 <div> UNIVERSIDAD NACIONAL DE COLOMBIA </div>	Flujos de Potencia Newton Raphson (Con SVC - FA Model)	
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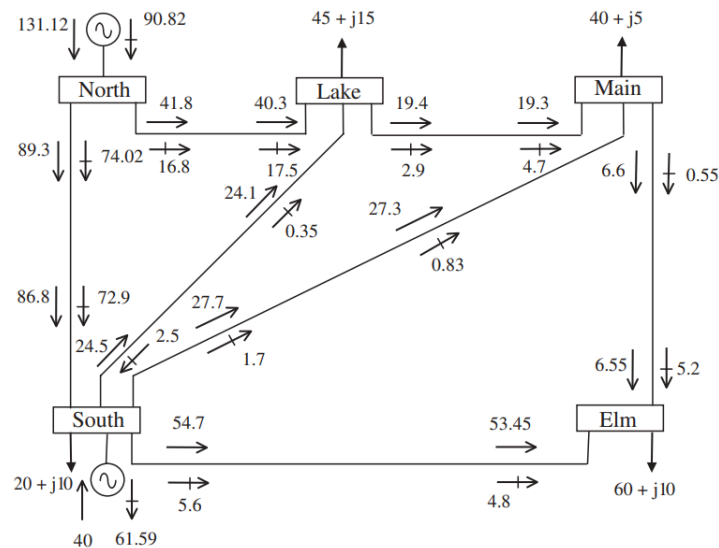
1) Se definen las bases del sistema

- Potencia base $S_b = 100 \cdot 10^6$ [VA]
- Voltaje base $V_b = 230 \cdot 10^3$ [V]

```
Sb = 100e6; %[VA]
Vb = 230e3; %[V]
```

2) Se crean las matrices con la información de la red (br_data, N_data):

Se deben crear dos matrices para ingresar la información referente al circuito. La primera (br_data) brinda información acerca de las conexiones entre buses como la impedancia de la línea o los buses entre los cuales se realiza la conexión , mientras que la segunda (N_data) da información acerca de la naturaleza de cada uno de los buses, tipo de bus (SL, PV o PQ).



a) Para la matriz **br_data** se tiene que el formato es

$brdata = [Bus_{from}, Bus_{to}, R, X, G, B]$ in p. u.

b) Para la matriz **N_data** se tiene que el formato es:

$Ndata = \{\#Bus, type('SL', 'PQ', 'PV'), V[p.u.], \angle V^\circ, PG[p.u.], QG[p.u.], PL[p.u.], QL[p.u.]\}$

```
% Branches data R, X, G, B
% Types: General in form of impedance. (G & B are split in half at both ends).
```

```

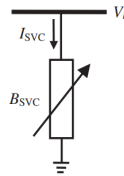
% br_data=[ bus1, bus2,      R,      X,      G,      B] in p.u.
br_data = [
    1,      2, 0.02,    0.06,    0.0,    0.06;
    1,      3, 0.08,    0.24,    0.0,    0.05;
    2,      3, 0.06,    0.18,    0.0,    0.04;
    2,      4, 0.06,    0.18,    0.0,    0.04;
    2,      5, 0.04,    0.12,    0.0,    0.03;
    3,      4, 0.01,    0.03,    0.0,    0.02;
    4,      5, 0.08,    0.24,    0.0,    0.05];

% Node definitions
% { #, type,  Vpu,    <V°,  PG pu,  QG pu,  PL pu, QL pu}
N_data = {
    1, 'SL',  1.06,    0.0,    0.0,    0.0,    0.00,    0.00;
    2, 'PV',  1.0,     0.0,    0.4,    0.0,    0.20,    0.10;
    3, 'PQ',  1.0,     0.0,    0.0,    0.0,    0.45,    0.15;
    4, 'PQ',  1.0,     0.0,    0.0,    0.0,    0.40,    0.05;
    5, 'PQ',  1.0,     0.0,    0.0,    0.0,    0.60,    0.10; };

br_data=array2table(br_data,'VariableNames',{'FromBus','ToBus','R','X','G','B'});
N_data=cell2table(N_data,'VariableNames',{'n','type','Vm','Va','PG','QG','PL','QL'});

