

Circuit Breakers and LULD efficacy

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Motivation

This work is meant to provide to the literature more evidence in support of the idea that Circuit Breaker regulations were not effective in avoiding huge spikes (as Flash Crashes continue to be a burden for financial markets) and thus, reducing volatility. The first analysis, which has been conducted by fitting a ARFIMA(1,0,0) - eGARCH(1,1) with Student's t-distribution, has given a further confirmation of the results already achieved by the literature (Santoni and Liu, 1993, Subrahmanyam, 1994, Liang, 2017). In particular, the announcement of new 'Circuit Breaker' regulations tends to increase volatility, as traders tend to increase the trading volume, to exit from markets where a Circuit Breaker has been activated and thus, increasing price variability. The novelty, proposed in this work, is the second analysis: the LULD Regulation and the effects that its implementation have brought to the U.S. stock volatility. It has been tested whether the two LULD Phases affected volatility. The estimated ARFIMA(1,0,0) - eGARCH(1,1) model, based on the Normal Distribution, provided a clear indication that only the first Phase affected the volatility, by increasing it.

The following ones are the lines of code, necessary to achieve the results that have been already showed:

```
#DATA
library(tidyquant)

## Loading required package: lubridate

##
## Attaching package: 'lubridate'

## The following objects are masked from 'package:base':
##
##   date, intersect, setdiff, union

## Loading required package: PerformanceAnalytics
## Loading required package: xts
## Loading required package: zoo

##
## Attaching package: 'zoo'

## The following objects are masked from 'package:base':
##
##   as.Date, as.Date.numeric

##
## Attaching package: 'PerformanceAnalytics'

## The following object is masked from 'package:graphics':
##
##   legend

## Loading required package: quantmod
```

```
## Loading required package: TTR

## Registered S3 method overwritten by 'quantmod':
##   method      from
##   as.zoo.data.frame zoo

## == Need to Learn tidyquant? =====
## Business Science offers a 1-hour course - Learning Lab #9: Performance Analysis & Portfolio Optimization
## </> Learn more at: https://university.business-science.io/p/learning-labs-pro </>

# Downloading SP500 using the library tidyquant

SP500= getSymbols("^GSPC", from = '1987-01-01',
                  to = "1998-01-01", auto.assign = FALSE)

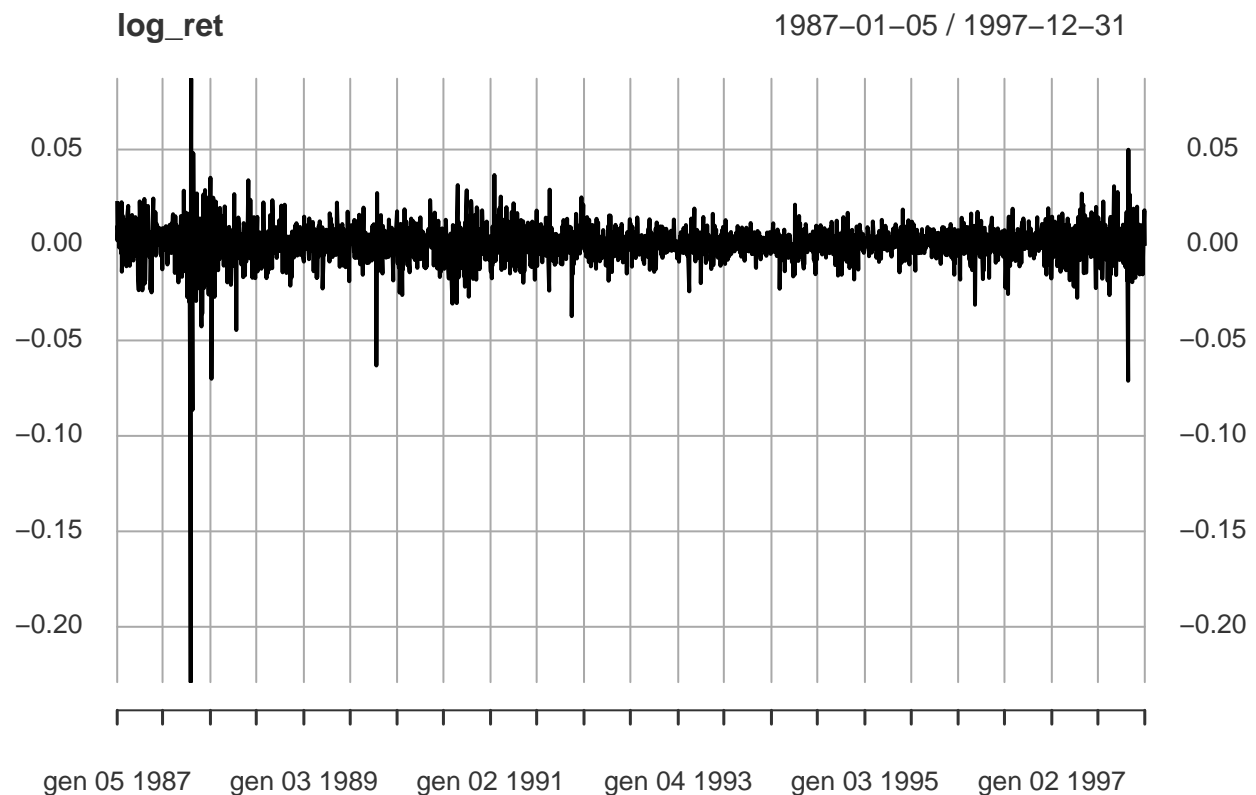
## 'getSymbols' currently uses auto.assign=TRUE by default, but will
## use auto.assign=FALSE in 0.5-0. You will still be able to use
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")
## and getOption("getSymbols.auto.assign") will still be checked for
## alternate defaults.
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.

head(SP500)

##           GSPC.Open GSPC.High GSPC.Low GSPC.Close GSPC.Volume GSPC.Adjusted
## 1987-01-02    242.17    246.45    242.17    246.45     91880000     246.45
## 1987-01-05    246.45    252.57    246.45    252.19    181900000     252.19
## 1987-01-06    252.20    253.99    252.14    252.78    189300000     252.78
## 1987-01-07    252.78    255.72    252.65    255.33    190900000     255.33
## 1987-01-08    255.36    257.28    254.97    257.28    194500000     257.28
## 1987-01-09    257.26    259.20    256.11    258.73    193000000     258.73

logret = diff(log(SP500$GSPC.Adjusted))
log_ret <- logret[-1]

plot(log_ret, length(log_ret))
```



```
#Stationarity test
```

```
library(tseries)
```

```
adf.test(log_ret, alternative = "stationary")
```

```
## Warning in adf.test(log_ret, alternative = "stationary"): p-value smaller than
## printed p-value
```

```
##
```

```
## Augmented Dickey-Fuller Test
```

```
##
```

```
## data: log_ret
```

```
## Dickey-Fuller = -14.056, Lag order = 14, p-value = 0.01
```

```
## alternative hypothesis: stationary
```

```
#ARCH EFFECT
```

```
library(fDMA)
```

```
archtest(as.vector(log_ret))
```

```
##
```

```
## Engle's LM ARCH Test
```

```
##
```

```
## data: as.vector(log_ret)
```

```
## statistic = 34.188, lag = 1, p-value = 5.002e-09
```

```
## alternative hypothesis: ARCH effects of order 1 are present
```

First analysis on Circuit Breakers effects on stock volatility

```
#DUMMY VARIABLES

n=length(log_ret)
#10/22/87

e1=which(row.names(as.matrix(log_ret))=="1987-10-20")
f1=which(row.names(as.matrix(log_ret))=="1987-10-21")
g1=which(row.names(as.matrix(log_ret))=="1987-10-22")
h1=which(row.names(as.matrix(log_ret))=="1987-10-23")
j1=which(row.names(as.matrix(log_ret))=="1987-10-26")

d1=rep(0,n)

d1[e1]=1
d1[f1]=1
d1[g1]=1
d1[h1]=1
d1[j1]=1

#1/14/88

e2=which(row.names(as.matrix(log_ret))=="1988-01-12")
f2=which(row.names(as.matrix(log_ret))=="1988-01-13")
g2=which(row.names(as.matrix(log_ret))=="1988-01-14")
h2=which(row.names(as.matrix(log_ret))=="1988-01-15")
j2=which(row.names(as.matrix(log_ret))=="1988-01-18")

d2=rep(0,n)

d2[e2]=1
d2[f2]=1
d2[g2]=1
d2[h2]=1
d2[j2]=1

#2/4/88

e3=which(row.names(as.matrix(log_ret))=="1988-02-02")
f3=which(row.names(as.matrix(log_ret))=="1988-02-03")
g3=which(row.names(as.matrix(log_ret))=="1988-02-04")
h3=which(row.names(as.matrix(log_ret))=="1988-02-05")
j3=which(row.names(as.matrix(log_ret))=="1988-02-08")

d3=rep(0,n)

d3[e3]=1
d3[f3]=1
d3[g3]=1
d3[h3]=1
d3[j3]=1

#10/20/88
```

```

e4=which(row.names(as.matrix(log_ret))=="1988-10-18")
f4=which(row.names(as.matrix(log_ret))=="1988-10-19")
g4=which(row.names(as.matrix(log_ret))=="1988-10-20")
h4=which(row.names(as.matrix(log_ret))=="1988-10-21")
j4=which(row.names(as.matrix(log_ret))=="1988-10-24")

d4=rep(0,n)

d4[e4]=1
d4[f4]=1
d4[g4]=1
d4[h4]=1
d4[j4]=1
#8/1/90

e5=which(row.names(as.matrix(log_ret))=="1990-07-30")
f5=which(row.names(as.matrix(log_ret))=="1990-07-31")
g5=which(row.names(as.matrix(log_ret))=="1990-08-01")
h5=which(row.names(as.matrix(log_ret))=="1990-08-02")
j5=which(row.names(as.matrix(log_ret))=="1990-08-03")

d5=rep(0,n)

d5[e5]=1
d5[f5]=1
d5[g5]=1
d5[h5]=1
d5[j5]=1
#7/22/96

e6=which(row.names(as.matrix(log_ret))=="1996-07-18")
f6=which(row.names(as.matrix(log_ret))=="1996-07-19")
g6=which(row.names(as.matrix(log_ret))=="1996-07-22")
h6=which(row.names(as.matrix(log_ret))=="1996-07-23")
j6=which(row.names(as.matrix(log_ret))=="1996-07-24")

d6=rep(0,n)

d6[e6]=1
d6[f6]=1
d6[g6]=1
d6[h6]=1
d6[j6]=1
#3/3/97

e7=which(row.names(as.matrix(log_ret))=="1997-02-27")
f7=which(row.names(as.matrix(log_ret))=="1997-02-28")
g7=which(row.names(as.matrix(log_ret))=="1997-03-03")
h7=which(row.names(as.matrix(log_ret))=="1997-03-04")
j7=which(row.names(as.matrix(log_ret))=="1997-03-05")

d7=rep(0,n)

d7[e7]=1

```

```

d7[f7]=1
d7[g7]=1
d7[h7]=1
d7[j7]=1

df_dummies=matrix(c(d1,d2,d3,d4,d5,d6,d7), ncol = 7)

# GARCH MODELS assuming a Normal distribution
#sGARCH
library(rugarch)

## Loading required package: parallel
##
## Attaching package: 'rugarch'
## The following object is masked from 'package:stats':
##
##      sigma
s_garchMod <- ugarchspec(mean.model = list(armaOrder = c(1, 0), include.mean = TRUE
),
variance.model = list(model = 'sGARCH',
                      garchOrder = c(1, 1),
                      external.regressors = df_dummies
),
distribution.model = "norm")

s_garchFit <- ugarchfit(spec=s_garchMod, data=log_ret)
s_garchFit

##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : sGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : norm
##
## Optimal Parameters
## -----
##      Estimate  Std. Error   t value Pr(>|t|)
## mu          0.000681    0.000139   4.885991 0.000001
## ar1          0.034238    0.019737   1.734658 0.082801
## omega        0.000002    0.000001   3.763065 0.000168
## alpha1       0.105806    0.000893 118.426971 0.000000
## beta1        0.875760    0.003518 248.906968 0.000000
## vxreg1       0.000000    0.001222   0.000007 0.999994
## vxreg2       0.000000    0.000042   0.000124 0.999901
## vxreg3       0.000000    0.000009   0.000375 0.999701
## vxreg4       0.000000    0.000003   0.010005 0.992017
## vxreg5       0.000039    0.000030   1.303237 0.192494

```

```

## vxreg6 0.000000 0.000029 0.000000 1.000000
## vxreg7 0.000000 0.000003 0.006297 0.994976
##
## Robust Standard Errors:
##      Estimate Std. Error   t value Pr(>|t|)
## mu      0.000681  0.000253   2.690277 0.007139
## ar1     0.034238  0.028212   1.213570 0.224912
## omega   0.000002  0.000003   0.630088 0.528637
## alpha1  0.105806  0.001017 104.010095 0.000000
## beta1   0.875760  0.011113  78.806466 0.000000
## vxreg1  0.000000  0.005394   0.000002 0.999999
## vxreg2  0.000000  0.000103   0.000051 0.999960
## vxreg3  0.000000  0.000024   0.000136 0.999892
## vxreg4  0.000000  0.000014   0.001962 0.998435
## vxreg5  0.000039  0.000013   2.976127 0.002919
## vxreg6  0.000000  0.000041   0.000000 1.000000
## vxreg7  0.000000  0.000020   0.001093 0.999128
##
## LogLikelihood : 9384.27
##
## Information Criteria
## -----
##
## Akaike      -6.7402
## Bayes      -6.7146
## Shibata    -6.7403
## Hannan-Quinn -6.7310
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              2.645 0.10385
## Lag[2*(p+q)+(p+q)-1] [2] 2.671 0.06628
## Lag[4*(p+q)+(p+q)-1] [5] 5.715 0.05930
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.466 0.2260
## Lag[2*(p+q)+(p+q)-1] [5] 1.541 0.7298
## Lag[4*(p+q)+(p+q)-1] [9] 1.963 0.9093
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##
##      Statistic Shape Scale P-Value
## ARCH Lag[3] 0.000941 0.500 2.000 0.9755
## ARCH Lag[5] 0.148262 1.440 1.667 0.9772
## ARCH Lag[7] 0.530647 2.315 1.543 0.9755
##
## Nyblom stability test
## -----

```

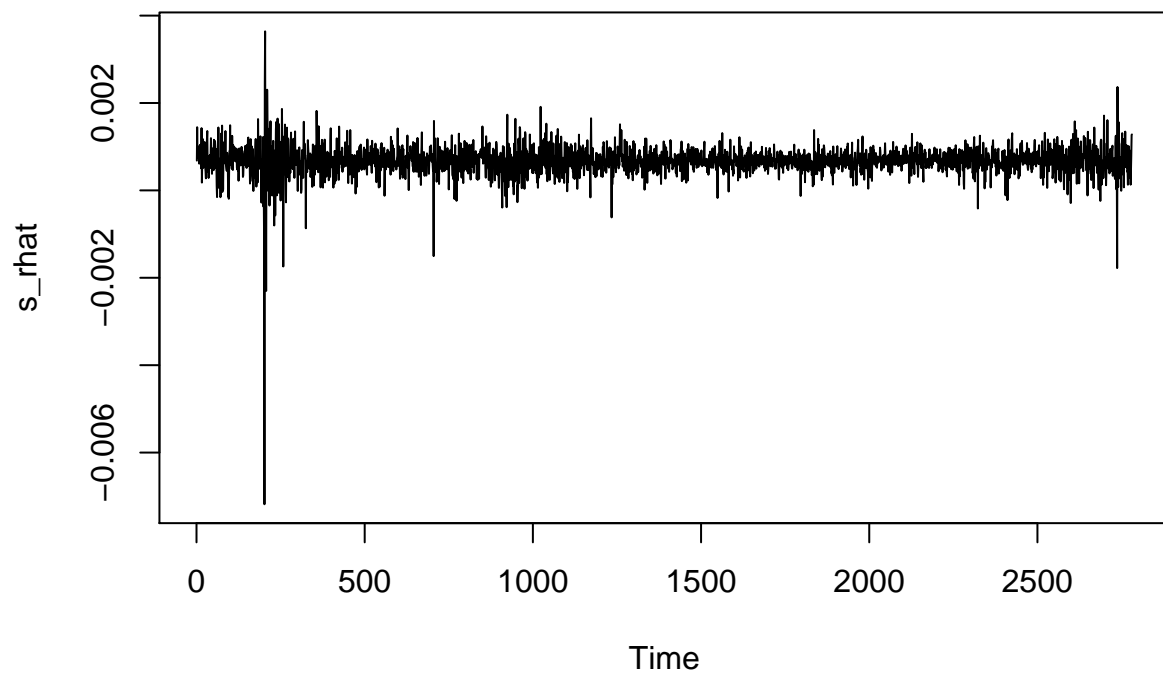
```

## Joint Statistic: 60.104
## Individual Statistics:
## mu      0.193060
## ar1     0.325178
## omega   1.841970
## alpha1  0.424701
## beta1   0.478137
## vxreg1  9.890775
## vxreg2  6.275548
## vxreg3  0.026626
## vxreg4  2.178759
## vxreg5  0.001121
## vxreg6  0.332870
## vxreg7  0.051772
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.69 2.96 3.51
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##              t-value      prob sig
## Sign Bias      0.03479 0.9722517
## Negative Sign Bias 3.39207 0.0007034 ***
## Positive Sign Bias 1.21699 0.2237118
## Joint Effect      19.57646 0.0002077 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      129.4    1.871e-18
## 2    30      143.0    5.042e-17
## 3    40      151.6    3.357e-15
## 4    50      169.9    3.019e-15
##
##
## Elapsed time : 1.314238
## Results review 1
coef(s_garchFit)

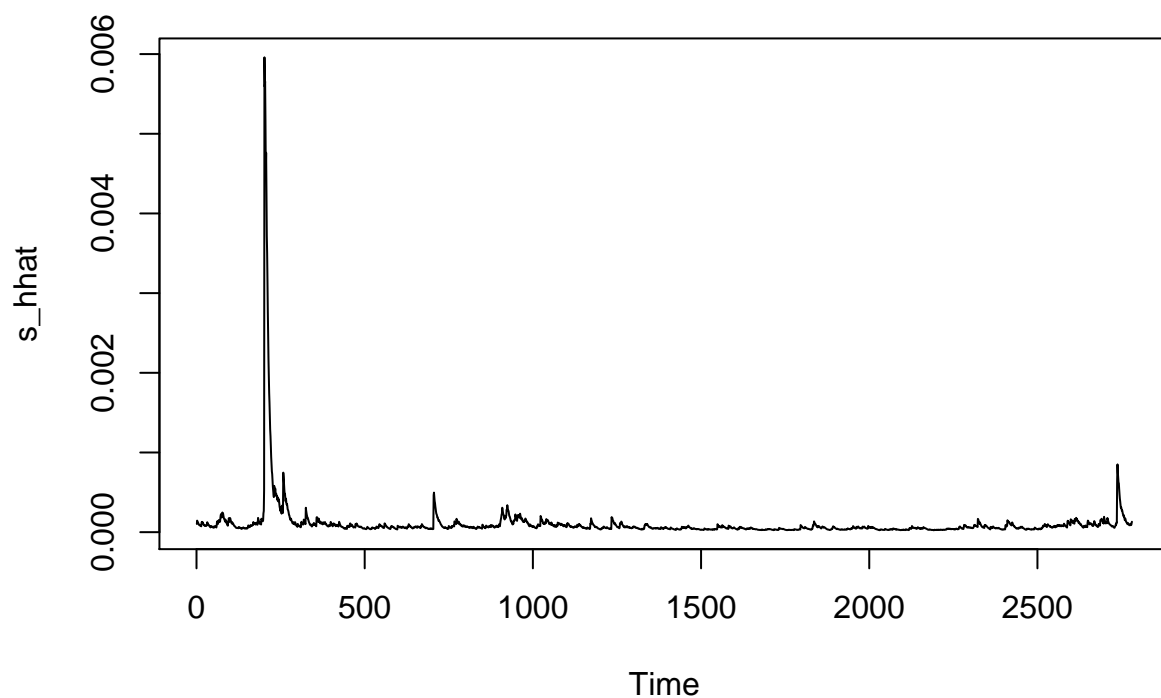
##              mu          ar1          omega          alpha1          beta1          vxreg1
## 6.811716e-04 3.423771e-02 2.129495e-06 1.058060e-01 8.757601e-01 9.032225e-09
##              vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 5.196942e-09 3.310499e-09 2.822589e-08 3.896673e-05 6.353554e-13 2.135644e-08

s_rhat <- s_garchFit@fit$fitted.values
plot.ts(s_rhat)

```

```
s_hhat <- ts(s_garchFit@fit$sigma^2)
plot.ts(s_hhat)
```



```
## Results review 2
```

```
fit.val      <- coef(s_garchFit)
fit.sd       <- diag(vcov(s_garchFit))
true.val = s_garchFit@fit$tval

fit.conf.lb <- fit.val + qnorm(0.025) * fit.sd
fit.conf.ub <- fit.val + qnorm(0.975) * fit.sd
print(fit.val)
```

```
##          mu          ar1          omega          alpha1          beta1          vxreg1
## 6.811716e-04 3.423771e-02 2.129495e-06 1.058060e-01 8.757601e-01 9.032225e-09
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 5.196942e-09 3.310499e-09 2.822589e-08 3.896673e-05 6.353554e-13 2.135644e-08
```

```
print(fit.sd)
```

```
## [1] 1.943604e-08 3.895666e-04 3.202357e-13 7.982141e-07 1.237930e-05
## [6] -1.493874e-06 -1.745845e-09 -7.810591e-11 -7.959431e-12 8.940069e-10
## [11] 8.448609e-10 -1.150296e-11
```

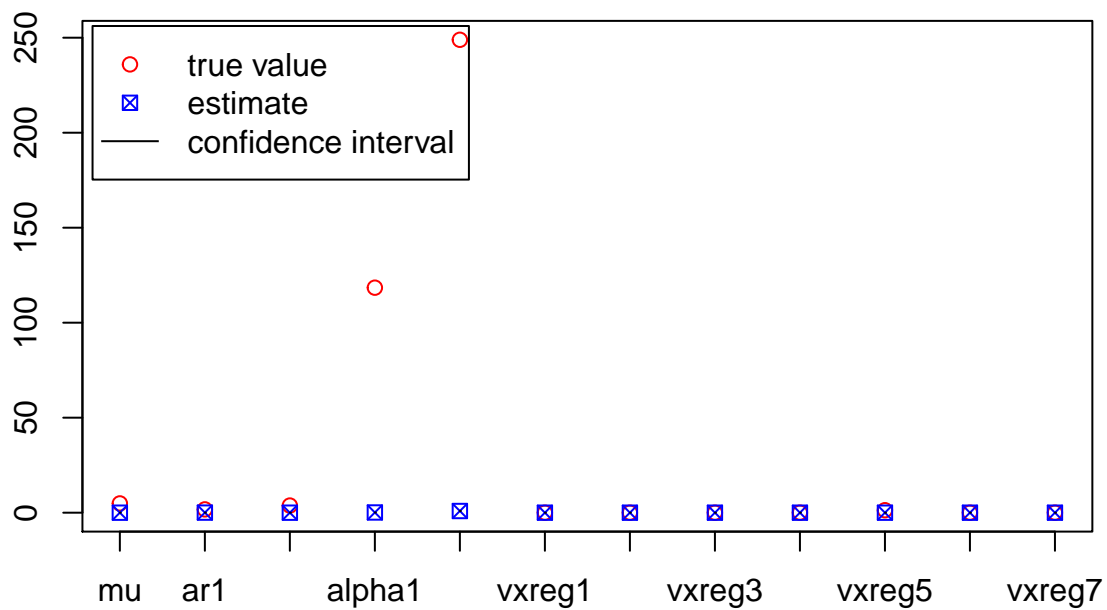
```
print(true.val)
```

```
##          mu          ar1          omega          alpha1          beta1          vxreg1
## 4.885991e+00 1.734658e+00 3.763065e+00 1.184270e+02 2.489070e+02 7.389886e-06
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 1.243784e-04 3.745860e-04 1.000476e-02 1.303237e+00 2.185869e-08 6.296858e-03
```

```

plot(true.val, pch = 1, col = "red",
     ylim = range(c(fit.conf.lb, fit.conf.ub, true.val)),
     xlab = "", ylab = "", axes = FALSE)
box(); axis(1, at = 1:length(fit.val), labels = names(fit.val)); axis(2)
points(coef(s_garchFit), col = "blue", pch = 7)
for (i in 1:length(fit.val)) {
  lines(c(i,i), c(fit.conf.lb[i], fit.conf.ub[i]))
}
legend("topleft", legend = c("true value", "estimate", "confidence interval"),
      col = c("red", "blue", 1), pch = c(1, 7, NA), lty = c(NA, NA, 1), inset = 0.01)

```



```

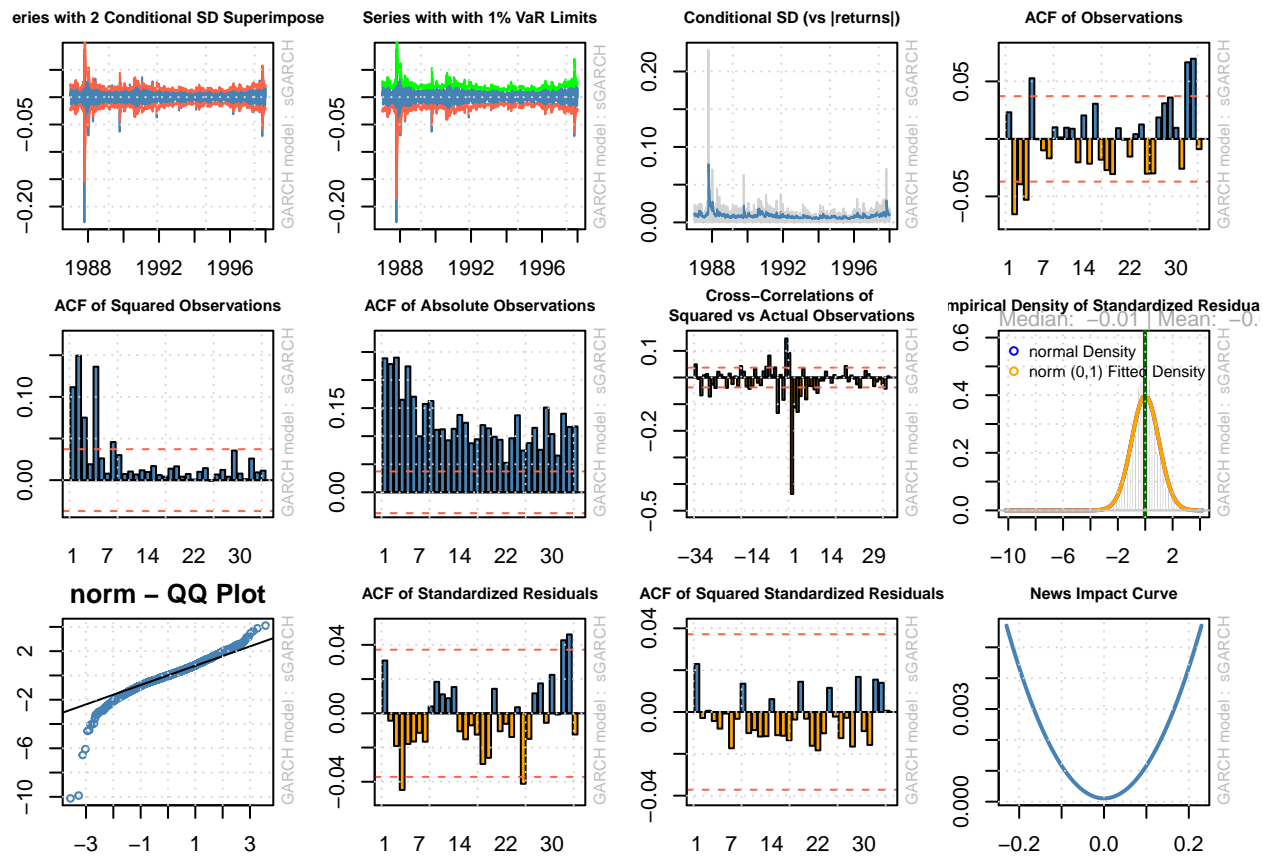
par(mfrow=c(2, 3))
par(mar = c(2, 2, 2, 2))
plot(s_garchFit, which="all")

```

```

##
## please wait...calculating quantiles...

