

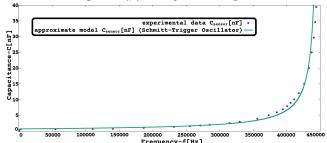


Figure 22:  $C_s[nF]$  versus frequency[0Hz, 450kHz] by approximate model ( $C_{approx}$ ,  $R_{approx}$ ; Multi-Sensor Int. with capacitive sensor)

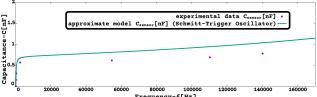


Figure 23:  $C_s[nF]$  versus frequency[0Hz, 170kHz] by approximate model ( $C_{approx}$ ,  $R_{approx}$ ; Multi-Sensor Int. with capacitive sensor)

## 3.4 Multiple-Sensor Interface for Inductive Sensors as Schmitt-Trigger Oscillator

Also is possible a theoretical analysis of the Multiple-Sensor Interface with an inductive sensor working continuously as a Schmitt-Trigger Oscillator observed when jumper configuration is JP.A on, JP.B off ( $C_1$ =2.2nF,  $C_2$ =21.78pF), although will be made some approximations to be able to obtain a  $L_s(f)$  function.

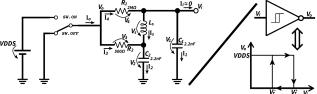


Figure 24: Multi-Sensor Int., inductive sensor(Schmitt-trigger osc.)

So the circuit of Fig.24 is here analyzed to obtain an approximation of  $f(L_s)$ , and of its inverse function  $L_s(f)=L_{sensor}$  that is useful for using/configuring the Multiple-Sensor Interface. Notice that  $i_i \approx 0$  since  $v_i$  is the input of the Schmitt-trigger inverter(high-speed Si-gate CMOS) that has a very high input impedance and so  $i_i \approx 0$ is an appropriate approximation simplifying the circuit. So from the circuit are obtained the equations:

Nodes and loops:  $i_4 = i_s + i_1$ ,  $i_0 = i_3 + i_4$ ,  $i_1 + i_2 = i_0$ ,  $i_1 + i_2 = i_3 + i_4$ ,  $v_1 - v_2 - v_s = 0$ ,  $v_4 + v_s + v_2 - v_o = 0$ ,  $v_4 + v_s - v_3 = 0$ ,  $v_3 = v_o - v_2$ ,  $v_4 = v_o - v_i$ ,  $v_2 = v_i - v_s$  $i_1=C_1(dv_1/dt),$ Components:  $i_2 = C_2(dv_2/dt),$  $v_3 = R_2 i_3$ ,  $v_4 = R_1 i_4$ ,  $v_s = L_s(di_s/dt)$ . Solving:

$$\frac{v_o - v_2}{R_2} + \frac{v_o - v_i}{R_1} = C_1 \frac{dv_i}{dt} + C_2 \frac{dv_2}{dt}$$
 (24)

$$v_2 = v_i - L_s \frac{di_s}{dt} \tag{25}$$

$$\frac{v_o - v_i}{R_1} = i_s + C_1 \frac{dv_i}{dt} \tag{26}$$

From (25) is obtained  $dv_2/dt = (dv_i/dt) - L_s(d^2i_s/dt^2)$ , and so using it on equation (24), is obtained:

$$(v_o - v_i) \left( \frac{1}{R_1} + \frac{1}{R_2} \right) + \frac{L_s}{R_2} \frac{di_s}{dt} = (C_1 + C_2) \frac{dv_i}{dt} - L_s C_2 \frac{d^2 i_s}{dt^2}$$
(27)

From equation (26) is obtained:

$$i_{s} = \frac{v_{o} - v_{i}}{R_{1}} - C_{1} \frac{dv_{i}}{dt} \quad \Rightarrow \quad \frac{di_{s}}{dt} = -\frac{1}{R_{1}} \frac{dv_{i}}{dt} - C_{1} \frac{d^{2}v_{i}}{dt^{2}}$$
$$\Rightarrow \quad \frac{d^{2}i_{s}}{dt^{2}} = -\frac{1}{R_{1}} \frac{d^{2}v_{i}}{dt^{2}} - C_{1} \frac{d^{3}v_{i}}{dt^{3}} \quad (28)$$

Then using equation (28),  $i_s$  can be eliminated from equation (27), obtaining:

$$\left(\frac{1}{R_1} + \frac{1}{R_2}\right)(v_o - v_i) =$$

$$\left(C_1 + C_2 + \frac{L_s}{R_1 R_2}\right) \frac{dv_i}{dt} + L_s \left(\frac{C_1}{R_2} + \frac{C_2}{R_1}\right) \frac{d^2 v_i}{dt^2} + L_s C_1 C_2 \frac{d^3 v_i}{dt^3}$$

The equation (29) is of the type:  $d(v_o - v_i) = c(dv_i/dt) +$  $b(d^2v_i/dt^2) + a(d^3v_i/dt^3)$  that has the general solution:  $v_i(t) = v_o + k_1e^{\lambda_1t} + k_2e^{\lambda_2t} + k_3e^{\lambda_3t}$ , where  $k_1, k_2, k_3$  are integration constants to be defined by 'initial conditions' and  $\lambda_1$ ,  $\lambda_2$ ,  $\lambda_3$  are defined by:  $a\lambda^3 + b\lambda^2 + c\lambda + d = 0$  and e is the Euler-Napier constant  $e = \sum_{n=0}^{\infty} (1/(n!))$ .

So defining here  $a_l$ ,  $b_l$ ,  $c_l$ ,  $d_l$  as the values of a, b, c, d for obtaining  $v_i(t)$  when using an inductive sensor, has:

$$a_l = L_s C_1 C_2$$
,  
 $b_l = L_s ((C_1/R_2) + (C_2/R_1))$ ,  
 $c_l = C_1 + C_2 + (L_s/(R_1R_2))$ ,  
 $d_l = (1/R_1) + (1/R_2)$ .

In order to obtain  $v_i(t)$  for this circuit is required to calculate  $k_1$ ,  $k_2$  and  $k_3$ , that are constants to be defined by 'initial conditions', the value of these constants is related to the voltage (or electrical charge) on capacitors  $C_1$  and  $C_2$ , and also to the electric current on the inductive sensor, at the moment the inverter gate changes its output voltage (high to low, or low to high), on the model used for analyzing the circuit that is when the 'theoretical switch'  $v_o$  changes state. Also, is only known the value of  $v_i$  (to be  $V_T^-$  or  $V_T^+$ ) when the inverter gate  $v_o$  changes value, so is very difficult to calculate  $k_1$ ,  $k_2$ ,  $k_3$  by algebraic manipulation. Admitting that  $R_1 \gg R_2$  and that  $C_1 \geq C_2$  (that is the case of the circuit that was studied and tested where  $R_1=2M\Omega$  and  $R_2=500\Omega$ ), then is known that the capacitor  $C_2$  will charge faster than  $C_1$  for all values of  $Z_s$  (determined by the value  $L_s$ ), and in case  $Z_s$  has an impedance comparable to  $R_2$  then  $C_2$  will charge much faster than  $C_1$ . So the voltage (and electrical charge) of  $C_2$  follows closely the values of  $v_0$  and so will be of small relevance to the initial conditions of the circuit.

