

FUNZIONI

3 mar '21

Funzioni esponenziali

ex $y = n \cdot e^n$ CE $n \in \mathbb{R}$

in questi casi
può servire
De L'Hôpital

limiti

$$\lim_{n \rightarrow -\infty} f(n) = [0 \cdot \infty] = \lim_{n \rightarrow -\infty} \frac{n}{e^{-n}} = \left[\frac{\infty}{\infty} \right] \stackrel{H}{=} \lim_{n \rightarrow -\infty} \frac{1}{-e^{-n}} = 0^-$$

$$y = 0 \quad \text{A.O. sx}$$

$$\lim_{n \rightarrow +\infty} f(n) = +\infty$$

asintoti obliqui? NO (...)

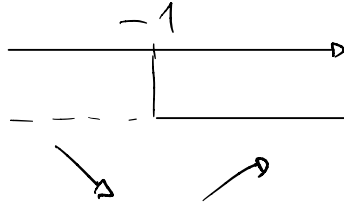
zeri $f(n)=0 \Leftrightarrow n=0 \leadsto f(n) > 0 \Leftrightarrow n > 0$

y'

$$y' = e^n(n+1)$$

$$y' = 0 \leadsto n = -1$$

$$y' > 0$$



$$A\left(-1; -\frac{1}{e}\right)$$

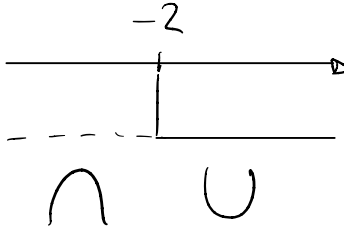
min

y''

