

# The basic `larcc` module \*

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## Contents

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\*This document is part of the *Linear Algebraic Representation with CoChains* (LAR-CC) framework [?].  
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# 1 Basic representations

A few basic representation of topology are used in LARCC. They include some common sparse matrix representations: CSR (Compressed Sparse Row), CSC (Compressed Sparse Column), COO (Coordinate Representation), and BRC (Binary Row Compressed).

## 1.1 BRC (Binary Row Compressed)

We denote as BRC (Binary Row Compressed) the standard input representation of our LARCC framework. A BRC representation is an array of arrays of integers, with no requirement of equal length for the component arrays. The BRC format is used to represent a (normally sparse) binary matrix. Each component array corresponds to a matrix row, and contains the indices of columns that store a 1 value. No storage is used for 0 values.

**BRC format example** Let  $A = (a_{i,j} \in \{0,1\})$  be a binary matrix. The notation  $\text{BRC}(A)$  is used for the corresponding data structure.

$$A = \begin{pmatrix} 0, 1, 0, 0, 0, 0, 0, 1, 0, 0 \\ 0, 0, 1, 0, 0, 0, 0, 0, 0, 0 \\ 1, 0, 0, 1, 0, 0, 0, 0, 0, 1 \\ 1, 0, 0, 0, 0, 0, 1, 0, 0, 0 \\ 0, 0, 0, 0, 0, 1, 1, 1, 0, 0 \\ 0, 0, 1, 0, 1, 0, 0, 0, 1, 0 \\ 0, 0, 0, 0, 0, 0, 0, 0, 0, 0 \\ 0, 1, 0, 0, 0, 0, 0, 1, 0, 1 \\ 0, 0, 0, 1, 0, 0, 0, 0, 1, 0 \\ 0, 1, 1, 0, 1, 0, 0, 0, 0, 0 \end{pmatrix} \mapsto \text{BRC}(A) = \begin{matrix} [[1,7], \\ [2], \\ [0,3,9], \\ [0,6], \\ [5,6,7], \\ [2,4,8], \\ [], \\ [1,7,9], \\ [3,8], \\ [1,2,4]] \end{matrix}$$

## 1.2 Format conversions

First we give the function `format` to make the transformation from the sparse matrix as a list of triples  $(row, column, value)$  for each non-zero element, to the `scipy.sparse` format corresponding to the `shape` parameter, set by default to "`csr`", that stands for *Compressed Sparse Row*, the normal matrix format of the LARCC framework. @d From list of triples to `scipy.sparse` @def format(triples,shape="csr"): n = len(triples) data = arange(n) ij = arange(2\*n).reshape(2,n) for k,item in enumerate(triples): ij[0][k],ij[1][k],data[k] = item return `scipy.sparse.coo_matrix((data,ij)).asformat(shape)@@dBrcToCooTransformation@defcooCreateFrom`

# 2 Matrix operations

@d Query Matrix shape @def csrGetNumberOfRows(CSRm): Int = CSRm.shape[0] return Int

```

def csrGetNumberOfColumns(CSRm): Int = CSRm.shape[1] return Int @ @d Test ex-
amples of Query Matrix shape @print "!!! csrGetNumberOfRows" print "(csrFV) =", csr-
GetNumberOfRows(csrFV) print "(csrEV) =", csrGetNumberOfRows(csrEV) print "!!!
csrGetNumberOfColumns" print "(csrFV) =", csrGetNumberOfColumns(csrFV) print "(csrEV)
=", csrGetNumberOfColumns(csrEV) @ @d Sparse to dense matrix transformation @def
csrToMatrixRepresentation(CSRm): nrows = csrGetNumberOfRows(CSRm) ncolums =
csrGetNumberOfColumns(CSRm) ScipyMat = zeros((nrows,ncolums),int) C = CSRm.tocoo()
for triple in zip(C.row,C.col,C.data): ScipyMat[triple[0],triple[1]] = triple[2] return Scipy-
Mat @ @d Test examples of Sparse to dense matrix transformation @print "!!! csr-
ToMatrixRepresentation" print "=", csrToMatrixRepresentation(csrFV) print "=", csr-
ToMatrixRepresentation(csrEV) @ @d Matrix product and transposition @def matrix-
Product(CSRm1,CSRm2): CSRm = CSRm1 * CSRm2 return CSRm
def csrTranspose(CSRm): CSRm = CSRm.T return CSRm @ @d Matrix filtering to
produce the boundary matrix @def csrBoundaryFilter(CSRm, facetLengths): maxs =
[max(CSRm[k].data) for k in range(CSRm.shape[0])] inputShape = CSRm.shape coo =
CSRm.tocoo() for k in range(len(coo.data)): if coo.data[k]==maxs[coo.row[k]]: coo.data[k]
= 1 else: coo.data[k] = 0 mtm = coo.matrix((coo.data, (coo.row, coo.col)), shape = inputShape)out =
mtm.tocsr()returnout@@@TestexampleofMatrixfilteringtoproducetheboundarymatrix@print" >>> csrBo