The inclusion of an inductor (the inductive sensor) makes the behavior of this circuit more complex and so the appearance of a 3rd degree differential equation; so in order to obtain an expression for  $L_s(f)$  in a similar way as previously for resistive and capacitive sensors, will be made the following approximations: 1 - The determination of  $L_s(f)$  will be made in two domains, one expression of  $L_s(f)$  valid for high frequency and other expression of  $L_s(f)$  for low and middle frequency of the operation of the Schmitt-Trigger Oscillator. The author observed that high frequency operation is dominated by the 1st-root of  $a\lambda^3 + b\lambda^2 + c\lambda + d = 0$ that is a real number; and observed that low and middle frequency operation is dominated by the 2nd-root and 3rd-root of  $a\lambda^3 + b\lambda^2 + c\lambda + d = 0$  that are imaginary numbers.

2 - Regarding the low and middle frequency operation that is dominated by the 2nd-root and 3rd-root of the 3rd degree equation, will be made a 'rude' approximation of  $v_i(t) \approx v_o +$  $k_{23}e^{\lambda_{23}t}$ , where  $k_{23}=(k_2+k_3)/2$  and  $\lambda_{23}=(\lambda_2+\lambda_3)/2$ . Also is relevant to note that by summing  $\lambda_2$  with  $\lambda_3$  will nullify the imaginary part resulting in a real number, and also that  $\lambda_{23} = (\lambda_2 + \lambda_3)/2 = Re[\lambda_2] = Re[\lambda_3].$ 

The mentioned approximations produce an approximated  $v_i(t)$  function that is a single exponential function, instead of the sum of 3 exponentials that was obtained as solution of the 3rd degree differential equation; then a  $v_i(t)$  that is a single exponential function allows the theoretical analysis already used for resistive and capacitive sensor to be reused (29) again here, for obtaining  $L_s(f)$ .

So for an inductive sensor, just like with resistive or capacitive sensor, is used the function  $v_i(t) = v_o + ke^{-t/\tau}$ , where  $\tau = -1/\lambda$ , and the constant 'H' defined by:  $H = ln\left(\frac{(V_T - VDDS)V_T^+}{(V_T^+ - VDDS)V_T^-}\right),$ 

$$H = ln\left(\frac{(V_T^- - VDDS)V_T^+}{(V_T^+ - VDDS)V_T^-}\right)$$

and 
$$f = 1/T \Leftrightarrow f = 1/(\tau H) \Leftrightarrow f = -\lambda/H$$
.

So applying the previously mentioned approximations is obtained:  $f_{high} \approx -\lambda_1/H$ ;  $f_{low,middle} \approx -\lambda_{23}/H$ .

So the expression (theoretical) of measured inductance  $L_{sensor}$  as a function of frequency(f) for high frequency is:

$$L_{sensor,HF} = L_{s,HF} = \frac{R_1 + R_2 - (C_1 + C_2)R_1R_2Hf}{Hf(C_1R_1Hf - 1)(C_2R_2Hf - 1)}$$
(30)

So the expression (theoretical) of measured inductance  $L_{sensor}$  as a function of frequency(f) for low and middle frequency is:

$$L_{sensor,LMF} = L_{s,LMF} = (C_1^2 R_1^2 R_2 + C_2^2 R_2^2 R_1 - 2R_1^2 R_2^2 H f (C_1^2 C_2 + C_2^2 C_1)) / (8C_1^2 C_2^2 R_1^2 R_2^2 H^3 f^3 - 8C_1 C_2^2 R_1 R_2^2 H^2 f^2 - 8C_1^2 C_2 R_1^2 R_2 H^2 f^2 + 2C_2^2 R_2^2 H f + 6C_1 C_2 R_1 R_2 H f + 2C_1^2 R_1^2 H f - C_1 R_1 - C_2 R_2)$$
(31)

Using the values  $C_1$ =2.2nF,  $C_2$ =21.78pF,  $R_2$ =500 $\Omega$ ,  $R_1$ =2 $M\Omega$ ,  $V_T^-$ =1.2V,  $V_T^+$ =2.2V, VDDS=4.18V, is obtained H=1.01496, Fig.25 shows the plot of  $L_{s,HF}(f)$  using (30) with the mentioned values of  $C_1$ ,  $C_2$ ,  $R_2$ ,  $R_1$ , H.

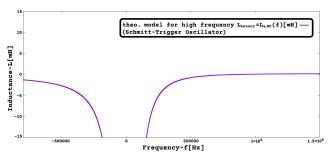


Figure 25:  $L_{s,LMF}(f)$  [mH] versus frequency[-800kHz, 1.5MHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, HF approx. model).

Observing Fig.25 is noticeable that  $L_{s,HF}(f)$  is almost always negative, except for frequency above around 900kHz. However drawing the plot of  $abs(L_{s,HF}(f))$  (=  $|L_{s,HF}(f)|$ ) along with experimental data for Multiple-Sensor Interface with various inductance values connected as the sensor (on Fig.26 and Fig.27 ), like was done before for the plots of a capacitive sensor, is then visible that the shape of  $abs(L_{s,HF}(f))$  resembles the experimental data, however significantly displaced above the experimental data for low and middle values of frequency, but for high frequency the plot of  $abs(L_{s,HF}(f))$  is much closer to the experimental data and correctly predicts that a value of  $L_s = 0$  will result on an oscillation frequency somewhat above 800kHz but lower than 900kHz.

The Fig.28 and Fig.29, shows experimental data for Multiple-Sensor Interface with various inductance values connected as the sensor, and the plot of  $L_{s,LMF}(f)$  using (31) with the mentioned values of  $C_1$ ,  $C_2$ ,  $R_2$ ,  $R_1$ , H.

A way for obtaining a theoretical function (by previously mentioned approximations/simplifications) valid for all values of frequency, that captures the behavior of the Multiple-Sensor Interface with an inductive sensor, is to combine both the expressions  $abs(L_{s,HF}(f))$  and  $L_{s,LMF}(f)$  into a single function. That function can be obtained for example by multiplying  $abs(L_{s,HF}(f))$  with a moderating function that silences it on low and middle frequency and by multiplying  $L_{s,LMF}(f)$  with a moderating function that silences it on high frequency, then sum these 2 parts to obtain  $L_s(f)$ .

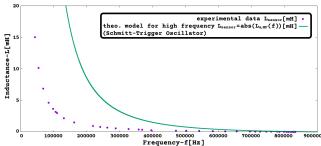


Figure 26:  $abs(L_{s,HF}(f))$  [mH] versus frequency[0Hz, 900kHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, HF approx. model).

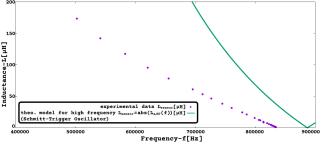


Figure 27:  $abs(L_{s,HF}(f))$  [ $\mu$ H] versus frequency[400kHz, 900kHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, HF approx. model).

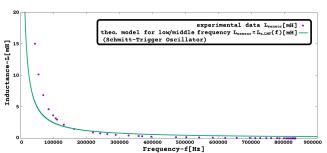


Figure 28:  $L_{s,LMF}(f)$  [mH] versus frequency[0Hz, 900kHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, LMF approx. model).

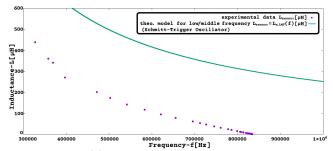


Figure 29:  $L_{s,LMF}(f)$  [ $\mu$ H] versus frequency[300kHz, 1MHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, LMF approx. model).

