# Principles of Biomedical Ultrasound and Photoacoustics hw03: Photoacoustic Depth Profiling and SO2 Measurement

Due on Tuesday, Dec 12, 2017

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# 1 Part I

## 1.1 Repeat Fig.1 in reference paper

In the reference paper, they had simulated an acoustic wave of forward and backward wave. In this problem, we need to reproduce this fig. Figure 1 shows the result.

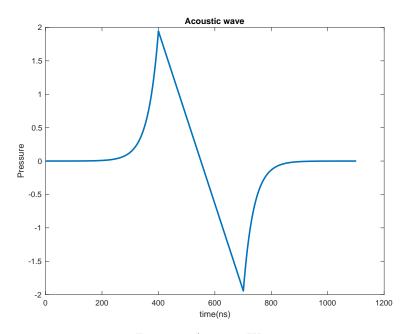


Figure 1: Acoustic Wave

Because the part between positive and negative wave is implicit, I only use a straight line connecting the two peak points by dynamically solving a linear equation and make the space between them 300 ns.

## 1.2 Repeat Fig.2 in reference paper

Now add a gaussian noise to our signal which the ratio of standard deviation of the noise to the peak of the simulated photoacoustic signal is 5%. Figure 2 shows the noisy signal and Figure 3 shows the exponential decay of signal.

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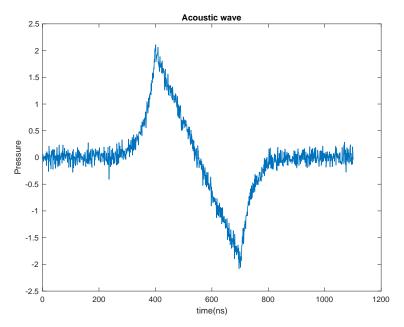


Figure 2: Acoustic Wave with noise

In the reference paper, there is a equation for curve fitting this decay from author's experimental result.

$$p(z) = 9.5 \exp^{-185z}$$

Because the parameters I used is different, I adjust the amplitude from 9.5 to 1.94 as shown in Equation 1.

$$p(z) = 1.94 \exp^{-185z} \tag{1}$$

Now Figure 3 show the noisy decay and curve of Equation 1.

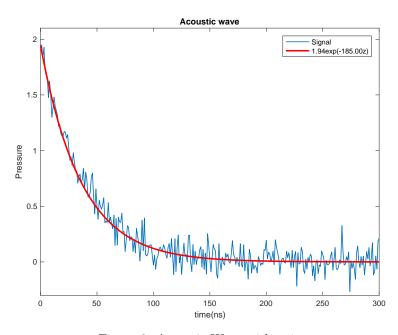


Figure 3: Acoustic Wave with noise

In this figure, we can find that Equation 1 is fitting well.

#### 1.3 Curve fitting for absorbtion coefficient

Now from Figure 3, we apply curve fitting and get our estimated  $\mu_a$  of noisy signal. Figure 4 shows the estimated curve and noisy signal.

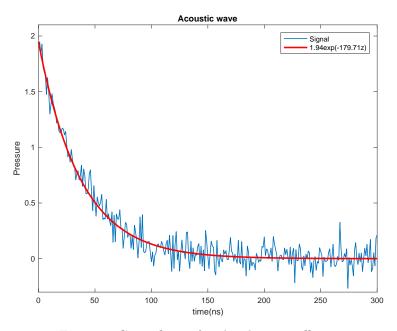


Figure 4: Curve fitting for absorbtion coefficient

From my experimental result, the range of estimated  $\mu_a$  is from 178 to 182 and the real  $\mu_a$  I used is 180. As a result, the curve fits the signal pretty well I think.

#### 1.4 Peak value vs absorbtion coefficient

Theoretically, the peak of signal will proportional to  $\mu_a$  which is  $\mu_a \times \Gamma \times H_0 = 0.0108\mu_a$  in my case. so in this part, we need to plot the peak value of different absorbtion coefficient from 10 to 180. Figure 5 shows the result.

