

1

SETTING UP

2 In this chapter we describe the environment we use to do our test, the tool

3 **1.1 PYTHON ENVIRONMENT**

4 The language used to interface with quantum computer is usually python, in
5 this section we create a virtual environment in python in order to communicate
6 with the IBM quantum Computer and the D-Wave quantum computer.

7 For our test we manage python environments with `conda`, let's start creating
8 the virtual env named `quantum` and activate it with:

```
1 conda create --name quantum python=3.12 pip  
2 conda activate quantum
```

9 For our test and to follow the various example presented both by IBM and
10 D-Wave is also useful to be able of running a Jupyter notebook. We can
11 install Jupyter with:

```
1 pip install jupyter
```

12 **1.2 IBM QISKIT**

13 To program an architecture gate based and to access IBM quantum computer
14 we use the *Qiskit* software stack. The name Qiskit is a general term referring
to a collection of software for executing programs on quantum computers.

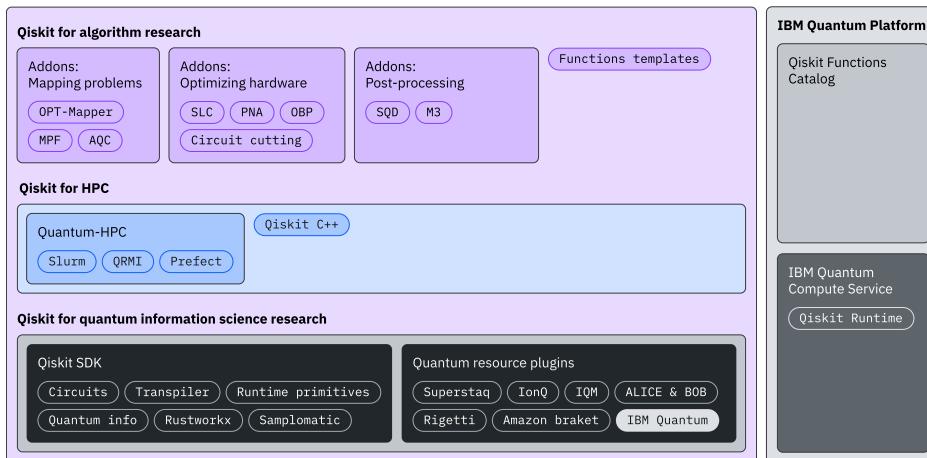


Figure 1.1: Qiskit software stack

15
16 The core components are *Qiskit SDK* and *Qiskit Runtime*, the first one is
17 completely open source and allows the developer to define his circuit; the

18 second one is a cloud-based service for executing quantum computations on
 19 IBM quantum computer.

20 **1.2.1 Hello World**

21 Following the IBM documentation¹ we can install the SDK and the Runtime
 22 with:

```
1 pip install qiskit matplotlib qiskit[visualization]
2 pip install qiskit-ibm-runtime
3 pip install qiskit-aer
```

23 Line 3 install Aer, that is a high performance simulator for quantum cir-
 24 cuits written in Qiskit. Aer includes realistic noise models, and we will use
 25 later to test our circuit.

26 Sometimes the Qiskit stack suffer from incompatibility between the vari-
 27 ous software that compose the environment. At the moment of writing the
 28 latest package seem to work without any problem. For our test we will use
 29 `qiskit: 2.2.3, qiskit-ibm-runtime: 0.43.1` and `qiskit-aer: 0.17.2`.

30 If the setup had success we are now able to run a small test to build a Bell
 31 state (two entangled qubits). The following code assemble the gates, show
 32 the final circuit and use a sampler to simulate on the CPU the result of 1024
 33 runs of the program.

```
1 from qiskit import QuantumCircuit
2 from qiskit.primitives import StatevectorSampler
3
4 qc = QuantumCircuit(2)
5 qc.h(0)
6 qc.cx(0, 1)
7 qc.measure_all()
8
9 sampler = StatevectorSampler()
10 result = sampler.run([qc], shots=1024).result()
11 print(result[0].data.meas.get_counts())
12 qc.draw("mpl")
```

Listing 1: hello qiskit

34 **1.2.2 Transpilation**

35 Each Quantum Processing Unit (QPU) has a specific topology, we need to
 36 rewrite our quantum circuit in order to match the topology of the selected
 37 device on which we want to run our program. This phase of rewriting, fol-
 38 lowed by an optimization, is called transpilation.