A set of 2 good moderating functions, considering the used values for the parameters  $C_1$ ,  $C_2$ ,  $R_2$ ,  $R_1$ , H, would be for example:

$$m_{HF,ef}(f) = (((-1 + (e^{(f/100000)-5}))/(1 + (e^{(f/100000)-5}))) + 1)/2$$
  

$$m_{LMF,ef}(f) = (((-1 + (e^{(-f/100000)+5}))/(1 + (e^{(-f/100000)+5}))) + 1)/2$$

These moderating functions are good because:  $m_{HF,ef}(f) + m_{LMF,ef}(f) \approx 1$ ,  $\forall f$  and also:  $m_{HF,ef}(f=0) \approx 0$ ;  $m_{HF,ef}(f=900 \text{kHz}) \approx 1$ ;  $m_{HF,ef}(f=+\infty) = 1$ ;  $m_{LMF,ef}(f=+\infty) = 0$ ;  $m_{LMF,ef}(f=0) \approx 1$ ;  $m_{LMF,ef}(f=900 \text{kHz}) \approx 0$ ;  $m_{LMF,ef}(f=500 \text{kHz}) \approx m_{LMF,ef}(f=500 \text{kHz}) \approx 0.5$ .

However the moderating functions  $m_{HF,ef}(f)$ ,  $m_{LMF,ef}(f)$  are exponential functions that are undesirably complex and heavy to evaluate; so here is suggested another set of 2 mod-

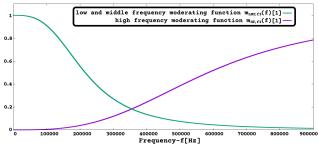


Figure 30:  $m_{LMF,f3}(f)$  and  $m_{HF,f3}(f)$  [1] versus frequency[0Hz, 900kHz]. erating functions that are simpler and faster to evaluate, although the property  $m_{HF}(f)+m_{LMF}(f)\approx 1$  will only be true on a small frequency range (not on the entire range [0Hz; 900kHz] as with previous moderating functions) and that will cause some distortion (undesirable change) on the theoretical model. Since the theoretical model is not accurate because of the approximations that were used for obtaining a solution to the initial value problem (that had 3 unknowns  $k_1$ ,  $k_2$ ,  $k_3$ , but was solved as if had a single unknown), and also knowing that  $abs(L_{s,HF}(f))$  is always above the experimental data and that  $L_{s,LMF}(f)$  is above the experimental data for most of the plot (except for f<200kHz), then can be selected moderating functions that have a 'distortion' that actually approximates(lowers the value of)  $abs(L_{s,HF}(f))$  and  $L_{s,LMF}(f)$  to the experimental data.

A set of 2 moderating functions that are more simple and fast/easy to evaluate, but 'distort' (lower) the value of  $L_s(f)$ :

$$m_{HF,f3}(f) = (a_{HF} \cdot f^3)/(1 + a_{HF} \cdot f^3)$$
  
 $m_{LMF,f3}(f) = 1/(1 + a_{LMF} \cdot f^3)$ 

where constant  $a_{HF}$  is selected/adjusted so that ideally when  $abs(L_{s,HF}(f)) = 0$  then  $m_{HF,f3}(f) \approx 1$ , or most likely since that is not easy/possible then somewhere above 0.7, while keeping  $m_{HF,f3}(f) < 0.3$  for frequencies where  $abs(L_{s,HF}(f))$  should be silenced; and constant  $a_{LMF}$  is selected/adjusted to not silencing  $L_{s,LMF}(f)$  except at high frequency close to the frequency where  $abs(L_{s,HF}(f)) = 0$ . So for this case with  $C_1$ =2.2nF,  $C_2$ =21.78pF,  $R_2$ =500 $\Omega$ ,  $R_1$ =2 $M\Omega$ , H=1.01496, the author chose/selected the values:  $a_{HF} = 5 \cdot 10^{-18} \ [s^3]$ ,  $a_{LMF} = 10^{-16} \ [s^3]$ .

So by first determining the frequency where  $abs(L_{s,HF}(f)) = 0$  for some selected values of the parameters  $C_1$ ,  $C_2$ ,  $R_2$ ,  $R_1$ , H, then is possible to create a theoretical function (by the previously mentioned approximations/simplifications) through  $m_{HF,f3}(f)$ ,  $m_{LMF,f3}(f)$ , to be valid for all values of frequency:

$$L_{s,LMF,HF}(f) = (L_{s,LMF}(f)) \cdot (m_{LMF,f3}(f)) + abs(L_{s,HF}(f)) \cdot (m_{HF,f3}(f))$$
(32)

The Fig. 31 and Fig. 32, shows experimental data for Multiple-Sensor Interface with various inductance values connected as the sensor, and the plot of  $L_{s,LMF,HF}(f)$  using (32) with  $C_1$ =2.2nF,  $C_2$ =21.78pF,  $R_2$ =500 $\Omega$ ,  $R_1$ =2 $M\Omega$ , H=1.01496,  $a_{HF}$  = 5 · 10<sup>-18</sup>  $s^3$ ,  $a_{LMF}$  = 10<sup>-16</sup>  $s^3$ .

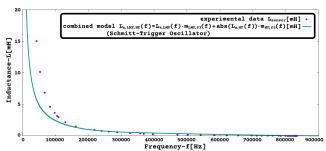


Figure 31:  $L_{s,LMF,HF}(f)$  [mH] versus frequency[0Hz, 900kHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, LMF and HF combined approx. model, with  $C_1$ =2.2nF,  $C_2$ =21.78pF).

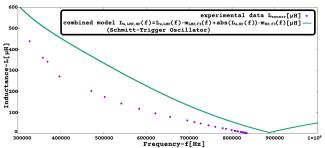


Figure 32:  $L_{s,LMF,HF}(f)$  [ $\mu$ H] versus frequency[300kHz, 1MHz] (Sch-Trig. Osc., Multi-Sensor Int. with inductive sensor, LMF and HF combined approx. model, with  $C_1$ =2.2nF,  $C_2$ =21.78pF).

### 4 Discussion

The experimental data obtained when testing the Multiple-Sensor Interface is in overall close to the values calculated using the formulas obtained from the circuit analysis, as it is visible on the various figures that show the plots of the experimental data along with graphs done using the mentioned formulas. In some graphs occurred a deviance or offset between the theoretical and experimental quantitative values, however the observable deviations are not reason for concern as they never affected the similitude between theoretical and experimental graphs (with exception of Fig.9 and Fig.10 that as explained, when using that specific configuration the device no longer behaves as Pierce oscillator, but instead as a Schmitt Trigger oscillator, as it was shown on later subsection using an 'Alternative Approximate Circuit Analysis'). The information that is made available on the article, besides explaining how the device works, may also be useful for a user of the device/technology for determining if a specific sensor of his interest is compatible/usable when connected to the Multiple-Sensor device, namely by observing on the graphs (or tables), for what range of values (min. and max.) of the sensor electrical quantity ( $R_s$  or  $C_s$ or  $L_s$ ) it is verified that a change on the quantity the sensor is measuring will produce/cause also a significant or measurable change of the signal frequency on the output of the oscillator used for sensor interfacing.

### 4.1 Future Work

Further work related to the content/topic and the sensor interface circuit could be developing a better understanding/prediction of why/when the Multiple-Sensor Interface with inductive sensor changes from working as Pierce Oscillator to Schmitt-Trigger Oscillator depending on the values of  $C_1$  and  $C_2$  capacitors (whose values can be adjusted by jumpers JP.A and JP.B).

Other future work, outside the scope of this article, could be characterizing, testing, and comparing this sensor interface circuit for specific sensor types and/or applications, thus allowing a performance comparison with other technologies on specific use cases.

# 4.2 Why $C_s(f) < 0$ on Multi-Sensor with capacitive sensor

About  $C_s(f)<0$  have in mind the Multiple-Sensor with capacitive sensor is studied on transient behavior (relaxation oscillator), where 'frequency' is a measure of the speed of charge and discharge on C1; and also of how fast the transient circuit analysis alternates between  $v_o=VDDS$  and  $v_o=0$ .