```

### 3 Topological operations

```

@d From cells and facets to boundary operator @def boundary(cells,facets): csrCV = csr-
Create(cells) csrFV = csrCreate(facets) csrFC = matrixProduct(csrFV, csrTranspose(csrCV))
facetLengths = [csrCell.getnnz() for csrCell in csrCV] return csrBoundaryFilter(csrFC,facetLengths)
def coboundary(cells,facets): Boundary = boundary(cells,facets) return csrTranspose(Boundary)
@@ @d Test examples of From cells and facets to boundary operator @V = [[0.0, 0.0, 0.0],
[1.0, 0.0, 0.0], [0.0, 1.0, 0.0], [1.0, 1.0, 0.0], [0.0, 0.0, 1.0], [1.0, 0.0, 1.0], [0.0, 1.0, 1.0], [1.0,
1.0, 1.0]]
CV =[[0, 1, 2, 4], [1, 2, 4, 5], [2, 4, 5, 6], [1, 2, 3, 5], [2, 3, 5, 6], [3, 5, 6, 7]]
FV =[[0, 1, 2], [0, 1, 4], [0, 2, 4], [1, 2, 3], [1, 2, 4], [1, 2, 5], [1, 3, 5], [1, 4, 5], [2, 3, 5],
[2, 3, 6], [2, 4, 5], [2, 4, 6], [2, 5, 6], [3, 5, 6], [3, 5, 7], [3, 6, 7], [4, 5, 6], [5, 6, 7]]
EV =[[0, 1], [0, 2], [0, 4], [1, 2], [1, 3], [1, 4], [1, 5], [2, 3], [2, 4], [2, 5], [2, 6], [3, 5], [3,
6], [3, 7], [4, 5], [4, 6], [5, 6], [5, 7], [6, 7]]
print "2 = ",csrToMatrixRepresentation(coboundary(CV,FV))print"1 = ",csrToMatrixRepresentation
",csrToMatrixRepresentation(coboundary(EV,AA(LIST)(range(len(V))))))@@@Fromcellsandfacetstobou
def totalChain(cells): return csrCreate([[0] for cell in cells])
def boundaryCells(cells,facets): csrBoundaryMat = boundary(cells,facets) csrChain
= totalChain(cells) csrBoundaryChain = matrixProduct(csrBoundaryMat, csrChain) for
k,value in enumerate(csrBoundaryChain.data): if value boundaryCells = [k for k,val in enu-
merate(csrBoundaryChain.data.tolist()) if val == 1] return boundaryCells @ @d Test ex-

```

```

amples of From cells and facets to boundary cells @boundaryCells2 = boundaryCells(CV, FV)boundaryCells1
boundaryCells([FV[k]forkinboundaryCells2], EV)
    print "2 = ", boundaryCells2print"1 = ", boundaryCells1
    boundary = (V,[FV[k] for k in boundaryCells2])VIEW(EXPLODE(1.5, 1.5, 1.5)(MKPOLS(boundary)))
    compute the [face, coface] pair as vertex lists vertLists = [[FV[pair[0]], CV[pair[1]]]for
pair in pairs]
    compute two n-cells to compare for sign cellPairs = [ [list(set(coface).difference(face))+face,coface]
for face,coface in vertLists]
    compute the local indices of missing boundary cofaces missingVertIndices = [ co-
face.index(list(set(coface).difference(face))[0]) for face,coface in vertLists]
    compute the point matrices to compare for sign pointArrays = [ [[V[k]+[1.0] for k in
facetCell], [V[k]+[1.0] for k in cofaceCell]] for facetCell,cofaceCell in cellPairs]
    signed incidence coefficients cofaceMats = TRANS(pointArrays)[1] cofaceSigns = AA(SIGN)(AA(np.linalg.
faceSigns = AA(C(POWER)(-1))(missingVertIndices) signPairProd = AA(PROD)(TRANS([cofaceSigns,faceS
signed boundary matrix csrSignedBoundaryMat = csr_matrix((signPairProd, TRANS(pairs)))returncsrS