$$y'' = e^n(n+2)$$

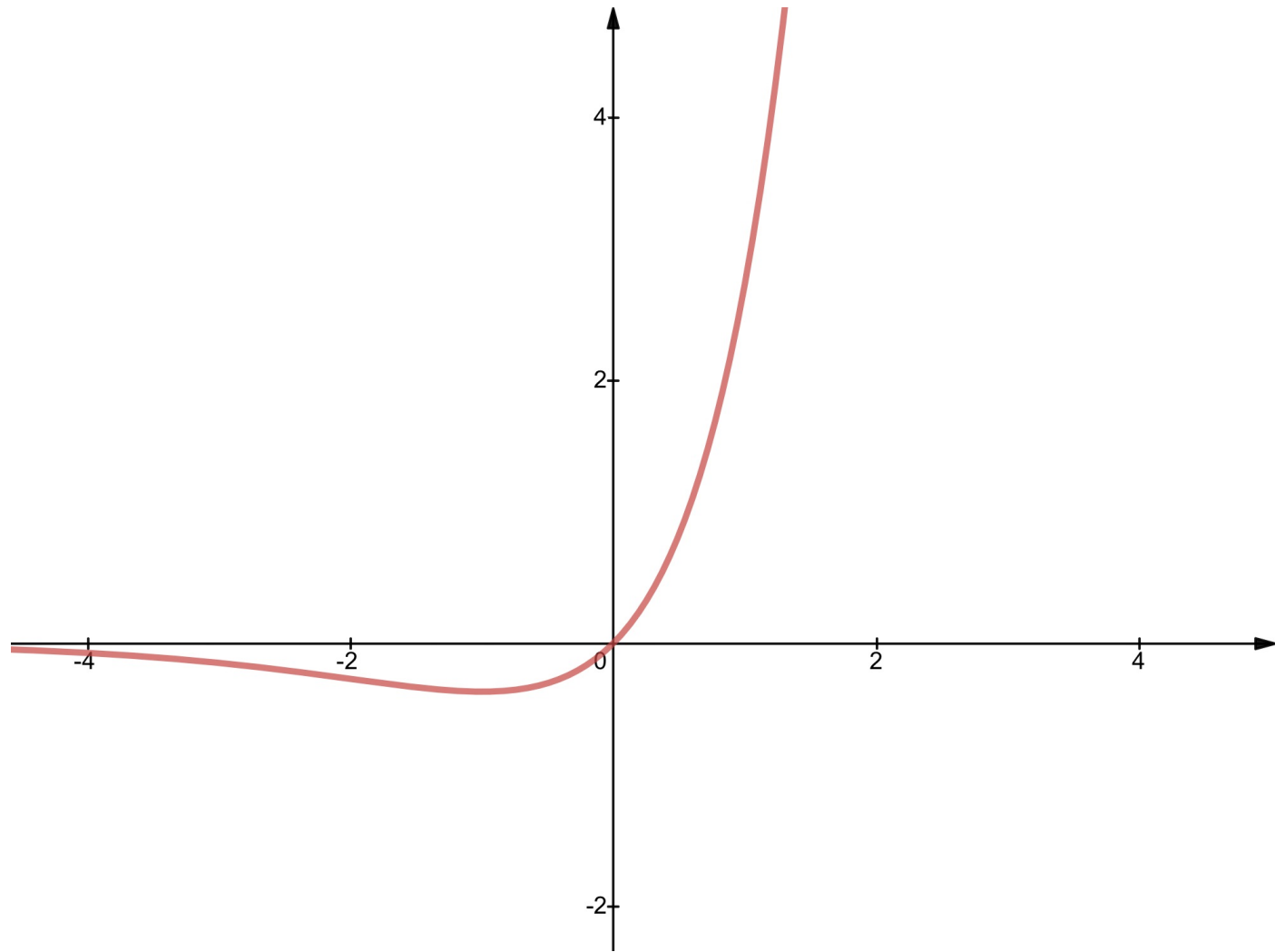
$$y'' = 0 \leadsto n = -2$$

$$y'' > 0$$



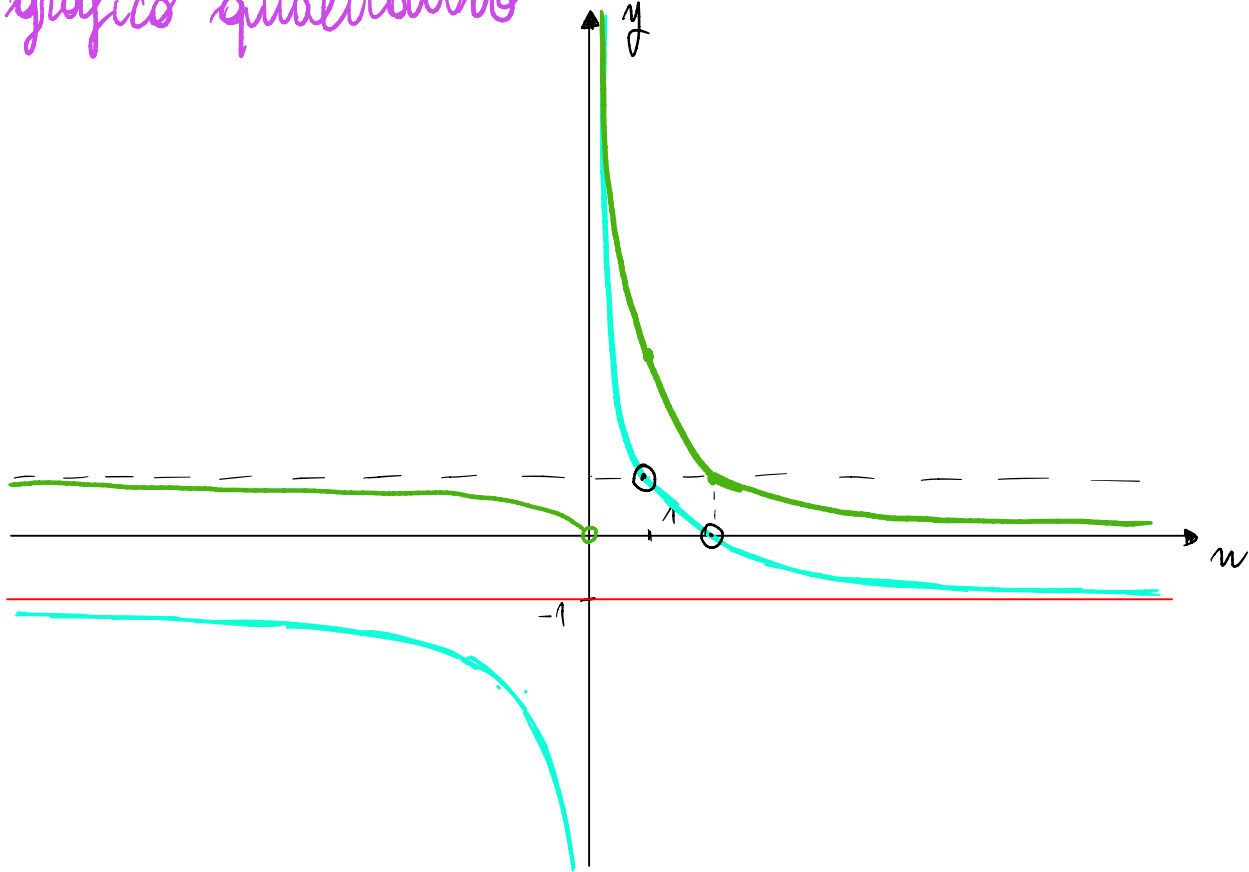
$$F\left(-2; -\frac{2}{e^2}\right)$$

flesso



ex $y = e^{\frac{2-n}{n}}$

grafico qualitativo



studio rigoroso

$$\underline{CE} \quad n \in (-\infty, 0) \cup (0, +\infty)$$

limiti

$$\lim_{n \rightarrow -\infty} f(n) = e^{-1}$$

$$\lim_{n \rightarrow +\infty} f(n) = e^{-1}$$

$$\lim_{n \rightarrow 0^-} f(n) = 0^+$$

$$\lim_{n \rightarrow 0^+} f(n) = +\infty$$

$$\left. \begin{array}{l} y = e^{-1} \quad \text{A.O. } s_x \\ y = e^{-1} \quad \text{A.O. } dx \end{array} \right] \quad y = e^{-1} \quad \text{A.O.}$$

$n = 0$ p.to discontinuità di
seconda specie

$$n = 0 \quad \text{A.V. } dx$$

$$f(n) > 0 \quad \forall n \in \mathbb{C}E$$

$$y' \quad y' = e^{\frac{2-n}{n}} \cdot \frac{-n + n - 2}{n^2} = e^{\frac{2-n}{n}} \cdot \left(\frac{-2}{n^2} \right)$$