```



```
#gjrGARCH
gjr_garchMod <- ugarchspec(
  variance.model=list(model="gjrGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="norm"
)
gjr_garchFit <- ugarchfit(spec=gjr_garchMod, data=log_ret)
coef(gjr_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1          gamma1
## 4.706382e-04 4.779133e-02 2.713057e-06 3.542937e-02 8.740424e-01 1.232974e-01
##          vxreg1          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6
## 9.200975e-09 5.765240e-09 5.258136e-09 3.479895e-08 9.636875e-08 3.098914e-10
##          vxreg7
## 1.908787e-08
```

```
gjr_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
```

```

## -----
## GARCH Model : gjrGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
##      Estimate Std. Error   t value Pr(>|t|)
## mu      0.000471   0.000106   4.428157 0.000010
## ar1      0.047791   0.019788   2.415197 0.015727
## omega    0.000003   0.000000   7.215401 0.000000
## alpha1   0.035429   0.003209  11.040880 0.000000
## beta1    0.874042   0.004868 179.559601 0.000000
## gamma1   0.123297   0.006114  20.165937 0.000000
## vxreg1   0.000000   0.001054   0.000009 0.999993
## vxreg2   0.000000   0.000148   0.000039 0.999969
## vxreg3   0.000000   0.000002   0.003019 0.997591
## vxreg4   0.000000   0.000001   0.062847 0.949888
## vxreg5   0.000000   0.000008   0.012061 0.990377
## vxreg6   0.000000   0.000026   0.000012 0.999991
## vxreg7   0.000000   0.000011   0.001713 0.998634
##
## Robust Standard Errors:
##      Estimate Std. Error   t value Pr(>|t|)
## mu      0.000471   0.000344   1.367242 0.171550
## ar1      0.047791   0.025801   1.852309 0.063981
## omega    0.000003   0.000002   1.397693 0.162205
## alpha1   0.035429   0.053475   0.662544 0.507623
## beta1    0.874042   0.014364  60.848264 0.000000
## gamma1   0.123297   0.091052   1.354136 0.175693
## vxreg1   0.000000   0.003746   0.000002 0.999998
## vxreg2   0.000000   0.000451   0.000013 0.999990
## vxreg3   0.000000   0.000004   0.001180 0.999059
## vxreg4   0.000000   0.000001   0.026586 0.978790
## vxreg5   0.000000   0.000015   0.006497 0.994816
## vxreg6   0.000000   0.000156   0.000002 0.999998
## vxreg7   0.000000   0.000020   0.000971 0.999225
##
## LogLikelihood : 9404.956
##
## Information Criteria
## -----
##
## Akaike      -6.7544
## Bayes       -6.7267
## Shibata     -6.7544
## Hannan-Quinn -6.7444
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.094 0.2957
## Lag[2*(p+q)+(p+q)-1] [2] 1.100 0.6789
## Lag[4*(p+q)+(p+q)-1] [5] 3.681 0.2808

```

```

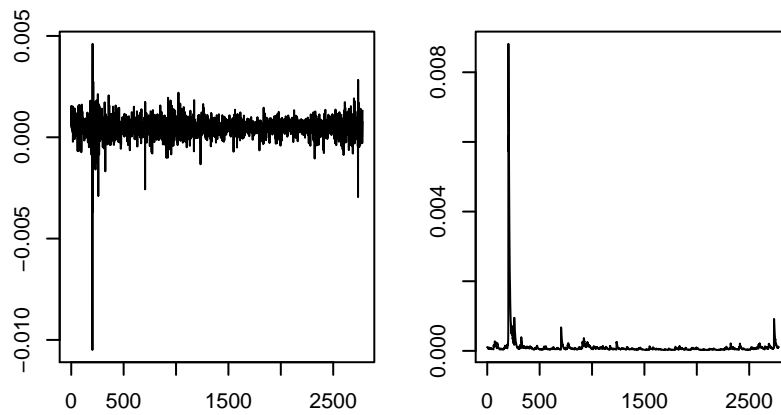
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.08143  0.7754
## Lag[2*(p+q)+(p+q)-1][5]  0.34966  0.9782
## Lag[4*(p+q)+(p+q)-1][9]  0.89798  0.9901
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##
##      Statistic Shape Scale P-Value
## ARCH Lag[3]    0.05316 0.500 2.000  0.8177
## ARCH Lag[5]    0.20537 1.440 1.667  0.9642
## ARCH Lag[7]    0.65759 2.315 1.543  0.9620
##
## Nyblom stability test
## -----
## Joint Statistic:  30.6529
## Individual Statistics:
## mu      0.50349
## ar1      0.33048
## omega    0.35684
## alpha1   0.68378
## beta1    0.73125
## gamma1   0.43983
## vxreg1   11.72363
## vxreg2    6.75182
## vxreg3    0.32478
## vxreg4    1.02959
## vxreg5    0.97464
## vxreg6    0.34190
## vxreg7    0.09879
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.89 3.15 3.69
## Individual Statistic:  0.35 0.47 0.75
##
## Sign Bias Test
## -----
##
##      t-value    prob sig
## Sign Bias      0.2058 0.83695
## Negative Sign Bias  2.0601 0.03948  **
## Positive Sign Bias  1.1551 0.24815
## Joint Effect      9.9600 0.01891  **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##      group statistic p-value(g-1)
## 1      20      116.2      5.613e-16
## 2      30      121.8      2.463e-13

```

```
## 3    40    144.0    5.880e-14
## 4    50    146.1    1.381e-11
##
##
## Elapsed time : 1.509532

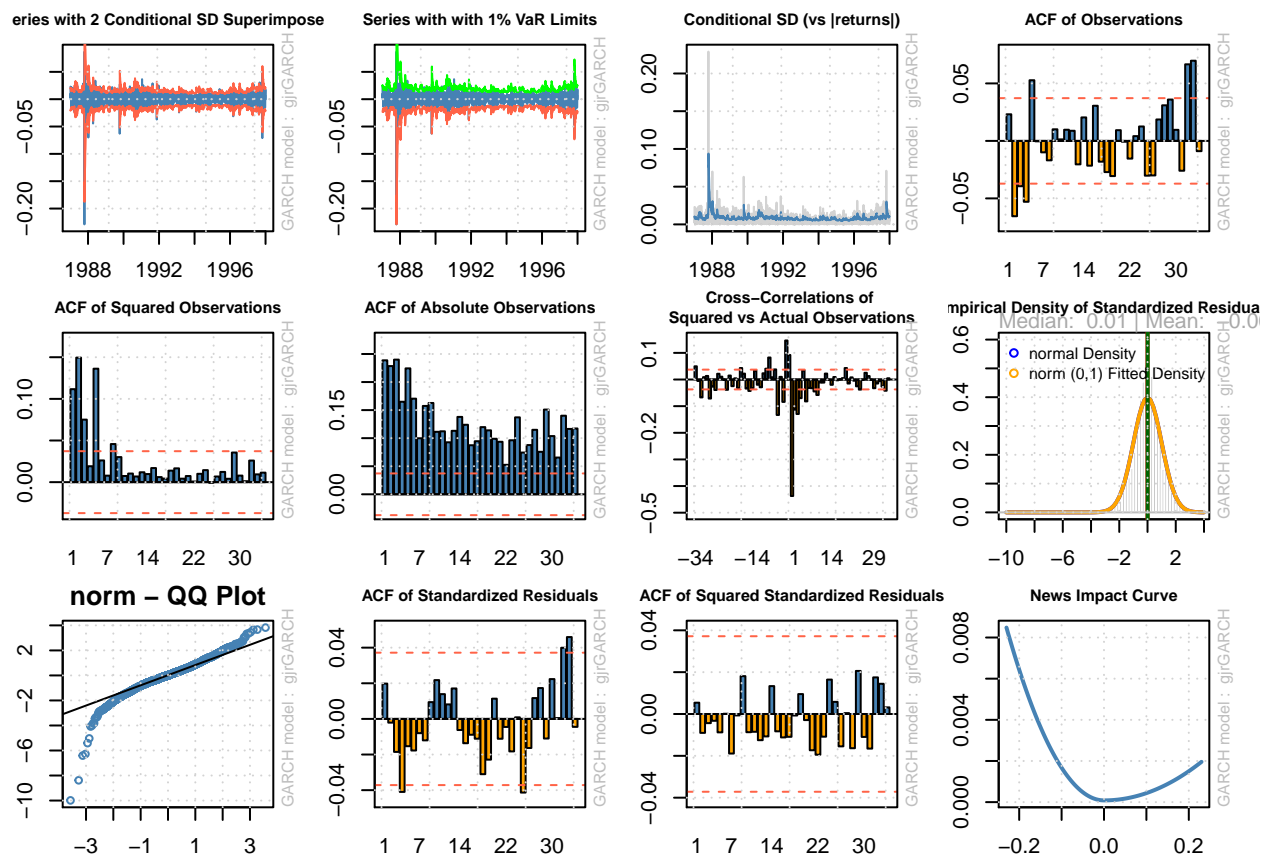
gjr_rhat <- gjr_garchFit@fit$fitted.values
plot.ts(gjr_rhat)
gjr_hhat <- ts(gjr_garchFit@fit$sigma^2)
plot.ts(gjr_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(gjr_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



```
#eGARCH
e_garchMod <- ugarchspec(
  variance.model=list(model="eGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="norm"
)
e_garchFit <- ugarchfit(spec=e_garchMod, data=log_ret)
coef(e_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 0.0003827276 0.0384915691 -0.2046065717 -0.0897420253 0.9773735780
##          gamma1          vxreg1          vxreg2          vxreg3          vxreg4
## 0.1612022863 -0.1784463983 -0.1148208973 -0.0945015117 0.0574193815
##          vxreg5          vxreg6          vxreg7
## 0.1548938323 -0.2241254159 -0.0352817475
```

```
e_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
```



```

## -----
## GARCH Model : eGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
##      Estimate Std. Error t value Pr(>|t|)
## mu      0.000383  0.000103  3.73113 0.000191
## ar1      0.038492  0.018484  2.08240 0.037306
## omega    -0.204607  0.011862 -17.24859 0.000000
## alpha1   -0.089742  0.012712  -7.05985 0.000000
## beta1     0.977374  0.001316 742.70921 0.000000
## gamma1    0.161202  0.018927  8.51700 0.000000
## vxreg1   -0.178446  0.111477  -1.60074 0.109434
## vxreg2   -0.114821  0.118882  -0.96584 0.334123
## vxreg3   -0.094502  0.130444  -0.72446 0.468782
## vxreg4    0.057419  0.122627  0.46824 0.639610
## vxreg5    0.154894  0.128575  1.20470 0.228319
## vxreg6   -0.224125  0.122193  -1.83420 0.066625
## vxreg7   -0.035282  0.129604  -0.27223 0.785448
##
## Robust Standard Errors:
##      Estimate Std. Error t value Pr(>|t|)
## mu      0.000383  0.000079  4.85477 0.000001
## ar1      0.038492  0.017878  2.15306 0.031314
## omega    -0.204607  0.013442 -15.22126 0.000000
## alpha1   -0.089742  0.033457  -2.68229 0.007312
## beta1     0.977374  0.001351 723.53874 0.000000
## gamma1    0.161202  0.049277  3.27138 0.001070
## vxreg1   -0.178446  0.098822  -1.80573 0.070960
## vxreg2   -0.114821  0.066012  -1.73939 0.081967
## vxreg3   -0.094502  0.062659  -1.50819 0.131506
## vxreg4    0.057419  0.067522  0.85038 0.395112
## vxreg5    0.154894  0.067504  2.29459 0.021756
## vxreg6   -0.224125  0.084755  -2.64438 0.008184
## vxreg7   -0.035282  0.064352  -0.54827 0.583509
##
## LogLikelihood : 9419.462
##
## Information Criteria
## -----
##
## Akaike      -6.7648
## Bayes       -6.7371
## Shibata     -6.7648
## Hannan-Quinn -6.7548
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.771  0.1832
## Lag[2*(p+q)+(p+q)-1] [2]  1.822  0.2805
## Lag[4*(p+q)+(p+q)-1] [5]  4.581  0.1472

```

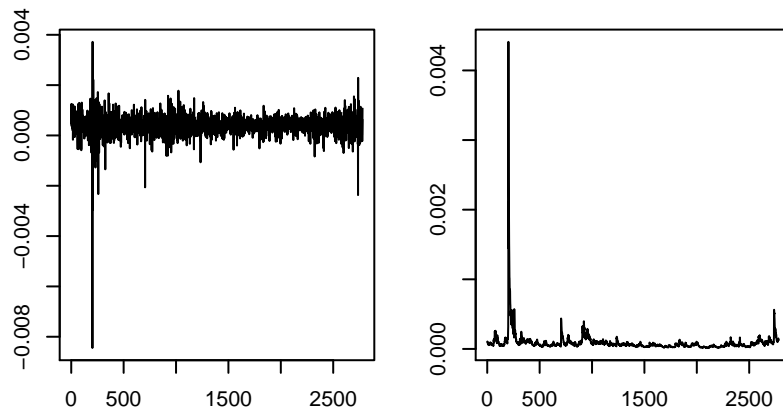
```

## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##               statistic p-value
## Lag[1]                0.8656 0.3522
## Lag[2*(p+q)+(p+q)-1][5] 0.9060 0.8806
## Lag[4*(p+q)+(p+q)-1][9] 1.3730 0.9653
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3] 0.01591 0.500 2.000 0.8996
## ARCH Lag[5] 0.08464 1.440 1.667 0.9896
## ARCH Lag[7] 0.42214 2.315 1.543 0.9849
##
## Nyblom stability test
## -----
## Joint Statistic: 1.3795
## Individual Statistics:
## mu      0.4839837
## ar1     0.2798858
## omega   0.6104227
## alpha1  0.0933716
## beta1   0.5983516
## gamma1  0.0978513
## vxreg1  0.0012195
## vxreg2  0.0003748
## vxreg3  0.0013128
## vxreg4  0.0009336
## vxreg5  0.0005639
## vxreg6  0.0016619
## vxreg7  0.0005274
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.89 3.15 3.69
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      0.3204 0.748676
## Negative Sign Bias 3.1572 0.001610 ***
## Positive Sign Bias 1.0562 0.290980
## Joint Effect    14.5938 0.002199 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      117.1    3.806e-16
## 2    30      124.1    9.871e-14

```

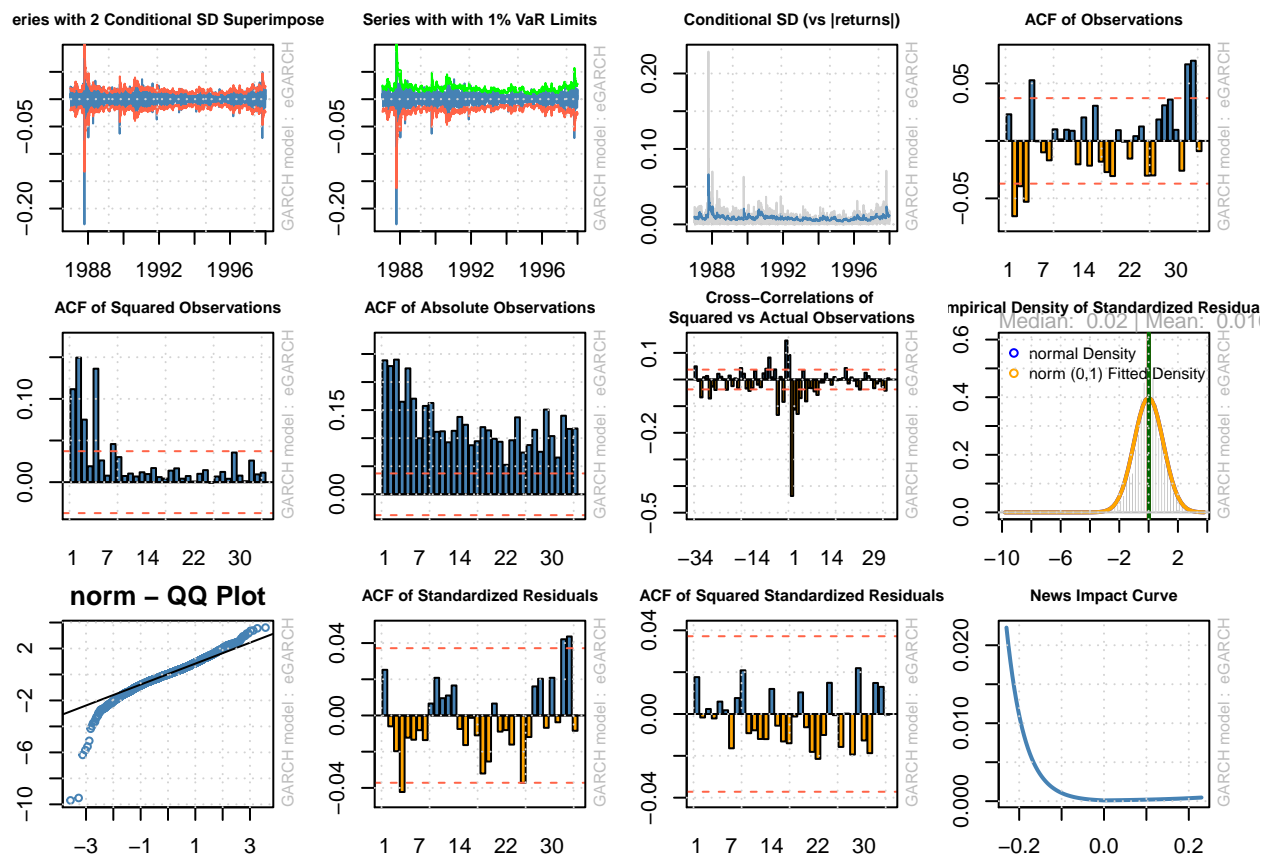
```
## 3    40    136.2    1.089e-12
## 4    50    159.4    1.300e-13
##
##
## Elapsed time : 3.489493
e_rhat <- e_garchFit@fit$fitted.values
plot.ts(e_rhat)
e_hhat <- ts(e_garchFit@fit$sigma^2)
plot.ts(e_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(e_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



```
# apARCH
apARCHMod <- ugarchspec(variance.model=list(model="apARCH",
                                             garchOrder=c(1,1),
                                             external.regressors = df_dummies ),
                        mean.model=list(armaOrder=c(1,0)),
                        distribution.model="norm")
apARCHFit <- ugarchfit(spec=apARCHMod, data= log_ret)
coef(apARCHFit)
```

```
##          mu          ar1          omega          alpha1          beta1          gamma1
## 4.659356e-04 4.892219e-02 2.409258e-07 7.505760e-02 8.567407e-01 2.905291e-01
##          delta          vxreg1          vxreg2          vxreg3          vxreg4          vxreg5
## 2.522832e+00 9.994818e-09 9.930641e-09 9.872127e-09 1.036614e-08 1.067708e-08
##          vxreg6          vxreg7
## 9.699512e-09 1.032048e-08
```

```
apARCHFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : apARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
```

```

## Distribution : norm
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000466    0.000150   3.112241 0.001857
## ar1     0.048922    0.021431   2.282731 0.022446
## omega   0.000000    0.000000   1.192373 0.233115
## alpha1  0.075058    0.002070  36.253493 0.000000
## beta1   0.856741    0.024203  35.398467 0.000000
## gamma1  0.290529    0.053116   5.469753 0.000000
## delta   2.522832    0.065925  38.268433 0.000000
## vxreg1  0.000000    0.000310   0.000032 0.999974
## vxreg2  0.000000    0.000000   0.552629 0.580517
## vxreg3  0.000000    0.000000   0.038988 0.968900
## vxreg4  0.000000    0.000000   0.040922 0.967358
## vxreg5  0.000000    0.000000   0.042247 0.966302
## vxreg6  0.000000    0.000000   0.038247 0.969490
## vxreg7  0.000000    0.000000   0.040818 0.967441
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000466    0.000264   1.766075 0.077383
## ar1     0.048922    0.024110   2.029088 0.042449
## omega   0.000000    0.000005   0.044990 0.964116
## alpha1  0.075058    0.032539   2.306677 0.021073
## beta1   0.856741    0.391588   2.187864 0.028680
## gamma1  0.290529    0.587117   0.494840 0.620713
## delta   2.522832    0.932690   2.704900 0.006833
## vxreg1  0.000000    0.001000   0.000010 0.999992
## vxreg2  0.000000    0.000000   0.048696 0.961162
## vxreg3  0.000000    0.000004   0.002383 0.998098
## vxreg4  0.000000    0.000004   0.002499 0.998006
## vxreg5  0.000000    0.000004   0.002591 0.997933
## vxreg6  0.000000    0.000004   0.002332 0.998139
## vxreg7  0.000000    0.000004   0.002503 0.998003
##
## LogLikelihood : 9393.595
##
## Information Criteria
## -----
##
## Akaike      -6.7455
## Bayes      -6.7156
## Shibata     -6.7455
## Hannan-Quinn -6.7347
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.120  0.2900
## Lag[2*(p+q)+(p+q)-1] [2]  1.128  0.6613
## Lag[4*(p+q)+(p+q)-1] [5]  3.829  0.2540
## d.o.f=1

```

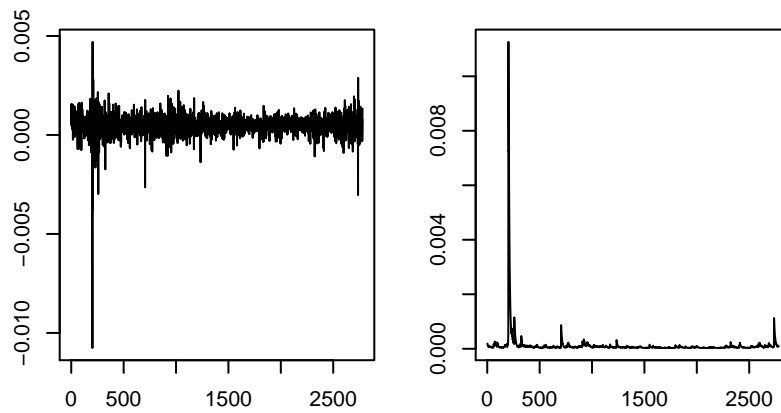
```

## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##                statistic p-value
## Lag[1]                0.009334 0.9230
## Lag[2*(p+q)+(p+q)-1][5] 0.365290 0.9763
## Lag[4*(p+q)+(p+q)-1][9] 0.927661 0.9891
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##
##      Statistic Shape Scale P-Value
## ARCH Lag[3]    0.1090 0.500 2.000 0.7413
## ARCH Lag[5]    0.2857 1.440 1.667 0.9440
## ARCH Lag[7]    0.7464 2.315 1.543 0.9510
##
## Nyblom stability test
## -----
## Joint Statistic:  NaN
## Individual Statistics:
## mu      0.4113
## ar1      0.3405
## omega 29.8360
## alpha1  0.5634
## beta1   0.8381
## gamma1  0.1392
## delta   0.9494
## vxreg1 12.7770
## vxreg2   NaN
## vxreg3   NaN
## vxreg4   NaN
## vxreg5   NaN
## vxreg6   NaN
## vxreg7   NaN
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      3.08 3.34 3.9
## Individual Statistic:  0.35 0.47 0.75
##
## Sign Bias Test
## -----
##
##                t-value    prob sig
## Sign Bias      0.3194 0.74948
## Negative Sign Bias 1.8156 0.06954 *
## Positive Sign Bias 1.1725 0.24108
## Joint Effect    9.2255 0.02644 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##      group statistic p-value(g-1)
## 1      20      114.2      1.328e-15
## 2      30      121.0      3.281e-13

```

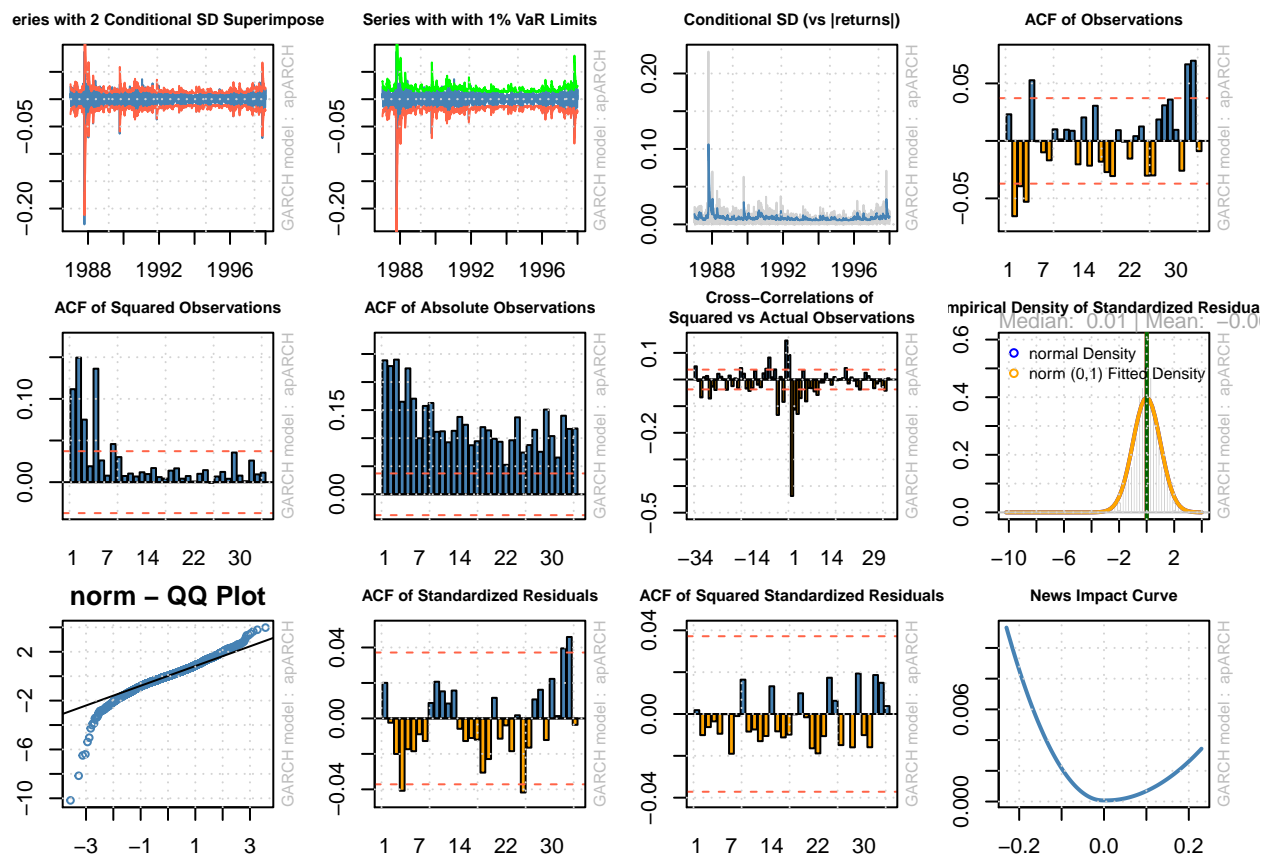
```
## 3    40    145.5    3.431e-14
## 4    50    153.9    9.159e-13
##
##
## Elapsed time : 1.979514
apARCH_rhat <- apARCHFit@fit$fitted.values
plot.ts(apARCH_rhat)
apARCH_hhat <- ts(apARCHFit@fit$sigma^2)
plot.ts(apARCH_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(apARCHFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



```
# iGARCH
i_garchMod <- ugarchspec(variance.model=list(model="iGARCH",
                                             garchOrder=c(1,1),
                                             external.regressors = df_dummies ),
                        mean.model=list(armaOrder=c(1,0)),
                        distribution.model="norm")
i_garchFit <- ugarchfit(spec=i_garchMod, data= log_ret)
coef(i_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1          vxreg1
## 6.718728e-04 3.460114e-02 1.304707e-06 1.107062e-01 8.892938e-01 9.129943e-09
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 5.410431e-09 3.307950e-09 1.726805e-08 1.948471e-07 4.802796e-12 1.505417e-08
```

```
i_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : iGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : norm
##
```



```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000672    0.000166   4.045965 0.000052
## ar1     0.034601    0.022170   1.560742 0.118585
## omega   0.000001    0.000000   2.960788 0.003069
## alpha1  0.110706    0.001635  67.707776 0.000000
## beta1   0.889294         NA         NA         NA
## vxreg1  0.000000    0.000932   0.000010 0.999992
## vxreg2  0.000000    0.000013   0.000429 0.999657
## vxreg3  0.000000    0.000002   0.001761 0.998595
## vxreg4  0.000000    0.000013   0.001370 0.998907
## vxreg5  0.000000    0.000005   0.036663 0.970754
## vxreg6  0.000000    0.000031   0.000000 1.000000
## vxreg7  0.000000    0.000010   0.001449 0.998844
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000672    0.000396   1.698429 0.089427
## ar1     0.034601    0.059119   0.585283 0.558358
## omega   0.000001    0.000003   0.447497 0.654516
## alpha1  0.110706    0.010167  10.889161 0.000000
## beta1   0.889294         NA         NA         NA
## vxreg1  0.000000    0.001276   0.000007 0.999994
## vxreg2  0.000000    0.000017   0.000324 0.999741
## vxreg3  0.000000    0.000007   0.000497 0.999603
## vxreg4  0.000000    0.000032   0.000547 0.999564
## vxreg5  0.000000    0.000013   0.015228 0.987850
## vxreg6  0.000000    0.000036   0.000000 1.000000
## vxreg7  0.000000    0.000050   0.000303 0.999758
##
## LogLikelihood : 9378.587
##
## Information Criteria
## -----
##
## Akaike      -6.7368
## Bayes       -6.7134
## Shibata     -6.7369
## Hannan-Quinn -6.7284
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##                                statistic p-value
## Lag[1]                                3.294 0.06953
## Lag[2*(p+q)+(p+q)-1] [2]          3.306 0.01895
## Lag[4*(p+q)+(p+q)-1] [5]          6.372 0.03374
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##                                statistic p-value
## Lag[1]                                1.261 0.2615

```

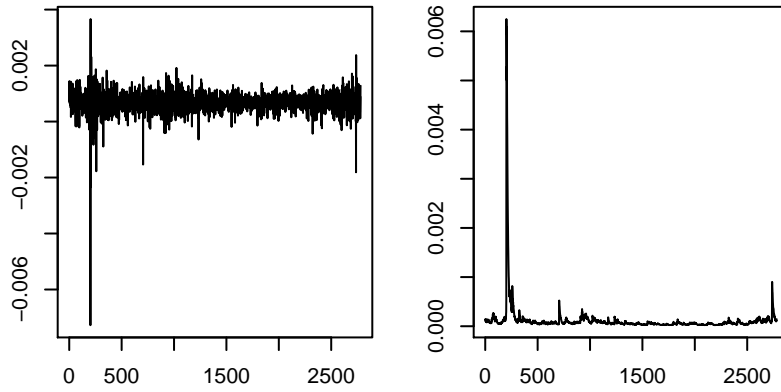
```

## Lag[2*(p+q)+(p+q)-1][5]      1.399  0.7647
## Lag[4*(p+q)+(p+q)-1][9]      1.908  0.9156
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]  0.008871 0.500 2.000  0.9250
## ARCH Lag[5]  0.253244 1.440 1.667  0.9524
## ARCH Lag[7]  0.722511 2.315 1.543  0.9540
##
## Nyblom stability test
## -----
## Joint Statistic:  44.3559
## Individual Statistics:
## mu      0.1944
## ar1     0.3350
## omega   7.7849
## alpha1  0.1040
## vxreg1 14.4927
## vxreg2 10.6094
## vxreg3  3.3986
## vxreg4  2.9878
## vxreg5  0.5660
## vxreg6  0.5595
## vxreg7  0.0348
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.49 2.75 3.27
## Individual Statistic:  0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      0.09377 0.9253025
## Negative Sign Bias  3.19389 0.0014194 ***
## Positive Sign Bias  1.35132 0.1767030
## Joint Effect      19.01009 0.0002721 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      138.8    3.107e-20
## 2    30      150.7    2.190e-18
## 3    40      168.4    5.233e-18
## 4    50      182.1    3.385e-17
##
##
## Elapsed time : 0.7031522

i_rhat <- i_garchFit@fit$fitted.values
plot.ts(i_rhat)
i_hhat <- ts(i_garchFit@fit$sigma^2)