```

c) Para el SVC:



```

% STATIC VAR COMPENSATION
% FIRING ANGLE MODEL

% NSVC : Number of SVC's
% SVCsend : Compensated bus
% Xc : Capacitive reactance (p.u.)
% Xl : Inductive reactance (p.u.)
% FA : Initial SVC's firing angle value (Deg)
% FALo : Lower limit of firing angle (Deg)
% BHi : Higher limit of firing angle (Deg)
% TarVol : Target nodal voltage magnitude to be controlled by SVC (p.u.)
% VSta : Indicate the status to get control over voltage magnitude nodal : 1
% is on; 0 is off

% SVCsend(1)=3; Xc(1)=1.07; Xl(1)=0.288; FA(1)=140; FALo(1)=90;
% FAHi(1)=180; TarVol(1)=1.0; VSta(1)=1;
% SVC_data = [SVC node, Xc, XL, FA, FAmx, Famin, SVC TarVol, SVC Vsta]
SVC_data = [ 3 , 1.07, 0.288, 140 , 180 , 90 , 1, 1 ];

SVC_data=array2table(SVC_data,'VariableNames',{'SVCBus','Xc','XL','FA','FAmax','Famin','TarVol','Vsta'});

SVC_data = 1x8 table

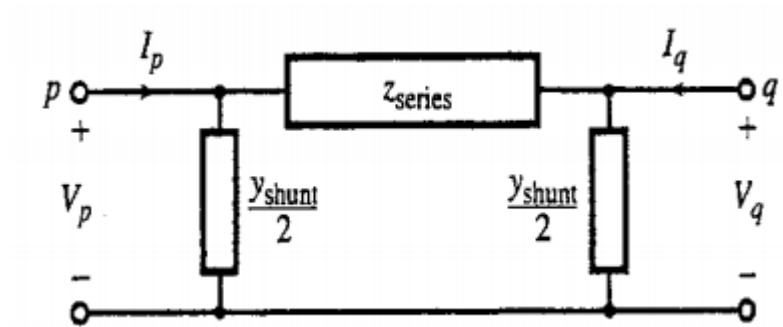
```

	SVCBus	Xc	XL	FA	FAMax	FAMin	Tv	Status
1	3	1.0700	0.2880	140	180	90	1	1

3) Se crea Ybus con las redes de 2 puertos:

Se tiene la siguiente red de dos puertos, que representa el circuito del modelo pi de la línea de transmisión

$$\begin{bmatrix} V_i \\ V_j \end{bmatrix} = \begin{bmatrix} \frac{1}{z} + \frac{y}{2} & -\frac{1}{z} \\ -\frac{1}{z} & \frac{1}{z} + \frac{y}{2} \end{bmatrix} \begin{bmatrix} I_i \\ I_j \end{bmatrix}$$



Pi-equivalent model of a transmission line (Pag 296, Bergen)

```

n_br = size(br_data, 1); % Number of branches
n = max(max([br_data.FromBus, br_data.ToBus])); % Number of nodes (starting at 1)
Ybus = zeros(n, n); % Empty Ybus Matrix

for kk = 1: size(br_data, 1) % Iter over branch Data
    ii = br_data.FromBus(kk); % From bus
    jj = br_data.ToBus(kk); % To Bus
    z = br_data.R(kk) + 1j * br_data.X(kk); % Line impedance
    y = br_data.G(kk) + 1j * br_data.B(kk); % Shunt admittance

    Ybr=[1 / z + y / 2 ,    -1 / z; ... % Ybr (Two-Port Network)
        -1 / z          , 1 / z + y / 2];

    Ybus([ii,jj],[ii,jj]) = Ybus([ii,jj],[ii,jj]) + Ybr; % Add the Two-Port
end