```

## Orienting polytopal cells

**input** : "cell" indices of a convex and solid polytopes and "V" vertices;

**output** : biggest "simplex" indices spanning the polytope.

**m** : number of cell vertices

**d** : dimension (number of coordinates) of cell vertices

**d+1** : number of simplex vertices

**vcell** : cell vertices

**vsimplex** : simplex vertices

**Id** : identity matrix

**basis** : orthonormal spanning set of vectors  $e_k$

**vector** : position vector of a simplex vertex in translated coordinates

**unUsedIndices** : cell indices not moved to simplex

```

@d Oriented boundary cells for simplicial models @def pivotSimplices(V, CV, d=3): sim-
plices = [] for cell in CV: vcell = np.array([V[v] for v in cell]) m, simplex = len(cell), []
translate the cell: for each k, vcell[k] -= vcell[0], and simplex[0] := cell[0] for k in range(m-1,-
1,-1): vcell[k] -= vcell[0] simplex = [0], basis = [], tensor = Id(d+1) simplex += [cell[0]] ba-
sis = [] tensor = np.array(IDNT(d)) look for most far cell vertex dists = [SUM([SQR(x) for

```

```

x in v])**0.5 for v in vcell] maxDistIndex = max(enumerate(dists),key=lambda x: x[1])[0]
vector = np.array([vcell[maxDistIndex]]) normalize vector den=(vector**2).sum(axis=-1)
**0.5 basis = [vector/den] simplex += [cell[maxDistIndex]] unUsedIndices = [h for h in
cell if h not in simplex]

```

```

for k in 2,d+1: for k in range(2,d+1): update the orthonormal tensor e = basis[-1]
tensor = tensor - np.dot(e.T, e) compute the index h of a best vector look for most far cell
vertex dists = [SUM([SQR(x) for x in np.dot(tensor,v)])**0.5 if h in unUsedIndices else 0.0
for (h,v) in zip(cell,vcell)] insert the best vector index h in output simplex maxDistIndex
= max(enumerate(dists),key=lambda x: x[1])[0] vector = np.array([vcell[maxDistIndex]])
normalize vector den=(vector**2).sum(axis=-1) **0.5 basis += [vector/den] simplex +=
[cell[maxDistIndex]] unUsedIndices = [h for h in cell if h not in simplex] simplices +=
[simplex] return simplices

```

```

def simplexOrientations(V,simplices): vcells = [[V[v]+[1.0] for v in simplex] for simplex
in simplices] return [SIGN(np.linalg.det(vcell)) for vcell in vcells] @ @d Computation of cell
adjacencies @def larCellAdjacencies(CSRm): CSRm = matrixProduct(CSRm,csrTranspose(CSRm))
return CSRm @ @d Test examples of Computation of cell adjacencies @print "lll larCel-
lAdjacencies" adj2cells = larCellAdjacencies(csrFV)print"2cells = ",csrToMatrixRepresentation(adj2cells)
larCellAdjacencies(csrEV)print"1cells = ",csrToMatrixRepresentation(adj1cells)@ @dExtractionof facet

