

# Avalanches of Neurons Project Report

---

Ruirong Huang 12/08/2022

## Overview

---

The project is based on the paper

Benayoun, M. Cowan, J.D. van Drongelen, W. Wallace, E. 2010.  
\*Avalanches in a Stochastic Model of Spiking Neurons.\* PLoS  
Computational Biology. Volume 6, Issue 7, e1000846.

which simulated the avalanches of neurons by the Gillespie algorithm.

## Matlab Codes

---

Here is the codes I wrote

```
% params
L = 100;
gamma = 0.1;
yita = 0.001;
deltaV = 0.1; % modify this
sumV = 0.004;
Ve = (deltaV + sumV) / 2;
Vi = sumV - Ve;
```

```

% init
y1 = 0;
y2 = 0;
t = 0;

% storage
t_track = [];
y1_track = [];
y2_track = [];

% simulation
for i = 1:10000

    % store
    t_track = [t_track, t];
    y1_track = [y1_track, y1];
    y2_track = [y2_track, y2];

    % synaptic input
    phi = Ve * y1 + Vi * y2 + yita;

    % propensities
    pi2 = gamma * y1;
    pi4 = gamma * y2;

    if phi > 0
        pi1 = (L/2 - y1) * tanh(phi);
        pi3 = (L/2 - y2) * tanh(phi);
    else
        pi1 = 0;
    end
end