```

Se extrae la información de las potencias y voltajes:

```

Vm_sp = N_data.Vm; % [V] Specified Voltages
th_sp = N_data.Va.* pi ./ 180; % [Rads] Specified Angles
PG = N_data.PG; % [p.u.] Active Power generators
QG = N_data.QG; % [p.u.] Reactive Power generators

```

```

PL = N_data.PL; % [p.u.] Active Power Loads
QL = N_data.QL; % [p.u.] Reactive Power Loads

%% Calculated NetPowers
P_sp = PG - PL; % [p.u.] Specified Active Power Pnet= (PGen - PLoad)
Q_sp = QG - QL; % [p.u.] Specified Reactive Power Qnet= (QGen - QLoad)

```

4) Construcción de la matriz Jacobiana

Se encuentran las dimensiones de la matriz jacobiana:

```

% Jacobian matrix size.

nL = sum(strcmp(N_data.type, 'PQ')); % Number of PQ nodes (#Loads)
nG = sum(strcmp(N_data.type, 'PV')); % Number of PV nodes (#Generators)

```

Se divide la matriz Jacobiana en la submatrices H-N-M-L

$$\begin{matrix} nL + nG \\ nL \end{matrix} \begin{bmatrix} \overbrace{H}^{nL + nG} & \overbrace{N}^{nL} \\ \underbrace{M}_{nL} & \underbrace{L}_{nL} \end{bmatrix}^k \begin{bmatrix} \Delta\theta \\ \Delta V/V \end{bmatrix}^k = \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix}^k$$

(Eq. 3.32, pag108, Gómez - Exposito)

$$\begin{aligned} H_{ij} &= \frac{\partial P_i}{\partial \theta_j}; & N_{ij} &= \frac{V_j}{\partial V_j} \frac{\partial P_i}{\partial V_j} \\ M_{ij} &= \frac{\partial Q_i}{\partial \theta_j}; & L_{ij} &= \frac{V_j}{\partial V_j} \frac{\partial Q_i}{\partial V_j} \end{aligned}$$

(Eq. 3.34, pag109, Gómez - Exposito)

```

H = zeros( nL + nG, nL + nG );
L = zeros( nL, nL );
N = zeros( nL + nG, nL );
M = zeros( nL, nL + nG );
J = [H, N; M, L];

```

Se crea el vector de estados ($X = [\theta|V]^T$) y el vector de funciones no lineales ($f(x) = [\Delta P|\Delta Q]$)

```

x_th = zeros( nL + nG, 1 ); % State vector for storing angles (theta)
x_v = zeros( nL, 1 ); % State vector for storing Voltages

```

$$x = [\theta|V]^T = [\theta_1, \theta_2, \dots, \theta_{n-1}|V_1, V_2, \dots, V_{n_L}]^T \quad \text{dim} = (2n_L + n_G)$$

```
x = [x_th; x_v];
```

- Donde se tiene que:

$$\Delta P_i = P_i^{\text{sp}} - V_i \sum_{j=1}^n V_j (G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij}) \quad i = 1, 2, \dots, n-1$$

$$\Delta Q_i = Q_i^{\text{sp}} - V_i \sum_{j=1}^n V_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij}) \quad i = 1, 2, \dots, n_L$$

(Eq. 3.30-3.31, pag108, Gómez - Exposito)

```
Dt_P = zeros( nL + nG, 1 ); % Delta P
Dt_Q = zeros( nL, 1);      % Delta Q
```