To understand why a normal capacitor behaves as a negative capacitance when connected as the sensor of the Multiple-Sensor Interface (this is, why  $C_s(f) < 0$ ), is important to highlight some things already explored on the previous sections:

- 1)  $C_1=C_2$ ,  $R_1\gg R_2$ .
- 2) The primary path (always available) to charge  $C_1$  is through  $R_1$ , the primary path (always available) to charge  $C_2$  is through  $R_2$ , since  $R_1 \gg R_2$  and  $C_1 = C_2$  this implies that capacitor  $C_2$  will charge/discharge much faster(takes less time) than capacitor  $C_1$ .
- 3) The purpose of sensor  $C_s$  on this circuit is to act as a variable impedance that can establish an alternative path on the circuit  $(V_o \rightarrow R_2 \rightarrow C_s \rightarrow C_1)$  to charge/discharge capacitor  $C_1$ ; so  $C_s \nearrow \Rightarrow |Z_s| \searrow \Rightarrow R_{approx} \searrow \Rightarrow \tau_2 \searrow \Rightarrow C_1$ charges faster.
- 4) No matter how small  $|Z_s|$  may be the capacitor  $C_2$  will always charge/discharge faster than capacitor  $C_1$ , and on the limit where  $|Z_s|$ =0 the capacitors  $C_1$  and  $C_2$  will be charged/discharged simultaneously.

For the following discussion was used as definition of capacitance the formula  $C_s = i_s/(dv_s/dt)$ , where the  $|C_s| = |Q_s|/|v_s|$  ( $C_s$ : [F] farad;  $Q_s$ : [C] coulomb;  $v_s$ : [V] volt), and since the only purpose is to show how  $C_s$  can be a negative number it was used the approximate expression  $C_s \approx \overline{i_s}/(\Delta v_s/\Delta t)$  that provides exactly the same sign as the exact formula. To show is possible  $C_s < 0$  were considered qualitative relations of the circuit electrical parameters on the RC network of the oscillator, the relevant electrical parameters and their variation between  $t=t_1$  and  $t=t_2$  is represented on Fig.33.

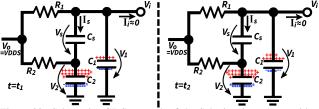


Figure 33: Schematic of RC network of the Schmitt-trigger osc. with a representation of electrical charge on  $C_1$ ,  $C_2$  on  $t=t_1$  and  $t=t_2$ .

It were assumed symbolic values for the voltages on the circuit, used as specimen values to determine how fast a voltage is changing between  $t_1$  and  $t_2$  time moments. So for representing a small amount of electrical charge are used the symbols: [+] for positive charge and [-] for negative charge, since already stated  $C_1 = C_2$  for each additional amount of [+] and [-] charge stored on each plate (of  $C_1$  or  $C_2$ ) will cause an increase of capacitor voltage that will be represented as  $[+\underline{\nu}]$ , where  $C_1 = C_2 = [+]/[+\underline{\nu}]$ .

As visible on Fig.33,  $V_o=VDDS\approx +4.18V$ , and so VDDS will eventually be the voltage on  $C_1$  and  $C_2$  when  $t\rightarrow \infty$ .

For making visual on the schematic the charging process, the charge accumulated in  $C_1$ ,  $C_2$  was divided in 20 sets, each represented by [+], [-]; and for each set of accumulated charge is associated a corresponding increase in voltage of  $[+\underline{y}]$ , and so  $[+\underline{y}] = VDDS/20$ .

Accordingly on Fig.33 is represented that  $C_2$  is charged to near the final value (VDDS) during the interval  $[0;t_1]$  while  $C_1$  charges much slower. During interval  $[t_1;t_2]$  is visible that  $C_2$  increased its charge only by 1[+] becoming charged to approximately(or practically) its final value( $v_2 \approx VDDS$ ), whether  $C_1$  is still charging and  $v_1$  is far from its final value(VDDS), but interestingly  $v_1$  is now increasing faster than  $v_2$ , because  $v_2$  already reached its final value, this is  $dv_1/dt > dv_2/dt, \forall t \in [t_1;t_2]$ . The specimen values here mentioned are in line with the exponential function typical of capacitors charging through a resistor, where lets say a capacitor initially charges very fast, when has some charge stored it charges more slowly, and when close to being full it charges very slowly (where full means the capacitor voltage is close to power supply voltage).

#### 4.2.1 Voltage and current specimens for $t=t_1$

So looking at the schematic on left side of Fig.33 is visible  $C_1$  and  $C_2$  are charging and for  $t=t_1$  the charge on  $C_1$  is 5[+] and on  $C_2$  is 19[+], so capacitor  $C_2$  is almost charged while  $C_1$  is still charging. Capacitor  $C_1$  is charging through the path  $V_o \rightarrow R_1 \rightarrow C_1$  but mainly is charging through path  $V_o \rightarrow R_2 \rightarrow C_s \rightarrow C_1$ , since  $v_2 > v_1$  then  $i_s(t=t_1) < 0$ . For  $t=t_1$ ,  $Q_1=5[+]$ ,  $Q_2=19[+]$ , then  $v_1=5[+\underline{v}]$ ,  $v_2=19[+\underline{v}]$ , since  $v_s=v_1-v_2$  then  $v_s(t=t_1)=5[+\underline{v}]-19[+\underline{v}]=-14[+\underline{v}]$ .

### 4.2.2 Voltage and current specimens for $t=t_2$

So looking at the schematic on right side of Fig.33 is visible  $C_1$  and  $C_2$  are charging and for t=t2 the charge on  $C_1$  is 9[+] and on  $C_2$  is 20[+], so capacitor  $C_2$  is fully charged while  $C_1$  is still charging. Capacitor  $C_1$  is charging through the path  $V_o \rightarrow R_1 \rightarrow C_1$  but mainly is charging through path  $V_o \rightarrow R_2 \rightarrow C_s \rightarrow C_1$ , since  $v_2 > v_1$  then  $i_s(t = t_2) < 0$ .

For  $t=t_2$ ,  $Q_1=9[+]$ ,  $Q_2=20[+]$ , then  $v_1=9[+\underline{v}]$ ,  $v_2=20[+\underline{v}]$ , since  $v_s=v_1-v_2$  then  $v_s(t=t_2)=9[+\underline{v}]-20[+\underline{v}]=-11[+\underline{v}]$ .

4.2.3 Sign of  $C_s$  as calculated from  $v_s$  and  $i_s$  during  $[t_1;t_2]$ 

The schematics on Fig.33 refer to a charging cycle of the Schmitt Trigger Oscillator. Also  $t_2 > t_1 \rightarrow \Delta t > 0$ .

For  $t \in [t_1;t_2]$  the capacitor  $C_1$  is being charged through the path  $V_o \rightarrow R_2 \rightarrow C_s \rightarrow C_1$  and so  $i_s(t) < 0, \forall t \in [t_1;t_2] \Rightarrow \overline{i_s} < 0$ . Also  $\Delta v_s$  between  $t_1$  and  $t_2$  is  $\Delta v_s = v_s(t=t_2) - v_s(t=t_1) = -11[+\underline{v}] - (-14[+\underline{v}]) = 3[+\underline{v}]$ , so  $\Delta v_s > 0$  between  $t_1$  and  $t_2$ .

So concluding between  $t_1$  and  $t_2$ ,  $\Delta t > 0$ ,  $\Delta v_s > 0$ ,  $\overline{t_s} < 0$   $\Rightarrow C_s < 0$  accordingly with  $C_s \approx \overline{t_s}/(\Delta v_s/\Delta t)$ .

