

## 2001 MANG SU PAPER Q1

A. Interpretation of t-test. p-value. 95% CI for slope coef.

Test hypothesis  $H_0: \beta_1 = 0$  vs  $H_1: \beta_1 \neq 0$

$$t_{\text{calc}} = 12.83$$

$$t_{\text{crit}} = "$$

$t_{\text{calc}} (12.83) > t_{\text{critical}}$  therefore we reject  $H_0$  that population slope is not 0

The p-value measures the probability of observing a more extreme t-value (in either direction) than the one calculated. p-value  $\neq 0$ .

$$95\% \text{ CI} = \text{estimator} \pm t_{\text{critical}} \cdot \text{se}(\text{estimator})$$

$$-0.09394 \pm t_{18, 0.975}$$

$$-0.09394 \pm 2.10 (0.01426)$$

$$(-0.12386, -0.06394)$$

we are 95% confident that true value for slope ( $\beta_1$ ) lies within this interval. As per above 0 does not lie within this interval so we reject  $H_0: \beta_1 = 0$

## C. Lack of fit test.

We use the F-test to test for lack of fit

$$F = 43.41$$

$$F_{\text{critical}} (0.975, 1, 18) = 3.0048$$

$$F_{\text{calc}} > F_{\text{critical}}$$

If  $F_{\text{calculated}} \leq F_{\text{critical}}$  do not reject  $H_0$

If  $F_{\text{calc}} > F_{\text{critical}}$  reject  $H_0$ .

$$\beta_1 \neq 0$$

$H_0: \mu \leq \text{number}$  vs  $H_1: \mu > \text{number}$

calculate normal  $t_{calc}$   
get  $t_{critical}$

if  $t_{calc} < t_{critical}$  do not reject  $H_0$

if  $t_{calc} > t_{critical}$  reject  $H_0$