```

```

def larFacets(model,dim=3): """ Estraction of (d-1)-cellFacets from "model" := (V,d-
cells) Return (V, (d-1)-cellFacets) """ V,cells,csr,csrAdjSquareMat = setup(model,dim)
cellFacets = [] for each input cell i for i in range(len(cells)): adjCells = csrAdjSquare-
Mat[i].tocoo() cell1 = csr[i].tocoo().col pairs = zip(adjCells.col,adjCells.data) for j,v in
pairs: if (ij): cell2 = csr[j].tocoo().col cell = list(set(cell1.intersection(cell2))) cellFacets.append(sorted(cell))
sort and remove duplicates cellFacets = sorted(AA(list)(set(AA(tuple)(cellFacets)))) re-
turn V,cellFacets @ @d Test examples of Extraction of facets of a cell complex @V =
[[0.,0.],[3.,0.],[0.,3.],[3.,3.],[1.,2.],[2.,2.],[1.,1.],[2.,1.]] FV = [[0,1,6,7],[0,2,4,6],[4,5,6,7],[1,3,5,7],[2,3,4,5],[0,1,2,3]]
EV = larFacets((V,FV),dim = 2)print" = ",EVVIEW(EXPLODE(1.5,1.5,1.5)(MKPOLLS((V,EV),
FV = [[0,1,3],[1,2,4],[2,4,5],[3,4,6],[4,6,7],[5,7,8], full [1,3,4],[4,5,7], empty [0,1,2],[6,7,8],[0,3,6],[2,5,8]]
exterior
EV = larFacets((V,FV),dim = 2)print" = ",EV@

```

## 4 Exporting the library

### 4.1 MIT licence

@d The MIT Licence @ """ The MIT License =====

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ware and associated documentation files (the 'Software'), to deal in the Software without  
restriction, including without limitation the rights to use, copy, modify, merge, publish,  
distribute, sublicense, and/or sell copies of the Software, and to permit persons to whom  
the Software is furnished to do so, subject to the following conditions:

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## 4.2 Importing of modules or packages

```
@d Importing of modules or packages @
from pyplasm import *
import collections
import scipy
import numpy as np
from scipy import zeros, arange, mat, amin, amax
from scipy.sparse import vstack, hstack, csr_matrix, coo_matrix, lil_matrix, triu
from lar2psm import *
```

## 4.3 Writing the library file

```
@o lib/py/larcc.py @
-*- coding: utf-8 -*- """ Basic LARCC library """ @
i The MIT Licence @
i Importing of modules or packages @
i From list of triples to scipy.sparse @
i Brc to Coor transformation @
i Coor to Csr transformation @
i Brc to Csr transformation @
i Query Matrix shape @
i Sparse to dense matrix transformation @
i Matrix product and transposition @
i Matrix filtering to produce the boundary matrix @
i Matrix filtering via a generic predicate @
i From cells and facets to boundary operator @
i From cells and facets to boundary cells @
i Signed boundary matrix for simplicial models @
i Oriented boundary cells for simplicial models @
i Computation of cell adjacencies @
i Extraction of facets of a cell complex @
if __name__ == "__main__": @ <Testexamples> @
```

## 5 Unit tests

```
@d Test examples @
i Test example of Brc to Coor transformation @
i Test example of Coor to Csr transformation @
i Test example of Brc to Csr transformation @
i Test examples of Query Matrix shape @
i Test examples of Sparse to dense matrix transformation @
i Test example of Matrix filtering to produce the boundary matrix @
i Test example of Matrix filtering via a generic predicate @
i Test examples of From cells and facets to boundary operator @
i Test examples of From cells and facets to boundary cells @
i Test examples of Computation of cell adjacencies @
i Test examples of Extraction of facets of a cell complex @
```

## A Tutorial

### A.1 Common macros

#### A.1.1 Model generation, skeleton and boundary extraction

@o test/py/larcc/ex1.py @ from larcc import \* from largrid import \* @i input of 2D topology and geometry data @i @i characteristic matrices @i @i incidence matrix @i @i boundary and coboundary operators @i @i product of cell complexes @i @i 2-skeleton extraction @i @i 1-skeleton extraction @i @i 0-coboundary computation @i @i 1-coboundary computation @i @i 2-coboundary computation @i @i boundary chain visualisation @i @

@d input of 2D topology and geometry data @ input of topology and geometry V2 = [[4,10],[8,10],[14,10],[8,7],[14,7],[4,4],[8,4],[14,4]] EV = [[0,1],[1,2],[3,4],[5,6],[6,7],[0,5],[1,3],[2,4],[3,6],[4,7]] FV = [[0,1,3,5,6],[1,2,3,4],[3,4,6,7]] @

@d characteristic matrices @ characteristic matrices csrFV = csrCreate(FV) csrEV = csrCreate(EV) print "=", csrToMatrixRepresentation(csrFV) print "=", csrToMatrixRepresentation(csrEV) @

