

Computer Vision & Multimedia Analysis Course

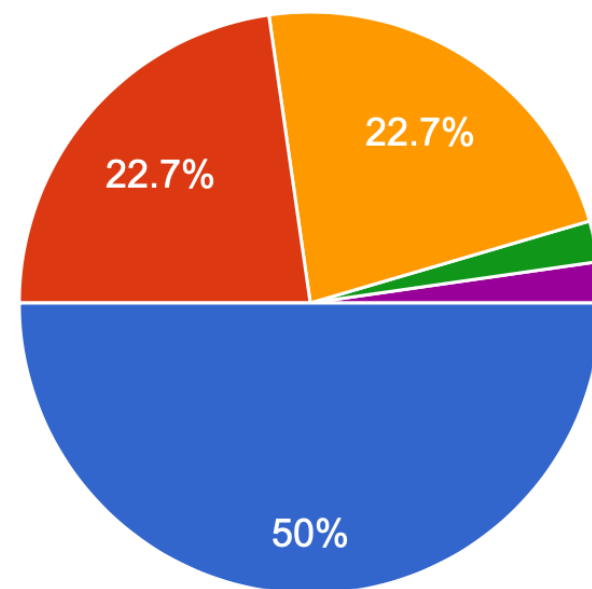
Lab 3: Tracking

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Feedback

Which is your background?

44 responses

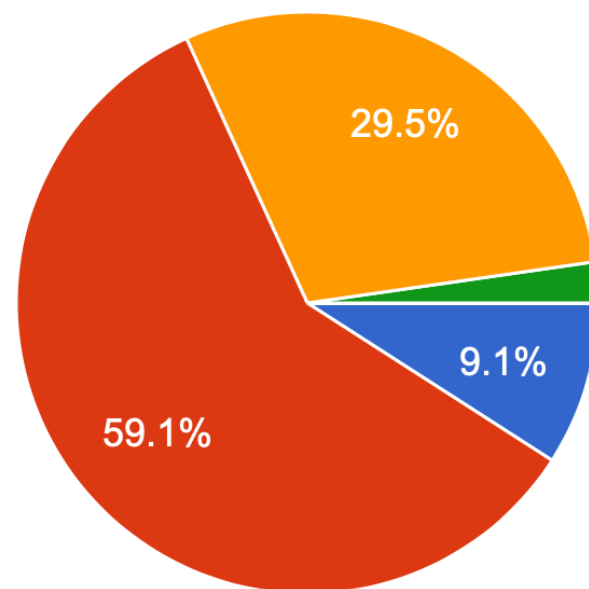


- Computer Science
- Communication Engineering
- Mechanical Engineering
- Information and business organization
- Economics & Management

Feedback

The Lab so far:

44 responses



- Too easy, I would like something more challenging
- It's ok, I can easily follow
- I'll need to look again into something, but mostly ok
- so-so, I'm not confident with what we have done so far
- hard to follow, it is not clear



Feedback

- ❖ Material before lectures
- ❖ Real-world applications examples
- ❖ More challenging suggestions / material



What's up today (and Monday)

- ❖ Good Features to Track + Lucas Kanade optical flow
- ❖ Meanshift / Camshift algorithm
- ❖ Kalman filter

Good Features to Track

- ❖ For each candidate point, compute:

$$Z = \begin{bmatrix} \sum_W J_x^2 & \sum_W J_x J_y \\ \sum_W J_y J_x & \sum_W J_y^2 \end{bmatrix}$$

- ❖ J_x and J_y are the gradients evaluated on the point in x and y direction within W ($n \times n$ window)
- ❖ A good feature point is where the smallest eigenvalue of Z is larger than a specified threshold
- ❖ In practice, it highlights corner points and textures

Lucas-Kanade optical flow estimation

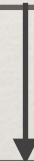
- ❖ Two-frame differential method for optical flow estimation developed by Bruce D. Lucas and Takeo Kanade (1981)
- ❖ Consider $u=[u_x, u_y]$ in frame I and $v=[v_x, v_y]$ in frame J
- ❖ The goal is to find \mathbf{d} that satisfies $\mathbf{v}=\mathbf{u}+\mathbf{d}$ such as I and J are similar (translational model)
- ❖ Because of the aperture problem, **similarity** must be defined in 2D
- ❖ \mathbf{d} is the vector that minimizes

$$\epsilon(d) = \epsilon(d_x, d_y) = \sum_{x=u_x-\omega_x}^{u_x+\omega_x} \sum_{y=u_y-\omega_y}^{u_y+\omega_y} (I(x, y) - J(x + d_x, y + d_y))^2$$