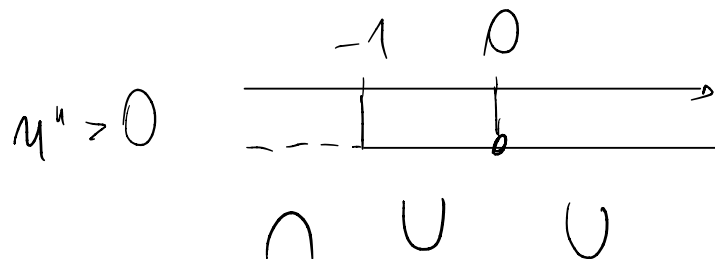
$$y' = 0 \quad \nexists n$$

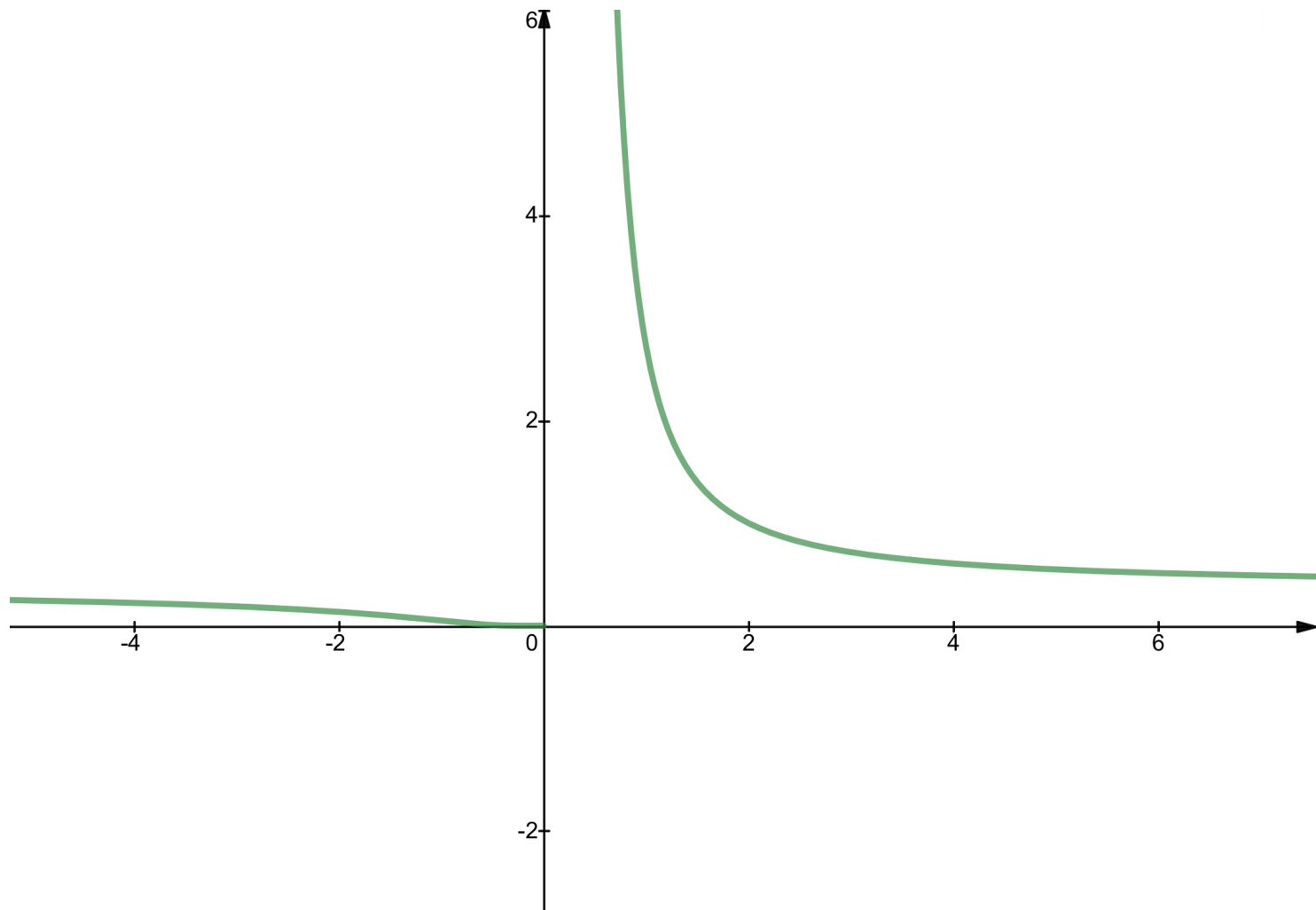
$$y' < 0 \quad \forall n \in \mathbb{C}E$$

$$y'' \quad y'' = 4 e^{\frac{2-n}{n}} \left(\frac{1+n}{n^2} \right)$$

$$y'' = 0 \Leftrightarrow n = -1$$

flesso





Funzioni logaritmiche

ex

$$y = \frac{\ln n}{n}$$

CE

$$n \in (0; +\infty)$$

limiti

$$\lim_{n \rightarrow 0^+} f(n) = \frac{-\infty}{0^+} = -\infty$$

$n = 0$ A.V. dx

$$\lim_{n \rightarrow +\infty} f(n) = \left[\frac{\infty}{\infty} \right]^H = \lim_{n \rightarrow +\infty} \frac{1}{n} = 0^+$$

$y = 0$ A.O. dx

zeri

$$f(n) = 0 \Leftrightarrow n = 1$$

$$f(n) > 0 \Leftrightarrow n \in (1; +\infty)$$

η'

$$\eta' = \frac{1 - \ln n}{n^2}$$

$$\eta' = 0 \Rightarrow n = e$$

$$\eta' > 0 \Rightarrow n \in (0, e)$$

$$A(e, 1/e) \quad \max$$

 η''

$$\eta'' = \frac{-3 + 2 \ln n}{n^3}$$

$$\eta'' = 0 \Rightarrow 2 \ln n = 3$$

$$n = e^{3/2}$$

$$F \left[e^{3/2}; \frac{3}{2e^{3/2}} \right]$$

 $\eta'' > 0$ 