

# Lecture #23: Iterators on Trees

## Slight Correction from Last Time

- In the last lecture, I defined

```
class BinTree(Tree):  
    def __iter__(self): return tree_iter(self)
```

- However, there is already an `__iter__` method on `BinTree`, inherited from `Tree`, which iterates over the tree's children.
- So instead, let's define (and document)

```
class BinTree(Tree):  
    def preorder_values(self):  
        """My labels, delivered in preorder (node label first, then labels  
        of left child in preorder, then labels of right child in preorder.  
>>> T = BinTree(10, BinTree(5, BinTree(2), BinTree(6)), BinTree(15))  
>>> for v in T.preorder_values(): print(v, end=" ")  
10 5 2 6 15  
>>> list(T.preorder_values())  
[10, 5, 2, 6, 15]"""  
    return tree_iter(self)
```

- The `for` statement above shows why it is useful to have iterators (like `tree_iter`) have an `__iter__` method: it allows a `for` loop to take *either* an iterable or an iterator.

# Iterating Over a Binary Tree: Strategy

- To create an iterator on a tree, consider this reimplement of `tree_to_list_preorder` from Lecture 21 (for binary trees):

```
def tree_to_list_preorder(T):  
    """The list of all labels in T, listing the labels  
    of trees before those of their children, and listing their  
    children left to right (preorder).  
    if T.is_empty:  
        return ()  
    else:  
        return (T.label,) + tree_to_list_preorder(T.left) \  
            + tree_to_list_preorder(T.right)
```

- Suppose that we wanted to return just the first item (T's label). What work would be left to do?
- Clearly, returning (iterating through) all the values in the left child and then on the right.
- To get the next value (after T's label), we'll need to *start* iterating through the left child, leaving *its* children to be processed.
- When the next tree in the queue is empty, discard it.

# Iterating Over a Binary Tree: Data Structure

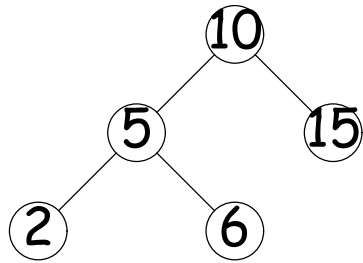
- So, to iterate over a tree, let's have our iterator consist of a *list of subtrees that still need iterating over*.

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]
    ...
    def __next__(self): ?

# Have iterator implement __iter__, so that it can
# be used in for statements, etc.
def __iter__(self): return self
```

# Iterating Over a Binary Tree: Example

- Suppose that we create `iter = T.preorder_values()` where `T` is



- Initially, `iter._work_queue` would contain just the tree rooted at the node labeled 10 (let's just say 'Tree 10' from now on).
- After the first call to `iter.__next__()`, which returns 10, `iter._work_queue` would contain [Tree 5, Tree 15]
- After the second call to `iter.__next__()`, which returns 5, `iter._work_queue` would contain [Tree 2, Tree 6, Tree 15]
- Then [Empty, Empty, Tree 6, Tree 15]
- Then, throw away the empty trees and process Tree 6, returning 6 and leaving its children: [Empty, Empty, Tree 15]

# Iterating Over a Binary Tree: Code

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while _____:
            subtree = self._work_queue.pop(0) # Get first item
            if subtree.is_empty:

            else:
                _____ = subtree.left, subtree.right
            return _____

        _____

    def __iter__(self): return self
```

# Iterating Over a Binary Tree: Code

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while len(self._work_queue) > 0:
            subtree = self._work_queue.pop(0) # Get first item
            if subtree.is_empty:
                _____
            else:
                _____ = subtree.left, subtree.right
            return _____
        _____

    def __iter__(self): return self
```

# Iterating Over a Binary Tree: Code

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while len(self._work_queue) > 0:
            subtree = self._work_queue.pop(0) # Get first item
            if subtree.is_empty:
                pass
            else:
                _____ = subtree.left, subtree.right
                return _____
        _____

    def __iter__(self): return self
```