- ❖ ω is the integration window

GFF+LK tracking

Use GFF to detect and select good Features



Track detected feature using LK optical flow



Exercise

Part 1

- ❖ Track features in the environment using
- ❖ `corners, status, err = cv2.calcOpticalFlowPyrLK(prev_frame, frame, prev_corners, None)`

Part 2 (optional)

- ❖ Draw trajectory of tracked points

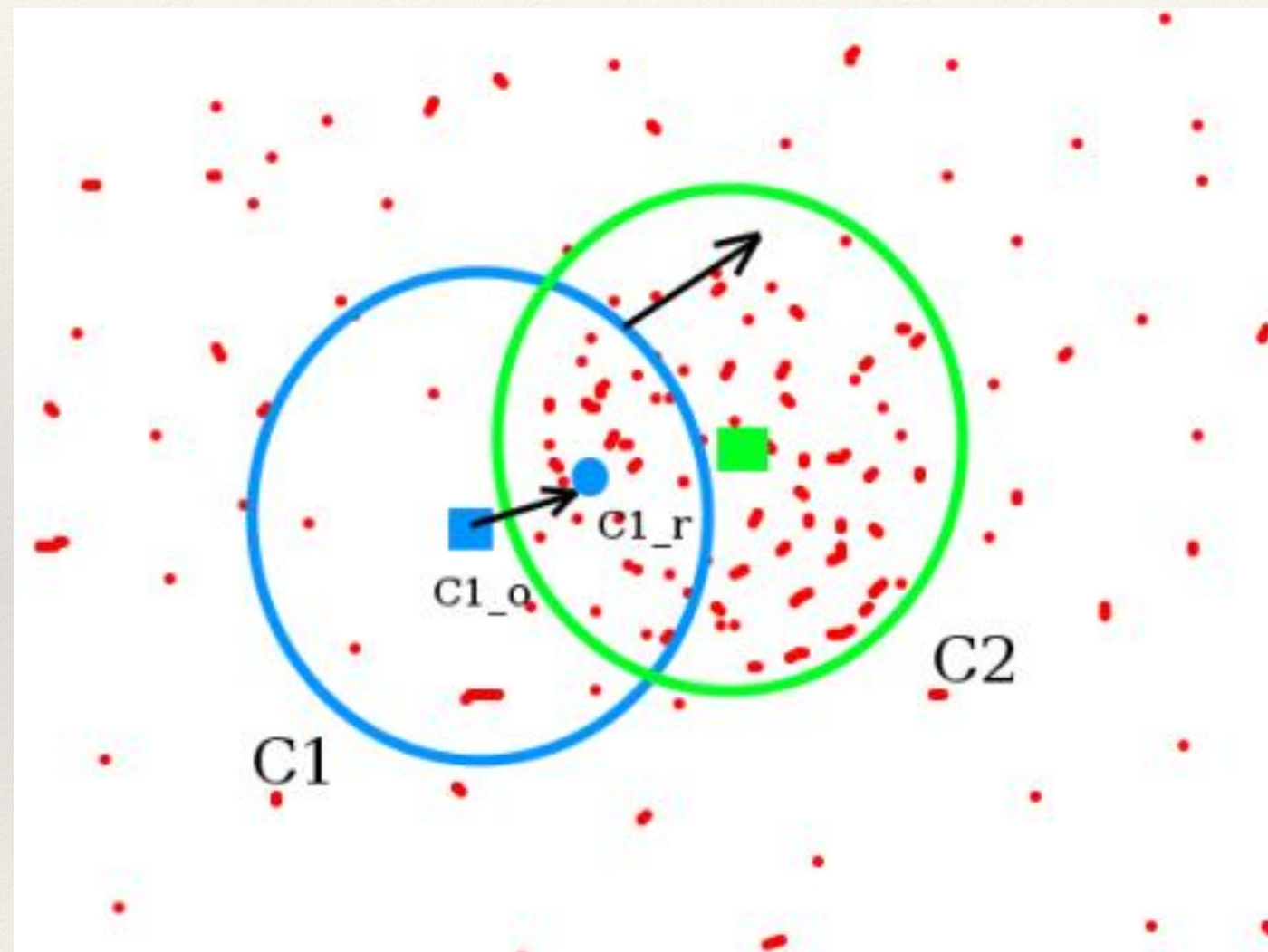


Exercise

Part 3

- ❖ How to avoid losing features after some time?
