

6. Assuming that the ~~investment~~ initial investment could earn interest let say 4% then my initial investment would be  $\frac{5000}{(1.04)^{10}} = 4852.95$

Professor Hartt - no idea how much he is so I would give him the 4852.95

Student - Well, since she is in MSIS they will get a good job in the next few years so I would happily give them the fair price

Close friend - I'd give him lower than the real value

Bank manager - I wouldn't give him any of my money nor any other bank - can't be trusted

7. Find its present value  $\frac{500}{1-r}$  or  $\frac{(1-r)^n}{1-r}$   
 $\frac{500(1.1) / (1 - (1.1)^{10})}{1 - 1.1}$   
 $= 2792.985$

Take 3200 from bank  
 $\frac{500(\frac{1}{x}) / (1 - (\frac{1}{x})^{10})}{1 - \frac{1}{x}} = 3200$

$$\frac{\frac{1}{x}}{\frac{1}{x} - 1} = \frac{x-1}{1-x}$$

$$\frac{500}{x} \left( \frac{1 - \frac{1}{x^{10}}}{1 - \frac{1}{x}} \right) = 3200 \left( \frac{1 - \frac{1}{x}}{1 - \frac{1}{x}} \right)$$

$$500 \left( 1 - \frac{1}{x^{10}} \right) = 3200 \left( 1 - \frac{1}{x} \right)$$

$$\frac{\frac{1}{x}}{\frac{1}{x} - 1} = \frac{x-1}{1-x}$$

22/1/12

Management Science Tutorial 1  
Time value of money 1.1

DAVID WEITBRECHT

123.00604

$$1 \quad F = (P \times 1)^n \quad 2000 = 1000 \left(1 + \frac{R}{100}\right)^7$$

$$2000 = 1000 \left(1 + \frac{R}{100}\right)^7$$

$$\sqrt[7]{2000} = 1000^{1/7}$$

$$2.96196 = 1000^{1/7}$$

$$i = 0.0029$$

$$1.0048 = 1 + \frac{R}{100}$$

$$0.0048 = \frac{R}{100}$$

$$R = 0.4\%$$

$$2 \quad F = P \left(1 + \frac{R}{100}\right)^n$$

$$F = 1200 \left(1.03\right)^{20}$$

$$= 2167.33$$

$$3 \quad \sqrt[12]{1.14}$$

$$1.0109 - 1 = 0.0109\%$$

$$4 \quad -10000 + \frac{3000}{1.15} + \frac{4000}{(1.15)^2} + \frac{3000}{(1.15)^3} + \frac{3000}{(1.15)^4} + \frac{5000}{(1.15)^5}$$

$$= -10000 + 11806.96263$$

$$= +1806.96$$

Assuming that the investment is today and all subsequent events happen at yearly intervals.

5. Payback project 1 occurs in year 4 = 12000  
project 2 occurs in year 4 = 13100

Project 1 10% discount  $\frac{2000}{1.1} + \frac{2000}{(1.1)^2} + \frac{3000}{(1.1)^3} + \frac{5000}{(1.1)^4} = 9140.10 + 840$

Choose Project 2 10% discount  $\frac{4000}{1.1} + \frac{3000}{(1.1)^2} + \frac{1100}{(1.1)^3} + \frac{4500}{(1.1)^4} = 10428.93$  more 428.93

Project 1 15% discount  $\frac{2000}{1.15} + \frac{2000}{(1.15)^2} + \frac{3000}{(1.15)^3} + \frac{5000}{(1.15)^4} = 8082$  more 1917.27

Project 2 15% discount  $\frac{4000}{1.15} + \frac{3000}{(1.15)^2} + \frac{1100}{(1.15)^3} + \frac{4500}{(1.15)^4} = 9420.92$  more 574.08



$$4 \text{ } \text{pymt} = \frac{a \times r \times (1+r)^n}{[(1+r)^n - 1]}$$

$$\frac{5000 \times 0.01 \times (1.01)^{60}}{[(1.01)^{60} - 1]} = 111.22 \text{ per month.}$$

$$\text{Total interest} = 673.2$$

② Start of year 2 owing = 5050

~~5050~~ 5634.13 owed at start of year 3

$$\frac{5634.13 \times (0.01) \times (1.01)^{48}}{[(1.01)^{48} - 1]} = 148.37 \text{ month}$$

$$\begin{aligned} & \times 48 = 7121.76 \\ & - 5000 = \\ & 2121.76 \text{ interest} - 673.2 \\ & = 1448.56 \text{ extra interest} \end{aligned}$$