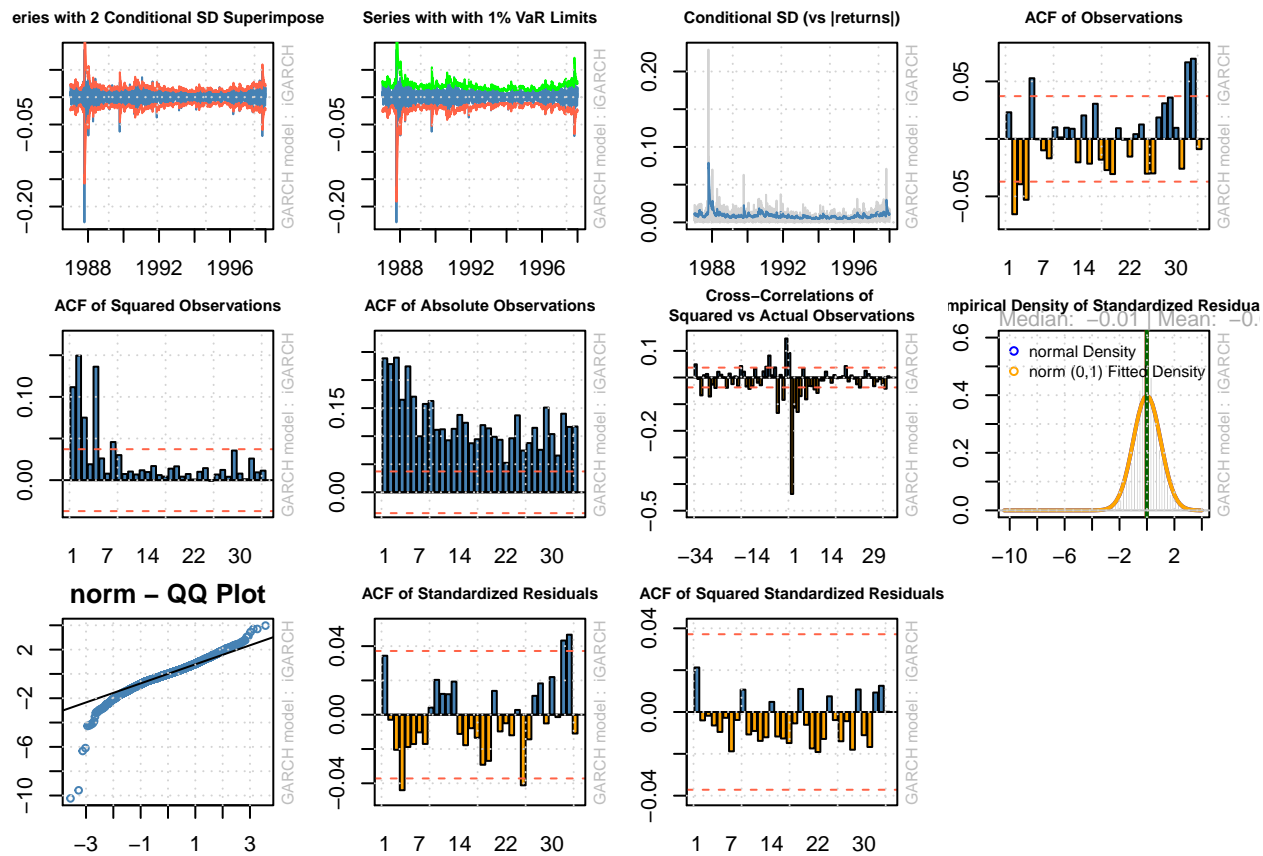
```

```
plot.ts(i_hhat)
par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(i_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
## Warning in FUN(x):
## plot-->: iGARCH and fiGARCH newsimpact not available
```



GARCH MODELS assuming a Student's t-distribution

Student's t-sGARCH ----> tsGARCH

```
library(rugarch)
```

```
ts_garchMod <- ugarchspec(mean.model = list(armaOrder = c(1, 0), include.mean = TRUE
),
variance.model = list(model = 'sGARCH',
                      garchOrder = c(1, 1),
                      external.regressors = df_dummies
),
distribution.model = "std")
```

```
ts_garchFit <- ugarchfit(spec=ts_garchMod, data=log_ret)
ts_garchFit
```

```
##
## *-----*
## *           GARCH Model Fit           *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : sGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : std
##
```

```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000681    0.000125   5.440424  0.00000
## ar1     0.016918    0.018124   0.933480  0.35057
## omega   0.000001    0.000001   0.716074  0.47395
## alpha1  0.046134    0.002604  17.719872  0.00000
## beta1   0.944010    0.010702  88.210378  0.00000
## vxreg1  0.000000    0.000745   0.000013  0.99999
## vxreg2  0.000000    0.000092   0.000108  0.99991
## vxreg3  0.000000    0.000092   0.000107  0.99991
## vxreg4  0.000000    0.000005   0.001912  0.99848
## vxreg5  0.000000    0.000005   0.002245  0.99821
## vxreg6  0.000000    0.000016   0.000610  0.99951
## vxreg7  0.000000    0.000002   0.004791  0.99618
## shape   4.874184    0.552438   8.823038  0.00000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000681    0.000281   2.422255  0.015425
## ar1     0.016918    0.025356   0.667226  0.504628
## omega   0.000001    0.000011   0.072052  0.942560
## alpha1  0.046134    0.028186   1.636776  0.101677
## beta1   0.944010    0.114764   8.225629  0.000000
## vxreg1  0.000000    0.008467   0.000001  0.999999
## vxreg2  0.000000    0.001194   0.000008  0.999993
## vxreg3  0.000000    0.000349   0.000028  0.999977
## vxreg4  0.000000    0.000111   0.000090  0.999928
## vxreg5  0.000000    0.000072   0.000143  0.999886
## vxreg6  0.000000    0.000160   0.000062  0.999950
## vxreg7  0.000000    0.000054   0.000188  0.999850
## shape   4.874184    1.764929   2.761688  0.005750
##
## LogLikelihood : 9561.356
##
## Information Criteria
## -----
##
## Akaike          -6.8669
## Bayes           -6.8391
## Shibata         -6.8669
## Hannan-Quinn   -6.8568
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic   p-value
## Lag[1]              5.889 1.524e-02
## Lag[2*(p+q)+(p+q)-1] [2]    5.895 5.124e-05
## Lag[4*(p+q)+(p+q)-1] [5]    8.789 3.606e-03
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----

```

```

##                                statistic  p-value
## Lag[1]                        9.663 0.001880
## Lag[2*(p+q)+(p+q)-1] [5]    10.695 0.006096
## Lag[4*(p+q)+(p+q)-1] [9]    11.110 0.028745
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.7348 0.500 2.000 0.3913
## ARCH Lag[5]    0.7478 1.440 1.667 0.8089
## ARCH Lag[7]    0.8544 2.315 1.543 0.9360
##
## Nyblom stability test
## -----
## Joint Statistic:  461.1365
## Individual Statistics:
## mu      0.220534
## ar1     0.096322
## omega   71.164742
## alpha1  0.195380
## beta1   0.199804
## vxreg1  7.965580
## vxreg2  6.415530
## vxreg3  3.725879
## vxreg4  0.005702
## vxreg5  2.052022
## vxreg6  0.740233
## vxreg7  0.178243
## shape   0.150245
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.89 3.15 3.69
## Individual Statistic:  0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      0.8530 3.937e-01
## Negative Sign Bias  5.9148 3.729e-09 ***
## Positive Sign Bias  0.8026 4.223e-01
## Joint Effect     41.0696 6.321e-09 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      27.39    0.09583
## 2    30      42.03    0.05580
## 3    40      59.23    0.01989
## 4    50      69.83    0.02690
##
##
## Elapsed time : 1.329262

```

```

## Results review 1
coef(ts_garchFit)

##          mu          ar1          omega          alpha1          beta1          vxreg1
## 6.808605e-04 1.691814e-02 7.986854e-07 4.613415e-02 9.440098e-01 9.986932e-09
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 9.947039e-09 9.929000e-09 1.002196e-08 1.031877e-08 9.961744e-09 1.018089e-08
##          shape
## 4.874184e+00

ts_rhat <- ts_garchFit@fit$fitted.values
plot.ts(ts_rhat)
ts_hhat <- ts(ts_garchFit@fit$sigma^2)
plot.ts(ts_hhat)

## Results review 2
tfit.val <- coef(ts_garchFit)
tfit.sd <- diag(vcov(ts_garchFit))
ttrue.val = ts_garchFit@fit$tval

tfit.conf.lb <- tfit.val + qnorm(0.025) * tfit.sd
tfit.conf.ub <- tfit.val + qnorm(0.975) * tfit.sd
print(tfit.val)

##          mu          ar1          omega          alpha1          beta1          vxreg1
## 6.808605e-04 1.691814e-02 7.986854e-07 4.613415e-02 9.440098e-01 9.986932e-09
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 9.947039e-09 9.929000e-09 1.002196e-08 1.031877e-08 9.961744e-09 1.018089e-08
##          shape
## 4.874184e+00

print(tfit.sd)

## [1] 1.566213e-08 3.284693e-04 -1.244043e-12 -6.778347e-06 -1.145285e-04
## [6] -5.547588e-07 8.488128e-09 8.550484e-09 -2.747755e-11 -2.112168e-11
## [11] -2.664448e-10 4.514746e-12 3.051880e-01

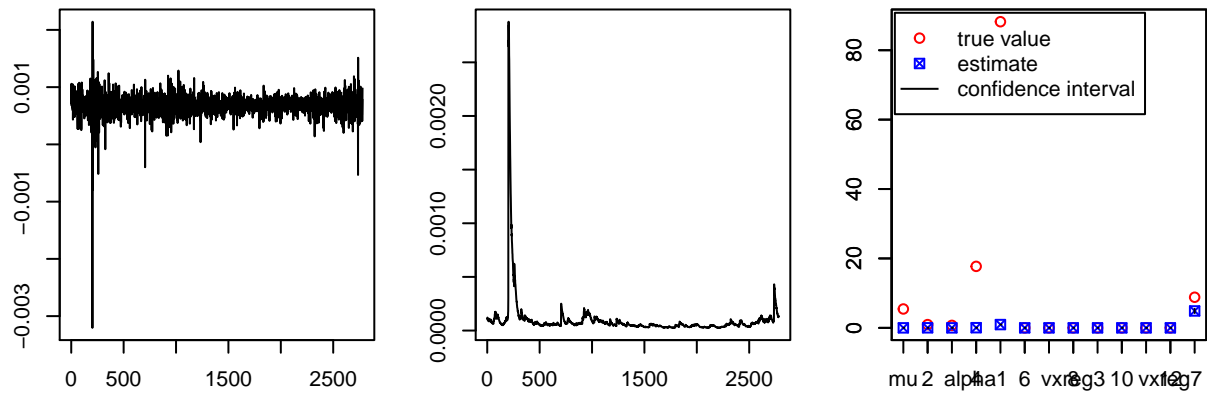
print(ttrue.val)

##          mu          ar1          omega          alpha1          beta1          vxreg1
## 5.440424e+00 9.334802e-01 7.160742e-01 1.771987e+01 8.821038e+01 1.340849e-05
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 1.079662e-04 1.073767e-04 1.911892e-03 2.245245e-03 6.102837e-04 4.791476e-03
##          shape
## 8.823038e+00

plot(ttrue.val, pch = 1, col = "red",
     ylim = range(c(tfit.conf.lb, tfit.conf.ub, ttrue.val)),
     xlab = "", ylab = "", axes = TRUE)
box(); axis(1, at = 1:length(tfit.val), labels = names(tfit.val)); axis(2)
points(coef(ts_garchFit), col = "blue", pch = 7)
for (i in 1:length(tfit.val)) {
  lines(c(i,i), c(tfit.conf.lb[i], tfit.conf.ub[i]))
}
legend("topleft", legend = c("true value", "estimate", "confidence interval"),
      col = c("red", "blue", 1), pch = c(1, 7, NA), lty = c(NA, NA, 1), inset = 0.01)

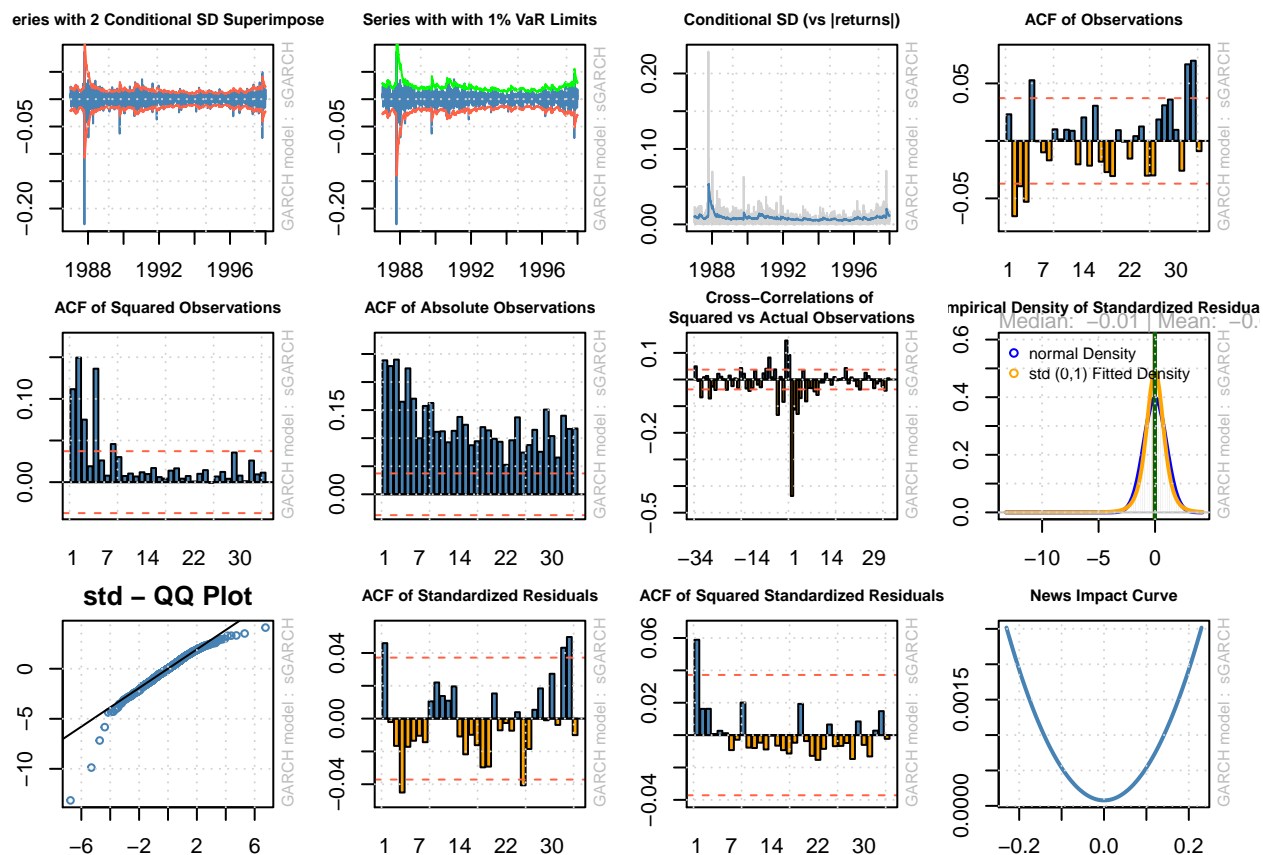
```

```
par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(ts_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```

```
#Student's t-gjrGARCH ---->tgjrGARCH
tgjr_garchMod <- ugarchspec(
  variance.model=list(model="gjrGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="std"
)
tgjr_garchFit <- ugarchfit(spec=tgjr_garchMod, data=log_ret)
coef(tgjr_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1          gamma1
## 6.495544e-04 2.037559e-02 8.937411e-07 3.027894e-02 9.444314e-01 2.250641e-02
##          vxreg1          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6
## 7.747261e-09 2.140205e-09 6.018121e-17 3.547505e-08 5.518537e-05 8.569491e-11
##          vxreg7          shape
## 1.107205e-05 5.025285e+00
```

```
tgjr_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
```

```

## -----
## GARCH Model : gjrGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : std
##
## Optimal Parameters
## -----
##      Estimate Std. Error   t value Pr(>|t|)
## mu      0.000650   0.000129 5.0455e+00 0.000000
## ar1      0.020376   0.018301 1.1134e+00 0.265547
## omega    0.000001   0.000000 2.4964e+00 0.012547
## alpha1   0.030279   0.002633 1.1501e+01 0.000000
## beta1    0.944431   0.000276 3.4200e+03 0.000000
## gamma1   0.022506   0.003266 6.8918e+00 0.000000
## vxreg1   0.000000   0.000453 1.7000e-05 0.999986
## vxreg2   0.000000   0.000183 1.2000e-05 0.999991
## vxreg3   0.000000   0.000114 0.0000e+00 1.000000
## vxreg4   0.000000   0.000008 4.2800e-03 0.996585
## vxreg5   0.000055   0.000034 1.6304e+00 0.103017
## vxreg6   0.000000   0.000002 3.7000e-05 0.999970
## vxreg7   0.000011   0.000026 4.3092e-01 0.666529
## shape    5.025285   0.519785 9.6680e+00 0.000000
##
## Robust Standard Errors:
##      Estimate Std. Error   t value Pr(>|t|)
## mu      0.000650   0.000116 5.586597 0.000000
## ar1      0.020376   0.017365 1.173353 0.240654
## omega    0.000001   0.000001 0.685138 0.493257
## alpha1   0.030279   0.017647 1.715801 0.086199
## beta1    0.944431   0.010215 92.455574 0.000000
## gamma1   0.022506   0.003971 5.668008 0.000000
## vxreg1   0.000000   0.001862 0.000004 0.999997
## vxreg2   0.000000   0.000632 0.000003 0.999997
## vxreg3   0.000000   0.000401 0.000000 1.000000
## vxreg4   0.000000   0.000016 0.002236 0.998216
## vxreg5   0.000055   0.000023 2.419107 0.015559
## vxreg6   0.000000   0.000003 0.000026 0.999979
## vxreg7   0.000011   0.000086 0.128287 0.897922
## shape    5.025285   1.297528 3.872967 0.000108
##
## LogLikelihood : 9568.568
##
## Information Criteria
## -----
##
## Akaike      -6.8713
## Bayes       -6.8415
## Shibata     -6.8714
## Hannan-Quinn -6.8605
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##                               statistic p-value
## Lag[1]                        4.149 0.04165

```

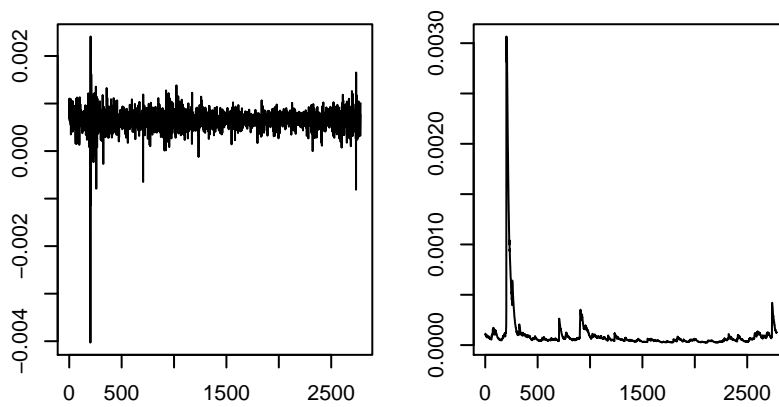
```

## Lag[2*(p+q)+(p+q)-1][2]      4.155 0.00305
## Lag[4*(p+q)+(p+q)-1][5]      7.126 0.01721
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##               statistic  p-value
## Lag[1]                8.138 0.004334
## Lag[2*(p+q)+(p+q)-1][5]      9.052 0.016057
## Lag[4*(p+q)+(p+q)-1][9]      9.488 0.064405
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.7338 0.500 2.000 0.3917
## ARCH Lag[5]    0.7430 1.440 1.667 0.8104
## ARCH Lag[7]    0.8567 2.315 1.543 0.9357
##
## Nyblom stability test
## -----
## Joint Statistic:  434.3182
## Individual Statistics:
## mu      0.265596
## ar1      0.110481
## omega 62.932791
## alpha1  0.226081
## beta1   0.237378
## gamma1  0.188567
## vxreg1  9.473552
## vxreg2  6.398403
## vxreg3  3.435132
## vxreg4  0.051169
## vxreg5  0.002212
## vxreg6  0.782884
## vxreg7  0.019797
## shape   0.150751
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      3.08 3.34 3.9
## Individual Statistic:  0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      0.6861 4.927e-01
## Negative Sign Bias  5.3773 8.188e-08 ***
## Positive Sign Bias  0.7909 4.291e-01
## Joint Effect     34.7582 1.370e-07 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----

```

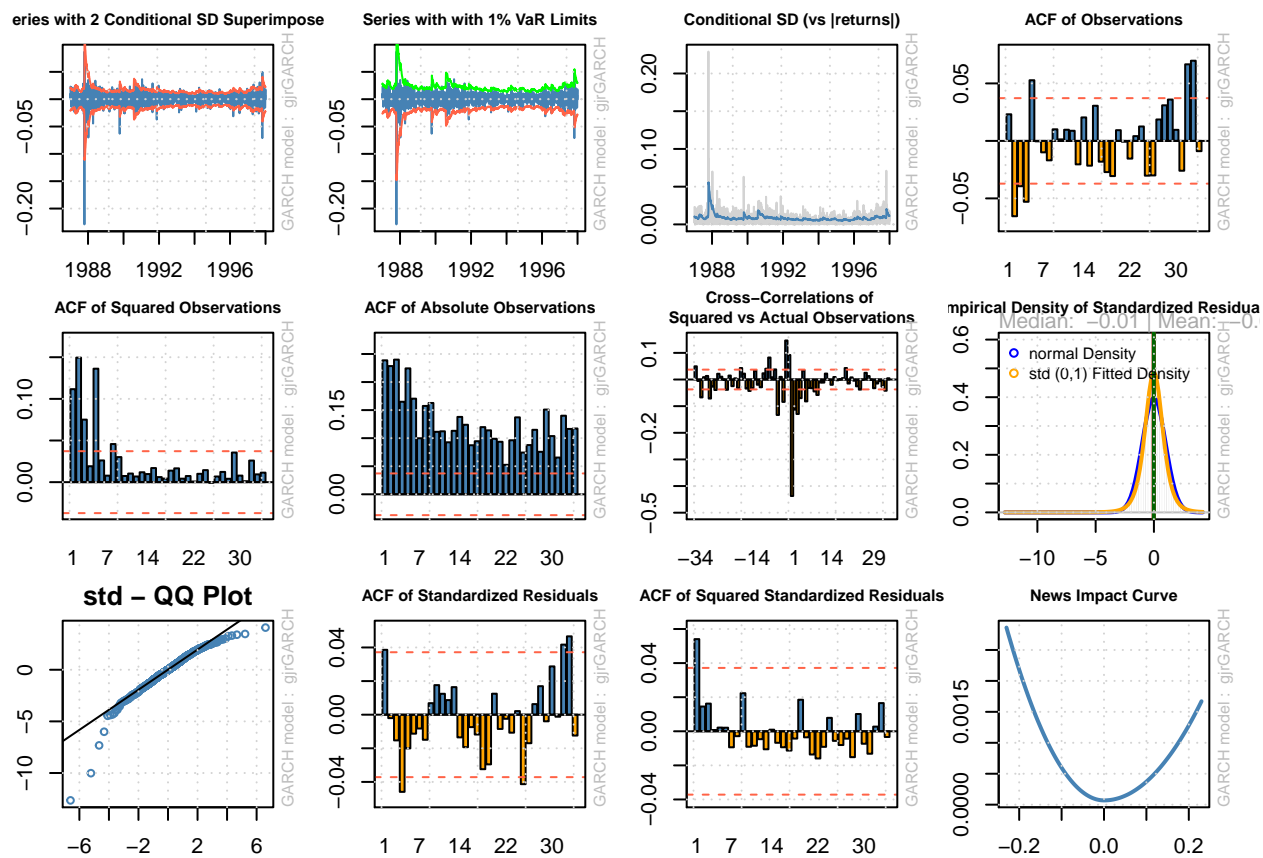
```
##      group statistic p-value(g-1)
## 1      20      28.27      0.07837
## 2      30      26.37      0.60577
## 3      40      57.16      0.03034
## 4      50      61.48      0.10866
##
##
## Elapsed time : 2.963501
tgjr_rhat <- tgjr_garchFit@fit$fitted.values
plot.ts(tgjr_rhat)
tgjr_hhat <- ts(tgjr_garchFit@fit$sigma^2)
plot.ts(tgjr_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(tgjr_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



```
#Student's t-eGARCH ---->teGARCH
te_garchMod <- ugarchspec(
  variance.model=list(model="eGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="std"
)
te_garchFit <- ugarchfit(spec=te_garchMod, data=log_ret)
coef(te_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 0.0005920684 0.0158498266 -0.0999985207 -0.0383220276 0.9897031782
##          gamma1          vxreg1          vxreg2          vxreg3          vxreg4
## 0.0947133145 -0.0260061486 -0.0502494495 -0.1012987398 0.0264633650
##          vxreg5          vxreg6          vxreg7          shape
## 0.2744948314 -0.0710716406 0.1056797395 5.1484659175
```

```
te_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
```

```

## -----
## GARCH Model : eGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : std
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000592    0.000122    4.87149 0.000001
## ar1     0.015850    0.017442    0.90873 0.363491
## omega  -0.099999    0.005057   -19.77544 0.000000
## alpha1 -0.038322    0.012193   -3.14295 0.001673
## beta1   0.989703    0.000528  1874.53024 0.000000
## gamma1  0.094713    0.022845    4.14585 0.000034
## vxreg1 -0.026006    0.130370   -0.19948 0.841888
## vxreg2 -0.050249    0.120515   -0.41696 0.676711
## vxreg3 -0.101299    0.123271   -0.82176 0.411215
## vxreg4  0.026463    0.118940    0.22249 0.823930
## vxreg5  0.274495    0.113468    2.41913 0.015557
## vxreg6 -0.071072    0.102020   -0.69665 0.486024
## vxreg7  0.105680    0.114059    0.92653 0.354169
## shape   5.148466    0.693757    7.42113 0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000592    0.000103    5.76118 0.000000
## ar1     0.015850    0.015530    1.02059 0.307450
## omega  -0.099999    0.011216   -8.91598 0.000000
## alpha1 -0.038322    0.021817   -1.75652 0.078999
## beta1   0.989703    0.001180  838.60657 0.000000
## gamma1  0.094713    0.057201    1.65581 0.097760
## vxreg1 -0.026006    0.160699   -0.16183 0.871438
## vxreg2 -0.050249    0.040259   -1.24815 0.211975
## vxreg3 -0.101299    0.049238   -2.05734 0.039653
## vxreg4  0.026463    0.062881    0.42085 0.673864
## vxreg5  0.274495    0.065825    4.17004 0.000030
## vxreg6 -0.071072    0.080319   -0.88486 0.376230
## vxreg7  0.105680    0.076963    1.37312 0.169714
## shape   5.148466    1.572399    3.27427 0.001059
##
## LogLikelihood : 9579.461
##
## Information Criteria
## -----
##
## Akaike      -6.8792
## Bayes       -6.8493
## Shibata     -6.8792
## Hannan-Quinn -6.8684
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##                                statistic p-value
## Lag[1]                        3.912 0.047951

```

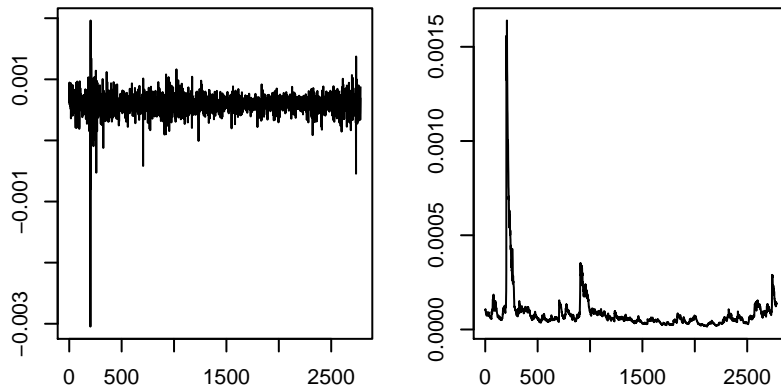
```