- ❖ Re-detect features using GFF

Meanshift algorithm



Meanshift algorithm

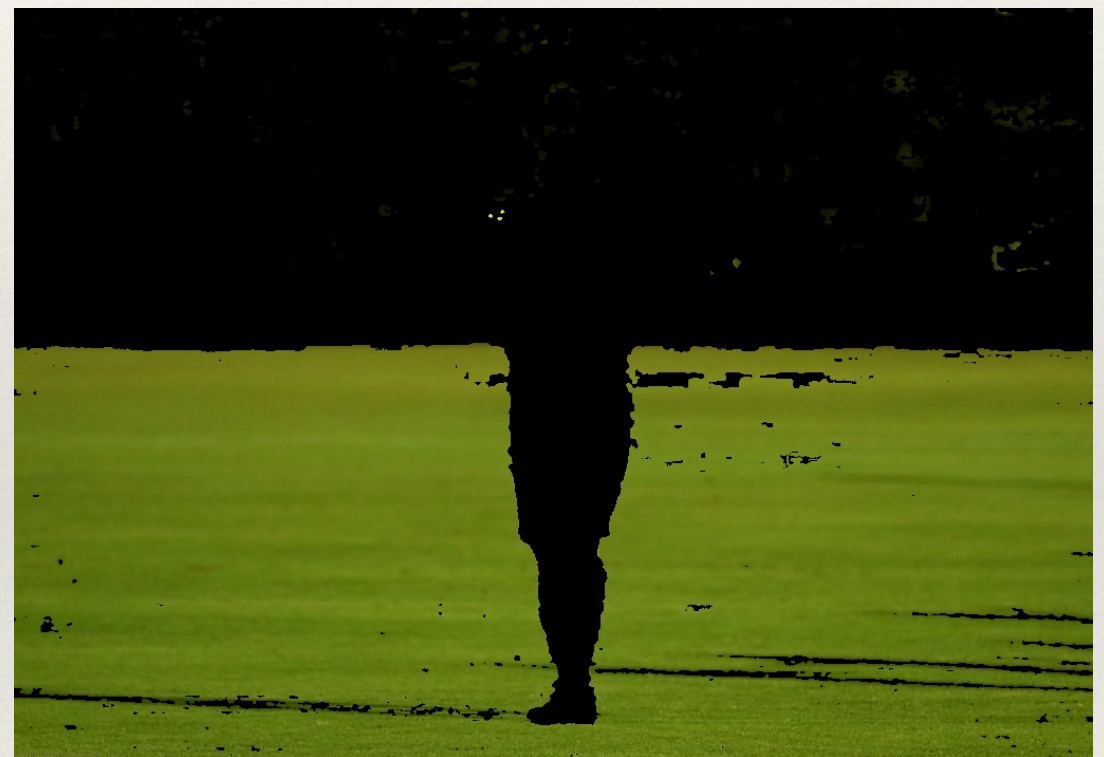


roi



Target

Meanshift algorithm



Meanshift algorithm

- ❖ RGB to HSV image conversion
- ❖ Manually select Region Of Interest (ROI)
- ❖ Calculate histogram of ROI
- ❖ Back projection of the histogram
- ❖ Tracking



Camshift algorithm

- ❖ Finds an object center using `meanShift()`
- ❖ Adjusts the window size and finds the optimal rotation.

