CS 61A Fall 2012

Structure and Interpretation of Computer Programs

ALTERNATE MIDTERM 1

INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the official 61A midterm 1 study guide attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

Last name	
First name	
SID	
Login	
TA & section time	
Name of the person to your left	
Name of the person to	
your right	
All the work on this exam	
is my own. (please sign)	

For staff use only

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Q. 1	Q. 2	Q. 3	Q. 4	Total	
/19	/19	/1.4	/0	/40	
/12	/12	/14	/8	/46	

1. (12 points) The Call Express is Hijacked

For each of the following call expressions, write the value to which it evaluates *and* what would be output by the interactive Python interpreter. The first two rows have been provided as examples.

- In the **Evaluates to** column, write the value to which the expression evaluates. If evaluation causes an error, write Error. If an expression evaluates to a function, write Function.
- In the column labeled **Interactive Output**, write all output that would be displayed during an interactive session, after entering each call expression. This output may have multiple lines. Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error.

Assume that you have started Python 3 and executed the following statements:

```
from operator import add, mul
def square(x):
    return mul(x, x)

def pirate(arggg):
    print('matey')
    def plunder(arggg):
        return arggg
    return plunder
```

Expression	Evaluates to	Interactive Output
square(5)	25	25
1/0	Error	Error
<pre>print(square(4))</pre>		
<pre>square(square(print(2)))</pre>		
<pre>print(square(3), print(5))</pre>		
pirate(square)(3)		
add(pirate(3)(square)(4), 1)		
<pre>pirate(pirate(pirate))(5)(7)</pre>		

2. (12 points) Protect the Environment

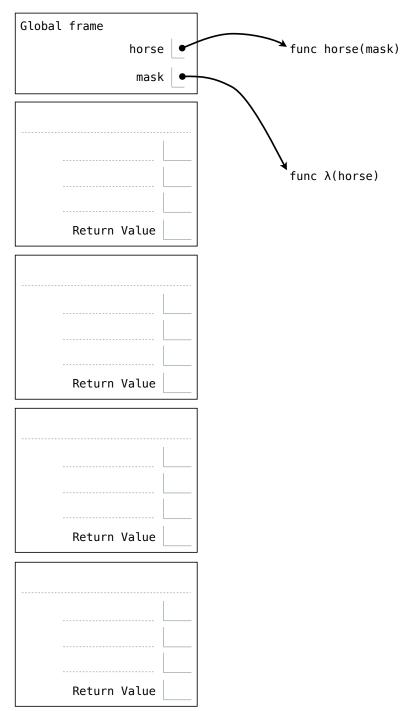
(a) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

A complete answer will:

- Add all missing names, labels, and parent annotations to all local frames.
- Add all missing values created during execution.
- Show the return value for each local frame.

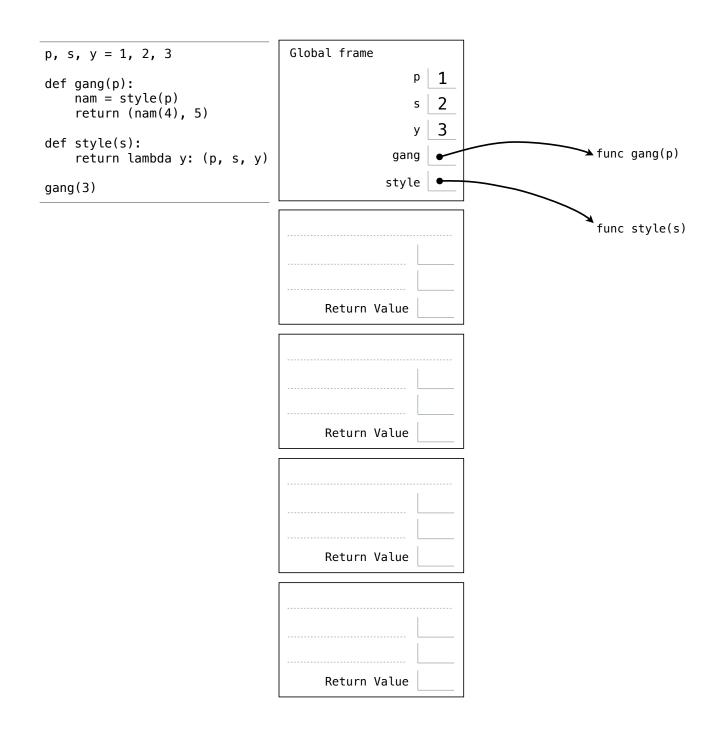
def horse(mask):
 horse = mask
 def mask(horse):
 return horse
 return horse(mask)

mask = lambda horse: horse(2)
horse(mask)



- (b) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

 A complete answer will:
 - Add all missing names, labels, and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.



