Progetto - Deep Learning on Temporal Data Confronto ARIMA model e ARMA(1,1)-sGARCH(1,1)

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Motivazione e data setting

L'analisi che viene qui proposta prende spunto dalle lezioni *Deep Learning on Temporal Data* e presenta un confronto tra i modelli ARIMA e un modello ARMA(1,1)-sGARCH(1,1) che presenta dunque anche l'equazione per la varianza. I modelli GARCH sono largamente usati in letteratura per catturare gli effetti disruptive a cui sono spesso soggetti i ticker azionari. Ho scelto i prezzi azionari di Amazon da Giugno 2015 a Giugno 2021.

```
#librerie necessarie
library(ggplot2)
library(tidyquant)
library(timetk)
library(tseries)
library(timeSeries)
library(forecast)
library(seastests)
library(rugarch)
library(fDMA)
library(dplyr)
set.seed(29)
amazon = tq_get("AMZN",
                  from = '2015-06-01',
                  to = "2021-06-01",
                  get = "stock.prices")
```

Data Visualization, calcolo log returns e fit del MACD

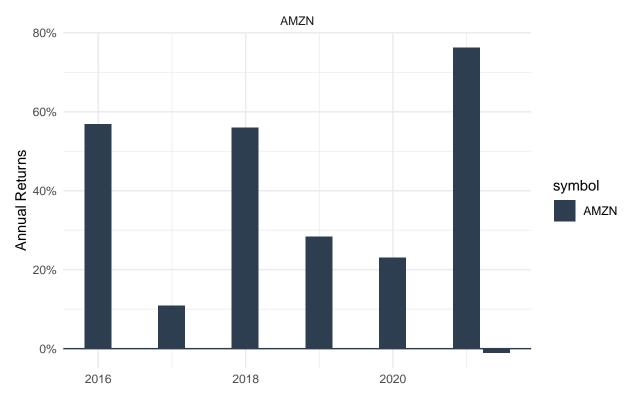
```
amazon %>%
  ggplot(aes(x = date, y = adjusted)) +
  geom_line() +
  ggtitle("Amazon") +
  labs(x = "Date", "Price") +
  scale_x_date(date_breaks = "years", date_labels = "%Y") +
  labs(x = "Data", y = "Adjusted Price") +
  theme_minimal()
```



```
AMZN_annual_returns = amazon %>%
  group_by(symbol) %>%
  tq_transmute(select
                          = adjusted,
               mutate_fun = periodReturn,
                         = "yearly",
               period
                          = "arithmetic")
               type
AMZN_annual_returns
## # A tibble: 7 x 3
## # Groups: symbol [1]
##
     symbol date
                       yearly.returns
##
     <chr> <date>
                                <dbl>
            2015-12-31
                               0.568
## 1 AMZN
## 2 AMZN
            2016-12-30
                               0.109
            2017-12-29
## 3 AMZN
                               0.560
## 4 AMZN
            2018-12-31
                               0.284
## 5 AMZN
            2019-12-31
                               0.230
## 6 AMZN
            2020-12-31
                               0.763
## 7 AMZN
            2021-05-28
                              -0.0104
AMZN_annual_returns %>%
  ggplot(aes(x = date, y = yearly.returns, fill = symbol)) +
  geom col() +
  geom_hline(yintercept = 0, color = palette_light()[[1]]) +
  scale_y_continuous(labels = scales::percent) +
  labs(title = "Amazon: Annual Returns",
       y = "Annual Returns", x = "") +
```