## Lag[2*(p+q)+(p+q)-1][2]      4.033 0.004001
## Lag[4*(p+q)+(p+q)-1][5]      7.190 0.016227
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##               statistic  p-value
## Lag[1]                9.369 0.002207
## Lag[2*(p+q)+(p+q)-1][5]    11.091 0.004812
## Lag[4*(p+q)+(p+q)-1][9]    11.828 0.019845
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.9059 0.500 2.000 0.3412
## ARCH Lag[5]    1.1939 1.440 1.667 0.6764
## ARCH Lag[7]    1.3687 2.315 1.543 0.8473
##
## Nyblom stability test
## -----
## Joint Statistic: 1.2799
## Individual Statistics:
## mu      0.3747720
## ar1     0.1383511
## omega   0.3793137
## alpha1  0.0728387
## beta1   0.3880465
## gamma1  0.1458148
## vxreg1  0.0028431
## vxreg2  0.0004189
## vxreg3  0.0007320
## vxreg4  0.0009185
## vxreg5  0.0008567
## vxreg6  0.0035727
## vxreg7  0.0015351
## shape   0.1283689
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      3.08 3.34 3.9
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      0.8890 3.741e-01
## Negative Sign Bias 5.8954 4.189e-09 ***
## Positive Sign Bias 0.6116 5.408e-01
## Joint Effect    39.7646 1.195e-08 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----

```

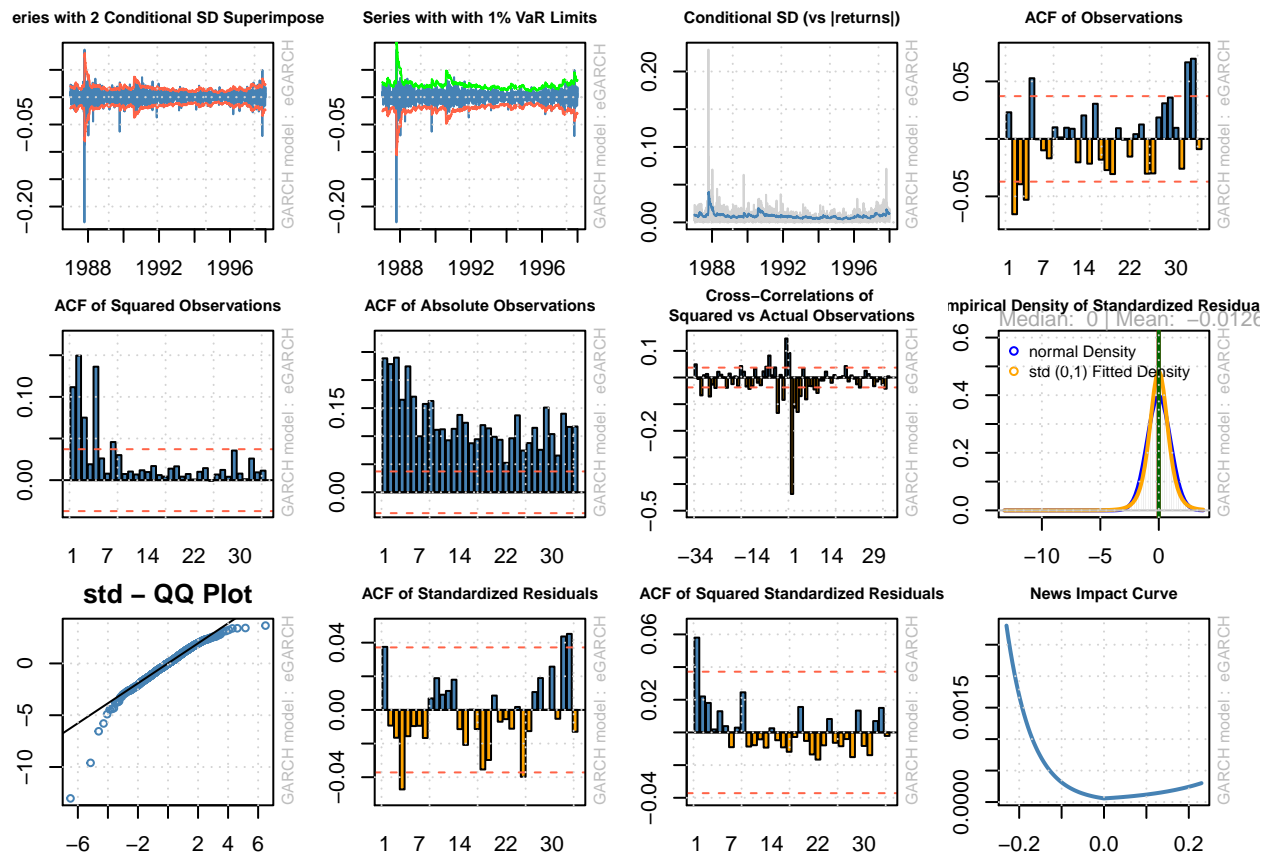
```
##      group statistic p-value(g-1)
## 1      20      22.82      0.2454
## 2      30      35.11      0.2011
## 3      40      42.32      0.3299
## 4      50      53.11      0.3189
##
##
## Elapsed time : 2.651492
te_rhat <- te_garchFit@fit$fitted.values
plot.ts(te_rhat)
te_hhat <- ts(te_garchFit@fit$sigma^2)
plot.ts(te_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(te_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```

#Student's t-apARCH ----> tapARCH

```
tapARCHMod <- ugarchspec(variance.model=list(model="apARCH",
                                             garchOrder=c(1,1),
                                             external.regressors = df_dummies ),
                        mean.model=list(armaOrder=c(1,0)),
                        distribution.model="std")
tapARCHFit <- ugarchfit(spec=tapARCHMod, data= log_ret)
coef(tapARCHFit)
```

```
##          mu          ar1          omega          alpha1          beta1          gamma1
## 6.159577e-04 2.094163e-02 6.378751e-06 5.353966e-02 9.410051e-01 2.772754e-01
##          delta          vxreg1          vxreg2          vxreg3          vxreg4          vxreg5
## 1.586309e+00 7.583722e-09 2.104194e-09 2.357757e-10 1.998229e-08 1.931712e-06
##          vxreg6          vxreg7          shape
## 1.514864e-19 1.801589e-07 5.101146e+00
```

tapARCHFit

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : apARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
```

```

## Distribution : std
##
## Optimal Parameters
## -----
##      Estimate   Std. Error    t value Pr(>|t|)
## mu      0.000616    0.000121    5.108084 0.00000
## ar1     0.020942    0.018183    1.151696 0.24945
## omega   0.000006    0.000004    1.498394 0.13403
## alpha1  0.053540    0.017326    3.090209 0.00200
## beta1   0.941005    0.002744 342.955312 0.00000
## gamma1  0.277275    0.084261    3.290658 0.00100
## delta   1.586309    0.021228   74.727252 0.00000
## vxreg1  0.000000    0.001177    0.000006 0.99999
## vxreg2  0.000000    0.000254    0.000008 0.99999
## vxreg3  0.000000    0.000072    0.000003 1.00000
## vxreg4  0.000000    0.000047    0.000427 0.99966
## vxreg5  0.000002    0.000041    0.046960 0.96254
## vxreg6  0.000000    0.000064    0.000000 1.00000
## vxreg7  0.000000    0.000037    0.004925 0.99607
## shape   5.101146    0.474191   10.757578 0.00000
##
## Robust Standard Errors:
##      Estimate   Std. Error    t value Pr(>|t|)
## mu      0.000616    0.000214    2.879988 0.003977
## ar1     0.020942    0.017034    1.229386 0.218927
## omega   0.000006    0.000020    0.323628 0.746220
## alpha1  0.053540    0.075567    0.708508 0.478630
## beta1   0.941005    0.005076 185.399597 0.000000
## gamma1  0.277275    0.563184    0.492336 0.622482
## delta   1.586309    0.159084    9.971507 0.000000
## vxreg1  0.000000    0.003102    0.000002 0.999998
## vxreg2  0.000000    0.000448    0.000005 0.999996
## vxreg3  0.000000    0.000306    0.000001 0.999999
## vxreg4  0.000000    0.000032    0.000629 0.999498
## vxreg5  0.000002    0.000118    0.016440 0.986883
## vxreg6  0.000000    0.000056    0.000000 1.000000
## vxreg7  0.000000    0.000109    0.001653 0.998681
## shape   5.101146    0.787032    6.481501 0.000000
##
## LogLikelihood : 9569.8
##
## Information Criteria
## -----
##
## Akaike      -6.8715
## Bayes       -6.8395
## Shibata     -6.8715
## Hannan-Quinn -6.8599
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##              statistic  p-value
## Lag[1]              4.302 0.038077
## Lag[2*(p+q)+(p+q)-1][2] 4.312 0.002144

```

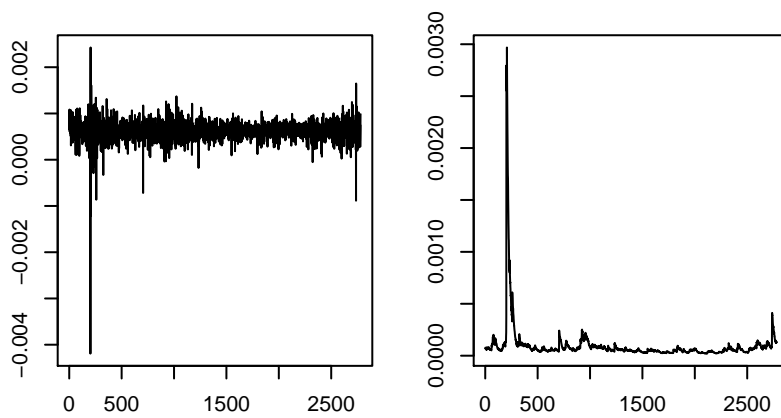
```

## Lag[4*(p+q)+(p+q)-1][5]      7.175 0.016451
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##               statistic p-value
## Lag[1]                6.017 0.01417
## Lag[2*(p+q)+(p+q)-1][5]      6.550 0.06659
## Lag[4*(p+q)+(p+q)-1][9]      6.953 0.20311
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.3841 0.500 2.000 0.5354
## ARCH Lag[5]    0.3894 1.440 1.667 0.9157
## ARCH Lag[7]    0.5706 2.315 1.543 0.9716
##
## Nyblom stability test
## -----
## Joint Statistic: 15.6833
## Individual Statistics:
## mu      0.32579
## ar1      0.11537
## omega    0.41155
## alpha1   0.27087
## beta1    0.27901
## gamma1   0.16959
## delta    0.41549
## vxreg1   5.44140
## vxreg2   4.54844
## vxreg3   2.55608
## vxreg4   0.07645
## vxreg5   1.63121
## vxreg6   0.09930
## vxreg7   0.10969
## shape    0.14823
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      3.26 3.54 4.07
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      0.5766 5.643e-01
## Negative Sign Bias 4.9687 7.149e-07 ***
## Positive Sign Bias 0.9091 3.634e-01
## Joint Effect    30.8613 9.092e-07 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----

```

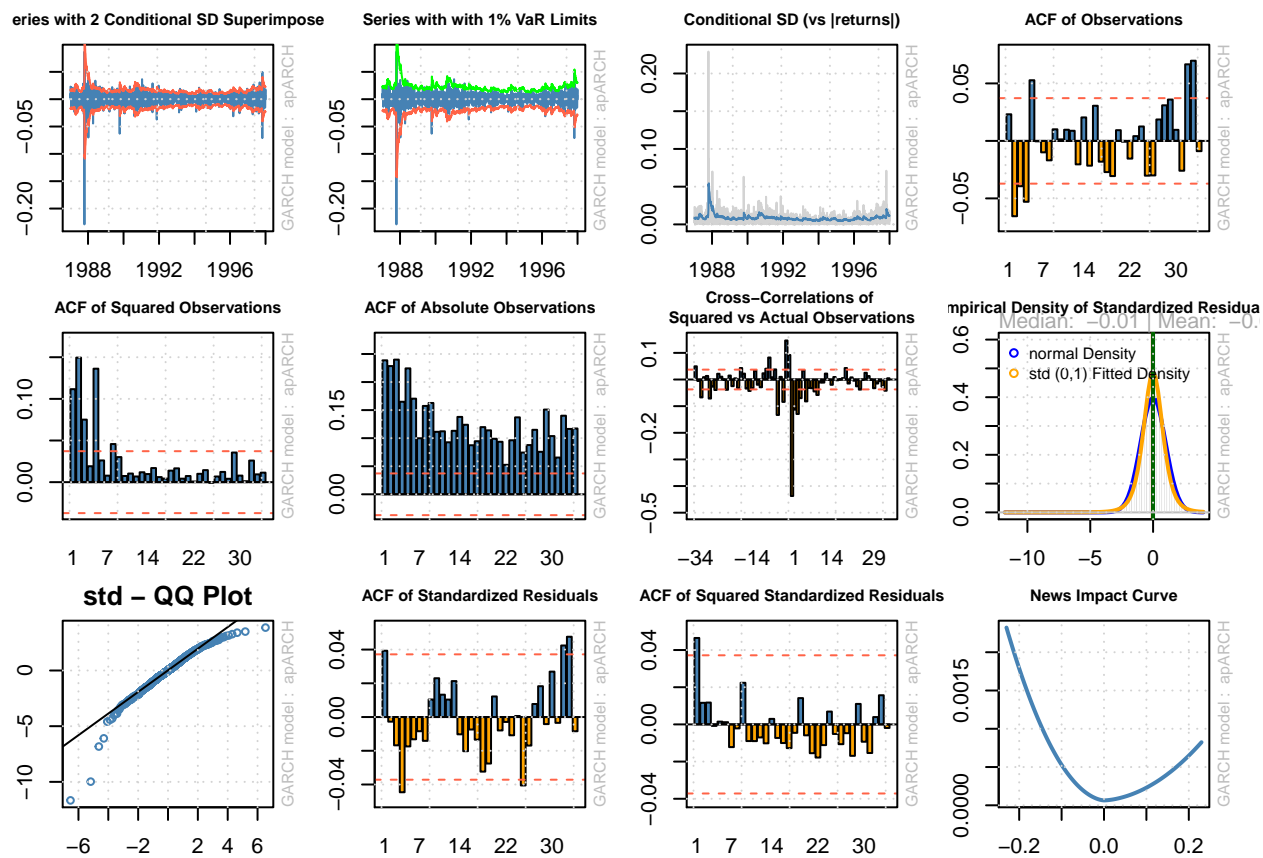
```
##      group statistic p-value(g-1)
## 1      20      22.98      0.2384
## 2      30      26.45      0.6011
## 3      40      47.61      0.1622
## 4      50      55.91      0.2313
##
##
## Elapsed time : 11.18811
tapARCH_rhat <- tapARCHFit@fit$fitted.values
plot.ts(tapARCH_rhat)
tapARCH_hhat <- ts(tapARCHFit@fit$sigma^2)
plot.ts(tapARCH_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(tapARCHFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



#Student's t-tiGARCH ----> tiGARCH

```
ti_garchMod <- ugarchspec(variance.model=list(model="iGARCH",
                                              garchOrder=c(1,1),
                                              external.regressors = df_dummies ),
                          mean.model=list(armaOrder=c(1,0), include.mean=TRUE),
                          distribution.model="std")
ti_garchFit <- ugarchfit(spec=ti_garchMod, data= log_ret)
coef(ti_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1          vxreg1
## 6.701593e-04 1.621996e-02 4.381322e-07 4.996179e-02 9.500382e-01 7.558834e-09
##          vxreg2          vxreg3          vxreg4          vxreg5          vxreg6          vxreg7
## 1.952047e-09 1.498418e-14 1.140755e-08 5.348527e-05 2.366768e-09 2.402249e-07
##          shape
## 4.392296e+00
```

```
ti_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : iGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
```

```

## Distribution : std
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000670    0.000124   5.416430 0.000000
## ar1      0.016220    0.017972   0.902495 0.366794
## omega    0.000000    0.000000   1.037008 0.299732
## alpha1   0.049962    0.000786  63.580084 0.000000
## beta1    0.950038         NA         NA         NA
## vxreg1   0.000000    0.000737   0.000010 0.999992
## vxreg2   0.000000    0.000210   0.000009 0.999993
## vxreg3   0.000000    0.000159   0.000000 1.000000
## vxreg4   0.000000    0.000012   0.000946 0.999245
## vxreg5   0.000053    0.000032   1.656886 0.097543
## vxreg6   0.000000    0.000014   0.000168 0.999866
## vxreg7   0.000000    0.000006   0.038706 0.969125
## shape    4.392296    0.338716  12.967475 0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000670    0.000172   3.886356 0.000102
## ar1      0.016220    0.023214   0.698716 0.484730
## omega    0.000000    0.000002   0.232836 0.815888
## alpha1   0.049962    0.005530   9.034103 0.000000
## beta1    0.950038         NA         NA         NA
## vxreg1   0.000000    0.001953   0.000004 0.999997
## vxreg2   0.000000    0.000396   0.000005 0.999996
## vxreg3   0.000000    0.000481   0.000000 1.000000
## vxreg4   0.000000    0.000045   0.000256 0.999796
## vxreg5   0.000053    0.000030   1.759295 0.078527
## vxreg6   0.000000    0.000022   0.000106 0.999916
## vxreg7   0.000000    0.000004   0.055097 0.956061
## shape    4.392296    0.897180   4.895668 0.000001
##
## LogLikelihood : 9562.43
##
## Information Criteria
## -----
##
## Akaike      -6.8683
## Bayes       -6.8428
## Shibata     -6.8684
## Hannan-Quinn -6.8591
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##              statistic   p-value
## Lag[1]              5.270 0.0216917
## Lag[2*(p+q)+(p+q)-1] [2]  5.280 0.0002264
## Lag[4*(p+q)+(p+q)-1] [5]  8.441 0.0050379
## d.o.f=1
## H0 : No serial correlation
##

```

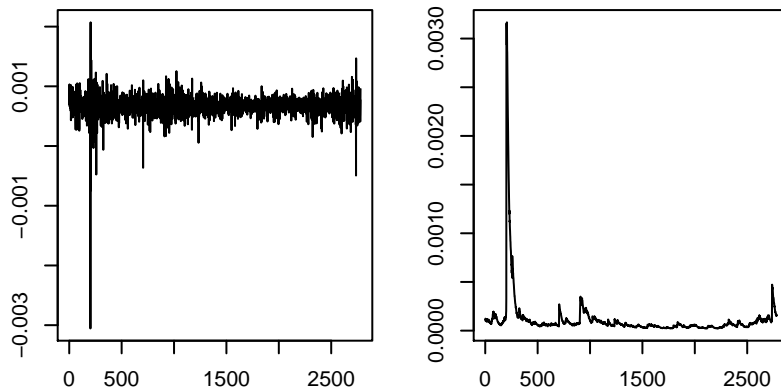
```

## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##               statistic  p-value
## Lag[1]                8.664 0.003245
## Lag[2*(p+q)+(p+q)-1] [5]    9.540 0.012069
## Lag[4*(p+q)+(p+q)-1] [9]    9.914 0.052334
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.6587 0.500 2.000 0.4170
## ARCH Lag[5]    0.6626 1.440 1.667 0.8348
## ARCH Lag[7]    0.7794 2.315 1.543 0.9466
##
## Nyblom stability test
## -----
## Joint Statistic: 268.9635
## Individual Statistics:
## mu      2.193e-01
## ar1     9.071e-02
## omega   1.111e+02
## alpha1  1.822e-01
## vxreg1  1.364e+01
## vxreg2  1.129e+01
## vxreg3  6.832e+00
## vxreg4  6.429e-01
## vxreg5  2.267e-03
## vxreg6  6.935e-01
## vxreg7  1.271e-01
## shape   2.355e-01
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.69 2.96 3.51
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##               t-value      prob sig
## Sign Bias      0.7488 4.540e-01
## Negative Sign Bias 5.5712 2.772e-08 ***
## Positive Sign Bias 0.9001 3.682e-01
## Joint Effect     37.4600 3.677e-08 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      22.55    0.25795
## 2    30      33.29    0.26606
## 3    40      49.19    0.12706
## 4    50      62.64    0.09126
##
##

```

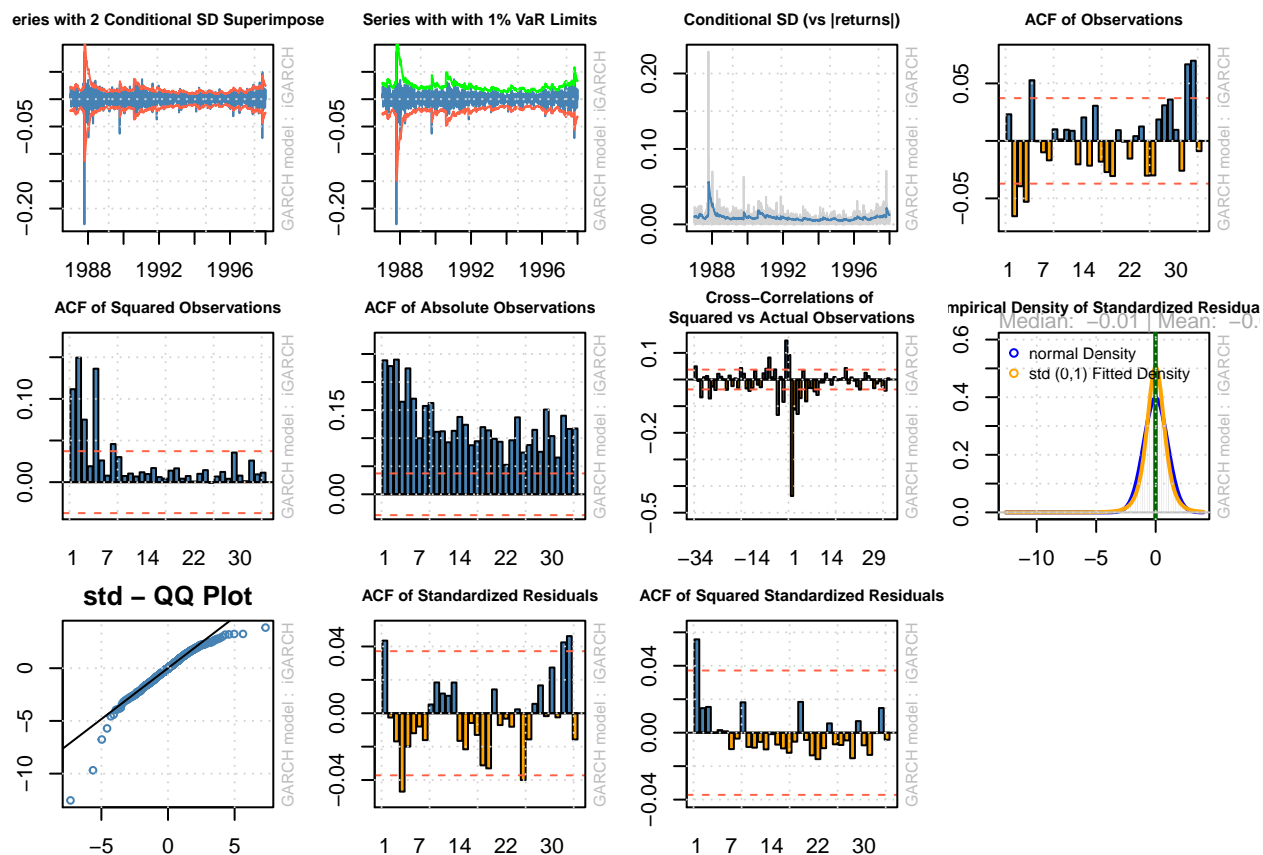
```
## Elapsed time : 1.380489
ti_rhat <- ti_garchFit@fit$fitted.values
plot.ts(ti_rhat)
ti_hhat <- ts(ti_garchFit@fit$sigma^2)
plot.ts(ti_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(ti_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
## Warning in FUN(x):
## plot-->: iGARCH and fiGARCH newsimpact not available
```

In order to chose the best model:

```
#Choose best GARCH model
#Normal
AIC= c(Infocriteria(s_garchFit)[1], Infocriteria(gjr_garchFit)[1],
        Infocriteria(e_garchFit)[1], Infocriteria(apARCHFit)[1], Infocriteria(i_garchFit)[1] )
rowSAIC= c("s_garch", "gjr_garchFit", "e_garchFit", "apARCHFit", "i_garchFit")

AIC_Results= data.frame(AIC, row.names = rowSAIC)
AIC_Results

##           AIC
## s_garch    -6.740216
## gjr_garchFit -6.754373
## e_garchFit   -6.764806
## apARCHFit    -6.745484
## i_garchFit   -6.736848

BestAICNorm=AIC_Results[which.min(AIC_Results$AIC),]
BestAICNorm

## [1] -6.764806

BIC= c(Infocriteria(s_garchFit)[2], Infocriteria(gjr_garchFit)[2],
        Infocriteria(e_garchFit)[2], Infocriteria(apARCHFit)[2], Infocriteria(i_garchFit)[2] )
rowSBIC= c("s_garch", "gjr_garchFit", "e_garchFit", "apARCHFit", "i_garchFit")
BIC_Results= data.frame(BIC, row.names = rowSBIC)
```

```

BIC_Results

##              BIC
## s_garch      -6.714626
## gjr_garchFit -6.726650
## e_garchFit   -6.737083
## apARCHFit    -6.715628
## i_garchFit   -6.713390

BestBICNorm=BIC_Results[which.min(BIC_Results$BIC),]
BestBICNorm

## [1] -6.737083

Best_Norm=c(BestAICNorm,BestBICNorm)
rowSBest_Norm= c("AICbest","BICbest")
Norm_Results= data.frame(Best_Norm, row.names =rowSBest_Norm)
Norm_Results

##           Best_Norm
## AICbest -6.764806
## BICbest -6.737083

#Student-t
tAIC= c(Infocriteria(ts_garchFit)[1], Infocriteria(tgjrgarchFit)[1],
        Infocriteria(te_garchFit)[1], Infocriteria(tapARCHFit)[1], Infocriteria(ti_garchFit)[1] )
trowSAIC= c("ts_garch", "tgjrgarchFit", "te_garchFit", "tapARCHFit", "ti_garchFit")

tAIC_Results= data.frame(tAIC, row.names = trowSAIC)
tAIC_Results

##           tAIC
## ts_garch     -6.866851
## tgjrgarchFit -6.871318
## te_garchFit  -6.879152
## tapARCHFit   -6.871485
## ti_garchFit  -6.868343

tAIC_Results[which.min(tAIC_Results$tAIC),]

## [1] -6.879152

tBIC= c(Infocriteria(ts_garchFit)[2], Infocriteria(tgjrgarchFit)[2],
        Infocriteria(te_garchFit)[2], Infocriteria(tapARCHFit)[2], Infocriteria(ti_garchFit)[2] )
trowSBIC= c("ts_garch", "tgjrgarchFit", "te_garchFit", "tapARCHFit", "ti_garchFit")
tBIC_Results= data.frame(tBIC, row.names = trowSBIC)
tBIC_Results

##           tBIC
## ts_garch     -6.839128
## tgjrgarchFit -6.841463
## te_garchFit  -6.849296
## tapARCHFit   -6.839497
## ti_garchFit  -6.842752

tBIC_Results[which.min(tBIC_Results$tBIC),]

## [1] -6.849296

```

```

#Goodness of Fit
Distribution=c("Normal", "Normal", "Normal", "Normal", "Normal",
              "Student's-t", "Student's-t", "Student's-t", "Student's-t", "Student's-t" )
rowsGARCH=c("s_garchFit", "gjr_garchFit", "e_garchFit", "apARCHFit", "i_garchFit",
            "ts_garchFit", "tgjr_garchFit", "te_garchFit", "tapARCHFit", "ti_garchFit")
Best=c("o", "o", "*", "o", "o",
       "o", "o", "*", "o", "o")
final_AIC=c(AIC,tAIC)
final_BIC=c(BIC,tBIC)
Results <- data.frame("AIC" = final_AIC, "BIC" = final_BIC , "Distribution" = Distribution,
                     "Best"= Best ,row.names = rowsGARCH)

Results

```

##		AIC	BIC	Distribution	Best
##	s_garchFit	-6.740216	-6.714626	Normal	o
##	gjr_garchFit	-6.754373	-6.726650	Normal	o
##	e_garchFit	-6.764806	-6.737083	Normal	*
##	apARCHFit	-6.745484	-6.715628	Normal	o
##	i_garchFit	-6.736848	-6.713390	Normal	o
##	ts_garchFit	-6.866851	-6.839128	Student's-t	o
##	tgjr_garchFit	-6.871318	-6.841463	Student's-t	o
##	te_garchFit	-6.879152	-6.849296	Student's-t	*
##	tapARCHFit	-6.871485	-6.839497	Student's-t	o
##	ti_garchFit	-6.868343	-6.842752	Student's-t	o

Validation of the model:

```

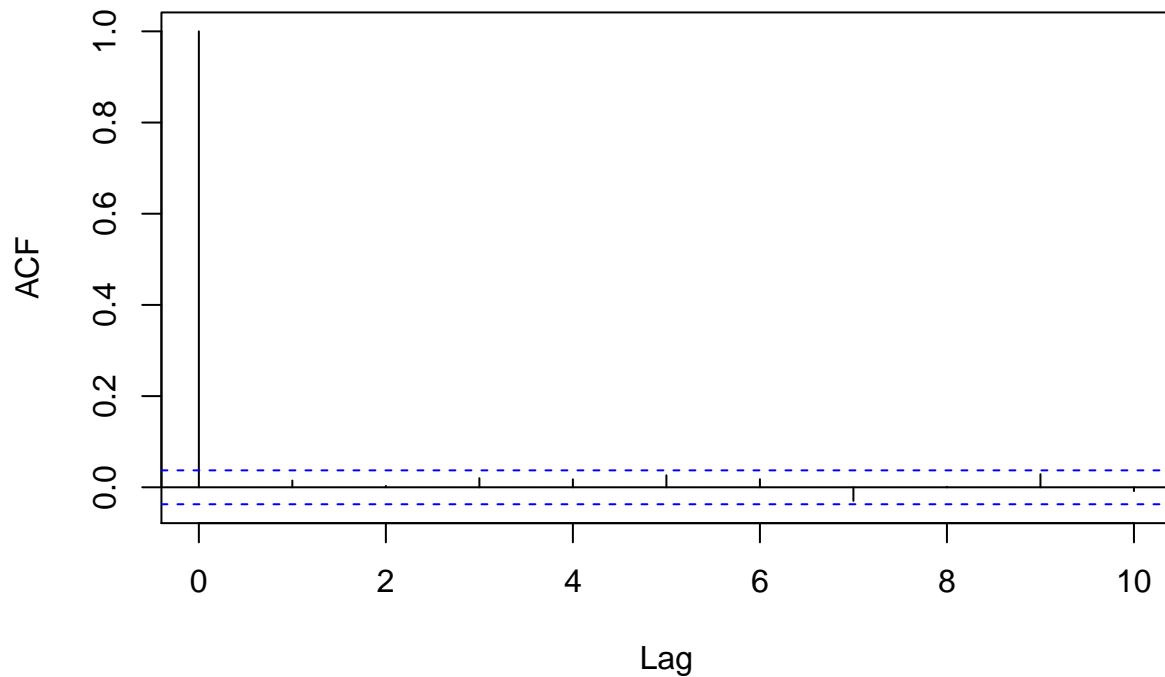
#Validation of the model
residual_bestModel= residuals(te_garchFit, standardize = TRUE)
Box.test(abs(residual_bestModel), 10, type = "Ljung-Box")

##
## Box-Ljung test
##
## data: abs(residual_bestModel)
## X-squared = 10.423, df = 10, p-value = 0.4042

acf(abs(residual_bestModel), 10)