#### 4.3 Comparison to known cases of negative capacitance

Aspects of Multiple Sensor Interface circuit possibly related to negative capacitance phenomenon:

- 1- Use of Schmitt-Trigger 'NOT' gate which exhibits hysteresis on its  $v_o(v_i)$  graph.
- 2- Multiple Sensor Interface with a capacitive sensor operates under transient(time domain) step voltage changes, caused by its 'NOT' gate(Schmitt-Trigger) alternating between 0V and +VDDS (relaxation oscillator).

Negative capacitance phenomenon is reported on some

scientific articles/texts, and interestingly with some coincidence to the 2 aspects mentioned above. Quotes:

- 1- "Effective negative capacitance has been postulated in ferroelectrics because there is hysteresis in plots of polarization-electric field.", article "Towards steep slope MOSFETs using ferroelectric negative capacitance", by A. O'Neill, year 2014 [4].
- 2- "The phenomenon of negative capacitance, which has been reported in a variety of situations involving electrolytic as well as electronic systems, ... . It is suggested that the physically correct approach lies in the analysis of the corresponding time-domain behavior under step function bias, which involves a current initially falling and then rising gradually over a period of time before finally decaying to zero.", article "The physical origin of negative capacitance", by A. K. Jonscher, year 1986 [5].

#### 5 Conclusions

The author demonstrated theoretically a more versatile design for use with sensor applications, also was provided experimental data that corroborates the presented theory. The motivation of the author was to make available an electronics design that could be more sustainable in terms of life-cycle duration, by making a design more customizable by the user and also not closed/locked to a specific application/purpose. No warranty is given that the design can provide accuracy or convenience to a specific application/use; as the article is focused on showing how a versatile design can be achieved.

#### **Conflicts of interest**

The author declares no conflict of interest.

### Acknowledgments

I thank all of the Open-Source community for making available technology that everyone can use and build-on freely, thus inspiring me to also release this project as Open-Source. Also thanks to GNUplot software, that was used for drawing the plots on this article [14].

Also thanks to Wolfram Research Inc. for providing Wolfram Mathematica<sup>®</sup> for Raspberry Pi with RaspberryPi-OS and so making their software easily available to use by everyone, it was used version 12 for obtaining/solving inverse function and algebraic manipulation of long equations [15].

### Appendix A. Analysis of Multiple-Sensor Interface as Pierce Oscillator

The analysis of the circuit as Pierce oscillator was made using the Barkhausen stability criterion, that says  $A\beta=1$  to be possible to occur sustained oscillations (oscillations on steady state analysis). The purpose/focus is to obtain the inductance(of sensor) as function of oscillation frequency, although most of the circuit analysis strategy used here is similar as for typical Pierce Oscillator with piezoelectric crystal, as available on the bibliography list "Crystal Oscillators for Digital Electronics" class notes by Peter McLean [2]. So from  $A\beta=1$  results:  $|A\beta|=1$  and  $\angle A\beta=\pm n2\pi$ . This mathematical expression simply says that a circuit with a feedback loop after reaching the steady-state is expected that any voltage signal (for example  $V_o$ ) will remain steady.

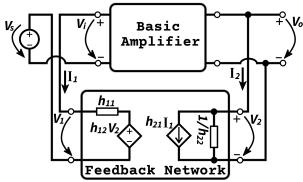


Figure 34: Representation of oscillator circuit by the h-parameters for feedback circuit (Pierce Osc.).

Starting the analysis on Fig.34, using a possible representation of Fig.6 diagram with the 'feedback network' represented by its hybrid parameters (2-port network h-parameters) [1], [2].

The Schmitt-Trigger inverter and resistors  $R_1$ ,  $R_2$  belong to block 'A', the capacitors  $C_1$ ,  $C_2$ , and inductive sensor  $L_s$  belong to block ' $\beta$ '.

Since the 'Basic Amplifier' has a very big input resistance the current  $I_1$  will be very small (the electric current on the input of the inverter, CMOS 'NOT' gate, is negligible), so by using the h-parameters to represent the feedback circuit block is possible to make the following simplifications/approximations (visible on figure 35): 1- The current source  $h_{21}I_1$  is also negligible (equal to zero, so removed from circuit); 2-The voltage drop across component  $h_{11}$  is negligible (since  $V_{11} = h_{11}I_1$ ,  $I_1 \to 0 \Rightarrow V_{11} \to 0$ ) and so  $h_{11}$  can be relocated to inside the circuit block 'A' keeping  $V_i$  as the name for the voltage drop on the input of 'A' block; 3- The  $1/h_{22}$  can be relocated to inside the circuit block 'A' since is connected in parallel to the input of ' $\beta$ ' block that is also the output of 'A' block [2] .

The block 'Basic Amplifier' is then replaced by its

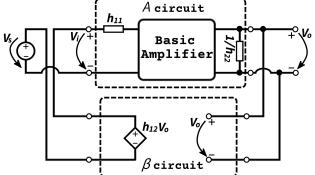


Figure 35: Simplified representation of oscillator circuit (Pierce osc.)

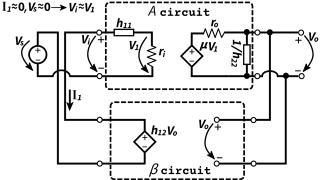


Figure 36: More simplified representation of the circuit (Pierce osc.)

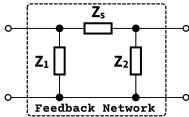


Figure 37: Feedback network of oscillator (Pierce Osc., Multiple-Sensor Int. with inductive sensor).

Thevenin equivalent circuit, obtaining Fig.36 circuit. From this is obtained the transfer function (Laplace transform) of 'A' block ( $V_o=AV_i$ ,  $1/h_{22}=h_{22}^{-1}$ ) and ' $\beta$ ' block ( $V_1=\beta V_2$ ):

$$A = \frac{h_{22}^{-1}}{h_{22}^{-1} + r_o} \mu \frac{r_i}{r_i + h_{11}} \qquad \beta = h_{12}$$

The feedback network (the same network displayed on Fig.34 represented by h-parameters) is the frequency-selecting  $\pi$ (shaped)-network on Fig.37, where  $Z_1$ ,  $Z_2$ ,  $Z_s$  are respectively  $C_1$ ,  $C_2$ ,  $L_{sensor}$  of the Multiple Sensor Interface with an inductive sensor (Pierce oscillator).

Based on the circuit of the feedback network and using the definitions of h-parameters of a 2-port network are obtained the values:

$$h_{11} = Z_1 || Z_s \qquad h_{22}^{-1} = Z_2 || (Z_1 + Z_s) \qquad h_{12} = \frac{Z_1}{Z_1 + Z_s}$$
 (where || is the impedance of 2 components in parallel,

(where || is the impedance of 2 components in parallel  $Z_1||Z_s = (Z_1Z_s)/(Z_1+Z_s)$ ;  $h_{11} = (V_1/I_1)|_{V_2=0}$ ;  $h_{12} = (V_1/V_2)|_{I_1=0}$ ;  $h_{22} = (I_2/V_2)|_{I_1=0}$ ) [1].