## Iterating Over a Binary Tree: Code

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while len(self._work_queue) > 0:
            subtree = self._work_queue.pop(0) # Get first item
            if subtree.is_empty():
                pass
            else:
                self._work_queue[0:0] = subtree.left, subtree.right
                return subtree.left

def __iter__(self): return self
```

# Iterating Over a Binary Tree: Code

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while len(self._work_queue) > 0:
            subtree = self._work_queue.pop(0) # Get first item
            if subtree.is_empty:
                pass
            else:
                self._work_queue[0:0] = subtree.left, subtree.right
                return subtree.label



---



    def __iter__(self): return self
```

# Iterating Over a Binary Tree: Code

```
class BinTree(Tree):
    ...
    def preorder_values(self): return tree_iter(self)
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while len(self._work_queue) > 0:
            subtree = self._work_queue.pop(0) # Get first item
            if subtree.is_empty:
                pass
            else:
                self._work_queue[0:0] = subtree.left, subtree.right
                return subtree.label
        raise StopIteration

    def __iter__(self): return self
```

## Small Technical Node on Speed

- Inserting and deleting from the beginning of a Python list can be slow (when?).
- So we usually add and delete from the end (reversing the lists):

```
class tree_iter:
    def __init__(self, the_tree):
        self._work_queue = [ the_tree ]

    def __next__(self):
        while len(self._work_queue) > 0:
            subtree = self._work_queue.pop()
            if subtree.is_empty:
                pass
            else:
                self._work_queue += subtree.right, subtree.left
                # Reversed!
                return subtree.label
        raise StopIteration
```

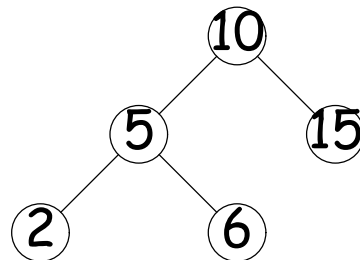
# Iterating Over a Binary Search Tree In Order

- The iterator we just defined iterates in *preorder*: first the root's label, then the labels of the left child in preorder, then the labels of the right child in preorder.
- But for a binary search tree, this gives the values out of order.
- Instead, we want the labels of the left child (in order), then the root's label, then those of the right.
- This is known as an *inorder traversal* of a binary tree. For search trees, it gives us the values in order.
- We could get this with a different iterator:

```
class BinTree(Tree):
    ...
    def inorder_values(self):
        """An iterator over my labels in order.
        >>> T = BinTree(10, BinTree(5, BinTree(2), BinTree(6)), BinTree(15))
        >>> for v in T.inorder_values():
        ...     print(v, end=" ")
        2 5 6 10 15"""
        return inorder_tree_iter(self)
```

# The Inorder Iterator

- To get this change, we have to put *both* trees and labels in the work queue.
- Let's simplify by assuming that we never use trees as labels (no trees of trees).
- So for the tree we looked at previously:



we'd start with Tree 10 (as before), and process that by replacing it with Tree 5, 10 (the label), and Tree 15 in the queue.

- When we get to a label in the queue, we return it.

# Using Inorder Iterators: A `__repr__` Method

- It would be nice to have a specialized way to print binary search trees, which we can do by redefining `BinTree.__repr__`:

```
class BinTree(Tree):
    ...
    def __repr__(self):
        """A string representing me (used by the interpreter).
        >>> T = BinTree(10, BinTree(5, BinTree(2), BinTree(6)), BinTree(15))
        >>> T
        {2, 5, 6, 10, 15}"""
        result = "{"
        for v in self.inorder_values():
            if result != "{":
                result += ", "
            result += repr(v)
        return result + "}"
        # Can you do it in one line?
        return
```

# Using Inorder Iterators: A `__repr__` Method

- It would be nice to have a specialized way to print binary search trees, which we can do by redefining `BinTree.__repr__`:

```
class BinTree(Tree):
    ...
    def __repr__(self):
        """A string representing me (used by the interpreter).
        >>> T = BinTree(10, BinTree(5, BinTree(2), BinTree(6)), BinTree(15))
        >>> T
        {2, 5, 6, 10, 15}"""
        result = "{"
        for v in self.inorder_values():
            if result != "{":
                result += ", "
            result += repr(v)
        return result + "}"
        # Can you do it in one line?
        return "{" + ', '.join(map(repr, self.inorder_values())) + "}"
```