@d incidence matrix @ product csrEF = matrixProduct(csrEV, csrTranspose(csrFV)) print "=", csrToMatrixRepresentation(csrEF) @

@d boundary and coboundary operators @ boundary and coboundary operators facetLengths = [csrCell.getnnz() for csrCell in csrEV] boundary = csrBoundaryFilter(csrEF,facetLengths) coboundary<sub>1</sub> = *csrTranspose(boundary)* print "1 = ", *csrToMatrixRepresentation(coboundary<sub>1</sub>)* @

@d product of cell complexes @ product operator mod<sub>2</sub>D = (V2, FV)V1, *topol*<sub>0</sub> = [[0.], [1.], [2.]], [[0], [1], [2]] *topol*<sub>1</sub> = [[0, 1], [1, 2]] mod<sub>0</sub>D = (V1, *topol*<sub>0</sub>) mod<sub>1</sub>D = (V1, *topol*<sub>1</sub>) V3, CV = *larModelProduct*([mod<sub>2</sub>D, mod<sub>1</sub>D]) mod<sub>3</sub>D = (V3, CV) VIEW(EXPLODE(1.2, 1.2, 1.2))(MKPOLLS(mod<sub>3</sub>D), len(CV), "" @

@d 2-skeleton extraction @ 2-skeleton of the 3D product complex mod<sub>2</sub>D<sub>1</sub> = (V2, EV) mod<sub>3</sub>D<sub>h</sub>2 = *larModelProduct*([mod<sub>2</sub>D, mod<sub>0</sub>D]) mod<sub>3</sub>D<sub>v</sub>2 = *larModelProduct*([mod<sub>2</sub>D<sub>1</sub>, mod<sub>1</sub>D]), FV<sub>h</sub> = mod<sub>3</sub>D<sub>h</sub>2, FV<sub>v</sub> = mod<sub>3</sub>D<sub>v</sub>2 FV3 = FV<sub>h</sub> + FV<sub>v</sub> SK2 = (V3, FV3) VIEW(EXPLODE(1.2, 1.2, 1.2))(MKPOLLS(mod<sub>3</sub>D, len(FV3), "" @

@d 1-skeleton extraction @ 1-skeleton of the 3D product complex mod<sub>2</sub>D<sub>0</sub> = (V2, AA(LIST)(range(len(V2)))) mod<sub>3</sub>D<sub>h</sub>1 = *larModelProduct*([mod<sub>2</sub>D<sub>1</sub>, mod<sub>0</sub>D]) mod<sub>3</sub>D<sub>v</sub>1 = *larModelProduct*([mod<sub>2</sub>D<sub>0</sub>, mod<sub>1</sub>D]), EV<sub>h</sub> = mod<sub>3</sub>D<sub>h</sub>1, EV<sub>v</sub> = mod<sub>3</sub>D<sub>v</sub>1 EV3 = EV<sub>h</sub> + EV<sub>v</sub> SK1 = (V3, EV3) VIEW(EXPLODE(1.2, 1.2, 1.2))(MKPOLLS(mod<sub>3</sub>D, len(EV3), "" @

@d 0-coboundary computation @ boundary and coboundary operators np.set\_printoptions(threshold = sys.maxint) csrFV3 = csrCreate(FV3) csrEV3 = csrCreate(EV3) csrVE3 = csrTranspose(csrEV3) facetLengths = [csrCell.getnnz() for csrCell in csrEV3] boundary = csrBoundaryFilter(csrVE3, facetLengths) coboundary<sub>0</sub> = csrTranspose(boundary) print "0 = ", csrToMatrixRepresentation(coboundary<sub>0</sub>) @

@d 1-coboundary computation @ csrEF3 = matrixProduct(csrEV3, csrTranspose(csrFV3)) facetLengths = [csrCell.getnnz() for csrCell in csrFV3] boundary = csrBoundaryFilter(csrEF3, facetLengths) coboundary<sub>1</sub> = *csrTranspose(boundary)* print "1.T = ", *csrToMatrixRepresentation(coboundary<sub>1</sub>.T)* @

```

@d 2-coboundary computation @csrCV = csrCreate(CV) csrFC3 = matrixProduct(csrFV3,
csrTranspose(csrCV)) facetLengths = [csrCell.getnnz() for csrCell in csrCV] boundary =
csrBoundaryFilter(csrFC3,facetLengths) coboundary2 = csrTranspose(boundary)print"2 =
",csrToMatrixRepresentation(coboundary2)@