```

```

    pi3 = 0;
end

% sample from exponential distribution
sum_pi = pi1 + pi2 + pi3 + pi4;
mu = 1 / sum_pi;

% choose delta_t
tao = exprnd(mu);

% choose reaction
rand_val = rand * sum_pi;
if rand_val < pi1()          % reaction 1
    y1 = y1 + 1;
elseif rand_val < pi1() + pi2() % reaction 2
    y1 = y1 - 1;
elseif rand_val < pi1() + pi2() + pi3() % reaction 3
    y2 = y2 + 1;
else                          % reaction 4
    y2 = y2 - 1;
end

% update time
t = t + tao;

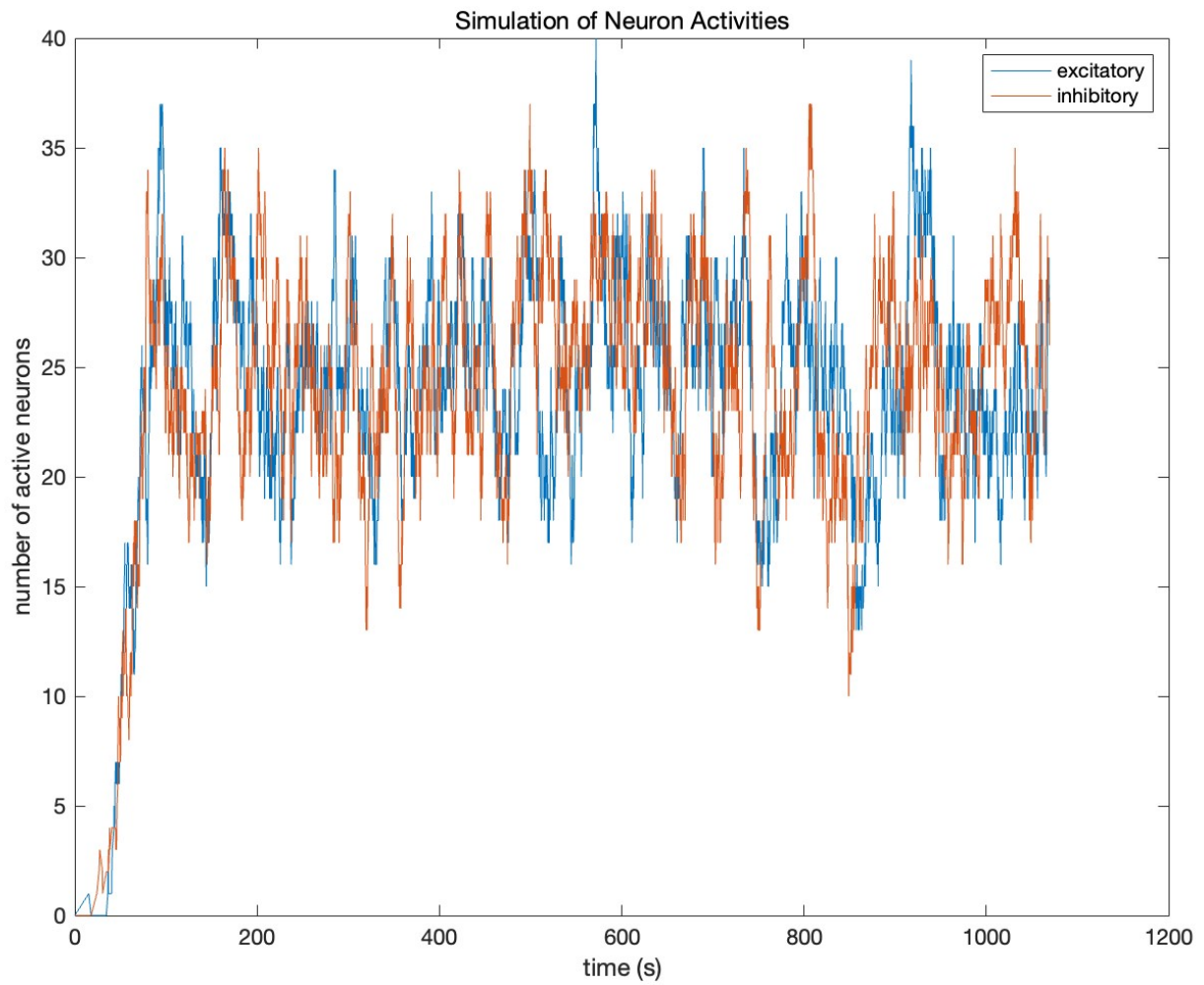
end

% plot
figure
plot(t_track, y1_track, t_track, y2_track);

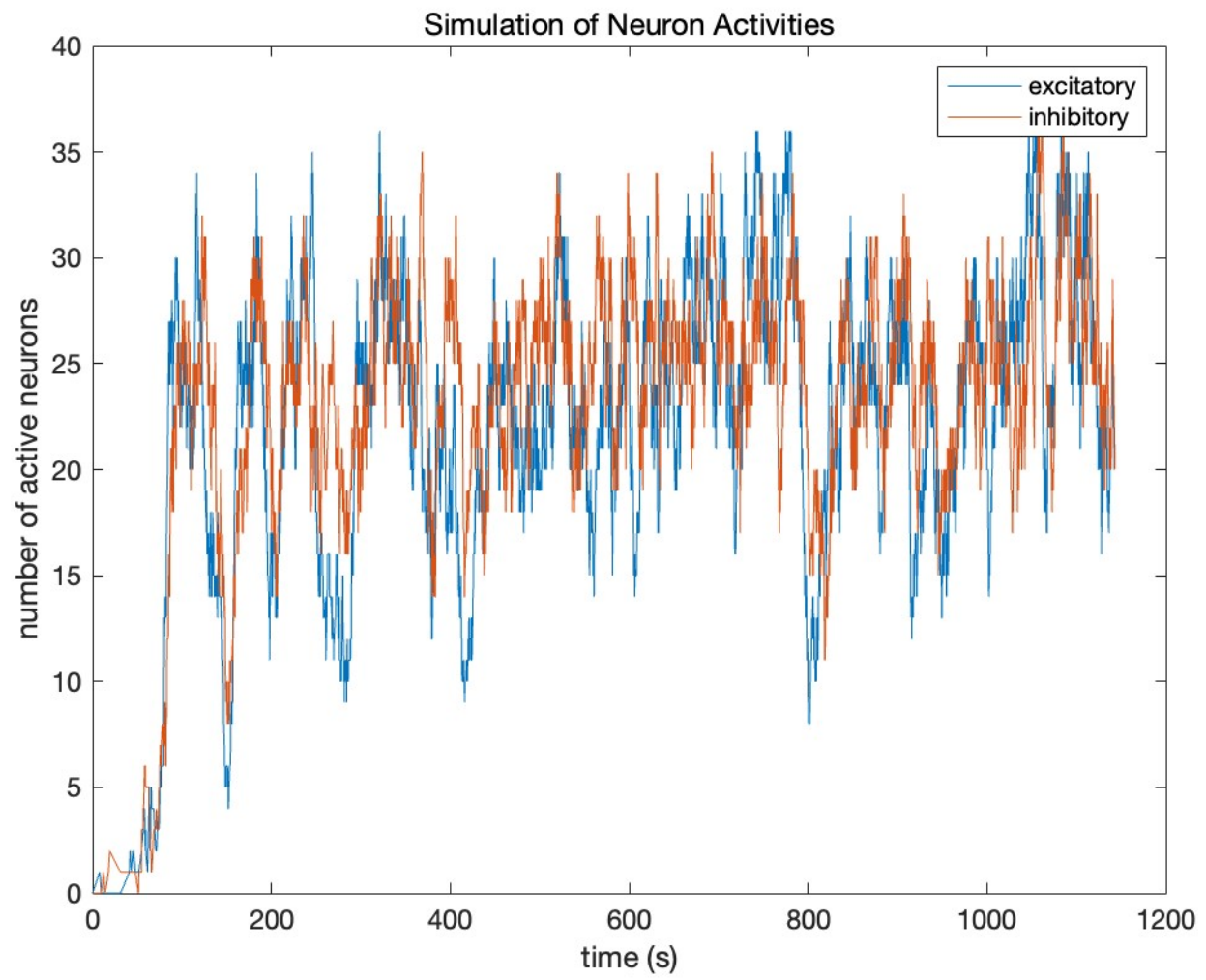
```