$$f(x) = [\Delta P|\Delta Q]^T = [\Delta P_1, \Delta P_2, \dots, \Delta P_{n-1}|\Delta Q_1, \Delta Q_2, \dots, \Delta Q_{n_L}]^T \quad \text{dim} = (2n_L + n_G)$$

```
Dt = [Dt_P;Dt_Q]; %Delta Vector (same as f(x) Vector)

%% Define Unkown Values (Voltage and angle in PQ node - Angle in PV node)
% #Buses with unkwnon voltage magnitudes ('PQ' buses) (Delta Q index)
x_v_n=N_data(strcmp(N_data.type,'PQ'),:).n;

% #Buses with unkwnon voltage angles ('PQ'|'PV' buses) (Delta P index)
x_th_n=N_data(strcmp(N_data.type,'PV')|strcmp(N_data.type,'PQ'),:).n;

x_n = [x_th_n; x_v_n]; % #Buses with unknown Angles and unknown voltages

max_iter = 100; %Define Max iteration number

V = zeros(n, max_iter); % Matrix for storing node voltages per iter
Vm = zeros(n, max_iter); % For storing node voltage magnitude per iter
th = zeros(n, max_iter); % For storing node voltage angles per iter
V(:,1) = Vm_sp .* exp(1j .* th_sp); % Fill with initial Specified Voltages
Vm(:,1) = Vm_sp; % Fill with initial Specified Magnitud
th(:,1) = th_sp; % Fill with initial Specified Angle

err = 1.0; % Define Error
k = 1; % iteration counter
```

5) Inicia el método Newton Raphson

```
while (err > 1e-12 && k < max_iter)
```

```
% for cc = 1 : 3
```

```
% ***** Jacobian Terms Calculation.
```

```
Vn = V( : , k ); % Phasors!!
```

```
Vd = diag( Vn ); % Voltages in a diagonal matrix
```

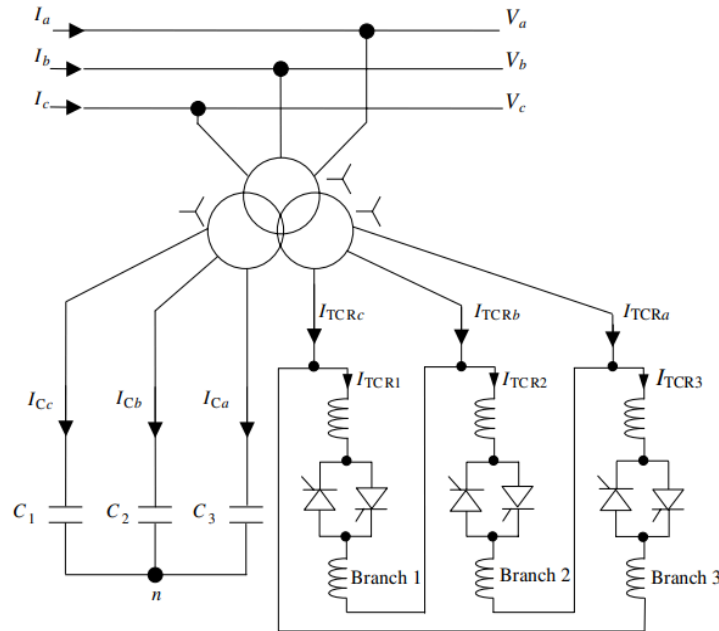
```
% Calculate active and reactive power per node
```

```
Sn = Vd * conj( Ybus * V( : , k ) ); % Sn=V(I)* | I=Y_bus·V | Sn=V·(Ybus·V)*
```

```
Pn = real(Sn); % Active Power calculated
```

```
Qn = imag(Sn); % Reactive Power calculated
```

Se tiene que para un SVC:



Para el delta de los TCR la susceptancia es:

$$B_{\text{TCR}} = \frac{2(\pi - \alpha) + \sin 2\alpha}{\omega L \pi} \quad (\text{Eq. 2.6, Acha})$$

Por ende en el SVC al tener en paralelo el banco de capacitores en Y con el delta de TCR:

$$\left. \begin{aligned} B_{\text{SVC}} &= B_{\text{C}} - B_{\text{TCR}} = \frac{1}{X_{\text{C}} X_{\text{L}}} \left\{ X_{\text{L}} - \frac{X_{\text{C}}}{\pi} [2(\pi - \alpha) + \sin 2\alpha] \right\}, \\ X_{\text{L}} &= \omega L, \\ X_{\text{C}} &= \frac{1}{\omega C}. \end{aligned} \right\} \quad (\text{Eq. 2.20, Acha})$$