Login:______

- 3. (14 points) Sequences
- (a) (2 pt) Fill in the blanks so that the final call expression below evaluates to a tuple value.

```
def tuple(x):
    if x == None:
        return lambda: (1, 2, 3)
    else:
        return lambda: 4
```

```
(lambda_____: lambda soda: hall_____)(tuple)("sequence")
```

(b) (2 pt) Draw a box and pointer diagram for the following rlist:

```
a = rlist(1, rlist((2, 3, 4), rlist(rlist(5, (6, empty_rlist)), empty_rlist)))
```

(c) (2 pt) What is the element at index 2 of this rlist, returned by getitem_rlist(a, 2)?

```
def getitem_rlist(s, i):
    """Return the element at index i of recursive list s."""
    while i > 0:
        s, i = rest(s), i - 1
    return first(s)
```

(d) (2 pt) What is the length of this rlist, returned by len_rlist(a)?

```
def len_rlist(s):
    """Return the length of recursive list s."""
    length = 0
    while s != empty_rlist:
        s, length = rest(s), length + 1
    return length
```

(e) (6 pt) When the int constructor is called on a float value, it "truncates toward zero," meaning that it returns the largest integer less than any positive argument, or the least integer greater than any negative argument. For example:

```
>>> int(2)
2
>>> int(2.7)
2
>>> int(-1.5)
-1
```

Assume that you have started Python 3 and executed the following statements:

```
def alt(f, g, z):
    while g(z) > 0 and z != 5:
        f, g = g, f
        z = g(z)
    return z

def grow(x):
    return int((x * 3) / 2)

def shrink(x):
    return x - 2

def flip(x):
    return int(10 / (x-2))
```

For each of the following call expressions, write the value to which it evaluates. If evaluation causes an error, write Error. If evaluation would run forever, write FOREVER.

```
• alt(shrink, grow, 6)
```

```
• alt(shrink, grow, 7)
```

```
• alt(flip, shrink, 3)
```

4. (12 points) In Verse

The inverse of some function F is a function of argument X that returns you the Y, such that when you apply F to Y you recover the X.

An invertible function is a function that takes and returns a single numeric value, is differentiable, and never returns the same value for two different arguments. Some examples:

```
def double(y):
    """Return twice the value of y."""
    return 2 * y

def cube(y):
    """Return y raised to the third power."""
    return pow(y, 3)

def pow2(y):
    """Return 2 raised to the power of y."""
    return pow(2, y)
```

(a) (4 pt) Implement a function invert that takes an invertible function argument and returns its inverse. You may call find_root, newton_update, approx_deriv, and/or iter_improve. You cannot use any assignment, conditional, while, or for statements.

```
def invert(f):
    """Return the inverse of invertible function f.

>>> halve = invert(double)
>>> halve(12)
6.0
>>> cube_root = invert(cube)
>>> cube_root(27)
3.0
>>> log2 = invert(pow2)
>>> log2(32)
5.0
"""
```

(b) (4 pt) A numpair is a pair of integers that have the same one's digit. Fill in the two missing expressions in the constructor below, which takes two non-negative integers less than 100, asserts that they have the same one's digit, and returns a numpair represented as a pair of tens digits and the shared one's digit.

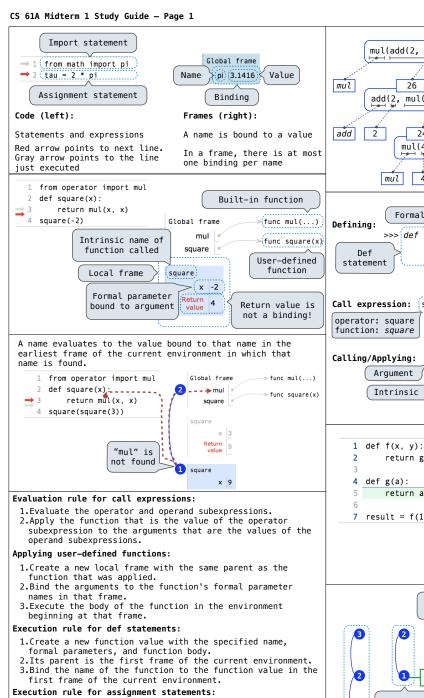
from operator import floordiv, mod # Use these functions or // and %

def numpair(first, second):
 """Return a numpair as a pair of ten's digits and a shared one's digit.

