

# INFORMATION SYSTEMS

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## Programming Techny 2011 exam Paper

Q.5. A1. i no saddle point

1	2	3	4		1
3	9	1	5		1
10	5	4	5		4
12	5	7	8		5
12	9	7	8		

ii. 4x4 1 saddle point.

7	8	9	10	7
6	2	7	8	2
5	3	6	1	1
4	1	5	9	1
7	8	9	10	

7 is saddle point

iii. 2 saddle point.

7	7	3	4
6	4	8	4
7	9	10	7
4	3	2	6
2	4	1	5
7	11	12	7

The 7's are saddle point

- Suppose a and b are two saddle point in matrix

- If they lie in same row, then since a is smallest entry in row,  $a \leq b$ , but b is also smallest entry in its row, so  $b \leq a \Rightarrow b = a$

- for some column, both are largest entry in the column, b both  $a \geq b$  and  $b \geq a \Rightarrow a = b$

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If they lie in different row and column, then they form opposite corners of a rectangle in the matrix,

a ... c  
:  
d ... b

- Since a is smallest entry in its row and b largest in its column we have  $a \leq c \leq b$

- but b is smallest entry in its row and d largest in its column so  $b \leq d \leq a$

- Putting together we have  $a \leq c \leq b \leq d \leq a$

- But since same number lies at both ends of equality, all four numbers must be equal

- Shows that a=b but cond d are all saddle points

ii. Basic-Matrix transpose() {  
Basic-Matrix result = new Basic-Matrix (cols, rows);  
for (int i=0; i < cols; i++) {  
for (int j=0; j < rows; j++) {  
result[i][j] = mat[j][i];  
}  
}  
return result;  
}

iii. void all-saddle (Basic-Matrix m) {  
double C; mins, maxes;  
boolean found = false;  
Basic-Matrix mt;

mins = m.min-row();

mt = m.transpose();

maxes = mt.max-row();

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Q.C.

```
For (int i=0; i < m.rows; i++) {  
    for (int j=0; j < m.rows; j++) {  
        if (minS[i] == maxS[j]) {  
            found = true;  
            print-Saddle (m.mat, i, j);  
        }  
    }  
}  
if (!found) print "no Saddle";  
}
```