Para los reactivos del sistema se sabe que:

$$Q_{SVC} = Q_k = -V_k^2 B_{SVC}. \quad (\text{Eq. 5.5, Acha})$$

es decir,

$$Q_k = \frac{-V_k^2}{X_C X_L} \left\{ X_L - \frac{X_C}{\pi} [2(\pi - \alpha_{SVC}) + \sin(2\alpha_{SVC})] \right\}. \quad (\text{Eq. 5.8, Acha})$$

```
%% Calculate injected bus powers by the SVC
for kk = 1 : size(SVC_data,1)
    FA=SVC_data{kk,"FA"}*pi/180; % Firing Angle [rads]
    SVC_data{kk,"B"} = (2*(pi-FA) + sin(2*FA))*SVC_data{kk,"Xc"}/pi; %Btcr
    SVC_data{kk,"B"} = (SVC_data{kk,"XL"} - SVC_data{kk,"B"})/(SVC_data{kk,"Xc"}*SVC_data{kk,"Xc"});
    Qn(SVC_data{kk,"SVCBus"})=Qn(SVC_data{kk,"SVCBus"})-(Vm(SVC_data{kk,"SVCBus"}))^2*SVC_data{kk,"B"};
end
```

Se obtienen las matrices H,L,N,M donde:

$$\begin{aligned} &\text{For } i \neq j \\ &H_{ij} = L_{ij} = V_i V_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij}) \\ &N_{ij} = -M_{ij} = V_i V_j (G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij}) \\ &\text{For } i = j \\ &H_{ii} = -Q_i - B_{ii} V_i^2 \quad L_{ii} = Q_i - B_{ii} V_i^2 \\ &N_{ii} = P_i + G_{ii} V_i^2 \quad M_{ii} = P_i - G_{ii} V_i^2 \end{aligned}$$

(Table 3.1, pag109, Gómez - Exposito)

```
% H Matrix.    H -> Dim: (nL+nG) X (nL+nG)

for mm = 1 : nL + nG      %Iter over rows H matrix
    for nn = 1 : nL + nG  %Iter over cols H matrix
        ii = x_th_n(mm);  % #node corresponding to row mm
        jj = x_th_n(nn);  % #node corresponding to column nn

        % From Prev Equations:
        if ii == jj
            H(mm,nn) = - Qn(ii) - imag( Ybus(ii,jj) ) .* abs( V(ii,k) ).^2;
        else
            H(mm,nn) = abs( V(ii,k) ) * abs( V(jj,k) ) .* ( ...
                real(Ybus(ii,jj)) * sin( th(ii,k) - th(jj,k) ) - ...
                imag(Ybus(ii,jj)) * cos( th(ii,k) - th(jj,k) ) );
        end
    end
end
```

```

% N Matrix. N -> Dim: (nL+nG) X (nL)
for mm = 1 : nL + nG      % Iter over rows N matrix
    for nn = 1 : nL        % Iter over cols N matrix
        ii = x_th_n(mm); % #node corresponding to row mm
        jj = x_v_n(nn);  % #node corresponding to column nn

        % From Prev Equations:
        if ii == jj
            N(mm,nn) = Pn(ii) + real(Ybus(ii,jj)) .* abs( V(ii,k) ).^2;
        else
            N(mm,nn) = abs( V(ii,k) ) * abs( V(jj,k) ) .* ( ...
                real(Ybus(ii,jj)) * cos( th(ii,k) - th(jj,k) ) + ...
                imag(Ybus(ii,jj)) * sin( th(ii,k) - th(jj,k) ) );
        end
    end
end

% M Matrix. M -> Dim: (nL) X (nL+nG)
for mm = 1 : nL          % Iter over rows M matrix
    for nn = 1 : nL + nG % Iter over cols M matrix
        ii = x_v_n(mm);  % #node corresponding to row mm
        jj = x_th_n(nn); % #node corresponding to column nn

        % From Prev Equations:
        if ii == jj
            M(mm,nn) = Pn(ii) - real(Ybus(ii,jj)) .* abs( V(ii,k) ).^2;
        else
            M(mm,nn) = -abs( V(ii,k) ) * abs( V(jj,k) ) .* ( ...
                real(Ybus(ii,jj)) * cos( th(ii,k) - th(jj,k) ) + ...
                imag(Ybus(ii,jj)) * sin( th(ii,k) - th(jj,k) ) );
        end
    end
end

% L Matrix. L -> Dim: (nL) X (nL)
for mm = 1 : nL          % Iter over rows L matrix
    for nn = 1 : nL      % Iter over cols L matrix
        ii = x_v_n(mm); % #node corresponding to row mm
        jj = x_v_n(nn); % #node corresponding to column nn

        % From Prev Equations:
        if ii == jj
            L(mm,nn) = Qn(ii) - imag(Ybus(ii,jj)) .* abs( V(ii,k) ).^2;
        else
            L(mm,nn) = abs( V(ii,k) ) * abs( V(jj,k) ) .* ( ...
                real(Ybus(ii,jj)) * sin( th(ii,k) - th(jj,k) ) - ...
                imag(Ybus(ii,jj)) * cos( th(ii,k) - th(jj,k) ) );
        end
    end
end

% The jacobian matrix results in:
J = [H, N;...
     M, L];

