

$$y = \arctan x + x$$

$$C.E. \mathbb{R}$$

$$\lim_{x \rightarrow -\infty} f(x) = -\infty$$

$$m = \lim_{x \rightarrow \infty} \left(\frac{\arctan x}{x} + 1 \right) = \frac{n}{\infty} + 1 = 0 + 1 = 1$$

$$\lim_{x \rightarrow +\infty} f(x) = +\infty$$

$$q = \lim_{x \rightarrow \infty} \arctan x = \begin{cases} -\infty & -\frac{\pi}{2} \\ +\infty & +\frac{\pi}{2} \end{cases}$$

$$\begin{aligned} x \rightarrow -\infty & \quad y = x - \frac{\pi}{2} \\ x \rightarrow +\infty & \quad y = x + \frac{\pi}{2} \end{aligned}$$

PARI o DISPARI

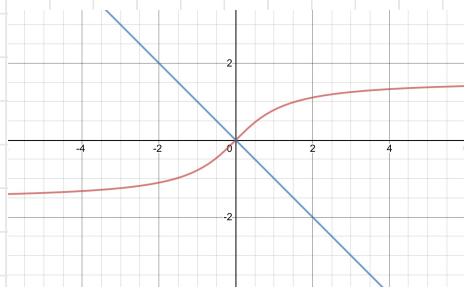
$$f(-x) = \arctan(-x) - x \rightarrow \text{non pari}$$

$$f(-x) = -\arctan x - x \rightarrow \text{disparsi}$$

INTERSEZIONI

$$y = 0 \quad \arctan x = -x$$

$$P(0;0)$$



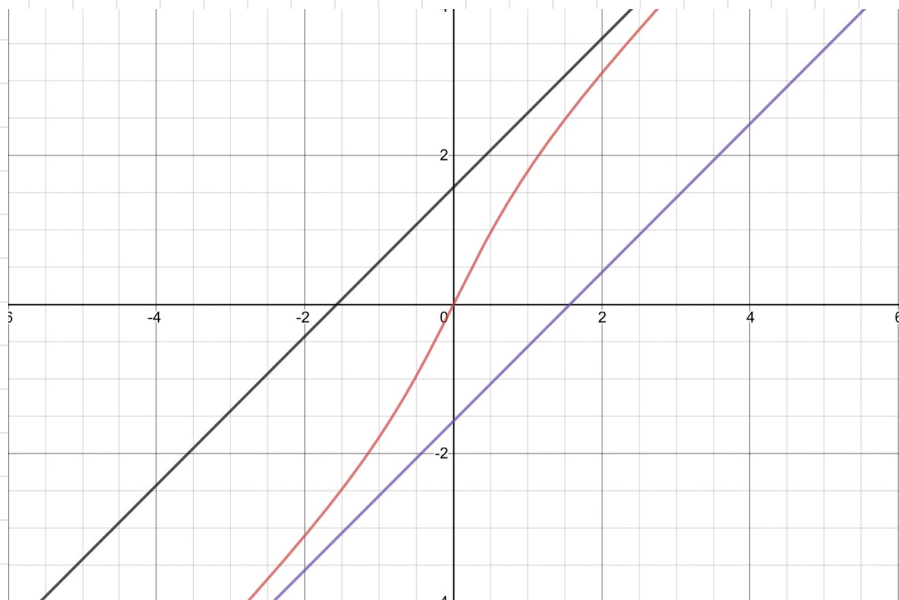
SEGNO

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$$\frac{x^2+2}{x^2+1}$$

$$y' = \frac{1}{x^2+1} + 1 \quad y' = 0 \rightarrow \emptyset \quad y' > 0 \text{ in } \mathbb{R} \text{ sempre crescente}$$

$$y'' = -\frac{2x}{(x^2+1)^2} \quad \begin{aligned} y'' = 0 & \quad x = 0 \quad P(0;0) \\ y'' > 0 & \quad x < 0 \\ y'' < 0 & \quad x > 0 \end{aligned}$$



$$y = \frac{\sin x}{x} \quad \text{C.E. } x \neq 0 \quad \text{PARI o DISPARI} \quad f(-x) = \frac{\sin(-x)}{-x} = \frac{-\sin x}{-x} = \frac{\sin x}{x} \quad \text{è PARI}$$

LIMITI $\lim_{x \rightarrow 0^+} \frac{\sin x}{x} = 1 \rightarrow \text{Discontinuità di 3° specie} \rightarrow \lim_{x \rightarrow x_0^-} = \lim_{x \rightarrow x_0^+} = l \quad f(x_0) \neq l$

$$\lim_{x \rightarrow +\infty} \frac{\sin x}{x} = \frac{-1 \leq \sin x \leq 1}{\infty} = 0 \quad y=0 \text{ è As ORIZZONTALE}$$

INTERSEZIONI

$$y=0 \quad \frac{\sin x}{x}=0 \quad \sin x=0 \rightarrow x=k\pi \quad k \neq 0$$

SEGNO

$$y > 0 \quad \frac{\sin x}{x} \quad (0; +\infty) \quad \sin x > 0$$

DERIVATA

$$y' = \frac{x \cos x - \sin x}{x^2} \quad y'=0 \quad x \cos x - \sin x = 0$$

$$x \cos x = \sin x$$

$$x = \tan x \quad \begin{cases} y=x \\ y=\tan x \end{cases}$$

→ si intersecano INFINITE volte
 ↳ distanziate $\pi \rightarrow \text{periodo} = \pi$

$$\rightarrow \frac{\sin x}{x} \rightarrow \frac{[-1; 1]}{x \rightarrow \infty} \rightarrow y \text{ DIMINUISCE} \rightarrow 0$$