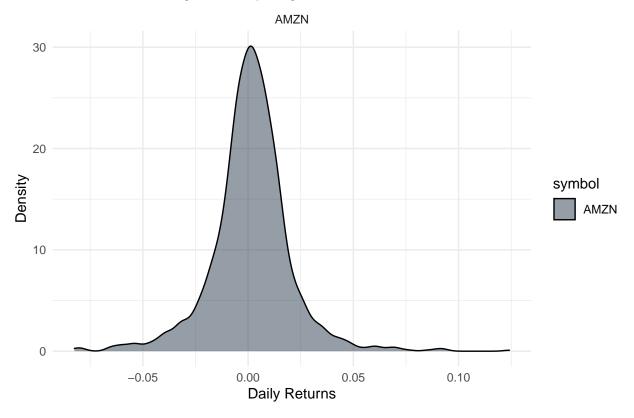
```
facet_wrap(~ symbol, ncol = 2, scales = "free_y") +
theme_minimal() +
scale_fill_tq()
```

Amazon: Annual Returns



```
AMZN_daily_log_returns = amazon %>%
  group_by(symbol) %>%
  tq_transmute(select
                          = adjusted,
               mutate_fun = periodReturn,
               period
                        = "daily",
                         = "log",
               type
               col_rename = "daily.returns")
AMZN_daily_log_returns %>%
  ggplot(aes(x = daily.returns, fill = symbol)) +
  geom_density(alpha = 0.5) +
  labs(title = "Amazon: Charting the Daily Log Returns",
       x = "Daily Returns", y = "Density") +
  theme_minimal() +
  scale_fill_tq() +
  facet_wrap(~ symbol, ncol = 2)
```

Amazon: Charting the Daily Log Returns



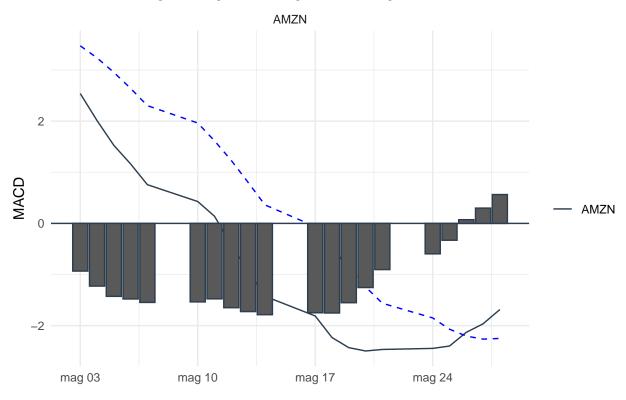
Calcolo e plot del Moving Average Convergence Divergence:

```
AMZN_macd = amazon %>%
  group_by(symbol) %>%
  tq_mutate(select
                       = close,
            mutate_fun = MACD,
                       = 12,
            nFast
            nSlow
                       = 26.
            nSig
                       = 9,
            maType
                       = SMA) %>%
  mutate(diff = macd - signal) %>%
  select(-(open:volume))
AMZN_macd
```

```
## # A tibble: 1,511 x 6
## # Groups:
               symbol [1]
##
      symbol date
                         adjusted macd signal
                                                 diff
##
      <chr>
             <date>
                            <dbl> <dbl>
                                          <dbl> <dbl>
    1 AMZN
             2015-06-01
                             431.
                                             NA
##
                                      NA
                                                    NA
##
    2 AMZN
             2015-06-02
                             431.
                                      NA
                                             NA
                                                    NA
                                      NA
                                                    NA
##
    3 AMZN
             2015-06-03
                             437.
                                             NA
   4 AMZN
             2015-06-04
                             431.
                                      NA
                                             NA
                                                    NA
##
    5 AMZN
             2015-06-05
                             427.
                                      NA
                                             NA
                                                    NA
    6 AMZN
             2015-06-08
                             424.
                                      NA
                                             NA
                                                    NA
##
                                             NA
##
   7 AMZN
             2015-06-09
                             425.
                                      NA
                                                    NA
##
   8 AMZN
             2015-06-10
                             431.
                                      NA
                                             NA
                                                   NA
    9 AMZN
             2015-06-11
                             433.
                                      NA
                                             NA
##
                                                    NA
```

```
## 10 AMZN
            2015-06-12
                            430.
                                    NA
                                           NA
                                                 NA
## # ... with 1,501 more rows
AMZN_macd %>%
  filter(date >= as date("2021-05-01")) %>%
  ggplot(aes(x = date)) +
  geom_hline(yintercept = 0, color = palette_light()[[1]]) +
  geom_line(aes(y = macd, col = symbol)) +
  geom_line(aes(y = signal), color = "blue", linetype = 2) +
  geom_bar(aes(y = diff), stat = "identity", color = palette_light()[[1]]) +
  facet_wrap(~ symbol, ncol = 2, scale = "free_y") +
  labs(title = "AMZN: Moving Average Convergence Divergence",
      y = "MACD", x = "", color = "") +
  theme_minimal() +
  scale_color_tq()
```