```

```

@d boundary chain visualisation @ boundary chain visualisation boundaryCells2 =
boundaryCells(CV, FV3)boundary = (V3, [FV3[k]forkinboundaryCells2])VIEW(EXPLODE(1.5, 1.5, 1.5))

```

### A.1.2 Boundary of 3D simplicial grid

```

@o test/py/larcc/ex2.py @ @i boundary of 3D simplicial grid @i @
@d boundary of 3D simplicial grid @from simplexn import * from larcc import *
V,CV = larSimplexGrid([10,10,3]) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOLs((V,CV))))
SK2 = (V,larSimplexFacets(CV)) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOLs(SK2))) ,FV =
SK2SK1 = (V,larSimplexFacets(FV)),EV = SK1VIEW(EXPLODE(1.5, 1.5, 1.5)(MKPOLs(SK1)))
boundaryCells2 = boundaryCells(CV, FV)boundary = (V, [FV[k]forkinboundaryCells2])VIEW(EXPL
",boundaryCells2@

```

### A.1.3 Oriented boundary of a random simplicial complex

```

@o test/py/larcc/ex3.py @@i Importing external modules @i @i Generating and viewing
a random 3D simplicial complex @i @i Computing and viewing its non-oriented boundary
@i @i Computing and viewing its oriented boundary @i @

```

```

@d Importing external modules @from simplexn import * from larcc import * from
scipy.spatial import Delaunay import numpy as np @

```

```

@d Generating and viewing a random 3D simplicial complex @verts = np.random.rand(10000,
3) 1000 points in 3-d verts = [AA(lambda x: 2*x)(VECTDIFF([vert,[0.5,0.5,0.5]])) for vert
in verts] verts = [vert for vert in verts if VECTNORM(vert) < 1.0] tetra = Delaunay(verts)
cells = [cell for cell in tetra.vertices.tolist() if ((verts[cell[0]][2]>0) and (verts[cell[1]][2]>0) and
(verts[cell[2]][2]>0) and (verts[cell[3]][2]>0) ) ] V, CV = verts, cells VIEW(MKPOL([V,AA(AA(lambda
k:k+1))(CV),[]])) @

```

```

@d Computing and viewing its non-oriented boundary @FV = larSimplexFacets(CV)
VIEW(MKPOL([V,AA(AA(lambda k:k+1))(FV),[]])) boundaryCells2 = boundaryCells(CV, FV)print"2 =
",boundaryCells2bndry = (V, [FV[k]forkinboundaryCells2])VIEW(EXPLODE(1.5, 1.5, 1.5)(MKPOLs(b

```

```

@d Computing and viewing its oriented boundary @boundaryCells2 = signedBoundaryCells(V, CV, FV)pr
",boundaryCells2def swap(mylist) : return[mylist[1]]+[mylist[0]]+mylist[2:]boundaryFV =
[FV[-k]if k < 0elseswap(FV[k])forkinboundaryCells2]bndry = (V, boundaryFV)VIEW(EXPLODE(1.5,

```

### A.1.4 Oriented boundary of a simplicial grid

```

@o test/py/larcc/ex4.py @@i Generate and view a 3D simplicial grid @i @i Computing
and viewing the 2-skeleton of simplicial grid @i @i Computing and viewing the oriented
boundary of simplicial grid @i @

```



```

@d Generate and view a 3D simplicial grid @from simplexn import * from larcc import
* V,CV = larSimplexGrid([4,4,4]) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOL((V,CV)))) @
@d Computing and viewing the 2-skeleton of simplicial grid @FV = larSimplexFacets(CV)
EV = larSimplexFacets(FV) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOL((V,FV)))) @
@d Computing and viewing the oriented boundary of simplicial grid @csrSignedBound-
aryMat = signedBoundary (V,CV,FV) boundaryCells2 = signedBoundaryCells(V,CV,FV)def swap(l) :
return[l[1],l[0],l[2]]boundaryFV = [FV[-k]if k < 0elseswap(FV[k])forkinboundaryCells2]boundary =
(V,boundaryFV)VIEW(EXPLODE(1.5,1.5,1.5)(MKPOL(boundary)))@

