

1

2010 MANG SCI PAPER 3 Q1 DAVID WENDECHT

1a

Basic	value	A	B	C	s_1	s_2	s_3	
s_1	0	1	2	-1	1	0	0	50
s_2	0	2	1	3	0	1	0	130
s_3	0	1.5	1	(2)	0	0	1	40
zr.		0	0	0	0	0	0	
$(5-2s_3)$		2	3	(4)	0	0	0	1

C enters, s_3 exits when $\frac{0}{1}$

$$r_3 \div 2 \quad r_2 - 3r_3 \quad r_1 + r_3$$

Basic	value	A	B	C	s_1	s_2	s_3	
s_1	0	$\frac{7}{4}$	$\frac{5}{2}$	0	1	0	$\frac{1}{2}$	90
s_2	0	$-\frac{1}{4}$	$-\frac{1}{2}$	0	0	1	$\frac{1}{2}$	10
C	4	$\frac{3}{4}$	$\frac{1}{2}$	1	0	0	$\frac{1}{2}$	20
zr.		3	2	4	0	0	2	80
$(5-2s_3)$		-1	(1)	0	0	0	-2	

B enters, s_1 leaves when $\frac{1}{\frac{5}{2}}$

$$r_1 \times \frac{2}{5} \quad r_2 + \frac{1}{2}r_1 \quad r_3 - \frac{1}{2}r_1$$

Basic	value	A	B	C	s_1	s_2	s_3	
B	3	$\frac{7}{10}$	1	0	$\frac{2}{5}$	0	$\frac{1}{5}$	36
s_2	0	$-\frac{4}{5}$	0	0	$\frac{1}{5}$	1	$-\frac{2}{5}$	28
C	4	$\frac{2}{5}$	0	1	$-\frac{1}{5}$	0	$\frac{2}{5}$	2
zr.		$\frac{37}{10}$	3	4	$\frac{2}{5}$	0	$\frac{11}{5}$	116
$(5-2s_3)$		-1.7	0	0	$-\frac{2}{5}$	0	$-\frac{11}{5}$	

1. ii. I would add in 4th variable D which will represent any units above 10 in A

$$\text{Max } 2A + 3B + 4C + 3.5D$$

$$\text{ST: } A + 2B + C + D \leq 50$$

$$2A + B + 3C + D \leq 130$$

$$1.5A + B + 2C + D \leq 40$$

$$D \geq A - 10$$

6

		x_1	x_2	x_3	x_4	s_1	s_2	s_3	s_4	
Value		1.8	15	2	1.2	0	0	0	0	
x_1	18	1	0	0	0.5	0	0.4	0.3	-0.2	30
x_2	15	0	1	0	0.6	0	0.3	0.7	-0.3	24
x_3	2	0	0	1	-0.3	0	1	0.1	0.4	21
s_1	0	0	0	0	-2	1	0.2	-0.6	0.1	18
Z		1.8	15	2	1.2	0	3.17	1.74	-0.01	132
C - Z		0	0	0	0	0	-3.17	-1.74	0.01	

current Solution is: $x_1 = 30$, $x_2 = 24$, $x_3 = 21$, $s_1 = 18$
 Value is 132

Answer is optimal if: values in (5-25) row are all negative, implying that optimal solution has been reached
 - values on rhs are all positive

Sensitivity of coefficient of x_1

$$\begin{array}{c|c|c|c} -0.5C_1 + 0.3 \leq 0 & -0.4C_1 - 2.45 \leq 0 & -0.3C_1 - 1.25 \leq 0 & -0.2C_1 - 1.15 \geq 0 \\ C_1 \geq 0.3 & C_1 \leq -6.125 & C_1 \geq -2.5 & C_1 \leq -5.75 \end{array}$$

3 2010 MANB SCI PAPER 3 G1 DAVID WEITBRECHT

We use the right hand side range to show how much extra units of a constraint we are allowed to add or to subtract to keep the updated solution optimal.

To obtain this we ^{add} multiply solution column ~~by~~ A_{s1} and column for s_2 multiplied by A_{s2} and ^{add} create an equality that they must be ≥ 0

$$\begin{array}{rcllcl} \text{C. Max} & 1100C & + 500S & -50W & -300B & \\ \text{ST:} & 0.75C & + S & + W & & \leq 100 & y_1 \\ & 20C & + 6S & + 25W & & \leq 1200 & y_2 \\ & & & -4W & -B & \leq 0 & y_3 \end{array}$$

this becomes objective function MIN $100y_1 + 1200y_2 + 0y_3$

$$\begin{array}{rcll} 0.75y_1 & + 20y_2 & + y_3 & \leq 1100 \\ y_1 & + 6y_2 & & \leq 500 \\ y_1 & + 25y_2 & - 4y_3 & \leq -50 \\ & & -y_3 & \leq -300 \end{array}$$

The solution is the same as per simplex solution above

$$\begin{array}{l} \text{Sheep} = 70.3704, \quad \text{WF} = 7.4071 \quad \text{Cows} = 24.6296 \\ \text{and Value} = 67407.6 \end{array}$$

$$\begin{array}{l} \text{Sheep land} = \frac{1}{12} \\ \text{man days} = 1.5 \end{array}$$

4

		rows	cols	WF	BWF	Sh	s ₁	s ₂	s ₃	s ₄
Row	value	1100	500	-50	-300	X	0	0	0	0
Soy	500	0	1	0	-0.05					
WF	-50	0	0	1	0.191					
rows	1100	1	0	0	-0.23					
S ₄	0	0	0	0						