Finally:

$$A = \frac{Z_2||(Z_1 + Z_s)}{Z_2||(Z_1 + Z_s) + r_o} \mu \frac{r_i}{r_i + (Z_1||Z_s)}$$

$$\beta = \frac{Z_1}{Z_1 + Z_s}$$

In the circuit of Pierce oscillator (Fig.2) the amplifier was made by a gate inverter (CMOS 'NOT' gate) and a feedback resistor ( $R_1$ =2 $M\Omega$ ), biasing the inverter and allowing it to function as a high-gain inverting amplifier. The input resistance of CMOS 'NOT' gate is very large and so making the approximation  $r_i$ = + $\infty$  the expression of 'A' is significantly simplified, So obtaining [2]:

$$A\beta = \left(\frac{Z_2||(Z_1 + Z_s)}{Z_2||(Z_1 + Z_s) + r_o}\mu\right) \left(\frac{Z_1}{Z_1 + Z_s}\right)$$

$$= \frac{Z_1Z_2\mu}{Z_2(Z_1 + Z_s) + r_o(Z_1 + Z_2 + Z_s)}$$
(33)

If  $Z_1$ ,  $Z_2$ ,  $Z_s$  are purely reactive impedances given by  $Z_1=jX_1$ ,  $Z_2=jX_2$ ,  $Z_s=jX_s$  ( $j=\sqrt{-1}$ ), then (33) becomes:

$$A\beta = \frac{X_1 X_2 \mu}{X_2 (X_1 + X_s) - j r_o (X_1 + X_2 + X_s)}$$
(34)

The Barkhausen criterion states  $A\beta=1 \rightarrow \angle A\beta=\pm n2\pi$ , this means the phase shift of the loop ' $A\beta$ ' must be zero, and so that implies that the imaginary part of (34) must be zero. That is, for stable oscillations on the circuit of Fig.34 with a Feedback Network of Fig.37, it must be assured [2]:

$$X_1(\omega_0) + X_2(\omega_0) + X_s(\omega_0) = 0 \tag{35}$$

At the frequency  $\omega_0$  (frequency of oscillation at steady state), using (35) with (34), is obtained [2]:

$$A(\omega_0)\beta(\omega_0) = -\mu \frac{X_1(\omega_0)}{X_2(\omega_0)}$$
 (36)

To start the oscillations the loop gain must be grater than unity (during Transient Response), but after achieving the Steady State Response on the Pierce oscillator for oscillations to occur the loop gain  $A(\omega_0)\beta(\omega_0)$  of (36) must be equal to '1'(unity). Since the amplifier is an inverter ('NOT' gate with  $R_1$  feedback resistor) then  $\mu$  is a negative number, and so  $X_1(\omega_0)$  and  $X_2(\omega_0)$  must have the same sign (both positive or negative).

Thus, if  $Z_1(\omega_0)$  is capacitive( $X_1(\omega_0) = -1/(\omega_0 C_1)$ ), then by (36)  $Z_2(\omega_0)$  must also be capacitive (( $X_2(\omega_0) = -1/(\omega_0 C_2)$ ) [2].

Considering this and using (35) its possible to conclude that  $Z_s(\omega_0)$  must be inductive since  $X_s(\omega_0) = -X_1(\omega_0) - X_2(\omega_0)$ , this is if  $X_1(\omega_0)$  and  $X_2(\omega_0)$  are negative numbers then  $X_s(\omega_0)$  must be a positive number, then  $X_s = \omega_0 L_s$ .

So having  $C_1$ ,  $C_2$ ,  $L_s$  on the feedback network (where  $L_s$  is the component representing the inductive sensor on the Multipl-Sensor Interface) the (35) becomes:

$$-\frac{1}{\omega_0 C_1} - \frac{1}{\omega_0 C_2} + \omega_0 L_s = 0 \tag{37}$$

So defining "load capacitance"  $C_L$  as [2]:

$$\frac{1}{C_L} = \frac{1}{C_1} + \frac{1}{C_2} \tag{38}$$

The frequency of oscillation on the Pierce oscillator (using  $C_1$ ,  $C_2$ ,  $L_s$ ) is:

$$\omega_0 = \frac{1}{\sqrt{L_s C_L}} \quad \Leftrightarrow \quad f_0 = \frac{1}{2\pi\sqrt{L_s C_L}} \quad (\text{REF: 1})$$

So the expression (theoretical) of measured inductance  $L_{sensor}$  as a function of frequency(f) is:

$$L_{sensor} = L_s = \frac{1}{4\pi^2 C_L f^2} = \frac{C_1 + C_2}{4\pi^2 C_1 C_2 f^2}$$
 (REF: 2)

### **Appendix B. Experimental Datasets**

Experimental data obtained (Fig.5) by using fixed value components connected as the sensor on the device. Were used arrays(PCBs) with inductors, resistors, capacitors that allow to obtain various different values just by changing a jumper/switch, and also single components (including in series or parallel association).

#### B.1 Frequency measurement by Multi-Sensor

The Multiple-Sensor device measures frequency using a counter inside the microcontroller and has some accuracy and range limitations, it can measure up to 3MHz (higher frequency causes counter overflow). The Multiple-Sensor device was tested with a square wave signal from the signal generator JDS6600 (by Joy-IT, frequency accuracy:  $\pm 20 \mathrm{ppm}$ ).

The Multiple-Sensor device measurement accuracy (percentage error) of frequency, is worst at low frequencies with 9% error at 100Hz and 0.7% error at 1kHz, above 5kHz the error was always smaller than 0.2% (ignoring any accuracy error by JDS6600 used as reference). The Multiple-Sensor device measurement precision (variation) for frequency was worst at low frequencies with 5% variation at 300Hz, above 1500Hz was always smaller than 1%, and above 15kHz was always smaller than 0.1%.

### B.2 Experimental data on Multi-Sensor Int

#### - Reference instruments:

The measurements of inductance( $L_s$ ) and capacitance( $C_s$ ) were obtained using the LCR meter TH2821A (by Tonghui, basic accuracy 0.3%), configured to 10Khz test signal.

The measurements of resistance( $R_s$ ) were obtained using the meter UT603 (by UNI-T, accuracy: 0.8% for R $\leq$ 2M $\Omega$ ; 2% for R $\geq$ 2M $\Omega$ ).

### - Jumper Configurations:

<sup>a</sup>(JPA on, JPB off):  $C_1$ =2.2nF;  $C_2$ =21.8pF.

<sup>b</sup>(JPA off, JPB on):  $C_1$ =21.8pF;  $C_2$ =2.2nF. <sup>c</sup>(JPA on, JPB on):  $C_1$ =2.2nF;  $C_2$ =2.2nF.

- Units: Hz=hertz, H=herry,  $\Omega$ =ohm, F=farad.

Here is made available, the sets of experimental data that were used for drawing the plots of  $L_s(f)$ ,  $R_s(f)$ ,  $C_s(f)$ , these are the measured values of inductance, resistance, capacitance paired with measured frequency on the Multiple Sensor Interface device.

Table 2: Set of experimental data for  $C_s(f)$ 

$C_s[nF]$	f[Hz] <sup>c</sup>	$C_s[nF]$	f[Hz] <sup>c</sup>		
Capacitance	JPA on, JPB on	Capacitance	JPA on, JPB on		
0	229	4.97	373045		
0.152	321	5.97	385032		
0.31	458	6.95	394283		
0.568	2614	7.94	400750		
0.615	54570	8.98	405766		
0.689	110286	10.07	411246		
0.776	140178	12.04	418028		
1.015	186522	15.02	426040		
1.34	231460	20.02	433089		
1.58	255526	24.97	437446		
1.79	271015	29.68	440382		
2	285020	34.62	442584		
2.56	314530	39.43	444235		
2.99	329820	44.38	445688		
3.98	356012	49.38	446712		

Precision error(maximum frequency variation):

- $\pm 3$ kHz (600pF< $C_s$ <1.6nF);
- $\pm 2$ kHz (1.6nF< $C_s$ <21nF);
- $\pm 1$ kHz ( $C_s > 21$ nF);  $\pm 50$ Hz ( $C_s < 600$ pF).