```

Series abs(residual_bestModel)



Second analysis on the Limit-Up/Limit-Down Regulation's effect on stock volatility

```
#DATA
library(tidyquant)

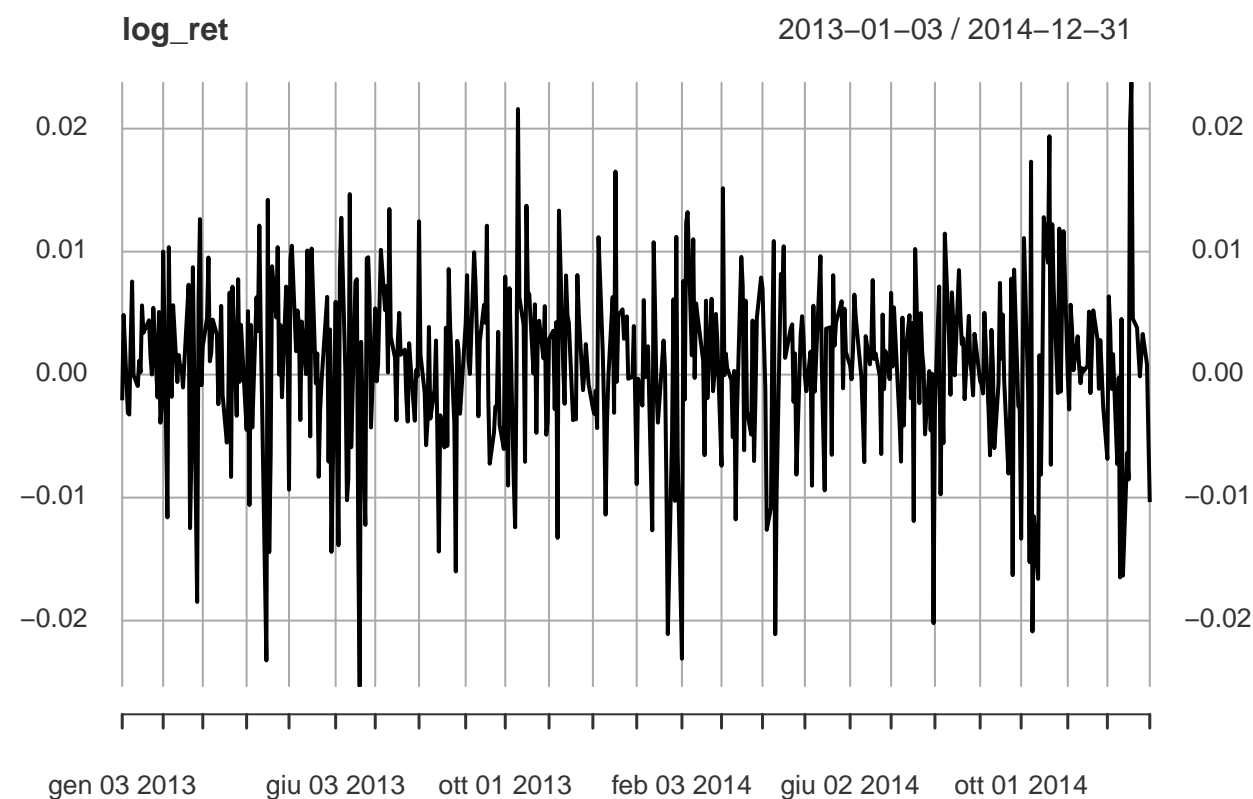
# Downloading SP500 using the library tidyquant

SP500= getSymbols("^GSPC", from = '2013-01-01',
                  to = "2015-01-01", auto.assign = FALSE)
head(SP500)
```

```
##           GSPC.Open GSPC.High GSPC.Low GSPC.Close GSPC.Volume GSPC.Adjusted
## 2013-01-02   1426.19   1462.43  1426.19   1462.42  4202600000      1462.42
## 2013-01-03   1462.42   1465.47  1455.53   1459.37  3829730000      1459.37
## 2013-01-04   1459.37   1467.94  1458.99   1466.47  3424290000      1466.47
## 2013-01-07   1466.47   1466.47  1456.62   1461.89  3304970000      1461.89
## 2013-01-08   1461.89   1461.89  1451.64   1457.15  3601600000      1457.15
## 2013-01-09   1457.15   1464.73  1457.15   1461.02  3674390000      1461.02
```

```
logret = diff(log(SP500$GSPC.Adjusted))
log_ret <- logret[-1]
```

```
plot(log_ret, length(log_ret))
```



log_ret

```
##          GSPC.Adjusted
## 2013-01-03 -2.087796e-03
## 2013-01-04  4.853300e-03
## 2013-01-07 -3.128003e-03
## 2013-01-08 -3.247640e-03
## 2013-01-09  2.652346e-03
## 2013-01-10  7.568700e-03
## 2013-01-11 -4.751492e-05
## 2013-01-14 -9.311048e-04
## 2013-01-15  1.128033e-03
## 2013-01-16  1.969725e-04
## 2013-01-17  5.627060e-03
## 2013-01-18  3.397492e-03
## 2013-01-22  4.418332e-03
## 2013-01-23  1.506342e-03
## 2013-01-24  6.614196e-06
## 2013-01-25  5.430709e-03
## 2013-01-28 -1.851334e-03
## 2013-01-29  5.093004e-03
## 2013-01-30 -3.907245e-03
## 2013-01-31 -2.566592e-03
## 2013-02-01  1.000251e-02
## 2013-02-04 -1.160583e-02
## 2013-02-05  1.036263e-02
```

2013-02-06 5.490198e-04
2013-02-07 -1.807031e-03
2013-02-08 5.641995e-03
2013-02-11 -6.063013e-04
2013-02-12 1.594001e-03
2013-02-13 5.920875e-04
2013-02-14 6.904334e-04
2013-02-15 -1.045628e-03
2013-02-19 7.309694e-03
2013-02-20 -1.248171e-02
2013-02-21 -6.323005e-03
2013-02-22 8.734214e-03
2013-02-25 -1.847928e-02
2013-02-26 6.090876e-03
2013-02-27 1.264570e-02
2013-02-28 -8.644531e-04
2013-03-01 2.321159e-03
2013-03-04 4.600127e-03
2013-03-05 9.520552e-03
2013-03-06 1.083925e-03
2013-03-07 1.814844e-03
2013-03-08 4.471129e-03
2013-03-11 3.243819e-03
2013-03-12 -2.406146e-03
2013-03-13 1.313190e-03
2013-03-14 5.587352e-03
2013-03-15 -1.619774e-03
2013-03-18 -5.525570e-03
2013-03-19 -2.425470e-03
2013-03-20 6.675164e-03
2013-03-21 -8.316924e-03
2013-03-22 7.148644e-03
2013-03-25 -3.345630e-03
2013-03-26 7.754964e-03
2013-03-27 -5.885231e-04
2013-03-28 4.048463e-03
2013-04-01 -4.483617e-03
2013-04-02 5.158934e-03
2013-04-03 -1.060213e-02
2013-04-04 4.040279e-03
2013-04-05 -4.304145e-03
2013-04-08 6.282959e-03
2013-04-09 3.538066e-03
2013-04-10 1.211544e-02
2013-04-11 3.545956e-03
2013-04-12 -2.840798e-03
2013-04-15 -2.323413e-02
2013-04-16 1.420584e-02
2013-04-17 -1.443131e-02
2013-04-18 -6.723556e-03
2013-04-19 8.808989e-03
2013-04-22 4.650798e-03
2013-04-23 1.036531e-02
2013-04-24 6.340319e-06

2013-04-25 4.026614e-03
2013-04-26 -1.843812e-03
2013-04-29 7.160315e-03
2013-04-30 2.481817e-03
2013-05-01 -9.351473e-03
2013-05-02 9.364004e-03
2013-05-03 1.047956e-02
2013-05-06 1.905961e-03
2013-05-07 5.216639e-03
2013-05-08 4.130539e-03
2013-05-09 -3.693918e-03
2013-05-10 4.312344e-03
2013-05-13 4.288884e-05
2013-05-14 1.009107e-02
2013-05-15 5.101103e-03
2013-05-16 -5.022332e-03
2013-05-17 1.024741e-02
2013-05-20 -7.078686e-04
2013-05-21 1.720905e-03
2013-05-22 -8.308074e-03
2013-05-23 -2.928115e-03
2013-05-24 -5.515174e-04
2013-05-28 6.320962e-03
2013-05-29 -7.072937e-03
2013-05-30 3.663625e-03
2013-05-31 -1.441058e-02
2013-06-03 5.918440e-03
2013-06-04 -5.526048e-03
2013-06-05 -1.387555e-02
2013-06-06 8.454455e-03
2013-06-07 1.274991e-02
2013-06-10 -3.468734e-04
2013-06-11 -1.020526e-02
2013-06-12 -8.404777e-03
2013-06-13 1.467607e-02
2013-06-14 -5.902401e-03
2013-06-17 7.538876e-03
2013-06-18 7.760964e-03
2013-06-19 -1.394830e-02
2013-06-20 -2.532842e-02
2013-06-21 2.666219e-03
2013-06-24 -1.221937e-02
2013-06-25 9.452456e-03
2013-06-26 9.544790e-03
2013-06-27 6.180691e-03
2013-06-28 -4.298789e-03
2013-07-01 5.389200e-03
2013-07-02 -5.450568e-04
2013-07-03 8.237078e-04
2013-07-05 1.015005e-02
2013-07-08 5.237805e-03
2013-07-09 7.203662e-03
2013-07-10 1.815761e-04
2013-07-11 1.346321e-02

2013-07-12 3.081730e-03
2013-07-15 1.373935e-03
2013-07-16 -3.715655e-03
2013-07-17 2.770206e-03
2013-07-18 5.020342e-03
2013-07-19 1.608756e-03
2013-07-22 2.030962e-03
2013-07-23 -1.853653e-03
2013-07-24 -3.818503e-03
2013-07-25 2.553210e-03
2013-07-26 8.279512e-04
2013-07-29 -3.743034e-03
2013-07-30 3.737472e-04
2013-07-31 -1.364188e-04
2013-08-01 1.246259e-02
2013-08-02 1.639114e-03
2013-08-05 -1.480931e-03
2013-08-06 -5.739473e-03
2013-08-07 -3.813126e-03
2013-08-08 3.877921e-03
2013-08-09 -3.576348e-03
2013-08-12 -1.153586e-03
2013-08-13 2.772210e-03
2013-08-14 -5.190063e-03
2013-08-15 -1.438457e-02
2013-08-16 -3.310067e-03
2013-08-19 -5.917778e-03
2013-08-20 3.813913e-03
2013-08-21 -5.796370e-03
2013-08-22 8.582442e-03
2013-08-23 3.939242e-03
2013-08-26 -4.047839e-03
2013-08-27 -1.600154e-02
2013-08-28 2.743878e-03
2013-08-29 1.961477e-03
2013-08-30 -3.179367e-03
2013-09-03 4.155575e-03
2013-09-04 8.084188e-03
2013-09-05 1.209132e-03
2013-09-06 5.442973e-05
2013-09-09 9.943282e-03
2013-09-10 7.318940e-03
2013-09-11 3.047635e-03
2013-09-12 -3.386142e-03
2013-09-13 2.711001e-03
2013-09-16 5.677009e-03
2013-09-17 4.208869e-03
2013-09-18 1.210412e-02
2013-09-19 -1.844654e-03
2013-09-20 -7.243054e-03
2013-09-23 -4.730759e-03
2013-09-24 -2.600522e-03
2013-09-25 -2.743225e-03
2013-09-26 3.479366e-03

2013-09-27 -4.082122e-03
2013-09-30 -6.047480e-03
2013-10-01 7.966725e-03
2013-10-02 -6.668919e-04
2013-10-03 -9.019973e-03
2013-10-04 7.028467e-03
2013-10-07 -8.542748e-03
2013-10-08 -1.240875e-02
2013-10-09 5.737416e-04
2013-10-10 2.159562e-02
2013-10-11 6.266595e-03
2013-10-14 4.066441e-03
2013-10-15 -7.088790e-03
2013-10-16 1.373280e-02
2013-10-17 6.721314e-03
2013-10-18 6.527406e-03
2013-10-21 9.173211e-05
2013-10-22 5.721116e-03
2013-10-23 -4.735753e-03
2013-10-24 3.252838e-03
2013-10-25 4.385215e-03
2013-10-28 1.328816e-03
2013-10-29 5.568661e-03
2013-10-30 -4.887849e-03
2013-10-31 -3.846771e-03
2013-11-01 2.899215e-03
2013-11-04 3.564199e-03
2013-11-05 -2.809531e-03
2013-11-06 4.256468e-03
2013-11-07 -1.327044e-02
2013-11-08 1.333821e-02
2013-11-11 7.226705e-04
2013-11-12 -2.373206e-03
2013-11-13 8.062753e-03
2013-11-14 4.825597e-03
2013-11-15 4.213147e-03
2013-11-18 -3.705053e-03
2013-11-19 -2.045055e-03
2013-11-20 -3.642236e-03
2013-11-21 8.095706e-03
2013-11-22 4.949190e-03
2013-11-25 -1.264141e-03
2013-11-26 1.497935e-04
2013-11-27 2.481998e-03
2013-11-29 -7.859980e-04
2013-12-02 -2.722724e-03
2013-12-03 -3.197956e-03
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2013-12-05 -4.349016e-03
2013-12-06 1.117520e-02
2013-12-09 1.815451e-03
2013-12-10 -3.184725e-03
2013-12-11 -1.138140e-02
2013-12-12 -3.777689e-03

2013-12-13 -1.014154e-04
2013-12-16 6.300152e-03
2013-12-17 -3.105806e-03
2013-12-18 1.651091e-02
2013-12-19 -5.800970e-04
2013-12-20 4.807155e-03
2013-12-23 5.304029e-03
2013-12-24 2.911504e-03
2013-12-26 4.734305e-03
2013-12-27 -3.366415e-04
2013-12-30 -1.792699e-04
2013-12-31 3.951856e-03
2014-01-02 -8.901413e-03
2014-01-03 -3.330203e-04
2014-01-06 -2.514927e-03
2014-01-07 6.063345e-03
2014-01-08 -2.122317e-04
2014-01-09 3.482487e-04
2014-01-10 2.304030e-03
2014-01-13 -1.265597e-02
2014-01-14 1.075988e-02
2014-01-15 5.152889e-03
2014-01-16 -1.348028e-03
2014-01-17 -3.902781e-03
2014-01-21 2.769912e-03
2014-01-22 5.746998e-04
2014-01-23 -8.929325e-03
2014-01-24 -2.109642e-02
2014-01-27 -4.888222e-03
2014-01-28 6.121875e-03
2014-01-29 -1.026170e-02
2014-01-30 1.120404e-02
2014-01-31 -6.486290e-03
2014-02-03 -2.309660e-02
2014-02-04 7.612043e-03
2014-02-05 -2.030282e-03
2014-02-06 1.236305e-02
2014-02-07 1.321419e-02
2014-02-10 1.568005e-03
2014-02-11 1.100138e-02
2014-02-12 -2.692985e-04
2014-02-13 5.793212e-03
2014-02-14 4.797689e-03
2014-02-18 1.157803e-03
2014-02-19 -6.545862e-03
2014-02-20 6.013342e-03
2014-02-21 -1.920567e-03
2014-02-24 6.167455e-03
2014-02-25 -1.348591e-03
2014-02-26 2.169971e-05
2014-02-27 4.935881e-03
2014-02-28 2.778824e-03
2014-03-03 -7.405866e-03
2014-03-04 1.515232e-02

2014-03-05 -5.335244e-05
2014-03-06 1.716933e-03
2014-03-07 5.379447e-04
2014-03-10 -4.633536e-04
2014-03-11 -5.095097e-03
2014-03-12 3.051242e-04
2014-03-13 -1.177009e-02
2014-03-14 -2.825766e-03
2014-03-17 9.567718e-03
2014-03-18 7.193682e-03
2014-03-19 -6.150525e-03
2014-03-20 6.022334e-03
2014-03-21 -2.936980e-03
2014-03-24 -4.876581e-03
2014-03-25 4.394271e-03
2014-03-26 -7.024937e-03
2014-03-27 -1.901892e-03
2014-03-28 4.629489e-03
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2014-04-04 -1.261654e-02
2014-04-07 -1.080831e-02
2014-04-08 3.743538e-03
2014-04-09 1.085904e-02
2014-04-10 -2.110597e-02
2014-04-11 -9.532060e-03
2014-04-14 8.183708e-03
2014-04-15 6.734579e-03
2014-04-16 1.043387e-02
2014-04-17 1.362924e-03
2014-04-21 3.768016e-03
2014-04-22 4.083789e-03
2014-04-23 -2.215767e-03
2014-04-24 1.715488e-03
2014-04-25 -8.129345e-03
2014-04-28 3.230812e-03
2014-04-29 4.749460e-03
2014-04-30 2.987550e-03
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2014-05-05 1.869467e-03
2014-05-06 -9.029031e-03
2014-05-07 5.600755e-03
2014-05-08 -1.374569e-03
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2014-05-13 4.216689e-04
2014-05-14 -4.712090e-03
2014-05-15 -9.405904e-03
2014-05-16 3.739962e-03
2014-05-19 3.837414e-03
2014-05-20 -6.519605e-03

2014-05-21 8.083340e-03
2014-05-22 2.359444e-03
2014-05-23 4.239393e-03
2014-05-27 5.969950e-03
2014-05-28 -1.114693e-03
2014-05-29 5.352759e-03
2014-05-30 1.841980e-03
2014-06-02 7.275617e-04
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2014-06-10 -2.460142e-04
2014-06-11 -3.543311e-03
2014-06-12 -7.114139e-03
2014-06-13 3.129659e-03
2014-06-16 8.363553e-04
2014-06-17 2.170212e-03
2014-06-18 7.689243e-03
2014-06-19 1.276663e-03
2014-06-20 1.728564e-03
2014-06-23 -1.324730e-04
2014-06-24 -6.456107e-03
2014-06-25 4.885558e-03
2014-06-26 -1.179579e-03
2014-06-27 1.909045e-03
2014-06-30 -3.723263e-04
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2014-07-02 6.585962e-04
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2014-07-08 -7.073762e-03
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2014-07-14 4.831861e-03
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2014-07-17 -1.190461e-02
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2014-07-25 -4.860946e-03
2014-07-28 2.881132e-04
2014-07-29 -4.538068e-03
2014-07-30 6.091086e-05
2014-07-31 -2.020193e-02
2014-08-01 -2.863216e-03
2014-08-04 7.163315e-03
2014-08-05 -9.732679e-03
2014-08-06 1.563827e-05

2014-08-07 -5.572115e-03
2014-08-08 1.146542e-02
2014-08-11 2.755625e-03
2014-08-12 -1.637982e-03
2014-08-13 6.684767e-03
2014-08-14 4.336398e-03
2014-08-15 -6.137475e-05
2014-08-18 8.495483e-03
2014-08-19 4.988191e-03
2014-08-20 2.474748e-03
2014-08-21 2.945547e-03
2014-08-22 -1.994575e-03
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2014-08-27 4.998575e-05
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2014-08-29 3.314914e-03
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2014-09-24 7.801977e-03
2014-09-25 -1.630091e-02
2014-09-26 8.539261e-03
2014-09-29 -2.550051e-03
2014-09-30 -2.789817e-03
2014-10-01 -1.333711e-02
2014-10-02 5.143449e-06
2014-10-03 1.110364e-02
2014-10-06 -1.566386e-03
2014-10-07 -1.524162e-02
2014-10-08 1.731095e-02
2014-10-09 -2.087785e-02
2014-10-10 -1.151708e-02
2014-10-13 -1.660503e-02
2014-10-14 1.577620e-03
2014-10-15 -8.133301e-03
2014-10-16 1.449675e-04
2014-10-17 1.280181e-02
2014-10-20 9.101116e-03
2014-10-21 1.938537e-02
2014-10-22 -7.326101e-03

```
## 2014-10-23 1.222831e-02
## 2014-10-24 7.028690e-03
## 2014-10-27 -1.502697e-03
## 2014-10-28 1.186836e-02
## 2014-10-29 -1.386316e-03
## 2014-10-30 6.210797e-03
## 2014-10-31 1.166311e-02
## 2014-11-03 -1.189288e-04
## 2014-11-04 -2.833853e-03
## 2014-11-05 5.684311e-03
## 2014-11-06 3.768404e-03
## 2014-11-07 3.495251e-04
## 2014-11-10 3.115327e-03
## 2014-11-11 6.964517e-04
## 2014-11-12 -7.013627e-04
## 2014-11-13 5.297044e-04
## 2014-11-14 2.402412e-04
## 2014-11-17 7.350888e-04
## 2014-11-18 5.120850e-03
## 2014-11-19 -1.502287e-03
## 2014-11-20 1.965164e-03
## 2014-11-21 5.223213e-03
## 2014-11-24 2.859930e-03
## 2014-11-25 -1.150692e-03
## 2014-11-26 2.802053e-03
## 2014-11-28 -2.545664e-03
## 2014-12-01 -6.852790e-03
## 2014-12-02 6.364167e-03
## 2014-12-03 3.757674e-03
## 2014-12-04 -1.162572e-03
## 2014-12-05 1.663831e-03
## 2014-12-08 -7.283022e-03
## 2014-12-09 -2.378522e-04
## 2014-12-10 -1.648612e-02
## 2014-12-11 4.525434e-03
## 2014-12-12 -1.634647e-02
## 2014-12-15 -6.362786e-03
## 2014-12-16 -8.525260e-03
## 2014-12-17 2.014807e-02
## 2014-12-18 2.373137e-02
## 2014-12-19 4.559638e-03
## 2014-12-22 3.803223e-03
## 2014-12-23 1.744839e-03
## 2014-12-24 -1.393062e-04
## 2014-12-26 3.304110e-03
## 2014-12-29 8.614030e-04
## 2014-12-30 -4.900593e-03
## 2014-12-31 -1.036438e-02
```

```
#Stationarity test
```

```
library(tseries)
```

```
adf.test(log_ret, alternative = "stationary")
```

```
## Warning in adf.test(log_ret, alternative = "stationary"): p-value smaller than
## printed p-value
```



```
## [297] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [334] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [371] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [408] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [445] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [482] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
```

```
df_dummies=matrix(c(d1,d2), ncol = 2)
```

Fitting GARCH models:

```
# GARCH MODELS assuming a Normal distribution
#sGARCH
library(rugarch)

s_garchMod <- ugarchspec(mean.model = list(armaOrder = c(1, 0), include.mean = TRUE
),
variance.model = list(model = 'sGARCH',
                      garchOrder = c(1, 1),
                      external.regressors = df_dummies
),
distribution.model = "norm")

s_garchFit <- ugarchfit(spec=s_garchMod, data=log_ret)
s_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : sGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : norm
##
## Optimal Parameters
## -----
##      Estimate  Std. Error  t value Pr(>|t|)
## mu      0.000840   0.000066  12.7866 0.000000
## ar1     -0.053777   0.026972  -1.9938 0.046176
## omega    0.000008   0.000000  17.0431 0.000000
## alpha1   0.201098   0.018897  10.6419 0.000000
## beta1    0.624838   0.029982  20.8404 0.000000
## vxreg1    0.000008   0.000001  15.2650 0.000000
## vxreg2    0.000001   0.000000 1085.2129 0.000000
##
## Robust Standard Errors:
##      Estimate  Std. Error  t value Pr(>|t|)
## mu      0.000840   0.000202   4.1497 0.000033
## ar1     -0.053777   0.048501  -1.1088 0.267524
## omega    0.000008   0.000001  11.5665 0.000000
## alpha1   0.201098   0.049469   4.0651 0.000048
## beta1    0.624838   0.030416  20.5431 0.000000
```



```

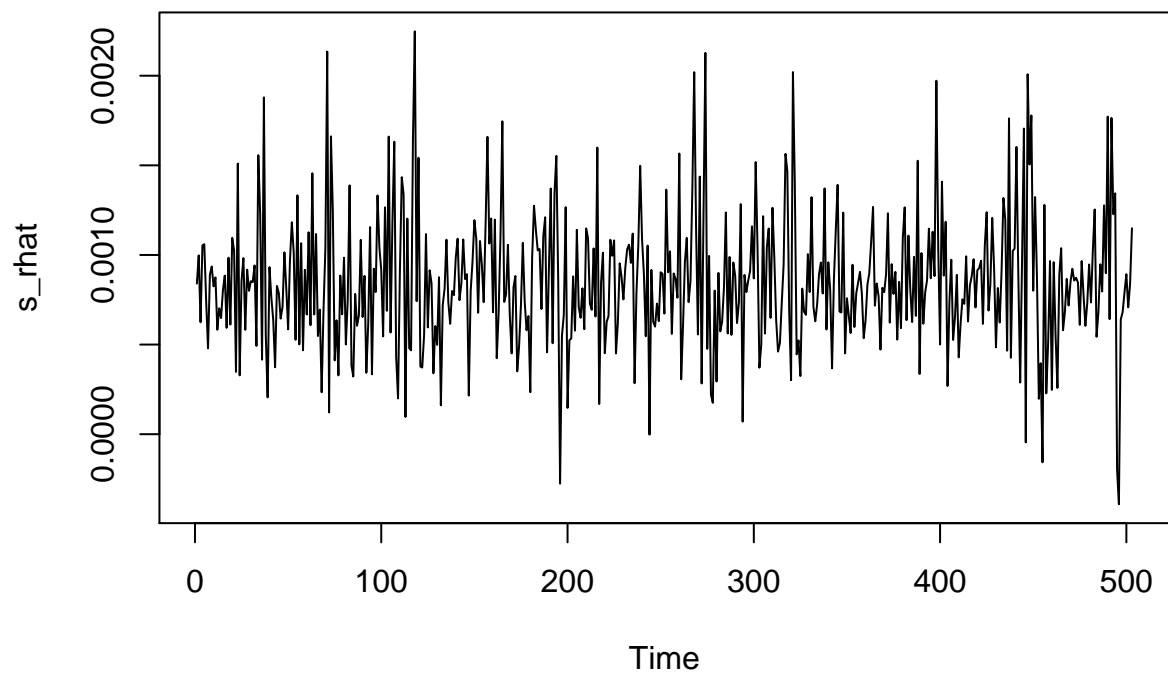
## vxreg1 0.000008 0.000001 10.2110 0.000000
## vxreg2 0.000001 0.000000 705.9982 0.000000
##
## LogLikelihood : 1807.367
##
## Information Criteria
## -----
##
## Akaike -7.1585
## Bayes -7.0998
## Shibata -7.1589
## Hannan-Quinn -7.1355
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
## statistic p-value
## Lag[1] 0.09561 0.7572
## Lag[2*(p+q)+(p+q)-1][2] 0.19632 0.9989
## Lag[4*(p+q)+(p+q)-1][5] 0.67587 0.9834
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
## statistic p-value
## Lag[1] 0.4936 0.4823
## Lag[2*(p+q)+(p+q)-1][5] 0.8012 0.9028
## Lag[4*(p+q)+(p+q)-1][9] 1.8493 0.9222
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##
## Statistic Shape Scale P-Value
## ARCH Lag[3] 0.1056 0.500 2.000 0.7452
## ARCH Lag[5] 0.6622 1.440 1.667 0.8349
## ARCH Lag[7] 1.1364 2.315 1.543 0.8904
##
## Nyblom stability test
## -----
## Joint Statistic: 19.2901
## Individual Statistics:
## mu 0.05189
## ar1 0.19398
## omega 3.70110
## alpha1 0.08649
## beta1 0.06999
## vxreg1 2.81711
## vxreg2 2.65670
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test

```

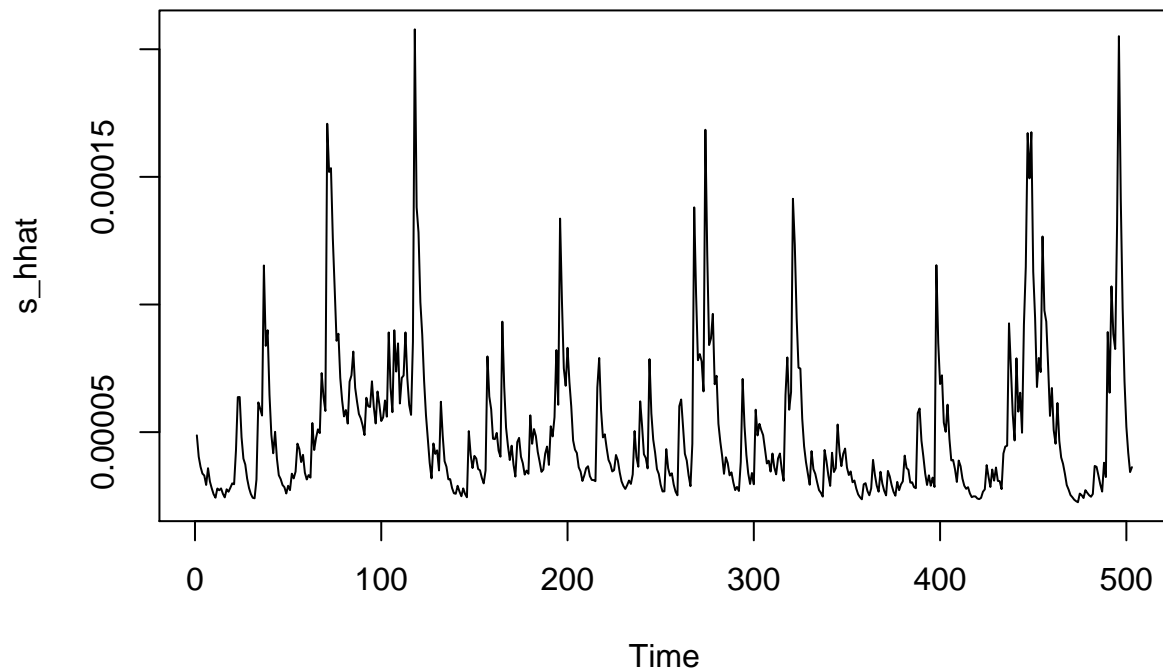
```
## -----
##               t-value   prob sig
## Sign Bias      2.4809 0.01344 **
## Negative Sign Bias 0.9585 0.33828
## Positive Sign Bias 0.2047 0.83788
## Joint Effect    9.3361 0.02514 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      32.63   0.026537
## 2    30      45.53   0.026122
## 3    40      65.35   0.005149
## 4    50      79.60   0.003710
##
##
## Elapsed time : 0.2375741
## Results review 1
coef(s_garchFit)

##           mu           ar1           omega           alpha1           beta1
## 8.402561e-04 -5.377668e-02 8.186756e-06 2.010979e-01 6.248384e-01
##           vxreg1           vxreg2
## 7.715679e-06 1.015541e-06

s_rhat <- s_garchFit@fit$fitted.values
plot.ts(s_rhat)
```



```
s_hhat <- ts(s_garchFit@fit$sigma^2)
plot.ts(s_hhat)
```



```
## Results review 2
```

```
fit.val      <- coef(s_garchFit)
fit.sd       <- diag(vcov(s_garchFit))
true.val = s_garchFit@fit$tval
```

```
fit.conf.lb <- fit.val + qnorm(0.025) * fit.sd
fit.conf.ub <- fit.val + qnorm(0.975) * fit.sd
print(fit.val)
```

```
##           mu           ar1           omega           alpha1           beta1
## 8.402561e-04 -5.377668e-02 8.186756e-06 2.010979e-01 6.248384e-01
##      vxreg1      vxreg2
## 7.715679e-06 1.015541e-06
```

```
print(fit.sd)
```

```
## [1] -4.318315e-09 7.275002e-04 -2.307418e-13 -3.570861e-04 8.989237e-04
## [6] -2.554793e-13 -8.757194e-19
```

```
print(true.val)
```