AMZN: Moving Average Convergence Divergence



Test: stazionarietà e presenza ARCH effect

```
#Stationarity test
#adf.test(AMZN_daily_log_returns$daily.returns, alternative = "stationary")
# p-value = 0.01 -> si rifiuta l'ipotesi nulla
ts= ts(AMZN_daily_log_returns)[,3]
# seasonality test
isSeasonal(ts, freq=1)
```

```
## [1] FALSE
#stationary test
adf.test(ts, alternative= "stationary")
##
##
  Augmented Dickey-Fuller Test
##
## data: ts
## Dickey-Fuller = -11.801, Lag order = 11, p-value = 0.01
## alternative hypothesis: stationary
#ARCH EFFECT
archtest(as.vector(AMZN_daily_log_returns$daily.returns))
  Engle's LM ARCH Test
##
## data: as.vector(AMZN_daily_log_returns$daily.returns)
## statistic = 53.451, lag = 1, p-value = 2.652e-13
## alternative hypothesis: ARCH effects of order 1 are present
# presenza ARCH effect
```

Fit modelli ARMA, verifica auto-correlation e valori BIC per scelta modello

```
n = length(ts)
## [1] 1511
nV=round(n/3) # Validation set (33% del totale)
nV
## [1] 504
nT=n-nV # training set - osservazioni
train=ts[c(1:nT)]
valid=ts[c((nT+1):n)]
auto_model1=auto.arima(train, ic="aic", stationary=FALSE,seasonal=FALSE)
auto_model1
## Series: train
## ARIMA(0,0,0) with non-zero mean
## Coefficients:
##
          mean
        0.0014
##
## s.e. 0.0006
## sigma^2 estimated as 0.0003423: log likelihood=2589.54
## AIC=-5175.08 AICc=-5175.07 BIC=-5165.25
```

```
res1=auto_model1$residuals

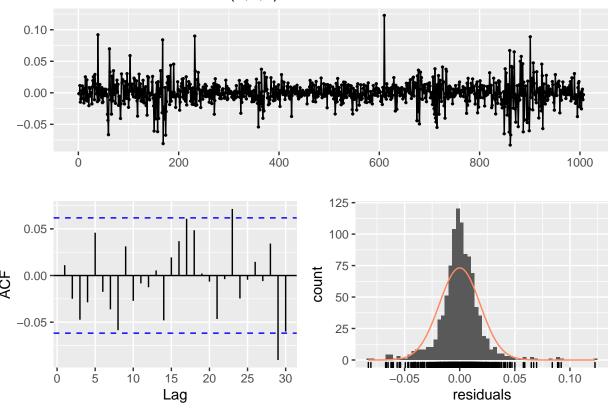
Box.test(res1, lag = 12, type = "Box-Pierce", fitdf=0)

##
## Box-Pierce test
##
## data: res1
## X-squared = 12.998, df = 12, p-value = 0.3692

Box.test(res1, lag = 12, type = "Ljung-Box", fitdf=0)

##
## Box-Ljung test
##
## data: res1
## X-squared = 13.104, df = 12, p-value = 0.3616
checkresiduals(auto_model1, include.mean=FALSE, plot=TRUE)
```