```


Se modifican los valores de J en el SVC.

$$\begin{bmatrix} \Delta P_k \\ \Delta Q_k \end{bmatrix}^{(i)} = \begin{bmatrix} 0 & 0 \\ 0 & \frac{2V_k^2}{\pi X_L} [\cos(2\alpha_{SVC}) - 1] \end{bmatrix}^{(i)} \begin{bmatrix} \Delta \theta_k \\ \Delta \alpha_{SVC} \end{bmatrix}^{(i)} \quad (\text{Eq. 5.9, Acha})$$

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%% SVC Jacobian Update

for ii = 1 : size(SVC_data,1)

    DQ_svc_Index= find(N_data(strcmp(N_data.type,'PQ'),:).n==SVC_data{ii,"SVCBus"});% get P
    DP_svc_Index =find(x_th_n==SVC_data{ii,"SVCBus"});

    if (SVC_data{ii,'Status'} == 1)
        %Delete the voltage magnitud for the SVC bus
        J( : , nL+nG+DQ_svc_Index) = 0; %Change DeltaV--->Delta alpha (DeltaV=0 - SVC Cor

        FA=SVC_data{ii,"FA"}*pi/180;
        % JAC(2*SVCsend(ii)-1,2*SVCsend(ii)-1) = ... % <- DeltaPk/Delta(Vangle)
        % JAC(2*SVCsend(ii)- 1,2*SVCsend(ii)-1)-Vm(SVCsend(ii))^2*B(ii); %Error?

        J(DP_svc_Index,DP_svc_Index)=J(DP_svc_Index,DP_svc_Index)-Vm(SVC_data{ii,"SVCBus"});
        % [deltaQk] = [Qk]*[delta(Bsvc)/Bsvc] -- k node= SVCnode
        J(nL+nG+DQ_svc_Index,nL+nG+DQ_svc_Index)=2*Vm(SVC_data{ii,"SVCBus"})^2*(cos(2*FA)-
        % [deltaQk]= J(nL+nG+PQ_Index,nL+nG+PQ_Index)
    end
end
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

Se calculan los términos residuales.

$$\Delta P_i = P_i^{\text{sp}} - V_i \sum_{j=1}^n \overbrace{V_j (G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij})}^{P_n} \quad i = 1, 2, \dots, n-1$$

$$\Delta Q_i = Q_i^{\text{sp}} - V_i \sum_{j=1}^n \overbrace{V_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij})}^{Q_n} \quad i = 1, 2, \dots, n_L$$

```

% ***** Residual Terms Calculations

% Delta P
Dt_P=P_sp(x_th_n(1:nL+nG))-Pn(x_th_n(1:nL+nG));
% Delta Q