39 Considering, for now, a fake hardware (so we don't need an API key)
 40 we can transpile the quantum circuit `qc`, from the code above, to match the
 41 topology of a precise QPU:

¹ <https://quantum.cloud.ibm.com/docs/en/guides/install-qiskit>

```

1  from qiskit_ibm_runtime.fake_provider import FakeWashingtonV2
2  from qiskit.transpiler import generate_preset_pass_manager
3
4  backend = FakeWashingtonV2()
5  pass_manager = generate_preset_pass_manager(backend=backend)
6
7  transpiled = pass_manager.run(qc)
8  transpiled.draw("mpl")

```

Listing 2: Transpilation

42 The following picture show (1.2a) the quantum circuit that build a Bell
 43 state, and (1.2b) the transpiled version where the Hadamard gate is replaced
 to match the actual topology of the QPU.

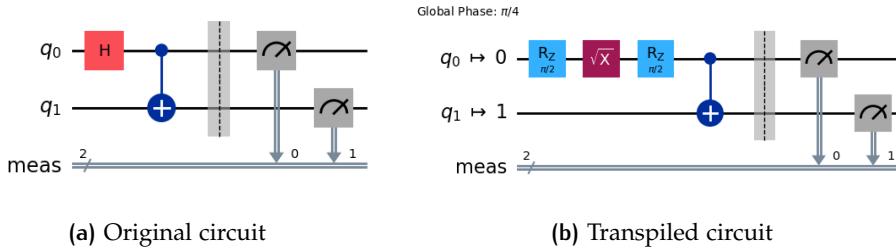


Figure 1.2: Transpilation example

44

45 1.2.3 Execution

46 To test our transpiled circuit we use Aer that allow us to simulate also the
 47 noise of a real quantum hardware. We can execute our program with:

```

1  from qiskit_aer.primitives import SamplerV2
2
3  sampler = SamplerV2.from_backend(backend)
4  job = sampler.run([transpiled], shots=1024)
5  result = job.result()
6  print(f"counts for Bell circuit : {result[0].data.meas.get_counts()}")

```

Listing 3: Simulated execution

48 If we look at the results of the execution we could observe that some
 49 answers present non entangled qbit, this is caused by the (simulated) noise
 50 of the quantum device. A typical output of the execution could be:

```
> counts for Bell circuit : {'00': 504, '11': 503, '01': 10, '10': 7}
```

51 Where state 01 and 10 should not be present in an ideal execution with no
 52 errors.

53 1.2.4 A complete example on real hardware

54 1.3 D-WAVE OCEAN

55 To define an optimization problem that can be resolved on a D-Wave quantum
 56 computer we use the Ocean software stack. Ocean, also, allow us to
 57 interact with D-Wave hardware, submit a problem and to simulate the execution on a classical CPU.

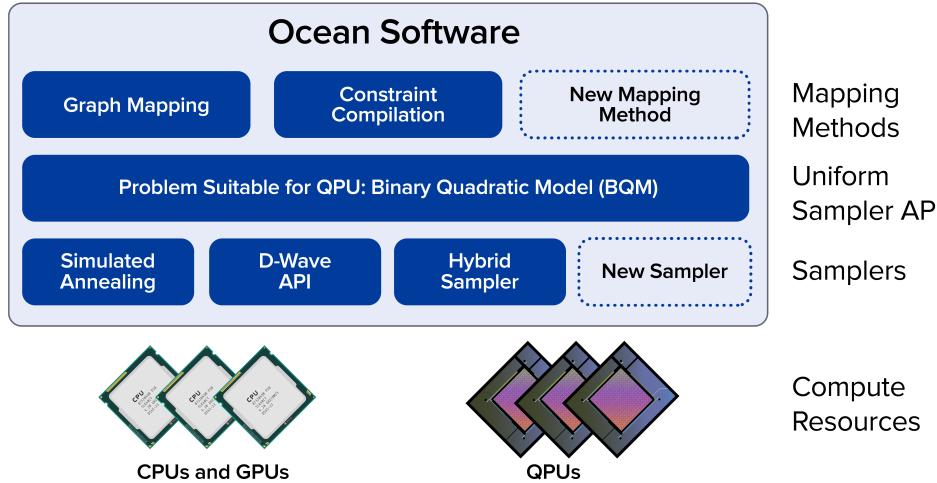


Figure 1.3: Ocean software stack

58
 59 All tools that implement the steps needed to solve your problem on a CPU,
 60 a D-Wave quantum computer, or a quantum-classical hybrid solver can be
 61 installed with:

```
1 pip install dwave-ocean-sdk
```

62 After the installation running the command `dwave setup` will start an interactive
 63 prompt that guide us through a full setup. During the setup is also
 64 possible adding a API token or connecting to the D-Wave account to import
 65 directly a key to use the quantum hardware.