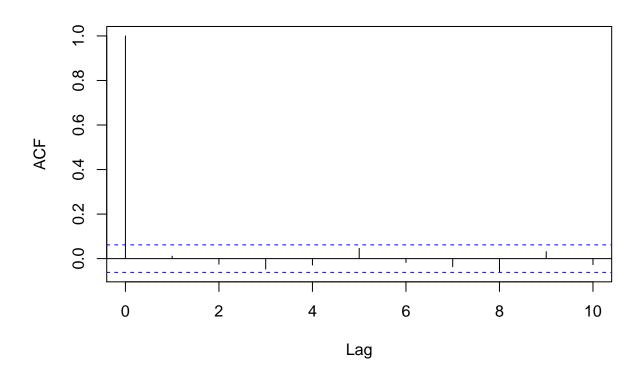
Residuals from ARIMA(0,0,0) with non-zero mean



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(0,0,0) with non-zero mean
## Q* = 12.87, df = 9, p-value = 0.1686
##
## Model df: 1. Total lags used: 10
```

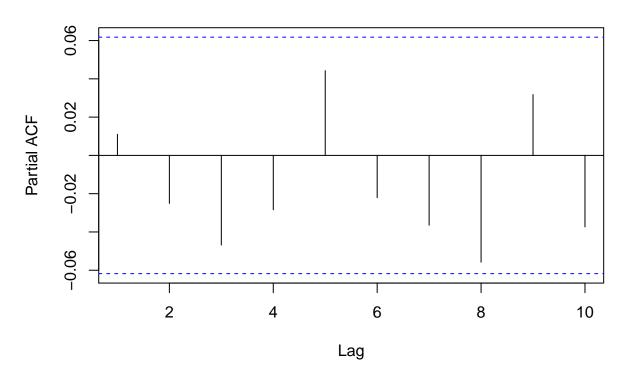
acf(train, lag=10)

Series train



pacf(train, lag=10)

Series train



```
arima_model=arima(train, order=c(1,0,1) )
arima_model
##
## Call:
## arima(x = train, order = c(1, 0, 1))
##
## Coefficients:
##
                         intercept
            ar1
                    ma1
##
         0.0051 0.0062
                            0.0014
## s.e. 1.2736 1.3051
                            0.0006
## sigma^2 estimated as 0.0003419: log likelihood = 2589.6, aic = -5171.2
BIC(auto_model1)
## [1] -5165.248
BIC(arima_model)
## [1] -5151.545
```

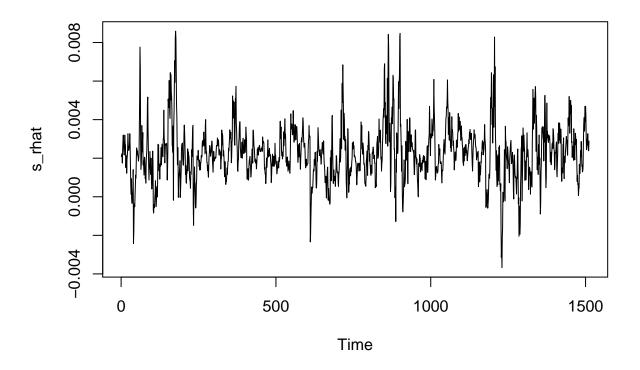
Modello ARMA(1,1)-sGARCH(1,1): fit, risultati e plot