Table 3: Set of experimental data for  $L_s(f)$ 

	Table 3: Set of experimental data for $L_s(f)$							
$L_s[\mu H]$	f[Hz] <sup>a</sup>	f[Hz] <sup>b</sup>	f[Hz] <sup>c</sup> JPA on, JPB on					
Inductance	JPA on, JPB off							
1.21	834161	879205	446590					
1.4	833855	885138	476589					
1.65	833350	888501	473393					
1.85	833014	887049	458577					
2.51	831302	881055	494096					
3.09	829880	892844	474739					
3.8	828045	898700	467354					
4.1	827433	891116	466711					
4.7	826011	881239	496405					
5.87	823121	873380	519263					
7.32	819681	915412	577595					
8.76	813947	864236	591646					
9.7	813397	858548	615743					
11.77	808321	936894	1432920					
12.84	805905	934723	1357220					
15.76	799009	895932	1251070					
21.39	785691	931940	1090760					
24.49	778123	978330	1011830					
31.8	760632	1056660	889633					
38.61	745112	1193360	809559					
46.7	726580	1369450	736014					
53.44	712070	2853370	690970					
61.3	695603	2662840	639014					
78.3	655604	2332760	568099					
95.34	620697	2103380	509845					
117.6	583023	1899190	464617					
142.28	541388	1722220	420062					
173.5	502398	1575330	382571					
201.5	471222	1464370	354070					
271.46	396546	1201810	292482					
341.8	368641	1112820	271168					
360.6	357938	1085180	261856					
438.7	327053	994721	239762					
558.1	287880	868105	212362					
660.7	262804	794697	194290					
777.6	241031	737803	178480					
921.2	218738	677591	163587					
1491	161768	606844	124338					
2171	130897	499264	102978					
2976	109912	446452	87856					
3170	105439	406011	84614					
3640	97779	383305	79110					
4646	84110	319423	69783					
6880	68162	282360	57750					
10140	54034	224090	47230					
15040	43377	192088	38790					
20375	36588	171981	33683					
Precision error(maximum frequency variation):								

 $\pm 2kHz$  (at high 'f[Hz]');  $\pm 300Hz$  (at low 'f[Hz]');

±5kHz (2.85MHz↔1.36MHz; at <sup>b</sup> JPA off, JPB on).

