

Lecture #7: Data Abstraction

- Reprise: An **Abstract Data Type** (or **ADT**) consists of
 - A set (**domain**) of possible values.
 - A set of **operations** on those values.
- ADTs are **conceptual**: a given programming language may or may not have constructs specifically designed for ADT definition, but programmers can choose to organize their programs as collections of ADTs in any case.
- We call them “abstract” because they abstract a particular **behavior**, which we document without being specific about what the values really consist of (their **internal representations**.)

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Data Structures

- The simplest ADTs are not particularly abstract: they are a collection of data values and their behavior consists entirely of selecting or modifying those individual data values.
- We sometimes use the term **data structure** for these, although the terminology is not particularly exactly firm.
- Example: A **tuple** is a sequence of values. It is entirely defined by those values.

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Tuples in Python (I)

- To create **construct** a tuple, use a sequence of expressions in parentheses:

```
()          # The tuple with no values
(1, 2)       # A pair: tuple with two items
(1, )       # A singleton tuple: use comma to distinguish from (1)
(1, "Hello", (3, 4)) # Any mix of values possible.
```
- When unambiguous, the parentheses are unnecessary:

```
x = 1, 2, 3      # Same as x = (1,2,3)
return True, 5    # Same as return (True, 5)
for i in 1, 2, 3: # Same as for i in (1,2,3):
```

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Tuples in Python (II)

- Basically, one can **select** values from a tuple and compare or print them, but little else.
- Select by item number:

```
x = (1, 7, 5)
print(x[1], x[2]) # Prints 7 and 5
from operator import getitem
print(getitem(x, 1), getitem(x, 2)) # Prints 7 and 5
print(x.__getitem__(1), x.__getitem__(2)) # Prints 7 and 5
```
- Or select by “unpacking” (syntactic sugar):

```
x = (1, (2, 3), 5)
a, b, c = x
print(b, c) # Prints (2, 3) and 5
d, (e, f), g = x
print(e, g) # Prints 2 and 5
```
- Tuples provide a useful way to return multiple things from a function.

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Rational Numbers

- The book uses “rational number” as an example of an ADT:

```
def make_rat(n, d):
    """The rational number n/d, assuming n, d are integers, d!=0"""

def add_rat(x, y):
    """The sum of rational numbers x and y."""

def mul_rat(x, y):
    """The product of rational numbers x and y."""

def numer(r):
    """The numerator of rational number r."""

def denom(r):
    """The denominator of rational number r."""
```
- These definitions pretend that **x**, **y**, and **r** really are rational numbers.
- But from this point of view, **numer** and **denom** are problematic. Why?

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Rational Numbers

- Problem is that “the numerator (denominator) of **r**” is not well-defined for a rational number.
- If **make_rat** really produced rational numbers, then **make_rat(2, 4)** and **make_rat(1, 2)** ought to be identical. So should **make_rat(1, -1)** and **make_rat(-1, 1)**.
- So a better specification would be

```
def numer(r):
    """The numerator of rational number r in lowest terms."""

def denom(r):
    """The denominator of rational number r in lowest terms.
    Always positive."""
```

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Representing Rationals (I)

- The obvious representation is as a pair of integers.
- Suppose we define

```
def make_rat(n, d):  
    """Rational number n/d, assuming n, d are integers, d!=0"""  
    return (n, d)
```

- From elementary-school math, we can then write

```
def add_rat(x, y):  
    """The sum of rational numbers x and y."""  
    (xn, xd), (yn, yd) = x, y  
    return (xn * yd + yn * xd, xd * yd) BAD STYLE?  
  
def mul_rat(x, y):  
    """The product of rational numbers x and y."""  
    (xn, xd), (yn, yd) = x, y  
    return (xn * yn, xd * yd) BAD STYLE?
```

- What about **numer** and **denom**?

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Use the Abstraction!

Better:

```
def add_rat(x, y):  
    """The sum of rational numbers x and y."""  
    return make_rat(numer(x) * denom(y) + numer(y) * denom(x),  
                    denom(x) * denom(y))  
  
def mul_rat(x, y):  
    """The product of rational numbers x and y."""  
    return make_rat(numer(x) * numer(y), denom(x) * denom(y))
```

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Implementing numer and denom (I)

```
from fractions import gcd  
# fractions.gcd(a,b), for b!=0, computes the largest integer in  
# absolute value that evenly divides both a and b and has  
# the sign of b. (Not quite the "official" gcd function).  
  
def numer(r):  
    """The numerator of rational number r in lowest terms."""  
    n, d = r  
    return n // gcd(n, d)  
  
def denom(r):  
    """The denominator of rational number r in lowest terms.  
    Always positive."""  
    n, d = r  
    return d // gcd(n, d)
```

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Representing Rationals (II)

- But the preceding implementation is problematic:
 - Each call to **denom** or **numer** has to recompute a value.
 - Intermediate values can get quite large.
- Suggests that we *always* keep rationals in lowest terms.
- How does the implementation change?

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Updated Implementation

```
from fractions import gcd  
  
def make_rat(n, d):  
    g = gcd(n, d)  
    return n//g, d//g  
  
def numer(r):  
    return r[0]  
  
def denom(r):  
    return r[1]  
  
# What about add_rat and mul_rat?
```

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Updated Implementation (contd.)

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Implementing Tuples (If You Had To)

- Using “data structure” to mean “unabstract ADT” is fuzzy.
- Even tuples need to be represented.
- Python has a built-in implementation, inaccessible to the user.
- They do this for speed, but we can get the same effect with what we already have: functions.

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Data Structures via Dispatching

```
def make_rat(n, d):
    g = gcd(n, d)
    n, d = n // g, d // g

    def result(key):
        if key == 0:
            return n
        else:
            return d
    return result

def numer(r):
    return r(0)

def denom(r):
    return r(1)
```

- The function `result` dispatches on the value of `key` to get its result.

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Discussion

- You'll sometimes see `key` described as a *message* and this technique called *message-passing*, (but your current instructor hates this terminology.)
- If we had persisted in defining `add_rat` and `mul_rat` using unpacking, as originally (see slide 7), we'd now have to rewrite them.
- But by using `numer` and `denom` in `add_rat` and `mul_rat` (slide 8), we have avoided having to touch them after this change in representation.
- The general lesson:

*Try to confine each design decision in your program
to as few places as possible.*

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