# Results

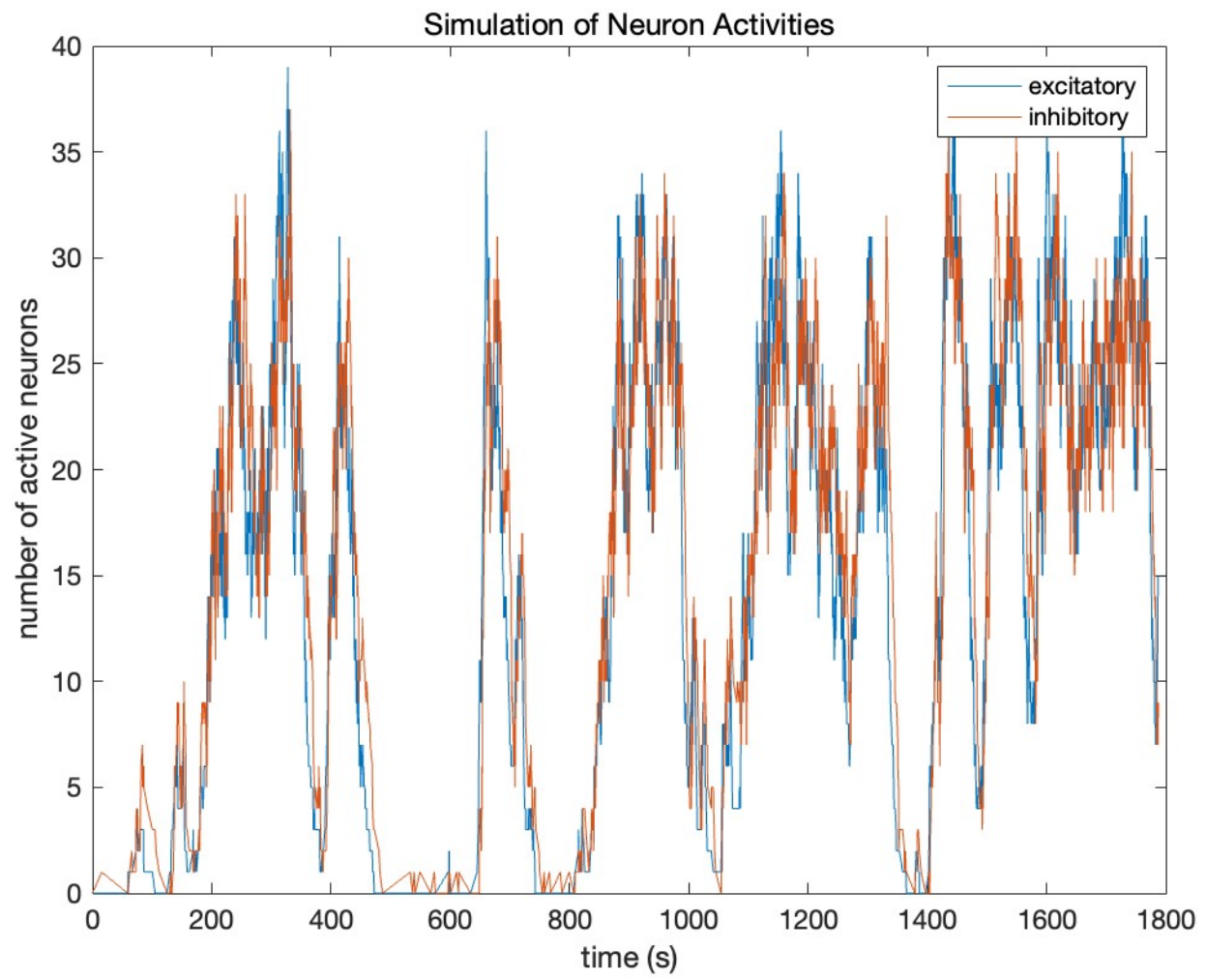
- $V_e - V_i = 0$



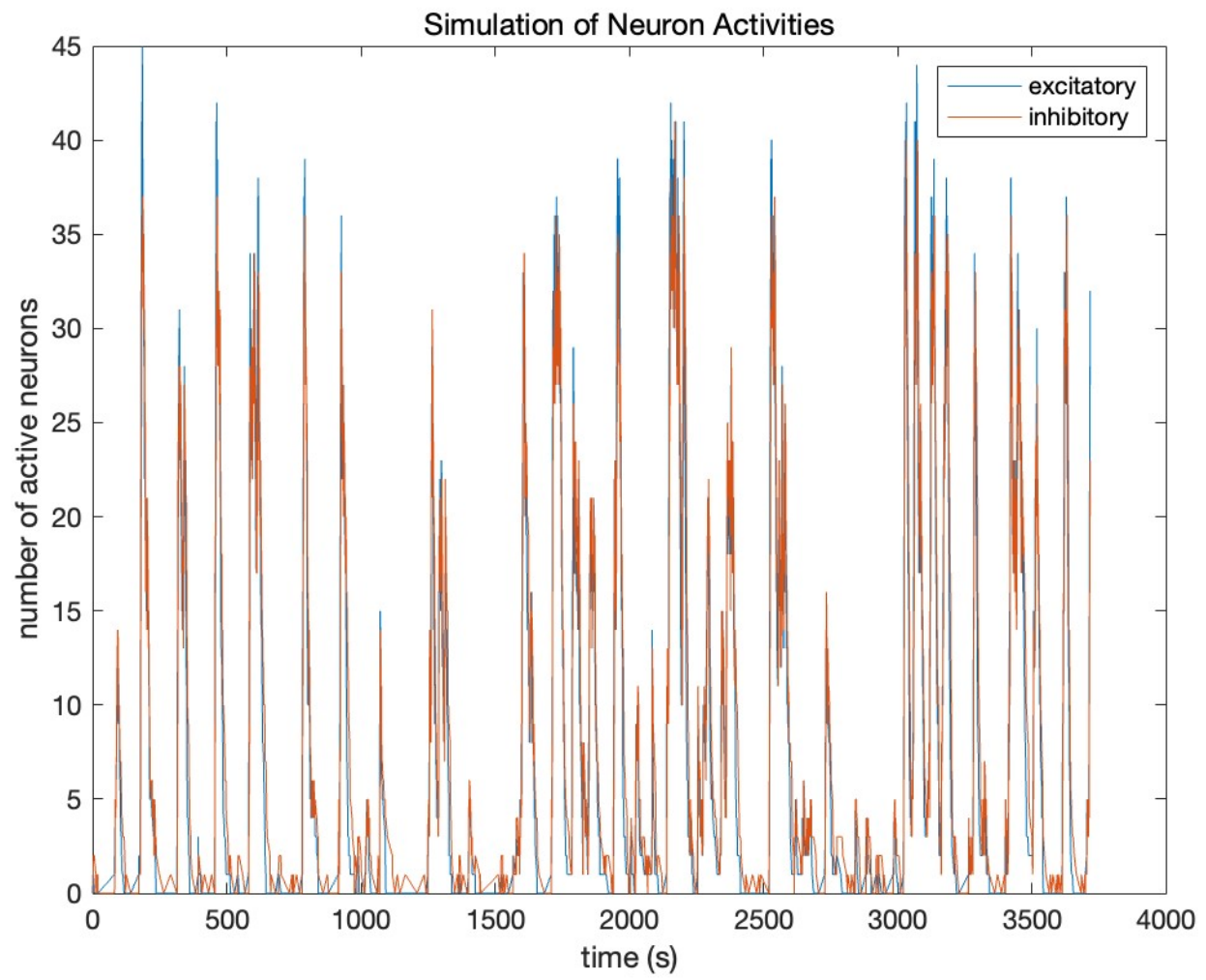
- $V_e - V_i = 0.005$



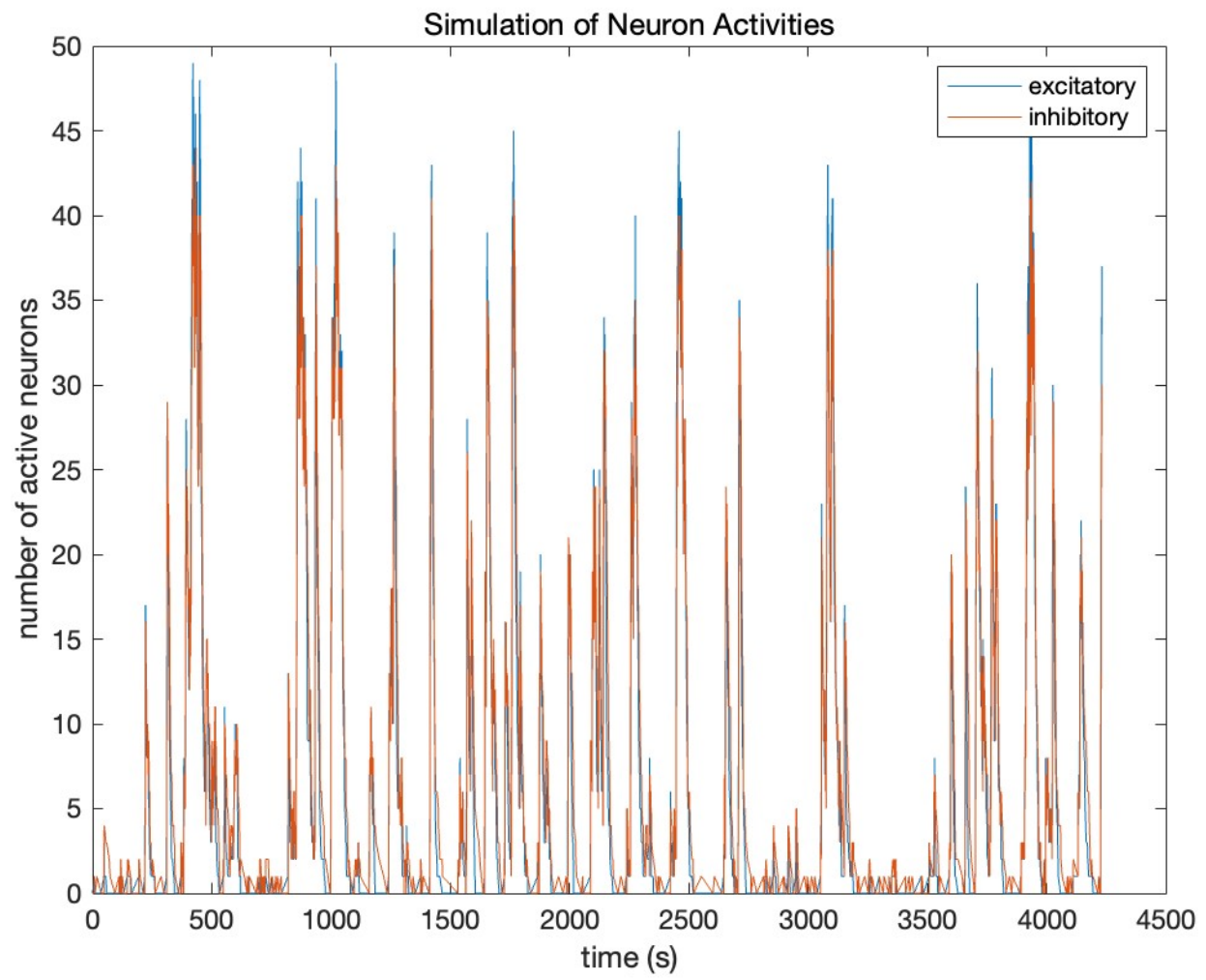
- $V_e - V_i = 0.01$