```

### A.1.5 Skeletons and oriented boundary of a simplicial complex

```

@o test/py/larcc/ex5.py @@i Skeletons computation and visualisation @i @i Oriented
boundary matrix visualization @i @i Computation of oriented boundary cells @i @

```

```

@d Skeletons computation and visualisation @from simplexn import * from larcc im-
port * V,FV = larSimplexGrid([3,3]) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOL((V,FV))))
EV = larSimplexFacets(FV) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOL((V,EV)))) VV =
larSimplexFacets(EV) VIEW(EXPLODE(1.5,1.5,1.5)(MKPOL((V,VV)))) @

```

```

@d Oriented boundary matrix visualization @np.set_printoptions(threshold = ' nan')csrSignedBoundaryM
signedBoundary(V,FV,EV)Z = csrToMatrixRepresentation(csrSignedBoundaryMat)print" =
",Zfrompylabimport * matshow(Z)show()@

```

```

@d Computation of oriented boundary cells @boundaryCells1 = signedBoundaryCells(V,FV,EV)print"
",boundaryCells1def swap(mylist) : return[mylist[1]]+[mylist[0]]+mylist[2:]boundaryEV =
[EV[-k]if k < 0elseswap(EV[k])forkinboundaryCells1]bndry = (V,boundaryEV)VIEW(EXPLODE(1.5,

```

### A.1.6 Boundary permutation of random 2D simplicial complex

```

@o test/py/larcc/ex5.py @@i Skeletons computation and visualisation @i @i Oriented
boundary matrix visualization @i @i Computation of oriented boundary cells @i @

```

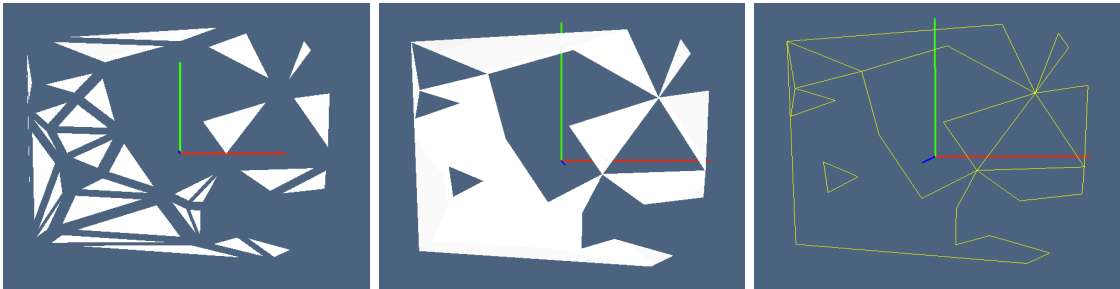


Figure 1: example caption

```

@d aaaaaa @from simplexn import * from larcc import * from scipy.spatial import
Delaunay def quasiEquilateral(tria): a = VECTNORM(VECTDIFF(tria[0:2])) b = VECT-

```

```

NORM(VECTDIFF(tria[1:3])) c = VECTNORM(VECTDIFF([tria[0],tria[2]])) m = max(a,b,c)
if m/a > 1.7 and m/b > 1.7 and m/c > 1.7: return True else: return False @
@d aaaaaa @verts = np.random.rand(20,2) verts = (verts - [0.5,0.5]) * 2 triangles
= Delaunay(verts) cells = [ cell for cell in triangles.vertices.tolist() if (not quasiEquilat-
eral([verts[k] for k in cell])) ] V, FV = AA(list)(verts), cells EV = larSimplexFacets(FV)
pols2D = MKPOLS((V,FV)) VIEW(EXPLODE(1.5,1.5,1.5)(pols2D)) @
@d aaaaaa @boundaryCells1 = signedBoundaryCells(V, FV, EV) print "1 = ", boundaryCells1 def swap(m
return [mylist[1]]+[mylist[0]]+mylist[2 :]) boundaryEV = [EV[-k] if k < 0 else swap(EV[k]) for k in boundaryC
(V, boundaryEV) VIEW(STRUCT(MKPOLS(bndry)+pols2D)) VIEW(COLOR(RED)(STRUCT(MKP

```

## A.2 Examples exporting

```

@d aaaaaa @ @j aaaaaa @i @

```