```
# GARCH MODEL assumendo una distribuzione Normale
#sGARCH
library(rugarch)
```

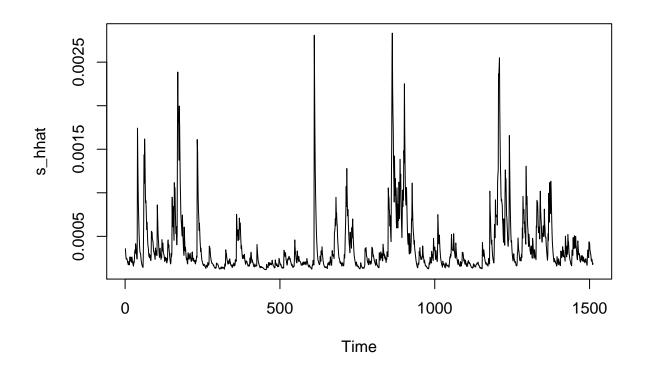
```
s_garchMod = ugarchspec(mean.model = list(armaOrder = c(1, 1), include.mean = TRUE
),
variance.model = list(model = 'sGARCH',
                 garchOrder = c(1, 1)),
distribution.model = "norm")
s_garchFit = ugarchfit(spec=s_garchMod, data=ts)
s garchFit
## *----*
    GARCH Model Fit *
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,1)
## Mean Model : ARFIMA(1,0,1)
## Distribution : norm
## Optimal Parameters
## -----
       Estimate Std. Error t value Pr(>|t|)
## mu
       0.002084 0.000315 6.6101 0
## ar1 0.797653 0.114210 6.9841
## ma1 -0.840888 0.101013 -8.3246
## omega 0.000027 0.000005 5.3200
## alpha1 0.181082 0.028111 6.4417
                                       0
## beta1 0.754320 0.030798 24.4923
                                        0
## Robust Standard Errors:
       Estimate Std. Error t value Pr(>|t|)
##
       0.002084 0.000405 5.1413 0.00000
## mu
       ## ar1
## ma1 -0.840888 0.111760 -7.5241 0.00000
## omega 0.000027 0.000011 2.5527 0.01069
## alpha1 0.181082 0.035858 5.0500 0.00000
## beta1 0.754320 0.043618 17.2939 0.00000
## LogLikelihood: 3999.049
## Information Criteria
##
## Akaike -5.2853
## Bayes
            -5.2642
## Shibata -5.2853
## Hannan-Quinn -5.2774
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                     statistic p-value
## Lag[1]
                        3.267 0.070701
```

```
## Lag[2*(p+q)+(p+q)-1][5] 4.934 0.004145
## Lag[4*(p+q)+(p+q)-1][9] 5.617 0.324344
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                        statistic p-value
                           0.3363 0.5620
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5]
                         0.6483 0.9326
## Lag[4*(p+q)+(p+q)-1][9] 1.0435 0.9844
## d.o.f=2
## Weighted ARCH LM Tests
   Statistic Shape Scale P-Value
## ARCH Lag[3] 0.06644 0.500 2.000 0.7966
## ARCH Lag[5] 0.30912 1.440 1.667 0.9378
## ARCH Lag[7] 0.44368 2.315 1.543 0.9832
## Nyblom stability test
## -----
## Joint Statistic: 0.6034
## Individual Statistics:
       0.14755
## mu
## ar1
      0.03782
## ma1 0.04302
## omega 0.05536
## alpha1 0.05712
## beta1 0.06437
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                    t-value prob sig
## Sign Bias 1.992939 0.04645 **
## Negative Sign Bias 0.594396 0.55234
## Positive Sign Bias 0.000715 0.99943
## Joint Effect 5.879244 0.11764
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##
   group statistic p-value(g-1)
## 1 20 90.5 2.709e-11
## 2 30 104.9 1.567e-10
## 3 40 109.5 1.313e-08
## 4 50 121.3 4.648e-08
##
##
## Elapsed time : 0.433579
```

```
## Risultati del modello
coef(s_garchFit)
##
                           ar1
                                         ma1
                                                     omega
                                                                  alpha1
             mu
   2.083982e-03
                 7.976531e-01 -8.408882e-01 2.717585e-05 1.810823e-01
##
##
           beta1
  7.543195e-01
s_rhat = s_garchFit@fit$fitted.values
plot.ts(s_rhat)
```

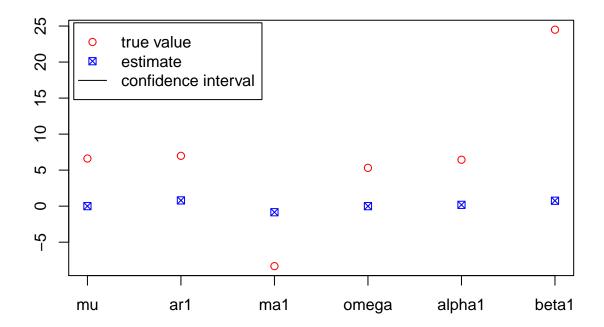