# Intersection

- In lab, you looked at intersection between Python sets.
- Since we're using **BinTrees** as sets, it makes sense to consider the same problem here.
- One approach is brute force, for value in one set, see if it is in the other:

```
def intersection(s1, s2):  
    """The intersection of the values in BinTrees S1 and S2."""  
    result = BinTree.empty_tree  
    for v in s1.preorder_values():  
        if tree_find(s2, v):  
            result = dtree_add(result, v)  
    return result
```

- If our trees remain “bushy” (shallow), how long does this take, as a function of  $N$ , the maximum of the sizes of **s1** and **s2**?

# Intersection

- In lab, you looked at intersection between Python sets.
- Since we're using **BinTrees** as sets, it makes sense to consider the same problem here.
- One approach is brute force, for value in one set, see if it is in the other:

```
def intersection(s1, s2):  
    """The intersection of the values in BinTrees S1 and S2."""  
    result = BinTree.empty_tree  
    for v in s1.preorder_values():  
        if tree_find(s2, v):  
            result = dtree_add(result, v)  
    return result
```

- If our trees remain “bushy” (shallow), how long does this take, as a function of  $N$ , the maximum of the sizes of **s1** and **s2**? **A:**  $O(N \lg N)$
- That's because there are  $O(N)$  items in **s1**; checking for each of them in **s2** takes  $O(\lg N)$  (if bushy); we add a maximum of  $N$  values to the result; and adding each of them also takes  $O(\lg N)$ .

# Using Inorder Iterators for Intersection

- We can avoid doing repeated searches by iterating through both sets of values simultaneously.
- Can use Python's built-in `next` function: `next(an_iterator, default)` returns the result of calling `an_iterator.__next__()`, except that if that causes an exception, `next` returns `default` instead.

```
def intersection(s1, s2):
    it1, it2 = s1.inorder_values(), s2.inorder_values()
    v1, v2 = next(it1, None), next(it2, None)
    result = BinTree.empty_tree
    while v1 is not None and v2 is not None:
        if v1 == v2:
            result = dtree_add(result, v1)
            v1, v2 = next(it1, None), next(it2, None)
        elif ____:
            _____
        else:
            _____
    return result
```

# Using Inorder Iterators for Intersection

- We can avoid doing repeated searches by iterating through both sets of values simultaneously.
- Can use Python's built-in `next` function: `next(an_iterator, default)` returns the result of calling `an_iterator.__next__()`, except that if that causes an exception, `next` returns `default` instead.

```
def intersection(s1, s2):
    it1, it2 = s1.inorder_values(), s2.inorder_values()
    v1, v2 = next(it1, None), next(it2, None)
    result = BinTree.empty_tree
    while v1 is not None and v2 is not None:
        if v1 == v2:
            result = dtree_add(result, v1)
            v1, v2 = next(it1, None), next(it2, None)
        elif v1 < v2:
            _____
        else:
            _____
    return result
```

# Using Inorder Iterators for Intersection

- We can avoid doing repeated searches by iterating through both sets of values simultaneously.
- Can use Python's built-in `next` function: `next(an_iterator, default)` returns the result of calling `an_iterator.__next__()`, except that if that causes an exception, `next` returns `default` instead.

```
def intersection(s1, s2):
    it1, it2 = s1.inorder_values(), s2.inorder_values()
    v1, v2 = next(it1, None), next(it2, None)
    result = BinTree.empty_tree
    while v1 is not None and v2 is not None:
        if v1 == v2:
            result = dtree_add(result, v1)
            v1, v2 = next(it1, None), next(it2, None)
        elif v1 < v2:
            v1 = next(it1, None)
        else:
            v2 = next(it2, None)
    return result
```