66 1.3.1 Hello World

67 To present simple optimization program we consider the minimum vertex
 68 cover (MVC) problem. Given a graph $G = (V, E)$ the problem asks to find a
 69 subset $V' \subseteq V$ that for each edge $\{u, v\} \in E$ at least one of v or u belongs to
 70 V' and the number of nodes in V' ($|V'|$) is the lowest possible.

71 The reduction from MVC to Ising formulation is well known, the cost
 72 function, that we want to minimize, could be expressed by:

$$\text{cost} = \sum_{i=1}^{|V|} v_i + 2 \cdot \sum_{\{i,j\} \in E} (1 - v_i - v_j + v_i v_j)$$

73 Where $v_i \in \{-1, 1\}$ and if $v_i = 1$ means that $v_i \in V'$, otherwise $v_i = -1$.

74 Like all problem in Ising form we can express the cost as a symmetrical
 75 matrix, so our function become

$$\text{cost} = \mathbf{v}^T \times \mathbf{M} \times \mathbf{v}$$

76 Were \mathbf{v} is the vector containing the binary variables v_i .

77 The figure shows an example graph (1.4a) and the corresponding matrix
 78 (1.4b) expressing the cost function.

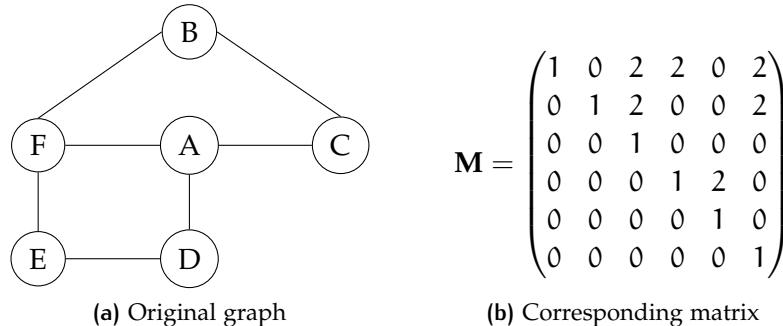


Figure 1.4: Ising formulation

79 The following code present a possible implementation of the Ising model
 80 described above. We have defined two dictionary to memorize the matrix
 81 coefficient. The last line of code founds ten possible answers to the problem
 82 using the simulated annealing function implemented by D-Wave.

```

1 from dwave.samplers import SimulatedAnnealingSampler
2 linear = {'A': 1, 'B': 1, 'C': 1, 'D': 1, 'E': 1, 'F': 1}
3 quadratic = {('B', 'C'): 2, ('B', 'F'): 2, ('C', 'A'): 2, ('D', 'A'): 2,
   ↳ ('E', 'D'): 2, ('E', 'F'): 2, ('F', 'A'): 2}
4 sampler = SimulatedAnnealingSampler()
5 result = sampler.sample_ising(linear, quadratic, num_reads=10)

```

Listing 4: Ising example

83 If we print the results with: `print(result.aggregate())` we could observe
 84 something similar to this:

```

1   A   B   C   D   E   F   energy  num_oc.
2   0  -1  -1  +1  +1  -1  +1   -14.0      6
3   1  +1  +1  -1  -1  +1  -1   -14.0      4
4   ['SPIN', 2 rows, 10 samples, 6 variables]

```

85 The two different results represent the two correct answer to our particular
 86 instance of the MVC problem.

87 **1.3.2 Example on real hardware**88 **1.3.3 Minor embedding**89 **1.4 PYQUBO AND QUBOVERT**

90 In listing ?? we have manually built the matrix representing the function
91 that we want to minimize. It can be useful to have some tools that allow us
92 working at higher level defining the function like:

$$\text{cost} = \text{objective} + \lambda \cdot \text{penalty}$$