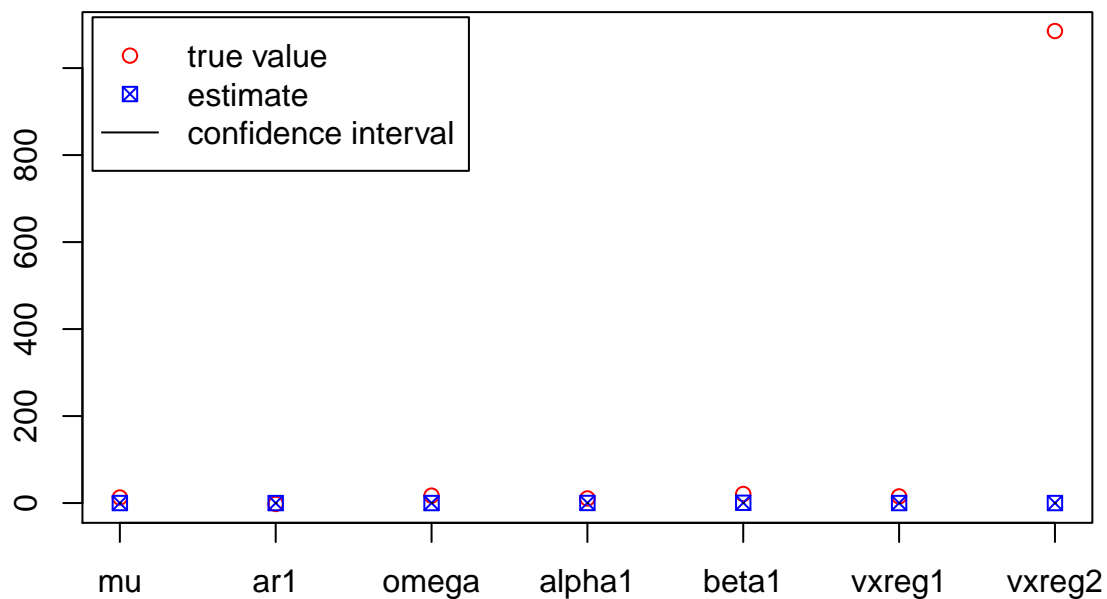
```
##           mu           ar1           omega           alpha1           beta1      vxreg1
## 12.786583    -1.993781    17.043105    10.641945    20.840414    15.264980
##      vxreg2
## 1085.212918
```

```
plot(true.val, pch = 1, col = "red",
      ylim = range(c(fit.conf.lb, fit.conf.ub, true.val)),
```

```

      xlab = "", ylab = "", axes = FALSE)
box(); axis(1, at = 1:length(fit.val), labels = names(fit.val)); axis(2)
points(coef(s_garchFit), col = "blue", pch = 7)
for (i in 1:length(fit.val)) {
  lines(c(i,i), c(fit.conf.lb[i], fit.conf.ub[i]))
}
legend( "topleft", legend = c("true value", "estimate", "confidence interval"),
      col = c("red", "blue", 1), pch = c(1, 7, NA), lty = c(NA, NA, 1), inset = 0.01)

```



```

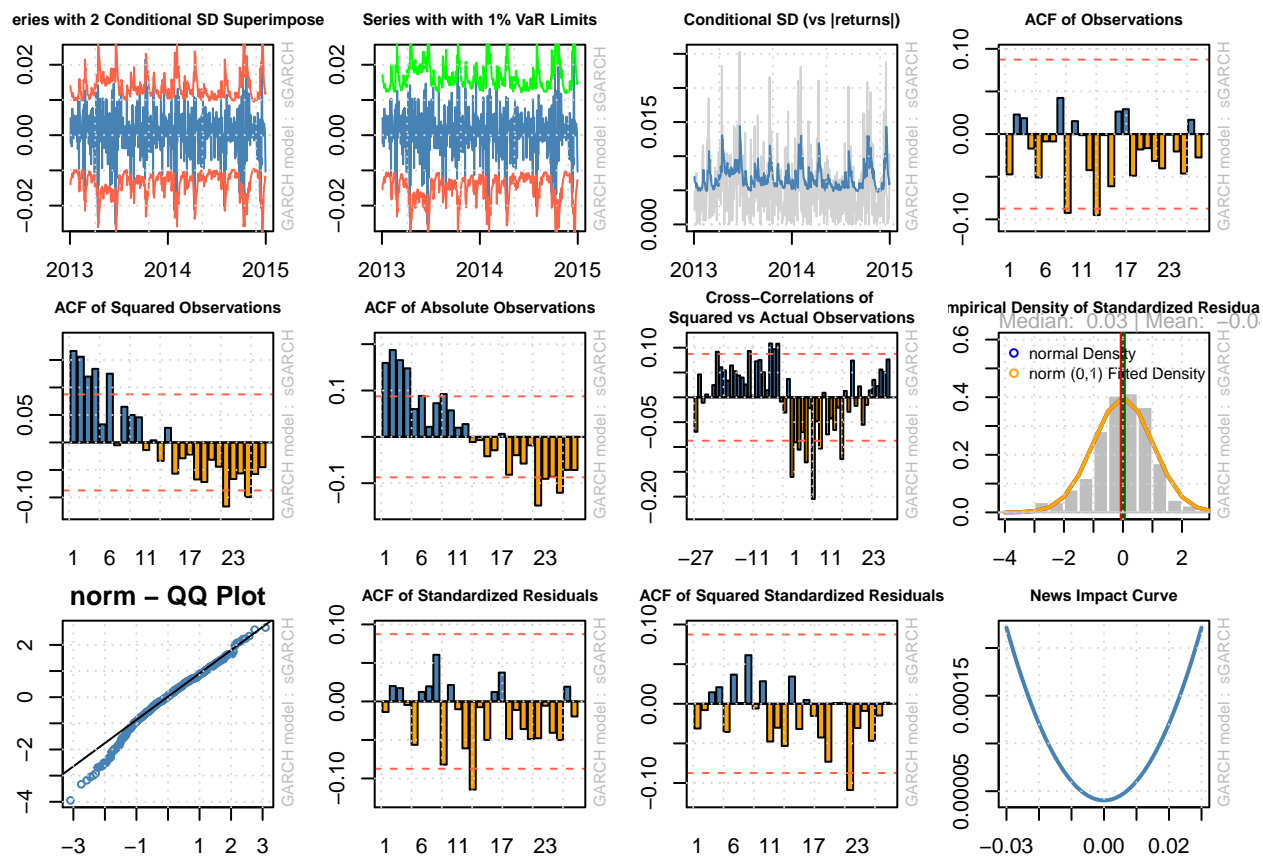
par(mfrow=c(2, 3))
par(mar = c(2, 2, 2, 2))
plot(s_garchFit,which="all")

```

```

##
## please wait...calculating quantiles...

```



```
#gjrGARCH
gjr_garchMod <- ugarchspec(
  variance.model=list(model="gjrGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE),
  distribution.model="norm"
)
gjr_garchFit <- ugarchfit(spec=gjr_garchMod, data=log_ret)
coef(gjr_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 6.013808e-04 -5.079000e-02 5.094779e-06 1.127093e-08 7.230763e-01
##          gamma1          vxreg1          vxreg2
## 3.238522e-01 7.249355e-06 9.747307e-07
```

```
gjr_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,1)
```

```

## Mean Model      : ARFIMA(1,0,0)
## Distribution    : norm
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000601   0.000117   5.16171 0.000000
## ar1     -0.050790   0.058495  -0.86828 0.385242
## omega    0.000005   0.000001   4.22847 0.000024
## alpha1   0.000000   0.023316   0.00000 1.000000
## beta1    0.723076   0.065324  11.06903 0.000000
## gamma1   0.323852   0.135816   2.38448 0.017103
## vxreg1   0.000007   0.000006   1.21559 0.224142
## vxreg2   0.000001   0.000000  152.56273 0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000601   0.000198   3.04198 0.002350
## ar1     -0.050790   0.132782  -0.38251 0.702086
## omega    0.000005   0.000003   1.47590 0.139971
## alpha1   0.000000   0.052155   0.00000 1.000000
## beta1    0.723076   0.178994   4.03967 0.000054
## gamma1   0.323852   0.373783   0.86642 0.386261
## vxreg1   0.000007   0.000017   0.42914 0.667820
## vxreg2   0.000001   0.000000  27.39545 0.000000
##
## LogLikelihood : 1819.663
##
## Information Criteria
## -----
##
## Akaike          -7.2034
## Bayes           -7.1363
## Shibata         -7.2039
## Hannan-Quinn   -7.1771
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.0142 0.9051
## Lag[2*(p+q)+(p+q)-1] [2] 0.2162 0.9984
## Lag[4*(p+q)+(p+q)-1] [5] 0.7039 0.9812
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.025 0.3114
## Lag[2*(p+q)+(p+q)-1] [5] 2.505 0.5049
## Lag[4*(p+q)+(p+q)-1] [9] 3.873 0.6104
## d.o.f=2
##
## Weighted ARCH LM Tests

```

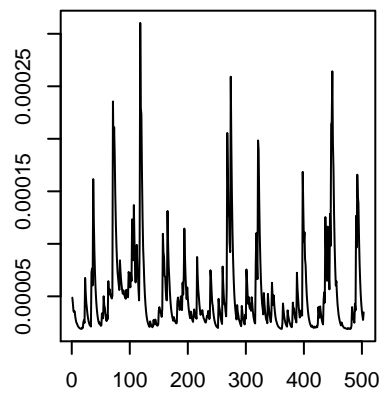
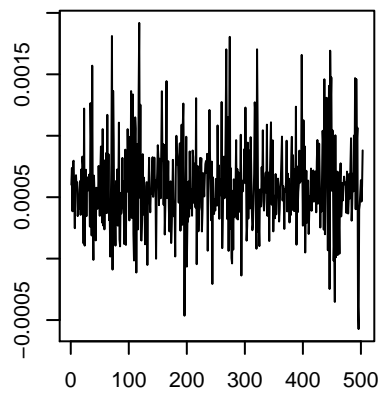
```

## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3] 0.0009615 0.500 2.000 0.9753
## ARCH Lag[5] 1.4261671 1.440 1.667 0.6119
## ARCH Lag[7] 1.7484958 2.315 1.543 0.7704
##
## Nyblom stability test
## -----
## Joint Statistic: 18.4937
## Individual Statistics:
## mu      0.04812
## ar1     0.28110
## omega   4.57960
## alpha1  0.35133
## beta1   0.03505
## gamma1  0.13483
## vxreg1  2.25484
## vxreg2  1.99854
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      2.8470 0.004596 ***
## Negative Sign Bias 2.0161 0.044321 **
## Positive Sign Bias 0.7082 0.479165
## Joint Effect      9.4240 0.024153 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      42.33   0.0016002
## 2    30      55.91   0.0019389
## 3    40      69.17   0.0020635
## 4    50     100.28   0.0000219
##
##
## Elapsed time : 0.5109761

gjr_rhat <- gjr_garchFit@fit$fitted.values
plot.ts(gjr_rhat)
gjr_hhat <- ts(gjr_garchFit@fit$sigma^2)
plot.ts(gjr_hhat)

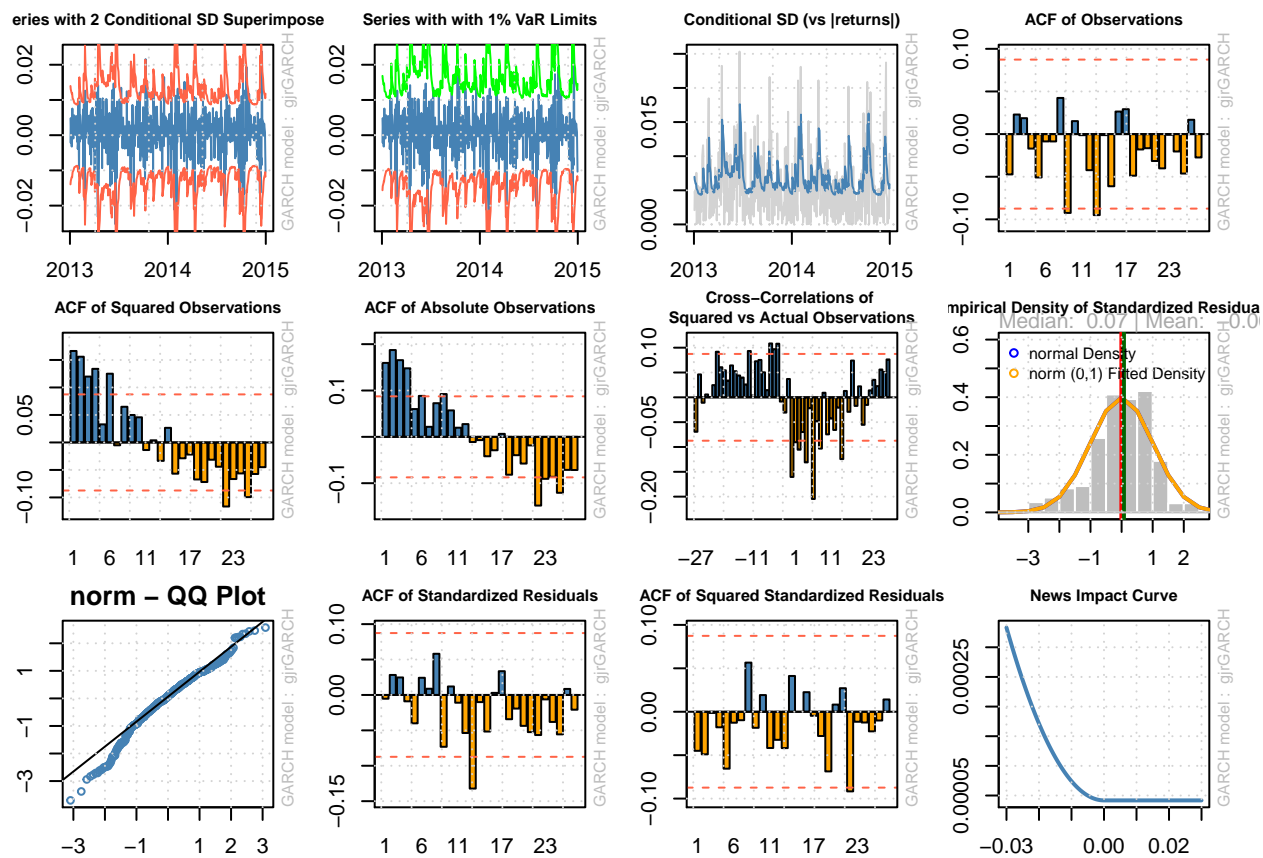
par(mfrow=c(2, 3))

```

```
par(mar = c(2, 2, 2, 2))  
plot(gjr_garchFit,which="all")
```

```
##  
## please wait...calculating quantiles...
```



```
#eGARCH
e_garchMod <- ugarchspec(
  variance.model=list(model="eGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="norm"
)
e_garchFit <- ugarchfit(spec=e_garchMod, data=log_ret)
coef(e_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 0.0004433548 -0.0384901499 -0.8373357009 -0.3060358058 0.9174478258
##          gamma1          vxreg1          vxreg2
## 0.0049793591 0.0702686146 0.0155810130
```

```
e_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : eGARCH(1,1)
```

```

## Mean Model      : ARFIMA(1,0,0)
## Distribution    : norm
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000443   0.000212    2.09038 0.036584
## ar1     -0.038490   0.046133   -0.83432 0.404099
## omega   -0.837336   0.013444  -62.28355 0.000000
## alpha1  -0.306036   0.031828   -9.61545 0.000000
## beta1    0.917448   0.000130 7079.54844 0.000000
## gamma1   0.004979   0.036065    0.13807 0.890187
## vxreg1   0.070269   0.022581    3.11192 0.001859
## vxreg2   0.015581   0.013590    1.14652 0.251580
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000443   0.000208    2.12931 0.033229
## ar1     -0.038490   0.051070   -0.75367 0.451045
## omega   -0.837336   0.014679  -57.04207 0.000000
## alpha1  -0.306036   0.033679   -9.08689 0.000000
## beta1    0.917448   0.000130 7071.33530 0.000000
## gamma1   0.004979   0.037696    0.13209 0.894910
## vxreg1   0.070269   0.022280    3.15388 0.001611
## vxreg2   0.015581   0.013468    1.15691 0.247309
##
## LogLikelihood : 1832.049
##
## Information Criteria
## -----
##
## Akaike          -7.2527
## Bayes           -7.1856
## Shibata         -7.2532
## Hannan-Quinn   -7.2263
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.1391 0.7092
## Lag[2*(p+q)+(p+q)-1] [2] 0.3472 0.9901
## Lag[4*(p+q)+(p+q)-1] [5] 0.9200 0.9581
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.004206 0.9483
## Lag[2*(p+q)+(p+q)-1] [5] 0.876356 0.8870
## Lag[4*(p+q)+(p+q)-1] [9] 1.980296 0.9073
## d.o.f=2
##
## Weighted ARCH LM Tests

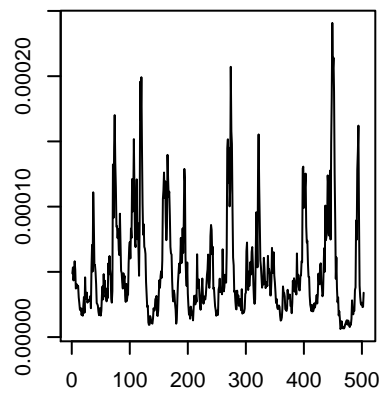
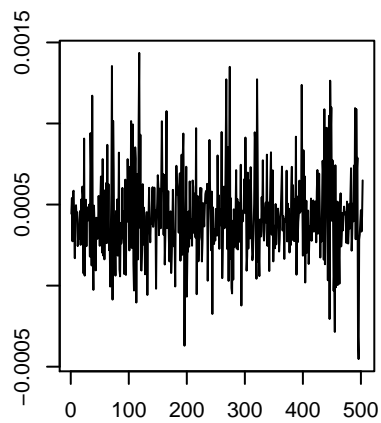
```

```

## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.7896 0.500 2.000 0.3742
## ARCH Lag[5]    1.9101 1.440 1.667 0.4915
## ARCH Lag[7]    2.2172 2.315 1.543 0.6714
##
## Nyblom stability test
## -----
## Joint Statistic: 1.2258
## Individual Statistics:
## mu      0.14122
## ar1     0.10416
## omega   0.10126
## alpha1  0.28898
## beta1   0.10825
## gamma1  0.29500
## vxreg1  0.01462
## vxreg2  0.01992
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value   prob sig
## Sign Bias      2.427 0.01556 **
## Negative Sign Bias 1.254 0.21043
## Positive Sign Bias 1.608 0.10845
## Joint Effect     5.999 0.11164
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      45.03   0.0006784
## 2    30      59.84   0.0006461
## 3    40      70.44   0.0015046
## 4    50      76.82   0.0067468
##
##
## Elapsed time : 0.924278
e_rhat <- e_garchFit@fit$fitted.values
plot.ts(e_rhat)
e_hhat <- ts(e_garchFit@fit$sigma^2)
plot.ts(e_hhat)

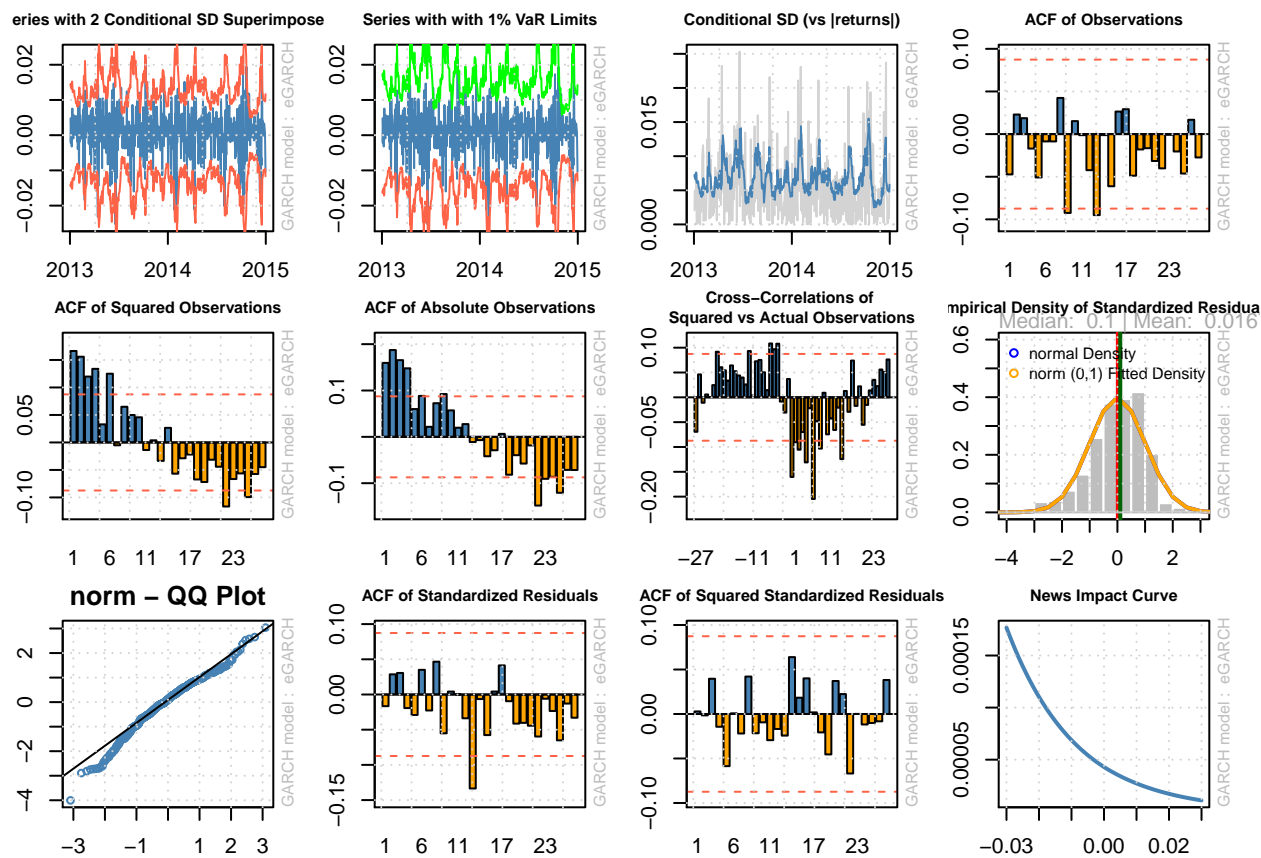
par(mfrow=c(2, 3))

```



```
par(mar = c(2, 2, 2, 2))  
plot(e_garchFit, which="all")
```

```
##  
## please wait...calculating quantiles...
```



```
# apARCH
apARCHMod <- ugarchspec(variance.model=list(model="apARCH",
                                             garchOrder=c(1,1),
                                             external.regressors = df_dummies ),
                        mean.model=list(armaOrder=c(1,0)),
                        distribution.model="norm")
apARCHFit <- ugarchfit(spec=apARCHMod, data= log_ret)
coef(apARCHFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 6.242414e-04 -3.546749e-02 1.875064e-08 6.259902e-02 6.520160e-01
##          gamma1          delta          vxreg1          vxreg2
## 6.260736e-01 3.111899e+00 4.802060e-08 1.265436e-08
```

```
apARCHFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : apARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
```

```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000624    0.000268   2.332026 0.019699
## ar1     -0.035467    0.050592  -0.701056 0.483268
## omega    0.000000    0.000000   0.071751 0.942800
## alpha1   0.062599    0.031673   1.976391 0.048110
## beta1    0.652016    0.012918  50.472089 0.000000
## gamma1   0.626074    0.229805   2.724366 0.006443
## delta    3.111899    0.033259  93.565469 0.000000
## vxreg1   0.000000    0.000001   0.069258 0.944784
## vxreg2   0.000000    0.000001   0.021642 0.982733
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000624    0.000654   0.955197 0.33948
## ar1     -0.035467    0.637195  -0.055662 0.95561
## omega    0.000000    0.000024   0.000774 0.99938
## alpha1   0.062599    0.167468   0.373796 0.70856
## beta1    0.652016    7.080015   0.092092 0.92663
## gamma1   0.626074    7.675691   0.081566 0.93499
## delta    3.111899    5.292779   0.587952 0.55656
## vxreg1   0.000000    0.000030   0.001577 0.99874
## vxreg2   0.000000    0.000028   0.000451 0.99964
##
## LogLikelihood : 1813.541
##
## Information Criteria
## -----
##
## Akaike          -7.1751
## Bayes           -7.0996
## Shibata         -7.1757
## Hannan-Quinn   -7.1455
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]                0.2314 0.6305
## Lag[2*(p+q)+(p+q)-1] [2] 0.4492 0.9752
## Lag[4*(p+q)+(p+q)-1] [5] 0.9864 0.9488
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]                0.7954 0.3725
## Lag[2*(p+q)+(p+q)-1] [5] 2.0776 0.6002
## Lag[4*(p+q)+(p+q)-1] [9] 3.2668 0.7142
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----

```

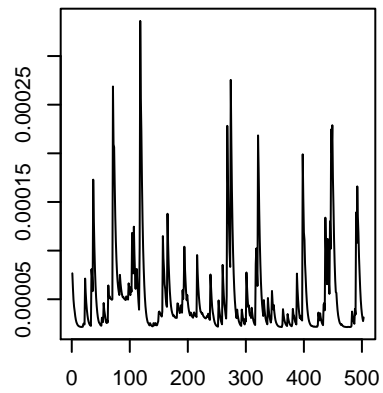
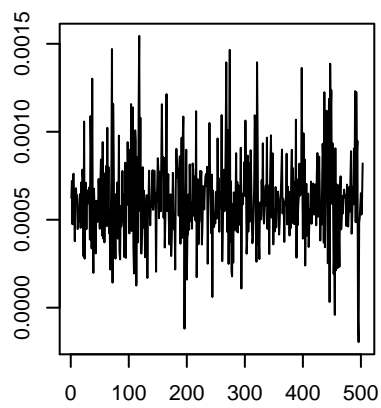
```

##          Statistic Shape Scale P-Value
## ARCH Lag[3] 1.629e-06 0.500 2.000 0.9990
## ARCH Lag[5] 1.001e+00 1.440 1.667 0.7327
## ARCH Lag[7] 1.213e+00 2.315 1.543 0.8767
##
## Nyblom stability test
## -----
## Joint Statistic: NaN
## Individual Statistics:
## mu      0.04770
## ar1     0.50384
## omega   29.08201
## alpha1  0.13025
## beta1   0.06022
## gamma1  0.10445
## delta   0.05598
## vxreg1   NaN
## vxreg2   NaN
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##          t-value      prob sig
## Sign Bias      2.9698 0.003124 ***
## Negative Sign Bias 1.9222 0.055146  *
## Positive Sign Bias 0.8558 0.392536
## Joint Effect      9.8702 0.019702  **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      46.70   3.940e-04
## 2    30      53.04   4.160e-03
## 3    40      81.89   7.046e-05
## 4    50      94.71   9.699e-05
##
##
## Elapsed time : 1.169584

apARCH_rhat <- apARCHFit@fit$fitted.values
plot.ts(apARCH_rhat)
apARCH_hhat <- ts(apARCHFit@fit$sigma^2)
plot.ts(apARCH_hhat)

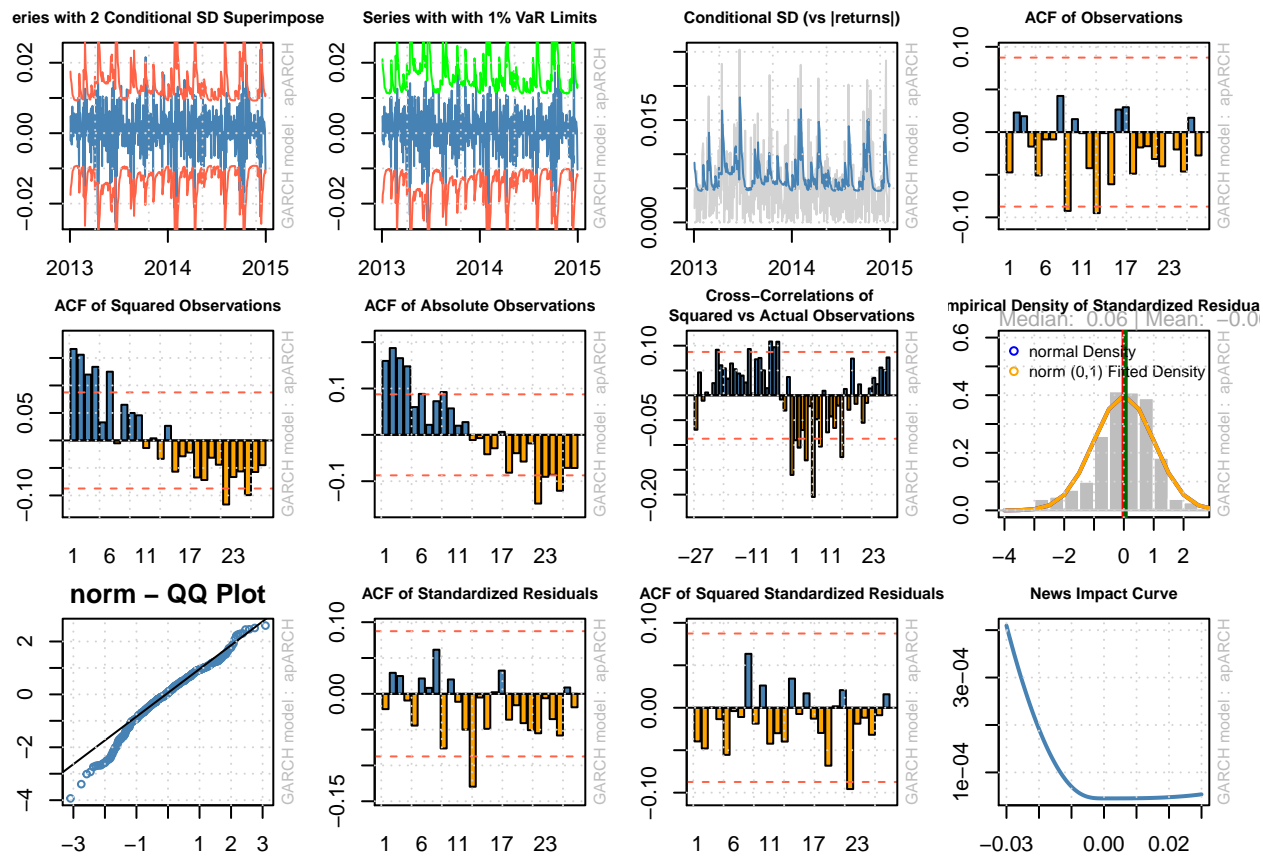
par(mfrow=c(2, 3))