```
s_hhat = ts(s_garchFit@fit$sigma^2)
plot.ts(s_hhat)
```



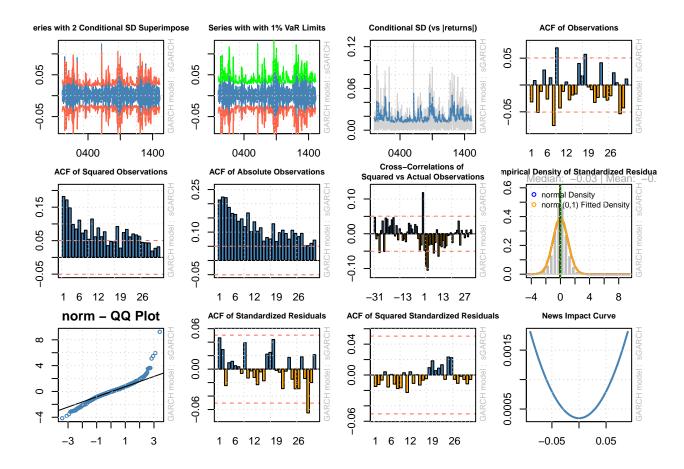
```
fit.val
            = coef(s_garchFit)
            = diag(vcov(s_garchFit))
fit.sd
true.val = s_garchFit@fit$tval
fit.conf.lb = fit.val + qnorm(0.025) * fit.sd
fit.conf.ub = fit.val + qnorm(0.975) * fit.sd
print(fit.val)
##
                                                     omega
                  7.976531e-01 -8.408882e-01 2.717585e-05 1.810823e-01
    2.083982e-03
##
##
           beta1
  7.543195e-01
print(fit.sd)
## [1] 9.939810e-08 1.304401e-02 1.020362e-02 2.609369e-11 7.902315e-04
## [6] 9.485306e-04
print(true.val)
##
                                              alpha1
          mu
                             ma1
                                     omega
                                                         beta1
                   ar1
   6.610052 6.984067 -8.324558
                                 5.320047
                                            6.441676 24.492306
plot(true.val, pch = 1, col = "red",
     ylim = range(c(fit.conf.lb, fit.conf.ub, true.val)),
     xlab = "", ylab = "", axes = FALSE)
box(); axis(1, at = 1:length(fit.val), labels = names(fit.val)); axis(2)
points(coef(s_garchFit), col = "blue", pch = 7)
```

```
for (i in 1:length(fit.val)) {
   lines(c(i,i), c(fit.conf.lb[i], fit.conf.ub[i]))
}
legend( "topleft", legend = c("true value", "estimate", "confidence interval"),
        col = c("red", "blue", 1), pch = c(1, 7, NA), lty = c(NA, NA, 1), inset = 0.01)
```



```
par(mfrow=c(2, 3))
par(mar = c(2, 2, 2, 2))
plot(s_garchFit,which="all")
```

##
please wait...calculating quantiles...



Confronto tra modelli

```
# confronto tra modelli
infocriteria(s_garchFit)[2] #BIC= -5.264179

## [1] -5.264179

BIC(auto_model1) # = -5165.248 -> è il valore più basso e quindi quello da

## [1] -5165.248

# scegliere. auto_model1 è il modello da scegliere

BIC(arima_model) # = -5151.545

## [1] -5151.545
```

Conclusione

Dopo una attenta analisi dei valori BIC, viene scelto il modello $\text{textbf}\{\text{auto_model1}\}$ poichè mostra il valore più basso di BIC. Tuttavia, il modello ARMA(1,1)-sGARCH(1,1), grazie alla presenza dell'equazione della varianza è in grado di fornire informazioni maggiori rispetto ai modelli ARMA che presentano la sola equazione della media.