$$5. \frac{1000}{(1.065)^0} + \frac{1000}{(1.065)^3} + \frac{1000}{(1.065)^2} + \frac{1000}{(1.065)^1} = 3425.798$$

$$= 3425.80$$

$$6 \text{ } \text{pymt} = \frac{a \times r \times (1+r)^n}{[(1+r)^n - 1]} \quad \frac{100000 \times 0.1 \times (1.1)^{15}}{[(1.1)^{15} - 1]} = 13147.37$$

$$\frac{10000 \times 0.15 \times (1.15)^{10}}{[(1.15)^{10} - 1]} = 17101.70 \text{ using } 15\%$$

$$7. \frac{60000 \times (0.009 \times 1.009) \times (1.009)^{240}}{(1.009)^{240} - 1} = 611.60 \text{ /2v}$$

$$\frac{60000 \times 0.01 \times (1.01)^{240}}{[(1.01)^{240} - 1]} = 600 =$$

113

Management Science

Tutorial: Time Value of Money III

DAVID WEITBRECHT

12300606

$$1 \quad \text{Interest} = \frac{2638.02}{(1.1)^3} + \frac{2638.02}{(1.1)^4}$$

$$2398.2 + 2180.18 \quad \text{capital paid off}$$

$$= 4578.38$$

$$1638.0 + 1801.80$$

$$3439.8 \quad \text{paid off}$$

$$2 \quad \text{Payment} = \frac{a \cdot r (1+r)^n}{[(1+r)^n - 1]}$$

$$\frac{10000 \times 0.1 (1.1)^{10}}{[(1.1)^{10} - 1]} = 1627.45 \quad \text{per year}$$

$$\times 10 = 16274$$

$$6274 \quad \text{interest}$$

$$\text{compared to } 3175.1$$

you pay more interest over 10 years

$$3 \quad \text{Payment} = \frac{a \cdot r \cdot (1+r)^n}{[(1+r)^n - 1]} \quad r = \sqrt[12]{1.04} - 1 = 0.4\%$$

$$0.004$$

$$\frac{10000 \times 0.004 (1.004)^{60}}{[(1.004)^{60} - 1]}$$

$$= 187.797$$

$$= 187.80 \quad \text{per month}$$

$$\times 60 = 11268$$

less interest than by pay yearly

$$1268 \div 60 = 21.13 \quad \text{interest per month}$$

$$= 0.002113$$

$$= 0.21\% \quad \text{per month}$$

Simple int'l



1/1/13 Managerial Science  
Tutorial 3: Future

DAVID WEITBRECHT 123006001

$$1. 10000 \times 50_{\text{eur}} = 50000 \text{ worth now, monthly rate} = 1.00246627$$

$$50000 \times (1.00246627)^6$$

$$= 5074.445789$$

$$= \text{€ } 5074.45 \approx \text{fair price of 10000 Libel in 6 months}$$

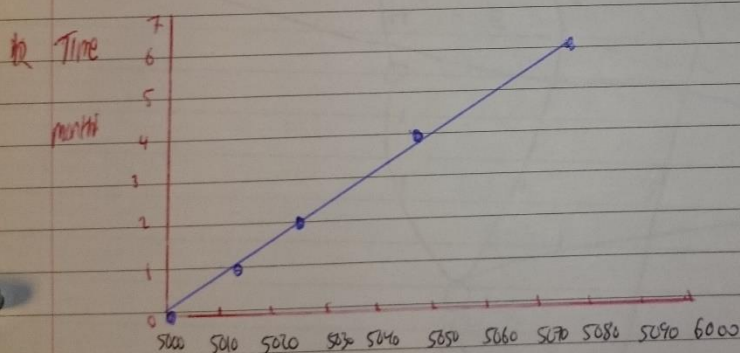
$$2. \text{Total} = 5000 \times 43.42 = \frac{217100}{(1.00012)^{94}} = \frac{214665.0172}{\approx 5000}$$

$$= 42.93 \text{ per bond}$$

$$3. a. 4 \text{ months} = 5000 \times (1.00246627)^4 = 5049.51$$

$$2 \text{ months} = 5000 \times (1.00246627)^2 = 5024.69$$

$$1 \text{ month} = 5000 \times (1.00246627) = 5012.33$$



c. The fair price increases by each month as it approaches the settlement date.

Starting price: 10.50      40000 shares

Day	Closing Price	Daily Movement To Market	Who pays
1	10.30	$\frac{42000}{41200} - 8000$	buyer.
2	10.35	+2000	seller
3	10.70	+14000	buyer
4	10.70	0	no one.
5	10.40	-12000	seller