```

```
par(mar = c(2, 2, 2, 2))  
plot(apARCHFit, which="all")
```

```
##  
## please wait...calculating quantiles...
```



```
# iGARCH
```

```
i_garchMod <- ugarchspec(variance.model=list(model="iGARCH",
                                             garchOrder=c(1,1),
                                             external.regressors = df_dummies ),
                        mean.model=list(armaOrder=c(1,0)),
                        distribution.model="norm")
i_garchFit <- ugarchfit(spec=i_garchMod, data= log_ret)
coef(i_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 9.053321e-04 -6.029347e-02 4.083878e-06 3.199365e-01 6.800635e-01
##          vxreg1          vxreg2
## 5.139090e-06 5.802993e-07
```

```
i_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : iGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : norm
##
```

```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value   Pr(>|t|)
## mu      0.000905    0.000004  237.2798  0.000000
## ar1     -0.060293    0.051343   -1.1743  0.240260
## omega    0.000004    0.000001    3.1447  0.001663
## alpha1   0.319936    0.018639   17.1649  0.000000
## beta1    0.680064         NA         NA         NA
## vxreg1   0.000005    0.000000  356.8550  0.000000
## vxreg2   0.000001    0.000000  229.0615  0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value   Pr(>|t|)
## mu      0.000905    0.000007  123.5023  0.000000
## ar1     -0.060293    0.052890   -1.1400  0.25430
## omega    0.000004    0.000003    1.5146  0.12987
## alpha1   0.319936    0.019301   16.5766  0.000000
## beta1    0.680064         NA         NA         NA
## vxreg1   0.000005    0.000000  354.0236  0.000000
## vxreg2   0.000001    0.000000   63.6517  0.000000
##
## LogLikelihood : 1800.636
##
## Information Criteria
## -----
##
## Akaike          -7.1357
## Bayes           -7.0854
## Shibata         -7.1360
## Hannan-Quinn   -7.1160
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.1921  0.6612
## Lag[2*(p+q)+(p+q)-1] [2]  0.2953  0.9946
## Lag[4*(p+q)+(p+q)-1] [5]  0.7580  0.9764
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.562  0.2114
## Lag[2*(p+q)+(p+q)-1] [5]  2.686  0.4674
## Lag[4*(p+q)+(p+q)-1] [9]  3.811  0.6210
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##
##      Statistic Shape Scale P-Value
## ARCH Lag[3]    0.08792 0.500 2.000  0.7668
## ARCH Lag[5]    1.10574 1.440 1.667  0.7018
## ARCH Lag[7]    1.41320 2.315 1.543  0.8386

```

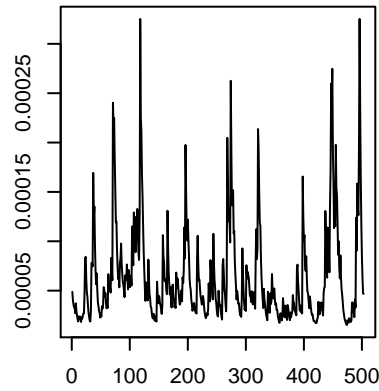
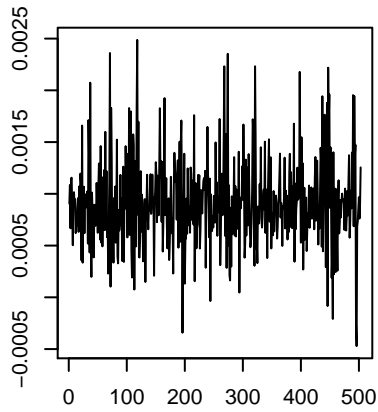
```

##
## Nyblom stability test
## -----
## Joint Statistic: 1.6731
## Individual Statistics:
## mu      0.05030
## ar1     0.30104
## omega   0.05761
## alpha1  0.09532
## vxreg1  0.01264
## vxreg2  1.05998
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##              t-value   prob sig
## Sign Bias      2.2288 0.02627 **
## Negative Sign Bias 1.8640 0.06292 *
## Positive Sign Bias 0.8016 0.42315
## Joint Effect    11.3449 0.01000 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      49.56   0.0001519
## 2    30      61.75   0.0003721
## 3    40      75.05   0.0004587
## 4    50      78.81   0.0044131
##
##
## Elapsed time : 0.2557809

i_rhat <- i_garchFit@fit$fitted.values
plot.ts(i_rhat)
i_hhat <- ts(i_garchFit@fit$sigma^2)
plot.ts(i_hhat)

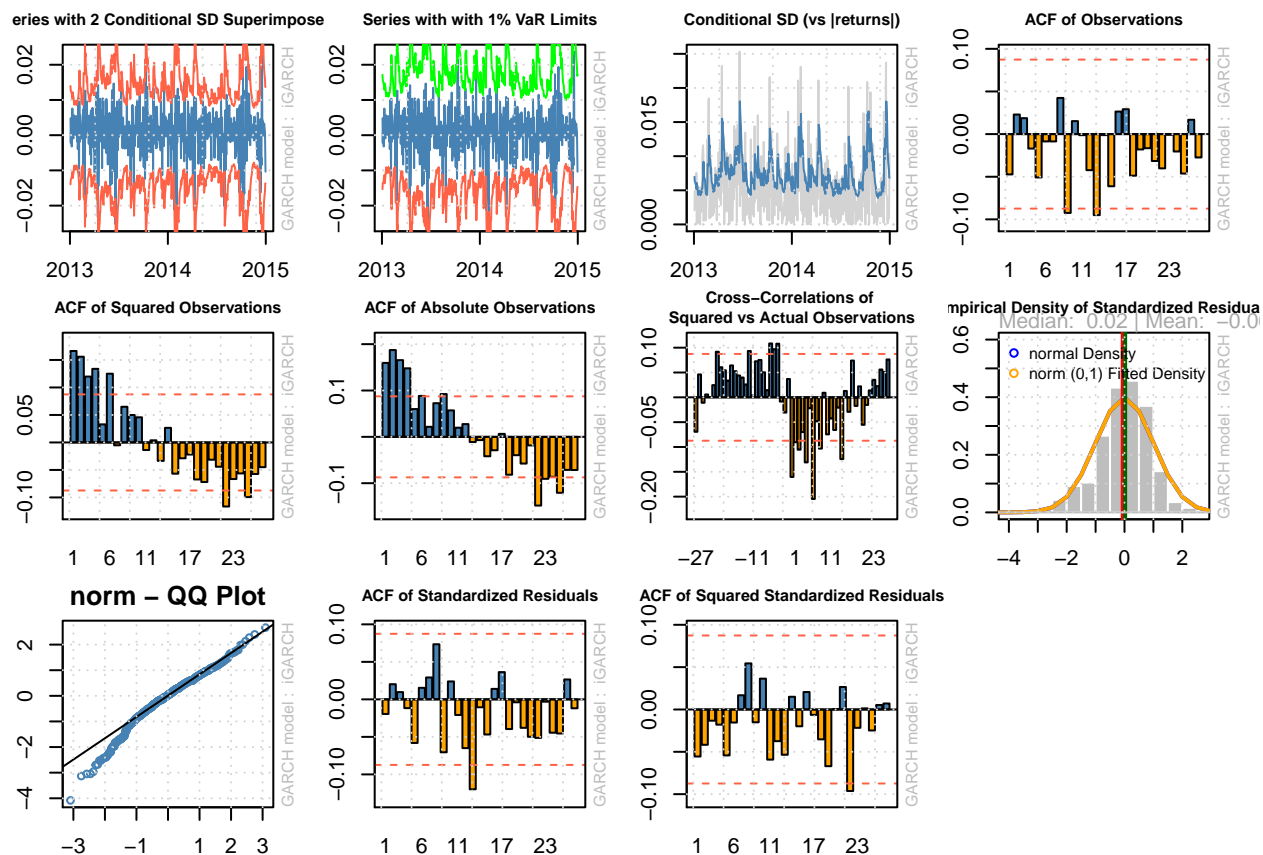
par(mfrow=c(2, 3))

```



```
par(mar = c(2, 2, 2, 2))
plot(i_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
## Warning in FUN(x):
## plot-->: iGARCH and fiGARCH newsim pact not available
```



GARCH MODELS assuming a Student's t-distribution

Student's t-sGARCH ----> tsGARCH

```
library(rugarch)
```

```
ts_garchMod <- ugarchspec(mean.model = list(armaOrder = c(1, 0), include.mean = TRUE),
  ),
  variance.model = list(model = 'sGARCH',
    garchOrder = c(1, 1),
    external.regressors = df_dummies
  ),
  distribution.model = "std")
```

```
ts_garchFit <- ugarchfit(spec=ts_garchMod, data=log_ret)
ts_garchFit
```

```
##
## *-----*
## *           GARCH Model Fit           *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : sGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : std
##
```

```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value   Pr(>|t|)
## mu      0.001077    0.000443    2.43255  0.014993
## ar1     -0.080107    0.145467   -0.55069  0.581847
## omega    0.000007    0.000004    1.72611  0.084327
## alpha1   0.202275    0.109803    1.84215  0.065453
## beta1    0.661366    0.027788   23.80006  0.000000
## vxreg1   0.000008    0.000007    1.02688  0.304478
## vxreg2   0.000002    0.000001    1.74037  0.081794
## shape    6.142083    0.822347    7.46896  0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value   Pr(>|t|)
## mu      0.001077    0.002446    0.44028  0.65974
## ar1     -0.080107    0.746648   -0.10729  0.91456
## omega    0.000007    0.000019    0.34617  0.72922
## alpha1   0.202275    0.553378    0.36553  0.71472
## beta1    0.661366    0.187497    3.52735  0.00042
## vxreg1   0.000008    0.000037    0.20445  0.83800
## vxreg2   0.000002    0.000007    0.34187  0.73245
## shape    6.142083    8.384014    0.73259  0.46381
##
## LogLikelihood : 1815.683
##
## Information Criteria
## -----
##
## Akaike          -7.1876
## Bayes           -7.1205
## Shibata         -7.1881
## Hannan-Quinn   -7.1613
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##                                statistic p-value
## Lag[1]                                0.01246  0.9111
## Lag[2*(p+q)+(p+q)-1] [2]    0.11314  0.9999
## Lag[4*(p+q)+(p+q)-1] [5]    0.61030  0.9879
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##                                statistic p-value
## Lag[1]                                0.4460  0.5042
## Lag[2*(p+q)+(p+q)-1] [5]    0.7543  0.9123
## Lag[4*(p+q)+(p+q)-1] [9]    1.8407  0.9231
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##      Statistic Shape Scale P-Value
## ARCH Lag[3]    0.0540 0.500 2.000  0.8163

```

```

## ARCH Lag[5]      0.7197 1.440 1.667 0.8175
## ARCH Lag[7]      1.1747 2.315 1.543 0.8836
##
## Nyblom stability test
## -----
## Joint Statistic: 17.8993
## Individual Statistics:
## mu      0.06043
## ar1     0.26102
## omega   1.71868
## alpha1  0.10781
## beta1   0.04842
## vxreg1  0.18054
## vxreg2  7.07380
## shape   0.04806
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##              t-value   prob sig
## Sign Bias      2.06328 0.03960 **
## Negative Sign Bias 0.84033 0.40113
## Positive Sign Bias 0.03896 0.96894
## Joint Effect      7.24575 0.06446 *
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      27.30      0.09790
## 2    30      43.26      0.04305
## 3    40      46.26      0.19743
## 4    50      47.00      0.55457
##
##
## Elapsed time : 0.4289579

## Results review 1
coef(ts_garchFit)

##              mu              ar1              omega              alpha1              beta1
## 1.077123e-03 -8.010700e-02 6.700036e-06 2.022749e-01 6.613660e-01
##              vxreg1              vxreg2              shape
## 7.621360e-06 2.445218e-06 6.142083e+00

ts_rhat <- ts_garchFit@fit$fitted.values
plot.ts(ts_rhat)
ts_hhat <- ts(ts_garchFit@fit$sigma^2)
plot.ts(ts_hhat)

## Results review 2
tfit.val <- coef(ts_garchFit)

```



```

tfit.sd      <- diag(vcov(ts_garchFit))
ttrue.val = ts_garchFit@fit$tval

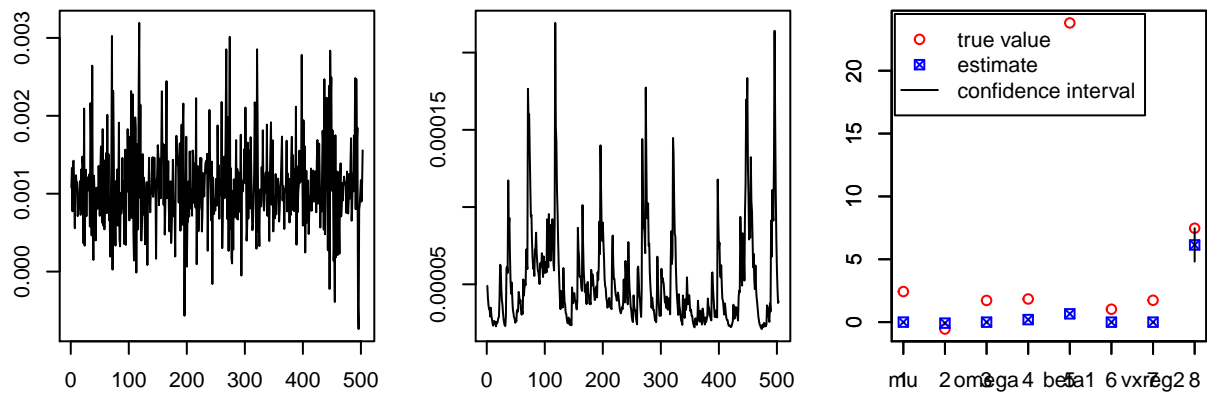
tfit.conf.lb <- tfit.val + qnorm(0.025) * tfit.sd
tfit.conf.ub <- tfit.val + qnorm(0.975) * tfit.sd
print(tfit.val)

##          mu          ar1          omega          alpha1          beta1
## 1.077123e-03 -8.010700e-02 6.700036e-06 2.022749e-01 6.613660e-01
##          vxreg1          vxreg2          shape
## 7.621360e-06 2.445218e-06 6.142083e+00
print(tfit.sd)

## [1] -1.960692e-07 -2.116061e-02 -1.506666e-11 -1.205680e-02 -7.721960e-04
## [6] -5.508434e-11 -1.974018e-12 -6.762552e-01
print(ttrue.val)

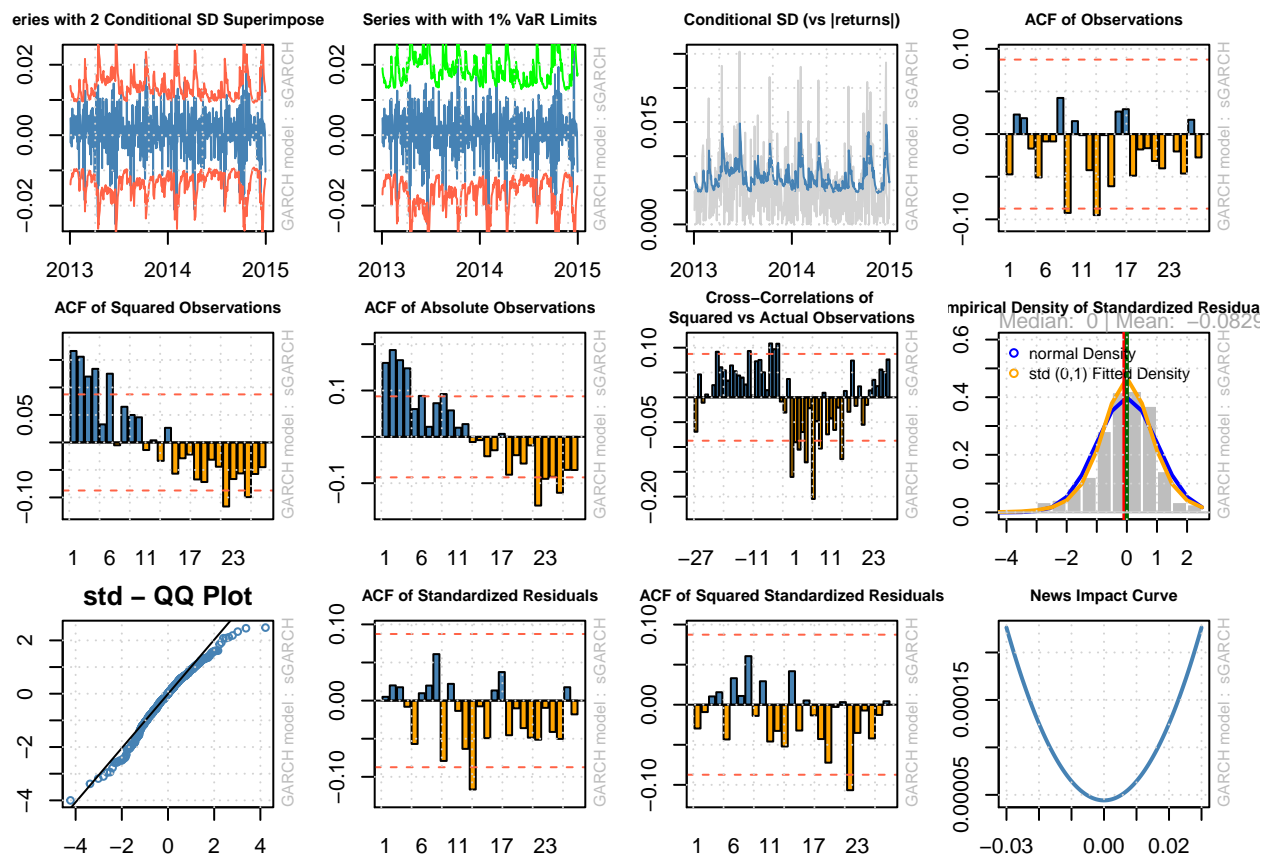
##          mu          ar1          omega          alpha1          beta1          vxreg1          vxreg2          shape
## 2.432545 -0.550689 1.726111 1.842154 23.800063 1.026877 1.740372 7.468964
plot(ttrue.val, pch = 1, col = "red",
     ylim = range(c(tfit.conf.lb, tfit.conf.ub, ttrue.val)),
     xlab = "", ylab = "", axes = TRUE)
box(); axis(1, at = 1:length(tfit.val), labels = names(tfit.val)); axis(2)
points(coef(ts_garchFit), col = "blue", pch = 7)
for (i in 1:length(tfit.val)) {
  lines(c(i,i), c(tfit.conf.lb[i], tfit.conf.ub[i]))
}
legend("topleft", legend = c("true value", "estimate", "confidence interval"),
      col = c("red", "blue", 1), pch = c(1, 7, NA), lty = c(NA, NA, 1), inset = 0.01)
par(mfrow=c(2, 3))

```



```
par(mar = c(2, 2, 2, 2))
plot(ts_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



```
#Student's t-gjrGARCH ---->tgjrGARCH
tgjr_garchMod <- ugarchspec(
  variance.model=list(model="gjrGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="std"
)
tgjr_garchFit <- ugarchfit(spec=tgjr_garchMod, data=log_ret)
coef(tgjr_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 8.809784e-04 -6.318676e-02 4.584431e-06 2.150762e-07 7.299537e-01
##      gamma1      vxreg1      vxreg2      shape
## 3.202011e-01 6.507069e-06 2.030656e-06 6.949425e+00
```

```
tgjr_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,1)
```

```

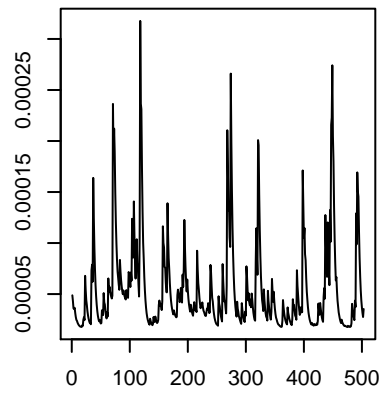
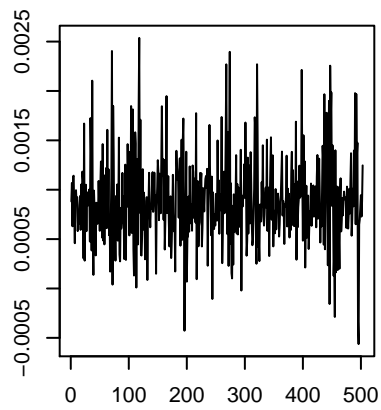
## Mean Model      : ARFIMA(1,0,0)
## Distribution : std
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000881    0.000223   3.946239 0.000079
## ar1     -0.063187    0.047453  -1.331555 0.183006
## omega    0.000005    0.000001   5.519614 0.000000
## alpha1   0.000000    0.014299   0.000015 0.999988
## beta1    0.729954    0.024061  30.337502 0.000000
## gamma1   0.320201    0.085879   3.728528 0.000193
## vxreg1   0.000007    0.000002   3.558969 0.000372
## vxreg2   0.000002    0.000000   4.294295 0.000018
## shape    6.949425    0.630171  11.027846 0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000881    0.000229   3.846445 0.000120
## ar1     -0.063187    0.053955  -1.171104 0.241557
## omega    0.000005    0.000001   7.252684 0.000000
## alpha1   0.000000    0.015446   0.000014 0.999989
## beta1    0.729954    0.026885  27.151180 0.000000
## gamma1   0.320201    0.095330   3.358853 0.000783
## vxreg1   0.000007    0.000002   2.748420 0.005988
## vxreg2   0.000002    0.000001   3.449096 0.000562
## shape    6.949425    1.978854   3.511843 0.000445
##
## LogLikelihood : 1825.735
##
## Information Criteria
## -----
##
## Akaike          -7.2236
## Bayes           -7.1481
## Shibata         -7.2242
## Hannan-Quinn   -7.1940
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##                                statistic p-value
## Lag[1]                                2.464e-06  0.9987
## Lag[2*(p+q)+(p+q)-1] [2]  1.723e-01  0.9994
## Lag[4*(p+q)+(p+q)-1] [5]  6.525e-01  0.9851
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##                                statistic p-value
## Lag[1]                                0.9704  0.3246
## Lag[2*(p+q)+(p+q)-1] [5]  2.5084  0.5041
## Lag[4*(p+q)+(p+q)-1] [9]  4.0526  0.5800
## d.o.f=2

```

```
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3] 1.231e-05 0.500 2.000 0.9972
## ARCH Lag[5] 1.698e+00 1.440 1.667 0.5418
## ARCH Lag[7] 2.068e+00 2.315 1.543 0.7028
##
## Nyblom stability test
## -----
## Joint Statistic: 15.3759
## Individual Statistics:
## mu      0.05929
## ar1     0.28809
## omega   1.75436
## alpha1  0.39316
## beta1   0.03791
## gamma1  0.14966
## vxreg1  2.55846
## vxreg2  4.46339
## shape   0.04297
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value      prob sig
## Sign Bias      2.4454 0.01482 **
## Negative Sign Bias 1.8461 0.06548 *
## Positive Sign Bias 0.4741 0.63562
## Joint Effect      7.3585 0.06131 *
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      38.43    0.005228
## 2    30      37.06    0.144705
## 3    40      55.49    0.042037
## 4    50      65.49    0.057705
##
##
## Elapsed time : 0.7116909

