

Tutorial 1 week 2

DAVID WEITBRECHT 12300644

9.5
10

iii. $u = (-2, -k, 0, k)$ $v = (0, -k, 1, 2)$

$$v+u = \begin{pmatrix} -2+0, & -k+(-k), & 0+1, & k+2 \\ -2, & -2k, & 1, & k+2 \end{pmatrix}$$

$$2v = \begin{pmatrix} 2(0), & 2(-k), & 2(1), & 2(2) \\ 0, & -2k, & 2, & 4 \end{pmatrix}$$

$$\|u\| = \frac{\sqrt{-2^2 + -k^2 + 0^2 + k^2}}{\sqrt{4 + 2k^2}}$$

$$\|v\| = \frac{\sqrt{0^2 + -k^2 + 1^2 + 2^2}}{\sqrt{5 + k^2}}$$

$$u \cdot v = \begin{pmatrix} -2(0) + -k(-k) + 0(1) + k(2) \\ -k^2 + k^2 + 2k \end{pmatrix}$$

$$\cos^{-1} \frac{-k^2 + 2k + k^2}{\sqrt{4 + 2k^2} \sqrt{5 + k^2}}$$

orthogonal when $-k^2 + 2k + k^2 = 0$ $k^2 + 2k = 0$
 $(k-2)(k+1)$ $k(k+2) = 0$

$$k = 0 \text{ or } k = -2$$

will be orthogonal.

DAVID WEITBRECHT 1230641

DW.

iv. $u = (a, c, 0, b, 0)$ $v = (c, -2a, c, 0, b+c)$

$$u+v = \begin{pmatrix} a+c & c-2a & 0+c & b+0 & 0+b+c \\ b+c & c-2a & c & b & b+c \end{pmatrix}$$

$$2v = (2c, -4a, 2c, 0, 2b+2c)$$

$$\|u\| = \sqrt{a^2 + c^2 + 0^2 + b^2 + 0^2} = \sqrt{a^2 + b^2 + c^2}$$

$$\|v\| = \frac{\sqrt{c^2 + 4a^2 + c^2 + b^2 + c^2 + 2bc}}{\sqrt{3c^2 + 4a^2 + b^2 + 2bc}}$$

4.5

angle $\theta = \cos^{-1}$

$$u \cdot v = a(c) + c(-2a) + 0(c) + b(0) + 0(b+c) = ac - 2ac = -ac$$

$$\theta = \cos^{-1} \frac{-ac}{\sqrt{a^2 + b^2 + c^2} \sqrt{3c^2 + 4a^2 + b^2 + 2bc}}$$

When $u \cdot v = 0$ orthogonal $-ac = 0$

$a=0$ or $c=0$
 $a=0$ and $c=0$ then $S \neq \emptyset$

2 i.

$$\begin{pmatrix} x & y & z \\ 2 & 0 & -1 \\ -1 & -1 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} -2 \\ 4 \end{pmatrix}$$

ii.

$$\begin{pmatrix} x & y & t & z \\ 2 & 0 & -1 & 1 \\ 0 & -2 & 1 & 0 \\ -1 & -1 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ t \\ z \end{pmatrix} = \begin{pmatrix} -1 \\ -7 \\ 4 \end{pmatrix}$$

4.5

Week 2 Set 1

20/1/14

Tutorial

DAVID WEITBRECHT 12300644

1i. $u = (1, 0, 2)$ $v = (2, 1, -1)$

$$v+u = (1+2, 0+1, 2+(-1)) \\ = (3, 1, 1)$$

$$2v = (2(2), 2(1), 2(-1)) \\ = (4, 2, -2)$$

$$\|u\| = \sqrt{1^2 + 0^2 + 2^2} \\ = \sqrt{5}$$

$$\|v\| = \sqrt{(2)^2 + (1)^2 + (-1)^2} \\ = \sqrt{6}$$

$$u \cdot v = 1(2) + 0(1) + 2(-1) \\ = 2 + 0 - 2 = 0$$

$$\text{angle } \theta = \cos^{-1} \frac{u \cdot v}{\|u\| \|v\|} = \frac{0}{\sqrt{5} \sqrt{6}} = \frac{\pi}{2}$$

Orthogonal if $\theta = \frac{\pi}{2}$

Not orthogonal angle = π not $\frac{\pi}{2}$

2
Dw.

ii. $u = (1, -1, 0, -1, 0, 1)$ $v = (0, 1, 0, -2, -1, 0)$

$$v+u = (1+0, -1+1, 0+0, -1-2, 0-1, 1+0)$$
$$(1, 0, 0, -3, -1, 1)$$

$$2v = (2(0), 2(1), 2(0), 2(-2), 2(-1), 2(0))$$
$$(0, 2, 0, -4, -2, 0)$$

$$\|u\| = \sqrt{1^2 + (-1)^2 + (0)^2 + (-1)^2 + (0)^2 + (1)^2}$$
$$\sqrt{4} = 2$$

$$\|v\| = \sqrt{0^2 + 1^2 + 0^2 + (-2)^2 + (-1)^2 + 0^2}$$
$$= \sqrt{6}$$

$$u \cdot v = (1)(0) + (-1)(1) + (0)(0) + (-1)(-2) + (0)(-1) + (1)(0)$$
$$= -1 + 2 = 1$$

$$\cos^{-1} \frac{1}{2\sqrt{6}} = 78^\circ$$

NOT ORTHOGONAL, Angle not 95