724 Macroeconomic Theory: Investment Adjustment Costs

Curtis Aquino & Juan David Rios April 30, 2017

Introduction

- Outline models being compared (no equations)
- Overview of analysis and results

Description

- Description of standard RBC model
- Description of investment adjustment costs
- Methods used to solve RBC model
- Methods used to solve investment adjustment costs
- How was RBC model simulated
- How was investment adjustment costs model simulated

Analysis

- Compare the two models
- table of moments reporting sd, sd relative to Y, and autocorrelations, correlation with output for all variables of interest.
- Highlight difference in the moments of the two models
- What is causing these differences?
- Key economic forces driving these results
- Use impulse response functions to clarify explanations and illustrate economics of the system.
- Check sensitivity of results to key parameter choices
- Compare your results to one published article using related models.

Conclusion

• A brief conclusion

Matlab Code

• Provide matlab code

Appendix

- Derivations of first order conditions
- Derivation of steady state.

Rough Work

RBC model

$$\max E_0 \sum_{t=0}^{\infty} \beta^t [\ln(c_t) + \psi \ln(1 - n_t)] \text{ s.t.}$$

$$y_t = c_t + i_t$$

$$y_t = A_t k_t^{\alpha} n_t^{1-\alpha}$$

$$k_{t+1} = i_t + (1 - \delta) k_t$$

$$\ln(A_{t+1}) = \rho \ln(A_t) + \epsilon_{t+1} \text{ where } \epsilon_{t+1} \sim iid(0, \sigma_{\epsilon}^2)$$

$$k_0 \text{ and } A_0 \text{ are given and } > 0$$

with $\psi > 0, \beta, \delta, \rho \in (0, 1)$

Choice variables being consumption, capital in the next period, investment, labour supply and leisure. Have subtituted out leisure for $(1 - n_t)$.

Solve through optimal control. Using the constraints for y_t and k_t

$$A_t k_t^{\alpha} n_t^{1-\alpha} = c_t + i_t$$

$$A_t k_t^{\alpha} n_t^{1-\alpha} = c_t + k_{t+1} - (1-\delta)k_t$$

$$0 = A_t k_t^{\alpha} n_t^{1-\alpha} - c_t - k_{t+1} + (1-\delta)k_t$$

Setting up Lagrange

$$L = E_0 \sum_{t=0}^{\infty} \beta^t [\ln(c_t) + \psi \ln(1 - n_t)] + \beta^t \lambda_t [A_t k_t^{\alpha} n_t^{1-\alpha} - c_t - k_{t+1} + (1 - \delta) k_t]$$

$$\frac{\partial L}{\partial c_t} : \frac{1}{c_t} = \lambda_t$$

$$\frac{\partial L}{\partial n_t} : \frac{\psi}{(1 - n_t)} = \lambda_t$$

$$: \frac{\psi}{(1 - n_t)} = \frac{1}{c_t} [(1 - \alpha) \frac{y_t}{n_t}]$$

$$\frac{\partial L}{\partial k_{t+1}} : \lambda_t = \lambda_{t+1} \beta [\alpha \frac{y_{t+1}}{k_{t+1}} + (1 - \delta)]$$

$$: \frac{1}{c_t} = \frac{1}{c_{t+1}} \beta [\alpha \frac{y_{t+1}}{k_{t+1}} + (1 - \delta)]$$

^{**} Need to solve for steady state**

Investment adjustment cost model

This model introduces adjustment cost to changing the level of investment between periods. Rational for introducing investment adjustment costs?.

Critical addition is in the capital accumulation equation.

$$k_{t+1} = i_t - \theta(\frac{i_t}{i_{t-1}})i_t + (1 - \delta)k_t$$

Where θ represents the cost of adjusting capital and is a function of both current period investment and previous periods investment.

Using the same preferences as RBC Not so sure this is the model we want to use

$$\max E_0 \sum_{t=0}^{\infty} \beta^t [\ln(c_t) + \psi \ln(1 - n_t)] \text{ s.t.}$$

$$y_t = c_t + i_t$$

$$y_t = A_t k_t^{\alpha} n_t^{1-\alpha}$$

$$k_{t+1} = [1 - \theta(\frac{i_t}{i_{t-1}})] i_t + (1 - \delta) k_t$$

$$\ln(A_{t+1}) = \rho \ln(A_t) + \epsilon_{t+1} \text{ where } \epsilon_{t+1} \sim iid(0, \sigma_{\epsilon}^2)$$

$$k_0 \text{ and } A_0 \text{ are given and } > 0$$