Exercise

- ❖ Implement `camShift` algorithm instead of `MeanShift`
- ❖ Check documentation on the website
- ❖ Display the window using the `poly lines` function

```
pts = cv2.boxPoints(ret)
```

```
pts = np.int0(pts)
```

```
img2 = cv2.polylines(frame,[pts],True, 255,2)
```

- ❖ Bonus: display backprojection and plot histograms



Kalman filter

- ❖ Inside the Virtual Machine (or in your programming environment)
- ❖ Go to this link and download the file
- ❖ https://github.com/mmlab-cv/CVLaboratories/Lab3/kalma_start.py

Kalman filter

$$\mathbf{x}_k = \mathbf{A}_k \mathbf{x}_{k-1} + \mathbf{w}_{k-1}$$

$$\mathbf{z}_k = \mathbf{H}_k \mathbf{x}_k + \mathbf{v}_k$$

- ❖ \mathbf{x}_k is the current state
- ❖ \mathbf{x}_{k-1} is the previous state
- ❖ \mathbf{A}_k is the state transition matrix
- ❖ \mathbf{w}_k is the process noise
- ❖ \mathbf{z}_k is the actual measurement
- ❖ \mathbf{H}_k is the measurement matrix
- ❖ \mathbf{v}_k is the measurement noise

Kalman filter

$$\hat{\mathbf{x}}_k^- = \mathbf{A}_k \hat{\mathbf{x}}_{k-1}$$

$$\mathbf{P}_k^- = \mathbf{A}_k \mathbf{P}_{k-1} \mathbf{A}_k^T + \mathbf{Q}_{k-1}$$

$$\mathbf{K}_k = \mathbf{P}_k^- \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_k^- \mathbf{H}_k^T + \mathbf{R}_k)^{-1}$$

$$\hat{\mathbf{x}}_k = \hat{\mathbf{x}}_k^- + \mathbf{K}_k (\mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_k^-)$$

$$\mathbf{P}_k = (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_k^-$$

Kalman filter applied on mouse motion

❖ Motion equation: $P_t = P_0 + V * t$

$$\mathbf{x}_k = \mathbf{A}_k \mathbf{x}_{k-1} + \mathbf{w}_{k-1}$$

$$\mathbf{z}_k = \mathbf{H}_k \mathbf{x}_k + \mathbf{v}_k$$

- ❖ \mathbf{x}_k is the current state —> a vector with the position and velocity
- ❖ \mathbf{A}_k is the state transition matrix —> matrix that describe the system, in our case the motion equation
- ❖ \mathbf{H}_k is the measurement matrix —> determined by the current measured position of the mouse
- ❖ \mathbf{z}_k is the actual measurement —> used to compute the “posteriori”

Transition matrix

$$\diamond X = [x, y, v_x, v_y]^t$$

$$\diamond x_{t+1} = x_t + v_x_t \longrightarrow [1, 0, 1, 0]$$

$$\diamond y_{t+1} = y_t + v_y_t$$

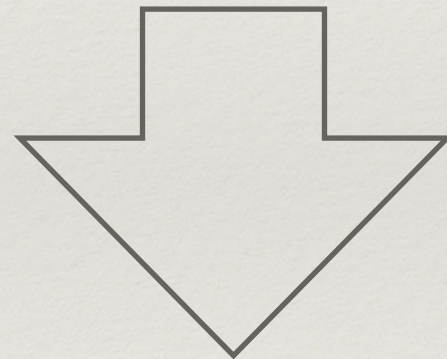
$$\diamond v_x_{t+1} = v_x_t \longrightarrow [0, 0, 1, 0]$$

$$\diamond v_y_{t+1} = v_y_t$$

Exercise

- ❖ Insert acceleration in the transition matrix of the Kalman filter

$$x_t = x_0 + v_x * t$$



$$x_t = x_0 + v_x * t + \frac{1}{2} a_x * t^2$$

Transition matrix

$$\diamond X = [x, y, v_x, v_y, a_x, a_y]^t$$

$$\diamond x_{t+1} = x_t + v_x t + 0.5 a_x t$$

$$\diamond y_{t+1} = y_t + v_y t + 0.5 a_y t$$

$$\diamond v_x_{t+1} = v_x t + a_x t$$

$$\diamond v_y_{t+1} = v_y t + a_y t$$

$$\diamond a_x_{t+1} = a_x t$$

$$\diamond a_y_{t+1} = a_y t$$