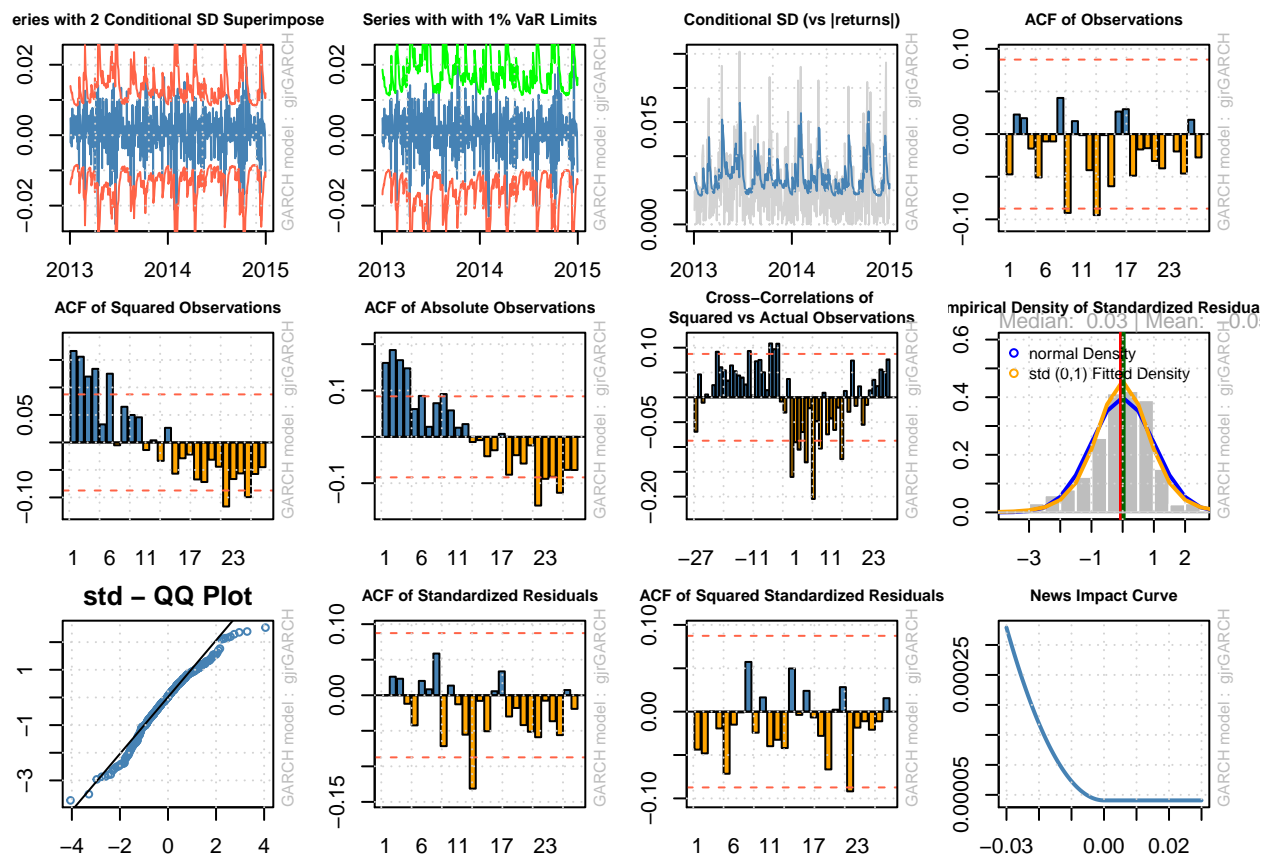
tgjr_rhat <- tgjr_garchFit@fit$fitted.values
plot.ts(tgjr_rhat)
tgjr_hhat <- ts(tgjr_garchFit@fit$sigma^2)
plot.ts(tgjr_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))
plot(tgjr_garchFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



```
#Student's t-eGARCH ---->teGARCH
te_garchMod <- ugarchspec(
  variance.model=list(model="eGARCH",
    garchOrder=c(1,1), external.regressors = df_dummies ),
  mean.model=list(armaOrder=c(1,0),
    include.mean=TRUE
  ),
  distribution.model="std"
)
te_garchFit <- ugarchfit(spec=te_garchMod, data=log_ret)
coef(te_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1          gamma1
## 0.002012785 -0.047107533 -0.696736218 -0.300660521 0.900010871 0.601751546
##          vxreg1          vxreg2          shape
## -2.529340859 -9.172391966 3.999483351
```

```
te_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : eGARCH(1,1)
```

```

## Mean Model      : ARFIMA(1,0,0)
## Distribution    : std
##
## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.002013    0.000002  1263.510      0
## ar1     -0.047108    0.000033 -1411.030      0
## omega   -0.696736    0.000615 -1133.607      0
## alpha1  -0.300661    0.000183 -1645.610      0
## beta1    0.900011    0.000299  3012.762      0
## gamma1   0.601752    0.000362  1660.753      0
## vxreg1  -2.529341    0.031686  -79.826       0
## vxreg2  -9.172392    0.008222 -1115.577      0
## shape    3.999483    0.002139  1869.912      0
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.002013    0.009895   0.20342  0.83880
## ar1     -0.047108    0.164329  -0.28667  0.77437
## omega   -0.696736    3.226641  -0.21593  0.82904
## alpha1  -0.300661    0.536478  -0.56043  0.57518
## beta1    0.900011    1.286992   0.69931  0.48436
## gamma1   0.601752    3.117495   0.19302  0.84694
## vxreg1  -2.529341   20.237763  -0.12498  0.90054
## vxreg2  -9.172392   69.834011  -0.13135  0.89550
## shape    3.999483    9.835073   0.40665  0.68426
##
## LogLikelihood : 779.7217
##
## Information Criteria
## -----
##
## Akaike          -3.0645
## Bayes           -2.9890
## Shibata         -3.0651
## Hannan-Quinn   -3.0349
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.03718  0.8471
## Lag[2*(p+q)+(p+q)-1] [2]  0.09626  0.9999
## Lag[4*(p+q)+(p+q)-1] [5]  0.53917  0.9919
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.02627  0.8712
## Lag[2*(p+q)+(p+q)-1] [5]  0.06793  0.9991
## Lag[4*(p+q)+(p+q)-1] [9]  0.21730  0.9999
## d.o.f=2

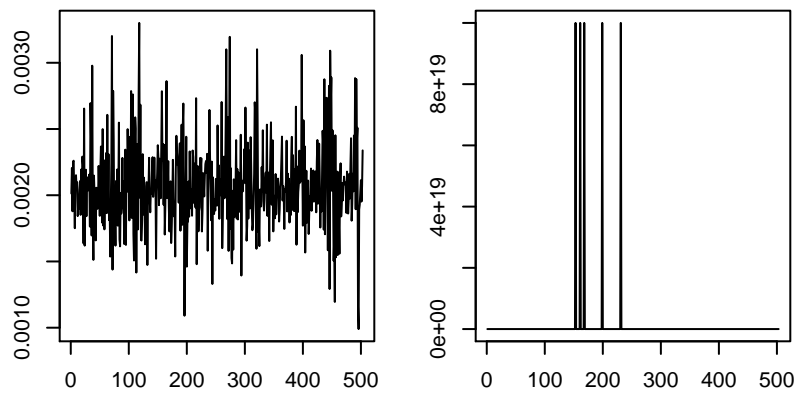
```



```
##
## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]    0.02628 0.500 2.000 0.8712
## ARCH Lag[5]    0.04269 1.440 1.667 0.9961
## ARCH Lag[7]    0.17215 2.315 1.543 0.9979
##
## Nyblom stability test
## -----
## Joint Statistic: 6.333
## Individual Statistics:
## mu      0.02455
## ar1     0.90921
## omega   0.41452
## alpha1  0.18684
## beta1   0.76394
## gamma1  0.01304
## vxreg1  0.66686
## vxreg2  0.29431
## shape   0.21633
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value   prob sig
## Sign Bias      1.028 0.3043
## Negative Sign Bias 0.991 0.3222
## Positive Sign Bias 1.643 0.1011
## Joint Effect    4.291 0.2317
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      197.6   1.042e-31
## 2    30      229.2   5.178e-33
## 3    40      280.2   3.011e-38
## 4    50      304.7   1.295e-38
##
##
## Elapsed time : 0.4163711

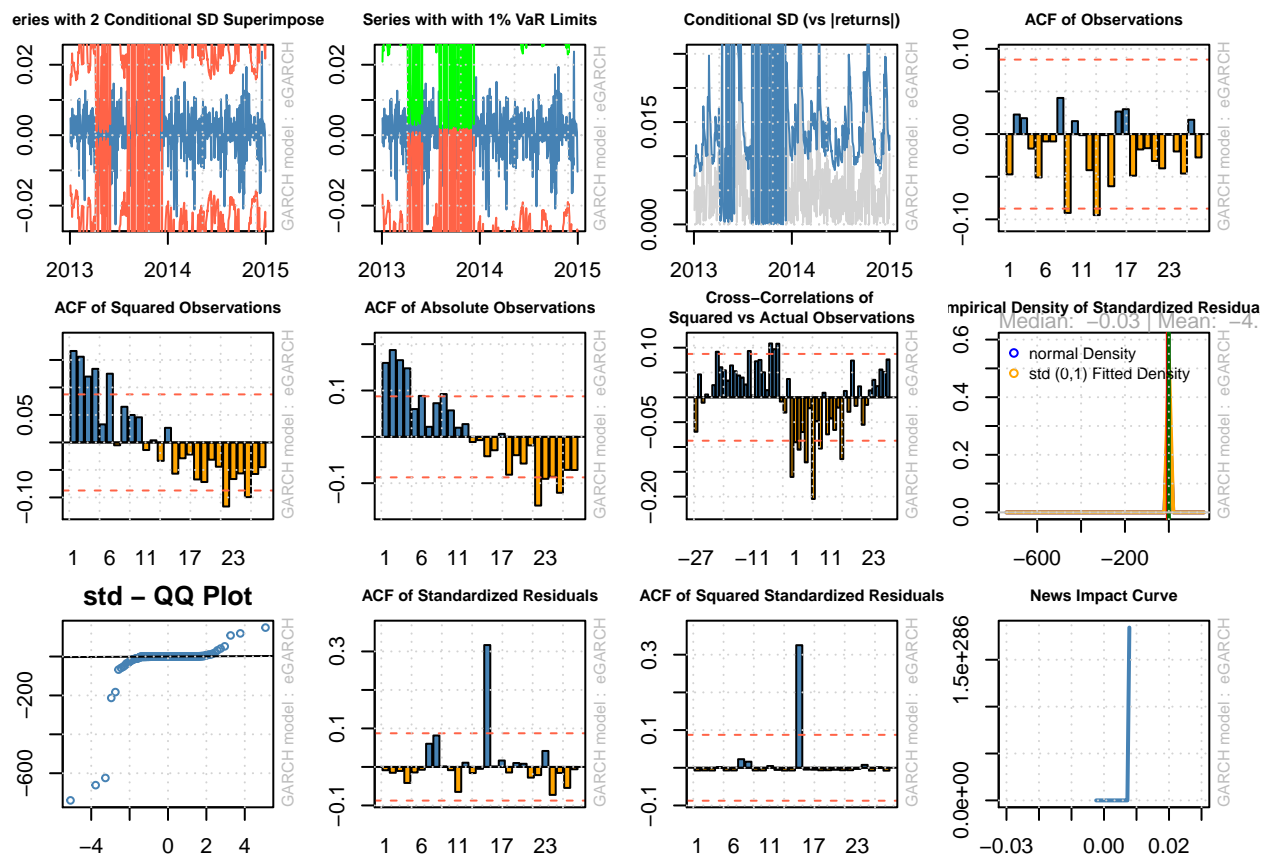
te_rhat <- te_garchFit@fit$fitted.values
plot.ts(te_rhat)
te_hhat <- ts(te_garchFit@fit$sigma^2)
plot.ts(te_hhat)

par(mfrow=c(2, 3))
```



```
par(mar = c(2, 2, 2, 2))  
plot(te_garchFit, which="all")
```

```
##  
## please wait...calculating quantiles...
```



```
#Student's t-apARCH ----> tapARCH
tapARCHMod <- ugarchspec(variance.model=list(model="apARCH",
                                             garchOrder=c(1,1),
                                             external.regressors = df_dummies ),
                        mean.model=list(armaOrder=c(1,0)),
                        distribution.model="std")
tapARCHFit <- ugarchfit(spec=tapARCHMod, data= log_ret)
coef(tapARCHFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 9.068272e-04 -4.473157e-02 2.271811e-08 7.601009e-02 6.835558e-01
##          gamma1          delta          vxreg1          vxreg2          shape
## 4.936238e-01 3.032251e+00 2.758024e-08 1.940875e-08 6.800218e+00
```

```
tapARCHFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : apARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : std
##
```

```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000907    0.000256   3.539729 0.000401
## ar1     -0.044732    0.049692  -0.900177 0.368026
## omega    0.000000    0.000001   0.022447 0.982091
## alpha1   0.076010    0.034534   2.201011 0.027735
## beta1    0.683556    0.106456   6.420991 0.000000
## gamma1   0.493624    0.207634   2.377380 0.017436
## delta    3.032251    0.092542  32.766234 0.000000
## vxreg1   0.000000    0.000001   0.024252 0.980652
## vxreg2   0.000000    0.000001   0.025265 0.979844
## shape    6.800218    2.028400   3.352503 0.000801
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value Pr(>|t|)
## mu      0.000907    0.003973   0.228225 0.81947
## ar1     -0.044732    1.822830  -0.024540 0.98042
## omega    0.000000    0.000196   0.000116 0.99991
## alpha1   0.076010    1.163708   0.065317 0.94792
## beta1    0.683556   14.759060   0.046314 0.96306
## gamma1   0.493624   11.219947   0.043995 0.96491
## delta    3.032251    8.354568   0.362945 0.71665
## vxreg1   0.000000    0.000164   0.000168 0.99987
## vxreg2   0.000000    0.000079   0.000246 0.99980
## shape    6.800218   73.106907   0.093017 0.92589
##
## LogLikelihood : 1820.434
##
## Information Criteria
## -----
##
## Akaike          -7.1985
## Bayes           -7.1146
## Shibata         -7.1993
## Hannan-Quinn   -7.1656
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.2135 0.6440
## Lag[2*(p+q)+(p+q)-1] [2] 0.3887 0.9851
## Lag[4*(p+q)+(p+q)-1] [5] 0.8706 0.9643
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.856 0.3549
## Lag[2*(p+q)+(p+q)-1] [5] 2.230 0.5652
## Lag[4*(p+q)+(p+q)-1] [9] 3.567 0.6628
## d.o.f=2
##

```

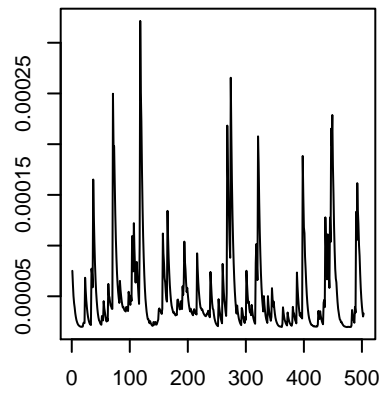
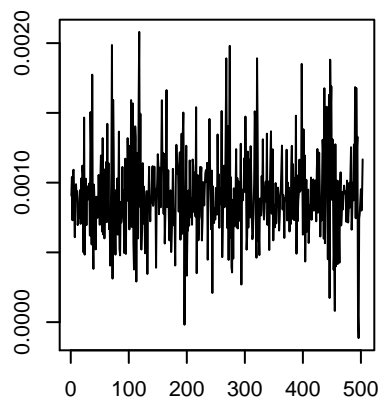
```

## Weighted ARCH LM Tests
## -----
##           Statistic Shape Scale P-Value
## ARCH Lag[3]   0.02027 0.500 2.000 0.8868
## ARCH Lag[5]   1.33998 1.440 1.667 0.6354
## ARCH Lag[7]   1.61356 2.315 1.543 0.7983
##
## Nyblom stability test
## -----
## Joint Statistic:  NaN
## Individual Statistics:
## mu      0.06654
## ar1     0.59291
## omega   59.72101
## alpha1  0.06882
## beta1   0.03319
## gamma1  0.04743
## delta   0.32302
## vxreg1   NaN
## vxreg2   NaN
## shape   0.05481
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      2.29 2.54 3.05
## Individual Statistic:  0.35 0.47 0.75
##
## Sign Bias Test
## -----
##           t-value   prob sig
## Sign Bias      2.5577 0.01083 **
## Negative Sign Bias 1.7100 0.08789 *
## Positive Sign Bias 0.5431 0.58727
## Joint Effect     7.8437 0.04936 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      39.86    0.003411
## 2    30      40.88    0.070590
## 3    40      64.55    0.006188
## 4    50      78.41    0.004809
##
##
## Elapsed time : 0.6622701

tapARCH_rhat <- tapARCHFit@fit$fitted.values
plot.ts(tapARCH_rhat)
tapARCH_hhat <- ts(tapARCHFit@fit$sigma^2)
plot.ts(tapARCH_hhat)

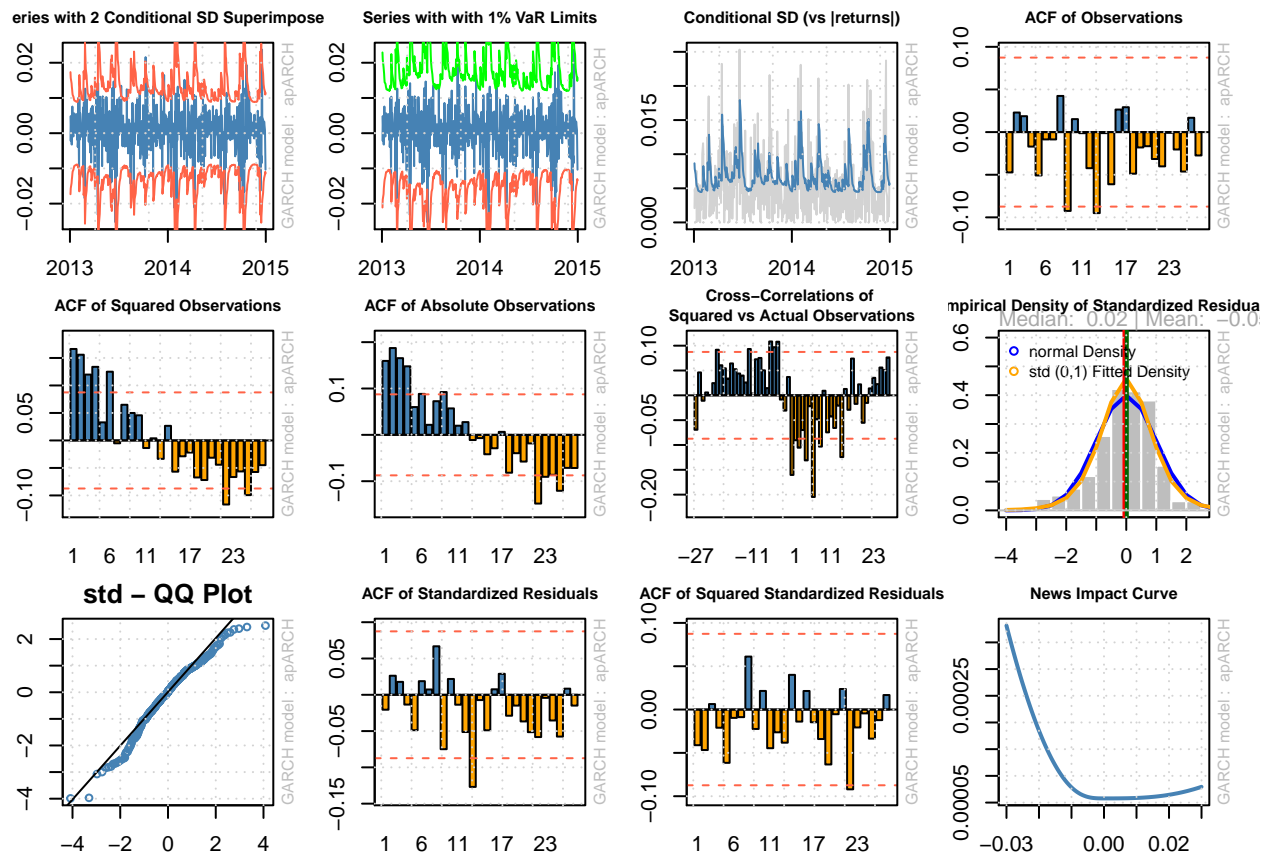
par(mfrow=c(2, 3))

```



```
par(mar = c(2, 2, 2, 2))
plot(tapARCHFit, which="all")
```

```
##
## please wait...calculating quantiles...
```



#Student's t-tiGARCH ----> tiGARCH

```
ti_garchMod <- ugarchspec(variance.model=list(model="iGARCH",
                                              garchOrder=c(1,1),
                                              external.regressors = df_dummies ),
                          mean.model=list(armaOrder=c(1,0), include.mean=TRUE),
                          distribution.model="std")
ti_garchFit <- ugarchfit(spec=ti_garchMod, data= log_ret)
coef(ti_garchFit)
```

```
##          mu          ar1          omega          alpha1          beta1
## 1.118378e-03 -8.467020e-02 4.767178e-06 3.118613e-01 6.881387e-01
##          vxreg1          vxreg2          shape
## 7.194076e-06 2.618257e-06 4.306351e+00
```

```
ti_garchFit
```

```
##
## *-----*
## *          GARCH Model Fit          *
## *-----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model   : iGARCH(1,1)
## Mean Model    : ARFIMA(1,0,0)
## Distribution   : std
##
```

```

## Optimal Parameters
## -----
##      Estimate   Std. Error   t value   Pr(>|t|)
## mu      0.001118    0.000068   16.3305  0.000000
## ar1     -0.084670    0.035998   -2.3521  0.018668
## omega    0.000005    0.000002    2.0359  0.041757
## alpha1   0.311861    0.041158    7.5773  0.000000
## beta1    0.688139         NA         NA         NA
## vxreg1   0.000007    0.000001    9.4146  0.000000
## vxreg2   0.000003    0.000000    6.6928  0.000000
## shape    4.306351    0.813634    5.2927  0.000000
##
## Robust Standard Errors:
##      Estimate   Std. Error   t value   Pr(>|t|)
## mu      0.001118    0.000036   30.9085  0.000000
## ar1     -0.084670    0.036050   -2.3487  0.018841
## omega    0.000005    0.000003    1.4843  0.137735
## alpha1   0.311861    0.036843    8.4646  0.000000
## beta1    0.688139         NA         NA         NA
## vxreg1   0.000007    0.000001    8.3143  0.000000
## vxreg2   0.000003    0.000000    6.2199  0.000000
## shape    4.306351    0.730499    5.8951  0.000000
##
## LogLikelihood : 1812.892
##
## Information Criteria
## -----
##
## Akaike          -7.1805
## Bayes           -7.1218
## Shibata         -7.1809
## Hannan-Quinn   -7.1574
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
##              statistic p-value
## Lag[1]              0.0001489  0.9903
## Lag[2*(p+q)+(p+q)-1] [2] 0.0988805  0.9999
## Lag[4*(p+q)+(p+q)-1] [5] 0.5856371  0.9894
## d.o.f=1
## H0 : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
##              statistic p-value
## Lag[1]              1.149  0.2838
## Lag[2*(p+q)+(p+q)-1] [5] 1.891  0.6444
## Lag[4*(p+q)+(p+q)-1] [9] 3.009  0.7574
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
##
##              Statistic Shape Scale P-Value
## ARCH Lag[3]    0.03201 0.500 2.000  0.8580

```



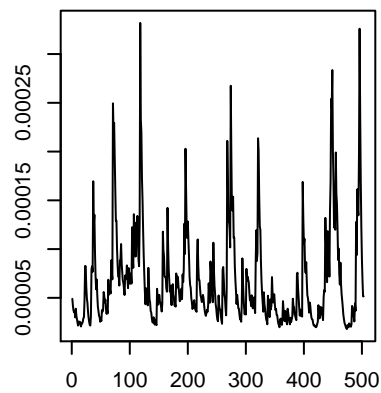
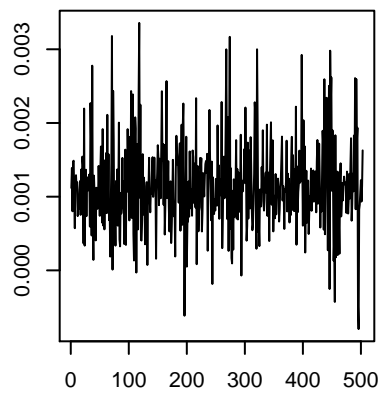
```

## ARCH Lag[5]    0.99270 1.440 1.667 0.7351
## ARCH Lag[7]    1.30432 2.315 1.543 0.8596
##
## Nyblom stability test
## -----
## Joint Statistic: 5.5534
## Individual Statistics:
## mu      0.05802
## ar1     0.28466
## omega   0.03804
## alpha1  0.06886
## vxreg1  0.13788
## vxreg2  4.59620
## shape   0.03198
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:      1.69 1.9 2.35
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##              t-value   prob sig
## Sign Bias      2.0547 0.04043 **
## Negative Sign Bias 1.5447 0.12306
## Positive Sign Bias 0.6405 0.52217
## Joint Effect      9.2030 0.02671 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##   group statistic p-value(g-1)
## 1    20      33.82    0.01930
## 2    30      40.64    0.07403
## 3    40      59.62    0.01832
## 4    50      51.37    0.38088
##
##
## Elapsed time : 0.3300061

ti_rhat <- ti_garchFit@fit$fitted.values
plot.ts(ti_rhat)
ti_hhat <- ts(ti_garchFit@fit$sigma^2)
plot.ts(ti_hhat)

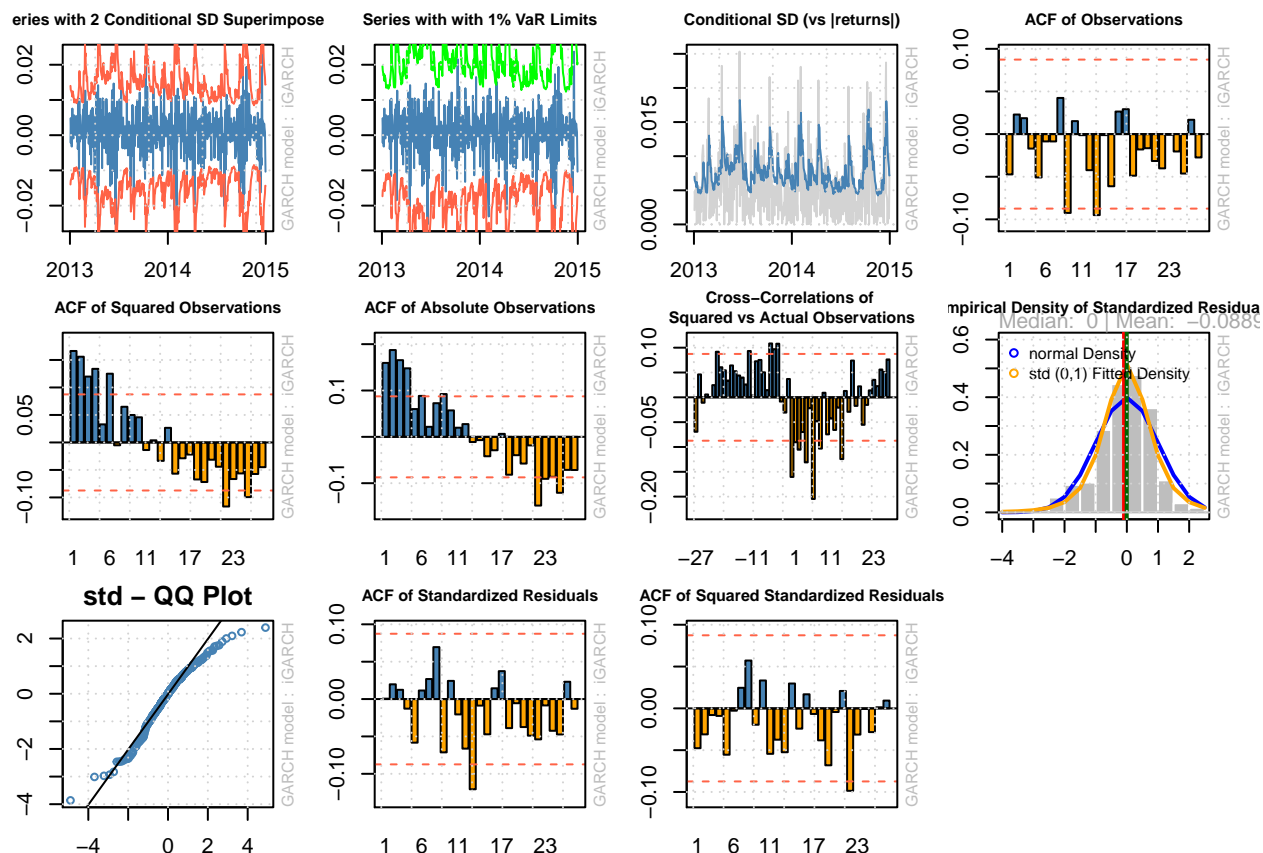
par(mfrow=c(2, 3))

```



```
par(mar = c(2, 2, 2, 2))
plot(ti_garchFit,which="all")
```

```
##
## please wait...calculating quantiles...
## Warning in FUN(x):
## plot-->: iGARCH and fiGARCH newsimpact not available
```



Choosing the best model:

```
#Choose best GARCH model
#Normal
AIC= c(Infocriteria(s_garchFit)[1], Infocriteria(gjr_garchFit)[1],
        Infocriteria(e_garchFit)[1], Infocriteria(apARCHFit)[1], Infocriteria(i_garchFit)[1] )
rowSAIC= c("s_garch", "gjr_garchFit", "e_garchFit", "apARCHFit", "i_garchFit")

AIC_Results= data.frame(AIC, row.names = rowSAIC)
AIC_Results

##              AIC
## s_garch      -7.158517
## gjr_garchFit -7.203430
## e_garchFit   -7.252679
## apARCHFit    -7.175112
## i_garchFit   -7.135728

BestAICNorm=AIC_Results[which.min(AIC_Results$AIC),]
BestAICNorm

## [1] -7.252679

BIC= c(Infocriteria(s_garchFit)[2], Infocriteria(gjr_garchFit)[2],
        Infocriteria(e_garchFit)[2], Infocriteria(apARCHFit)[2], Infocriteria(i_garchFit)[2] )
rowSBIC= c("s_garch", "gjr_garchFit", "e_garchFit", "apARCHFit", "i_garchFit")
BIC_Results= data.frame(BIC, row.names = rowSBIC)
```

```

BIC_Results

##              BIC
## s_garch      -7.099782
## gjr_garchFit -7.136303
## e_garchFit   -7.185552
## apARCHFit    -7.099595
## i_garchFit   -7.085383

BestBICNorm=BIC_Results[which.min(BIC_Results$BIC),]
BestBICNorm

## [1] -7.185552

Best_Norm=c(BestAICNorm,BestBICNorm)
rowSBest_Norm= c("AICbest","BICbest")
Norm_Results= data.frame(Best_Norm, row.names =rowSBest_Norm)
Norm_Results

##           Best_Norm
## AICbest -7.252679
## BICbest -7.185552

#Student-t
tAIC= c(Infocriteria(ts_garchFit)[1], Infocriteria(tgjrgarchFit)[1],
        Infocriteria(te_garchFit)[1], Infocriteria(tapARCHFit)[1], Infocriteria(ti_garchFit)[1] )
trowSAIC= c("ts_garch", "tgjrgarchFit", "te_garchFit", "tapARCHFit", "ti_garchFit")

tAIC_Results= data.frame(tAIC, row.names = trowSAIC)
tAIC_Results

##              tAIC
## ts_garch      -7.187608
## tgjrgarchFit  -7.223597
## te_garchFit   -3.064500
## tapARCHFit    -7.198545
## ti_garchFit   -7.180487

tAIC_Results[which.min(tAIC_Results$tAIC),]

## [1] -7.223597

tBIC= c(Infocriteria(ts_garchFit)[2], Infocriteria(tgjrgarchFit)[2],
        Infocriteria(te_garchFit)[2], Infocriteria(tapARCHFit)[2], Infocriteria(ti_garchFit)[2] )
trowSBIC= c("ts_garch", "tgjrgarchFit", "te_garchFit", "tapARCHFit", "ti_garchFit")
tBIC_Results= data.frame(tBIC, row.names = trowSBIC)
tBIC_Results

##              tBIC
## ts_garch      -7.120481
## tgjrgarchFit  -7.148079
## te_garchFit   -2.988982
## tapARCHFit    -7.114637
## ti_garchFit   -7.121751

tBIC_Results[which.min(tBIC_Results$tBIC),]

## [1] -7.148079

```

```

#Goodness of Fit
Distribution=c("Normal", "Normal", "Normal", "Normal", "Normal",
              "Student's-t", "Student's-t", "Student's-t", "Student's-t", "Student's-t" )
rowsGARCH=c("s_garchFit", "gjr_garchFit", "e_garchFit", "apARCHFit", "i_garchFit",
            "ts_garchFit", "tgjr_garchFit", "te_garchFit", "tapARCHFit", "ti_garchFit")
Best=c("o", "o", "*", "o", "o",
       "o", "*", "o", "o", "o")
final_AIC=c(AIC,tAIC)
final_BIC=c(BIC,tBIC)
Results <- data.frame("AIC" = final_AIC, "BIC" = final_BIC , "Distribution" = Distribution,
                     "Best"= Best ,row.names = rowsGARCH)

Results

```

##		AIC	BIC	Distribution	Best
##	s_garchFit	-7.158517	-7.099782	Normal	o
##	gjr_garchFit	-7.203430	-7.136303	Normal	o
##	e_garchFit	-7.252679	-7.185552	Normal	*
##	apARCHFit	-7.175112	-7.099595	Normal	o
##	i_garchFit	-7.135728	-7.085383	Normal	o
##	ts_garchFit	-7.187608	-7.120481	Student's-t	o
##	tgjr_garchFit	-7.223597	-7.148079	Student's-t	*
##	te_garchFit	-3.064500	-2.988982	Student's-t	o
##	tapARCHFit	-7.198545	-7.114637	Student's-t	o
##	ti_garchFit	-7.180487	-7.121751	Student's-t	o

Validation:

```

#Validation of the model
residual_bestModel= residuals(e_garchFit, standardize = TRUE)
Box.test(abs(residual_bestModel), 10, type = "Ljung-Box")

##
## Box-Ljung test
##
## data: abs(residual_bestModel)
## X-squared = 2.9893, df = 10, p-value = 0.9817

acf(abs(residual_bestModel), 10)

```

Series abs(residual_bestModel)

