

17/05/15

# FORECASTING EXAM PAPER 2004

6 a Trend - upward  
Seasonality

b 1) Is it stationary? Stationary in mean?  
Not because of upward trend and slight seasonality.

c.

e.i. LHS:  $(1-B)(1-B^{12})y_t$

$$[1 - B^{12} - B + B^{13}]y_t = y_t - B^{12}y_t - B y_t + B^{13}y_t \quad \text{recall } B^k y_t = y_{t-k}$$

$$= y_t - y_{t-12} - y_{t-1} + y_{t-13}$$

$$\text{RHS: } (1 - \theta_1 B)(1 - \alpha_1 B^{12} - \theta_2 B + \alpha_2 B^{13})\epsilon_t$$

$$= [1 - \alpha_1 B^{12} - \theta_2 B + \alpha_2 B^{13}]\epsilon_t$$

$$= \epsilon_t - \alpha_1 \epsilon_{t-12} - \theta_2 \epsilon_{t-1} + \alpha_2 \epsilon_{t-13}$$

ii proposed  $ARIMA(0,1,1)(0,1,1)_{12}$  Seasonal 12  $\Rightarrow$  acf

No obvious trend

	ACF	PAF
AR <sub>p</sub>		Spikes at <del>lags</del> 1 to p
MA <sub>q</sub>	Spikes at 1 to q	
SAR <sub>p</sub>	ACP	PAF
SMA <sub>q</sub>	Spikes at lags q, 2q, 3q, ...	Spikes at lags 1, 2, 3, ...

ARIMA (0, 1, 1)

ma  
Spike at lag  
1 in a/cf

(0, 1, 11)<sub>12</sub>

Sma Spike at lag 12  
in a/cf

Integral difference remove trend and seasonality - now stationary  
i.e. TS is now stationary