```

```
Dt_Q=Q_sp(x_v_n(1:nL))-Qn(x_v_n(1:nL));
```

```
Dt = [ Dt_P ; ...
      Dt_Q ];
```

Se actualiza la solución del sistema donde:

$$\begin{bmatrix} \theta_{k+1} \\ V_{k+1} \end{bmatrix} = \begin{bmatrix} \theta_k \\ V_k \end{bmatrix} + J^{-1} \cdot \begin{bmatrix} \Delta P_k \\ \Delta Q_k \end{bmatrix}$$

```
% ***** System Solution
x = inv(J)*Dt; % Delta theta -> inv(J)*Dt
x_th = x( 1 : nL + nG ); % Adjust in unknown Angles
x_v = x( nL + nG + 1 : 2 * nL + nG ); % Adjust in unknown Voltages

Vm(:,k + 1) = Vm(:,k); % new magnitudes
th(:,k + 1) = th(:,k); % new Angles

th(x_th_n, k + 1) = x_th + th(x_th_n, k); % New angle = Adjust in unknown Angle + prev
Vm(x_v_n, k + 1) = x_v.*Vm(x_v_n, k) + Vm(x_v_n, k); % new voltage = Adjust in unknown
```

$$\alpha_{SVC}^{(i)} = \alpha_{SVC}^{(i-1)} + \Delta \alpha_{SVC}^{(i)}.$$

(Eq. 5.10, Acha)

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% SVC Update Adjust

for ii = 1 : size(SVC_data,1)
    if (SVC_data{ii,'Status'} == 1)

        DQ_svc_Index= find(N_data(strcmp(N_data.type,'PQ'),:).n==SVC_data{ii,"SVCBus"});% g

        % Adjust the Voltage Magnitud target
        Vm(SVC_data{ii,"SVCBus"},k + 1) =SVC_data{ii,"Tv"}; %Voltage at SVCnode -> Voltage

        % SVC Susceptance - Delta(Bsvc)
        value = x(nL+nG+DQ_svc_Index); % delta(alpha)

        %% If high or low delta(FA)
        if (value > 0.5236)
            value = 0.5236;
        elseif (value < -0.5236)
            value = -0.5236;
        end

        % Update FA
        SVC_data{ii,'FA'}=SVC_data{ii,'FA'}+ value*180/pi;
```



```

S_pf = zeros( 2*size(br_data, 1) , 5);

bc = 1;
for kk = 1: size(br_data, 1)
    ii = br_data.FromBus(kk);
    jj = br_data.ToBus(kk);
    z = br_data.R(kk) + 1j * br_data.X(kk);
    y = br_data.G(kk) + 1j * br_data.B(kk);
    Ybr=[1 / z + y / 2 ,      -1 / z;      ...      % Ybr (Two-Port Network)
         -1 / z      , 1 / z + y / 2];
    S_br=diag([Vn(ii),Vn(jj)])*conj(Ybr*[Vn(ii);Vn(jj)]);

    S_pf_br= [ii, jj, real(S_br(1)), imag(S_br(1)), abs(S_br(1));...% Apparent power from i to j
              jj, ii, real(S_br(2)), imag(S_br(2)), abs(S_br(2))]; % Apparent power from j to i

    S_pf(2*kk-1:2*kk,:)=S_pf_br;
end

```

7) Se presentan los resultados obtenidos

```

%% Results printing.

for i=1:1 % This "for" is used to display everything once.

    fprintf('          ***** \n')
    fprintf('          **          Newton-Raphson Results          ** \n')
    fprintf('          ***** \n\n')

    fprintf('-- Number of Iterarions: %d \n', k-1)
    fprintf('-- Error: %6.3e p.u.\n\n', err)

