

3a)

i) Initialize weights ($q_i \times k_j$)

$$\text{Score}_{11} = q_1 \cdot k_1 = (1 \times 1) + (2 \times 1) + (3 \times 1) = 6$$

$$\text{Score}_{12} = q_1 \cdot k_2 = (1 \times 0) + (2 \times 0) + (3 \times 0) = 0$$

$$\text{Score}_{13} = q_1 \cdot k_3 = (1 \times 2) + (2 \times 2) + (3 \times 0) = 6$$

ii) scale w/ $\sqrt{|k_i|}$: $\sqrt{|k_1|} \approx 2$

$$a'_{11} = 6/2 = 3$$

$$a'_{12} = 0/2 = 0$$

$$a'_{13} = 6/2 = 3$$

b) Normalize weights (sum = $3+0+3=6$)

$$a_{11} = 3/6 = 0.5$$

$$a_{12} = 0/6 = 0$$

$$a_{13} = 3/6 = 0.5$$

c) Weight 1: $0.5 \times v_1 = 0.5 \times [2, 0, 1] = [1.0, 0.0, 0.5]$

Weight 2: $0 \times v_2 = [0, 0, 0]$

Weight 3: $0.5 \times v_3 = 0.5 \times [1, 2, 2] = [0.5, 1, 1]$

Sum: $[1.0, 0.0, 0.5] + [0, 0, 0] + [0.5, 1, 1]$

$$Z_1 = [1.5, 1.0, 1.5]$$