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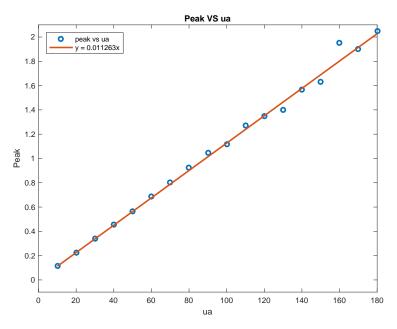


Figure 5: peak vs absorbtion coefficient

For better visualization, I also plot the curve fitting result for peak and  $\mu_a$  and the slope is 0.011 which is very close to theoretical value 0.0108. So the peak value of noisy signal is still proportional to  $\mu_a$ .

# 1.5 $\mu_a$ (estimated) vs $\mu_a$ (real)

Similar to Section 1.4, now for each  $\mu_a$  we need to use curve fitting to estimate absorbtion coefficient for them. Figure 6 shows the result.

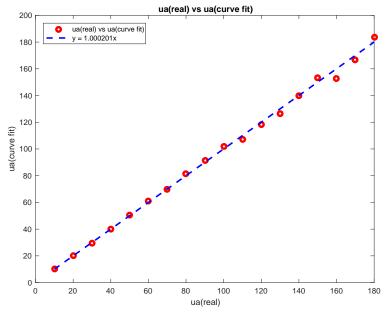


Figure 6:  $\mu_a$  (estimated) vs  $\mu_a$  (real)

For better visualization, I use curve fitting for  $\mu_a$  (estimated) vs  $\mu_a$  (real) in Figure 6 and the slope is about 1. As a result, our estimated  $\mu_a$  is really close to real one.

#### 1.6 Repeat 4 and 5 with transducer impulse response

Now we repeat 4 and 5 but considering transducer impulse response. Assume the impulse responses of the transducer used are Gaussian pulse centered at 5 MHz, 10 MHz, 25 MHz, and 50 MHz, respectively, with -6 dB fractional bandwidth of 60%

#### 1.6.1 Peak value vs absorbtion coefficient

Figure 7 show the result of Peak value vs absorbtion coefficient.

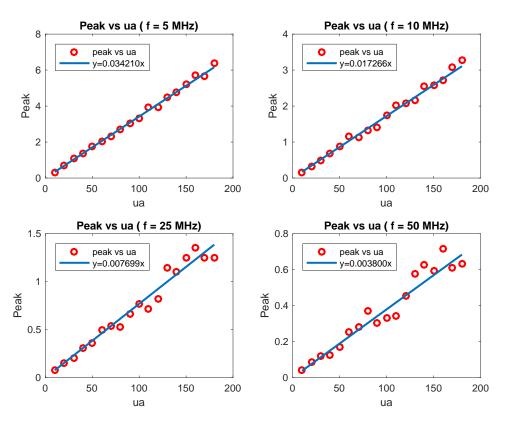


Figure 7: Peak value vs absorbtion coefficient

In Figure 7, the scalar of between peal and  $\mu_a$  is not 0.011. However, we can find that their relation is still proportional from the four sub figures. And when center frequency of transducer become larger, the figure become more noisy

#### 1.6.2 $\mu_a$ (estimated) vs $\mu_a$ (real)

Figure 8 show the result.

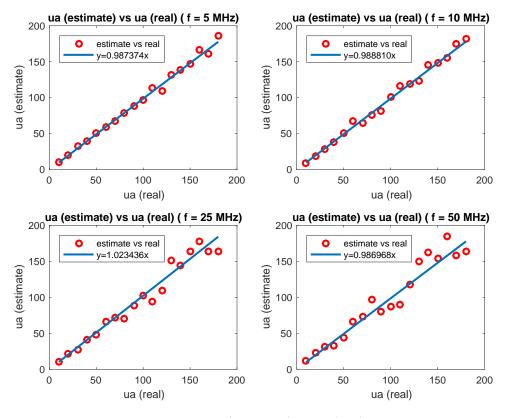


Figure 8:  $\mu_a$  (estimated) vs  $\mu_a$  (real)

In Figure 8, we can find that the estimated  $\mu_a$  is still close to real  $\mu_a$  and the slope is about 1, but when transducer center frequency gets larger, the points become much noisier.