Table 4: Set of experimental data for  $R_s(f)$ 

R_1			Г			l OI CX	<u> </u>	ata for $R_s(f)$		
0         456284         577         231735         4180         79553         28900         16666           1.2         454678         597         228447         4380         77107         29900         16666           2.2         453149         637         222178         4780         72612         33900         14418           4.2         452400         657         219228         4980         70593         35900         13027           5.2         451605         677         216353         5180         68682         37800         13027           7.2         449923         717         210971         5580         66863         39800         12430           8.2         449067         736         208402         5770         63514         43800         11375           9.2         448272         756         205910         5970         61985         45800         10017           10.2         447385         776         203464         6170         60517         47800         10488           15.2         432226         796         201139         6370         59111         49800         10091           25.1         4	$R_s[\Omega]$	f[Hz] <sup>c</sup>		$R_s[\Omega]$	f[Hz] <sup>c</sup>		$R_s[\Omega]$	f[Hz] <sup>c</sup>	$R_s[\Omega]$	f[Hz] <sup>c</sup>
1.2         454678         597         228447         4380         77107         29900         16176           3.2         453149         637         222178         4780         72612         33900         15244           4.2         452400         657         219228         4980         70593         35900         13669           5.2         451605         677         216333         5180         68682         37800         13027           7.2         449923         717         210971         5580         66133         39800         12430           7.2         449923         717         210971         5580         65135         41800         11880           8.2         449067         736         208402         5770         651514         43800         11375           9.2         448272         756         205910         5970         61985         45800         10917           10.2         447385         776         201139         6370         59111         49800         10091           25.1         435183         836         196659         6770         5611         5980         10091           25.1										
2.2         453975         617         225252         4580         74783         31900         15244           4.2         452400         637         222178         4780         72612         33900         14418           4.2         452400         657         219228         4980         70593         35900         13669           5.2         451605         677         216353         5180         68682         37800         13027           7.2         449923         717         210971         5580         65135         41800         11880           8.2         449067         736         208402         5770         63514         43800         11375           9.2         448272         756         205910         5970         61985         45800         10917           10.2         447385         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         1091           25.1         435183         836         194504         6970         55288         64800         7994           35.1		l I					1			
3.2         453149         637         222178         4780         72612         33900         14418           5.2         451605         657         219228         4980         70593         35900         13669           5.2         451605         677         216353         5180         68682         37800         13027           6.2         450718         697         213647         5380         66135         41800         113027           7.2         449027         736         208402         5770         63514         43800         11375           9.2         448272         736         203404         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         10991           20.1         439144         816         198877         6570         57765         54800         9235           25.1         435183         836         196659         6770         56511         59800         8531           30.1         4372447         876         192409         7170         5126         6900         7385           40         42							1			
4.2         452400         657         219228         4980         70593         35900         13669           5.2         451605         677         216353         5180         68682         37800         13027           6.2         450718         697         213647         5380         66863         39800         12430           7.2         449923         717         210971         5580         65135         41800         11880           8.2         449067         736         208402         5770         63514         43800         11375           9.2         448272         756         205910         5970         61985         45800         10917           10.2         447385         776         203464         6170         60517         47800         10917           10.2         447385         776         203464         6170         60517         47800         10488           20.1         439144         816         198877         6570         57765         54800         9235           23.1         435183         836         194504         6970         55288         64800         7994           35.1 <td< td=""><td></td><td> </td><td></td><td></td><td></td><td></td><td>1</td><td></td><td></td><td></td></td<>							1			
5.2         451605         677         216353         5180         68682         37800         13027           7.2         449023         717         210971         5580         66863         39800         12430           8.2         449067         736         208402         5770         63514         43800         11880           8.2         448272         756         205910         5970         61985         45800         10917           10.2         447385         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         10917           20.1         43144         816         198877         6570         57765         54800         9235           25.1         435183         836         196599         6770         56511         59800         8531           35.1         427447         876         192409         7170         54126         69700         7385           45         420016         916         188418         7570         51940         79700         6513           55         4128	3.2	453149		637	222178		4780	72612	33900	14418
6.2         450718         697         213647         5380         66863         39800         12430           7.2         449923         717         210971         5580         65135         41800         11880           8.2         449067         736         208402         5770         63514         43800         11375           9.2         448272         756         205910         5970         61985         45800         10917           10.2         447325         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         10091           20.1         439144         816         198877         6570         5765         54800         9235           25.1         43183         36         196659         6770         56511         59800         9353           30.1         43169         856         194504         6970         55288         64800         7904           35.1         427447         876         192409         7170         54126         69700         7385           40         42365	4.2	452400		657	219228		4980	70593	35900	13669
7.2         449923         717         210971         5580         65135         41800         11880           9.2         448272         756         208402         5770         63514         43800         11375           9.2         448272         756         203464         6170         60517         47800         10917           10.2         447385         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         10091           20.1         439144         816         198877         6570         57765         54800         9235           25.1         435183         836         196659         6770         56511         59800         8531           30.1         431269         856         194504         6970         52288         64800         7904           35.1         427447         876         192409         7170         54126         69700         7385           45         420016         916         188418         7570         50915         84600         74700         6513	5.2	451605		677	216353		5180	68682	37800	13027
8.2         449067         736         208402         5770         63514         43800         11375           9.2         448272         756         205910         5970         61985         45800         10917           10.2         447385         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         10091           20.1         439144         816         198877         6570         57765         54800         9235           25.1         435183         836         196569         6770         56511         59800         8531           30.1         431269         856         194504         6970         55288         64800         790           40         423655         896         19409         7170         54126         69700         7385           45         420016         916         188418         7570         59040         79700         6513           50         416407         936         186476         7760         50915         84600         7620         47643         94600         55	6.2	450718		697	213647		5380	66863	39800	12430
9.2         448272         756         205910         5970         61985         45800         10917           10.2         447385         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         57765         54800         10917           20.1         439144         816         198877         6570         57765         54800         9235           25.1         435183         836         196659         6770         36511         59800         8531           30.1         431269         856         194504         6970         55288         64800         7904           35.1         427447         876         192409         7170         54126         69700         7385           40         423655         896         190406         7370         53010         74700         6926           45         42016         916         188418         7570         5915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359 <td>7.2</td> <td>449923</td> <td></td> <td>717</td> <td>210971</td> <td></td> <td>5580</td> <td>65135</td> <td>41800</td> <td>11880</td>	7.2	449923		717	210971		5580	65135	41800	11880
10.2         447385         776         203464         6170         60517         47800         10488           15.2         443226         796         201139         6370         59111         49800         10091           20.1         439144         816         198877         6570         57655         54800         29235           25.1         435183         836         196659         6770         56511         59800         8531           30.1         431269         856         194504         6970         55288         64800         7904           40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         7940           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65.4         40610 <td>8.2</td> <td>449067</td> <td></td> <td>736</td> <td>208402</td> <td></td> <td>5770</td> <td>63514</td> <td>43800</td> <td>11375</td>	8.2	449067		736	208402		5770	63514	43800	11375
15.2         443226         796         201139         6370         59111         49800         10091           20.1         439144         816         198877         6570         57765         54800         9235           25.1         435183         836         196659         6770         55288         64800         7904           35.1         427447         876         192409         7170         54126         69700         7385           35.1         427447         876         192409         7170         54126         69700         7385           40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         99400         5320           699         402601	9.2	448272		756	205910		5970	61985	45800	10917
20.1         439144         816         198877         6570         57765         \$4800         9235           25.1         435183         836         196659         6770         \$55288         64800         7904           35.1         427447         876         192409         7170         54126         69700         7385           40         423655         896         190406         7370         53010         74700         6926           45         42016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         8825           66         409359         975         182776         8460         47643         94600         5520           65         406010         996         180865         8960         48548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328	10.2	447385		776	203464		6170	60517	47800	10488
25.1         435183         836         196659         6770         56511         59800         8531           30.1         431269         856         194504         6970         55288         64800         7904           40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         180865         8960         45548         99400         3320           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209 <td>15.2</td> <td>443226</td> <td></td> <td>796</td> <td>201139</td> <td></td> <td>6370</td> <td>59111</td> <td>49800</td> <td>10091</td>	15.2	443226		796	201139		6370	59111	49800	10091
25.1         435183         836         196659         6770         56511         59800         8531           30.1         431269         856         194504         6970         55288         64800         7904           40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209 <td>20.1</td> <td>439144</td> <td></td> <td>816</td> <td>198877</td> <td></td> <td>6570</td> <td>57765</td> <td>54800</td> <td>9235</td>	20.1	439144		816	198877		6570	57765	54800	9235
30.1         431269         856         194504         6970         55288         64800         7904           35.1         427447         876         192409         7170         54126         69700         7385           40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         1646           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060 </td <td></td> <td>435183</td> <td></td> <td>836</td> <td>196659</td> <td></td> <td>6770</td> <td>56511</td> <td>59800</td> <td>8531</td>		435183		836	196659		6770	56511	59800	8531
35.1         427447         876         192409         7170         54126         69700         7385           40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5550           66         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390117	1						1			
40         423655         896         190406         7370         53010         74700         6926           45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3663           94.8         387							1			
45         420016         916         188418         7570         51940         79700         6513           50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         13930         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9 <td< td=""><td></td><td> </td><td></td><td></td><td></td><td></td><td>1</td><td></td><td></td><td></td></td<>							1			
50         416407         936         186476         7760         50915         84600         6146           55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           119.7							I	l		
55         412845         955         184611         7960         49952         89600         5825           60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3833           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7		l I					1			
60         409359         975         182776         8460         47643         94600         5550           65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           159.		l I					1			
65         406010         996         180865         8960         45548         99400         5320           69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         122569         13950         31680         199100         2798 <t< td=""><td></td><td>l I</td><td></td><td></td><td></td><td></td><td>1</td><td></td><td></td><td></td></t<>		l I					1			
69.9         402601         1096         172578         9460         43622         109400         4862           74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         129353         13450         32659         189100         2935           159.6         351608         1992         1225699         13950         31680         199100         2798							1			
74.9         399328         1195         165208         9960         41879         119300         4479           79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1882         129353         13450         32659         189100         2935           159.6         351608         1992         125699         13950         31680         199100         2798           179.5         342205         2090         122258         14450         30732         299000         1972							1			
79.9         396209         1295         158603         10460         40243         129300         4158           84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         129353         13450         32659         189100         2935           159.6         351608         1992         1225699         13950         31680         199100         2798           179.5         342205         2090         122258         14450         30732         299000         1972           199.5         333306         2190         119017         14950         29861         398000         1544							1			
84.9         393060         1394         152594         10960         38760         139300         3883           89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         129353         13450         32659         189100         2935           159.6         351608         1992         125699         13950         31680         199100         2798           179.5         342205         2090         122258         14450         30732         299000         1972           199.5         333306         2190         119017         14950         29861         398000         1544           219         325050         2290         115974         15440         29035         498000         1284							1			
89.9         390017         1494         147150         11460         37353         149300         3623           94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         129353         13450         32659         189100         2935           159.6         351608         1992         125699         13950         31680         199100         2798           179.5         342205         2090         122258         14450         30732         299000         1972           199.5         333306         2190         119017         14950         29861         398000         1544           219         325050         2290         115974         15440         29035         498000         1284           239         317236         2390         113115         15940         28255         597000         1100							1			
94.8         387005         1593         142135         11960         36053         159200         3440           99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         129353         13450         32659         189100         2935           159.6         351608         1992         125699         13950         31680         199100         2798           179.5         342205         2090         122258         14450         30732         299000         1972           199.5         333306         2190         119017         14950         29861         398000         1544           219         325050         2290         115974         15440         29035         498000         1284           239         317236         2390         113115         15940         28255         597000         1100           259         309836         2490         107855         16940         26818         796000         886							1			
99.9         383396         1693         137548         12450         34861         169200         3256           119.7         372387         1792         133298         12960         33714         179100         3073           139.7         361700         1892         129353         13450         32659         189100         2935           159.6         351608         1992         125699         13950         31680         199100         2798           179.5         342205         2090         122258         14450         30732         299000         1972           199.5         333306         2190         119017         14950         29861         398000         1544           219         325050         2290         115974         15440         29035         498000         1284           239         317236         2390         113115         15940         28255         597000         1100           259         309836         2490         110409         16440         27522         697000         978           279         302879         2590         107855         16940         26818         796000         886							1			
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							1		9040000	305
557   235144     3980   82153     27900   17201							1			
	557	235144	ļ	3980	82153		27900	17201		

Precision error(maximum frequency variation):

 $<sup>\</sup>pm 1 \text{kHz}(\text{at low } R_s); \pm 300 \text{Hz}(\text{at } 30 \text{k}\Omega); \pm 100 \text{Hz}(\text{at high } R_s).$ 

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