    VarNames = {'Node#', 'Type', 'V p.u.', '∠V(°)', 'PG p.u.', 'QG p.u.', 'PL p.u.', 'QL p.u.'};
    fprintf(1, '\t%s\t%s\t%s\t%s\t%s\t%s\t%s\t%s\n', VarNames{:})
    fprintf(1, '-----\n')

    for ii = 1 : n
        fprintf('      \t%d\t%s\t%6.3f\t%6.3f\t%6.3f\t%6.3f\t%6.3f\t%6.3f\t\n', ii, char(N_data{ii}),
            abs(Vn(ii)), angle(Vn(ii)).*180./pi, real(SGn(ii)), imag(SGn(ii)), real(SLn(ii)), i
    end
end

```

```

*****
**          Newton-Raphson Results          **
*****

-- Number of Iterarions: 6
-- Error: 1.274e-14 p.u.
Node# Type V p.u.  ∠V(°) PG p.u. QG p.u. PL p.u. QL p.u.
-----
1 SL  1.060  0.000  1.311  0.853  0.000  0.000
2 PV  1.000 -2.053  0.400 -0.771  0.200  0.100
3 PQ  1.000 -4.838  0.000  0.205  0.450  0.150
4 PQ  0.994 -5.107  0.000 -0.000  0.400  0.050

```

5 PQ 0.975 -5.797 0.000 0.000 0.600 0.100

```
array2table(S_pf, 'VariableNames', {'FromBus', 'ToBus', 'P', 'Q', 'S'});
```

Table 5.1 Nodal voltages of modified network

Nodal voltage	Network bus				
	North	South	Lake	Main	Elm
Magnitude (p.u.)	1.06	1	1	0.994	0.975
Phase angle (deg)	0	-2.05	-4.83	-5.11	-5.80

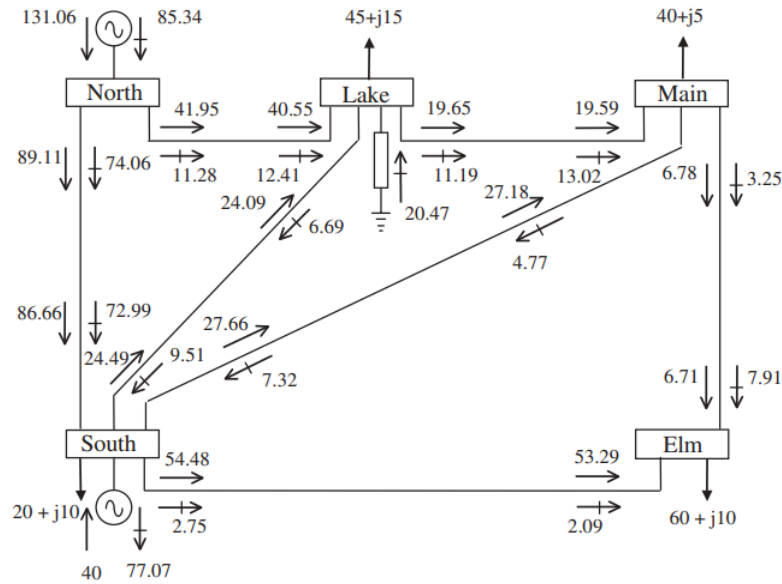


Figure 5.8 Power flow results in the five-bus network with one static VAR compensator

SVC_data

SVC_data = 1×9 table

	SVCBus	Xc	XL	FA	FAMax	FAMin	Tv	Status
1	3	1.0700	0.2880	132.5393	180	90	1	1

Table 5.2 Static VAR compensator state variables

Iteration	Susceptance model		Firing-angle model	
	B_{SVC} (p.u.)		B_{SVC} (p.u.)	α_{SVC} (deg)
1	0.1		0.4798	140
2	0.1679		0.1038	130.23
3	0.2047		0.2013	132.47
4	0.2047		0.2047	132.55
5	0.2047		0.2047	132.55

Referencias:

[1] Gomez - Exposito,A. Electrica Energy Systems, Analysis and operation. 2nd Edition. Boca Raton : Taylor & Francis, CRC Press, 2018.

[2] Acha,E. FACTS Modelling and Simulation in Power Networks. 1st Edition. Boca Raton : John Wiley & Sons Inc,2004