

# Exercise 24

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I present a possible list of inference-rule specifications for the five statement types other than while in the language described in Exercise 4.22 (page 122) of *Essentials of Programming Languages, Third Edition* by Daniel P. Friedman and Mitchell Wand.

Assignment statements

$$\frac{(\text{value-of } \text{exp } \rho \sigma_0) = (val, \sigma_1)}{(\text{result-of } (\text{assignment-stmt } id \text{ exp}) \rho \sigma_0) = [\rho(id) = val]\sigma_1}$$

Print statements

$$\frac{(\text{value-of } \text{exp } \rho \sigma_0) = (val, \sigma_1)}{(\text{result-of } (\text{print-stmt } \text{exp}) \rho \sigma_0) = [\text{print-}n = val]\sigma_1}$$

Where  $n$  is the lowest positive integer such that  $\text{print-}n$  is not in  $\sigma_1$ . An external device seeking to determine the output of a program should examine the final store or any intermediary store's entries for  $\text{print-}n$  for positive integers  $n$ .

Block statements

$$\frac{(\text{null? } \text{stmts}) = \#t}{(\text{result-of } (\text{block-stmt } \text{stmts}) \rho \sigma) = \sigma}$$

$$\frac{(\text{null? } \text{stmts}) = \#f \quad (\text{result-of } (\text{car } \text{stmts}) \rho \sigma_0) = \sigma_1}{(\text{result-of } (\text{block-stmt } \text{stmts}) \rho \sigma_0) = (\text{result-of } (\text{block-stmt } (\text{cdr } \text{stmts})) \rho \sigma_1)}$$

If statements

$$\frac{(\text{value-of } \text{exp } \rho \sigma_0) = (\#t, \sigma_1)}{(\text{result-of } (\text{if-stmt } \text{test consequent alternative}) \rho \sigma_0) = (\text{result-of } \text{consequent } \rho \sigma_1)}$$

$$\frac{(\text{value-of } \text{exp } \rho \sigma_0) = (\#f, \sigma_1)}{(\text{result-of } (\text{if-stmt } \text{test consequent alternative}) \rho \sigma_0) = (\text{result-of } \text{alternative } \rho \sigma_1)}$$

Var statements

$$\frac{(\text{null? } \text{ids}) = \#t}{(\text{result-of } (\text{var-stmt } \text{ids stmt}) \rho_0 \sigma) = (\text{result-of } \text{stmt } \rho_0 \sigma)}$$

$$\frac{(\text{null? } \text{ids}) = \#f \quad [(\text{car } \text{ids}) = l] \rho_0 = \rho_1}{(\text{result-of } (\text{var-stmt } \text{ids stmt}) \rho_0 \sigma) = (\text{result-of } (\text{var-stmt } (\text{cdr } \text{ids}) \text{stmt}) \rho_1 \sigma)}$$

Where  $l$  is neither in  $\sigma$  nor of the form `print-n` where  $n$  is a positive integer.