- $V_e - V_i = 0.05$

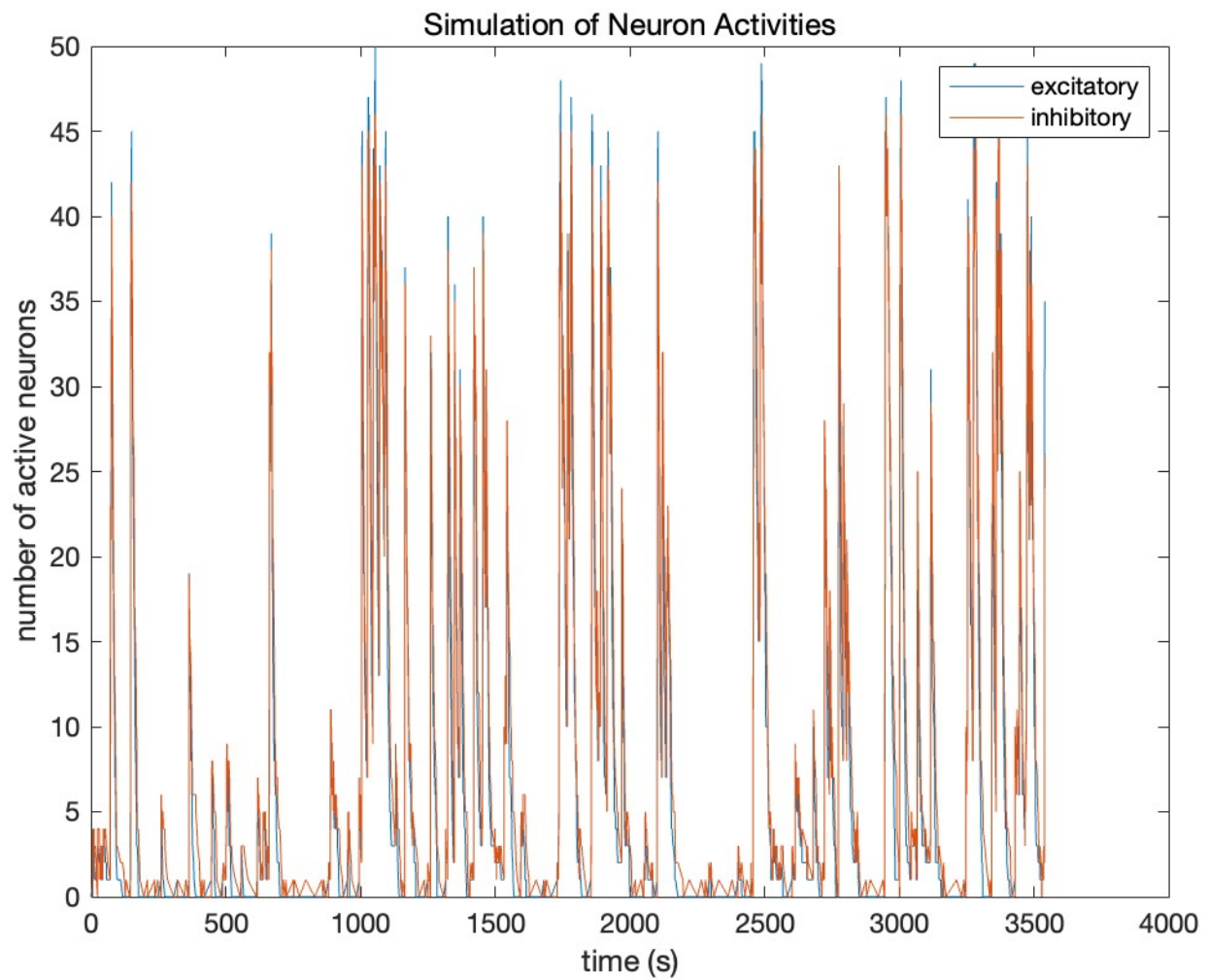


- $V_e - V_i = 0.1$



- $V_e - V_i = 1$





## Conclusion

---

We successfully simulated the avalanches of neurons by the Gillespie algorithm. The activities of excitatory and inhibitory neurons are similar. Once the network switch to synchronous mode, the avalanche pattern keeps stable and almost irrelevant to  $V_e - V_i$ .