>>> numpair(24, 64)
 ((2, 6), 4)
 >>> numpair(67, 7)
 ((6, 0), 7)
 """

assert first >= 0 and first < 100 and second >= 0 and second < 100

assert _______, "different one's"</pre>



1.Evaluate the expression(s) on the right of the equal sign. 2.Simultaneously bind the names on the left to those values. in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order.

1.Evaluate the header's expression

2.If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- 1.Evaluate the subexpression <left>
- 2.If the result is a true value v, then the expression evaluates to v.
- 3.0therwise, the expression evaluates to the value of the subexpression <code><right>.</code>

Evaluation rule for and expressions:

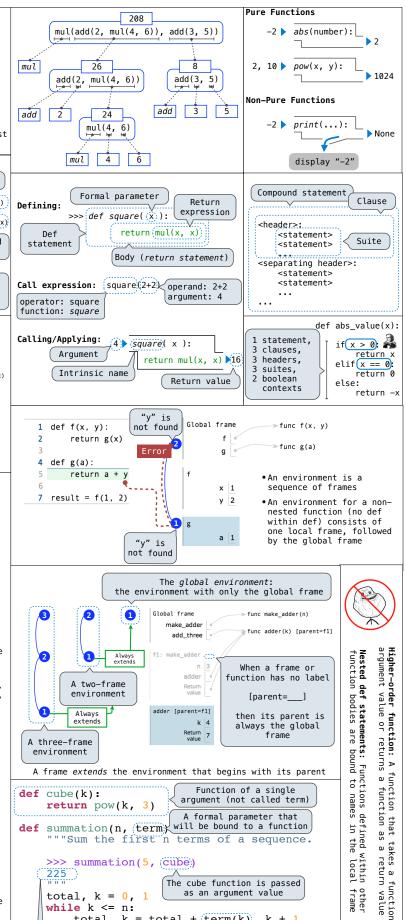
- 1.Evaluate the subexpression <left>.
- 2.If the result is a false value v, then the expression evaluates to v.
- 3.0 therwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

1.Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

- 1. Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.



>>> summation(5, cube)

total, k = 0, 1

while k <= n:</pre>

return total

 $0 + 1^3 + 2^3 + 3^3 + 4^3 + 5^5$

The cube function is passed

as an argument value

The function bound to term

gets called here

total, k = total + term(k), k + 1

other frame

as

an

```
square = lambda \times y: x * y
                                                                                                                                                 def square(x):
                                                           @trace1
                                                                                                                                      VS
                                                                                               square = lambda x: x * x
                                                           def triple(x):
                                                                                                                                                       return x * x
             A function
                                                                return 3 * x
                                                                                             • Both create a function with the same arguments & behavior
                  with formal parameters x and y
                                                              is identical to
                         and body "return (x * y)"
                                                                                             • Both of those functions are associated with the environment
                                                                                                in which they are defined
                                                           def triple(x):
         Must be a single expression
                                                                return 3 *

    Both bind that function to the name "square"

                                                            triple = trace1(triple)
                                                                                             • Only the def statement gives the function an intrinsic name
                            A function that returns a function
 def make_adder(n):
                                                                                             How to find the square root of 2?
                                                                                                                                               -f(x)/f'(x)
          Return a function that takes one argument k and returns k + n.
                                                                                             >>> f = lambda x: x*x - 2
                                                                                             >>> find_zero(f, 1)
                                                 The name add_three is bound to a function
      >>> add_three = make_adder(3)
>>> add_three(4)
                                                                                             1.4142135623730951
                                   A local
                               def statement
                                                                                             Begin with a function f and
                                                                                                                                                 (x, f(x))
     def adder(k):
      return k +(n)
return adder
                                                                                             an initial quess x
                                                                                                  Compute the value of f at the guess: f(x) Compute the derivative of f at the guess: f'(x)
                                Can refer to names in
                               the enclosing function
                                                                                                  Update guess to be: x - \frac{f(x)}{f'(x)}
                                                                                             3.
                                                                 ⇒func square(x)
      1 def square(x):
2 return x *
                                             3 square
                                                                  ≻func make_adder(n)
                                                                                            def iter_improve(update, done, guess=1, max_updates=1000):
    """Iteratively improve guess with update until done returns a true value.
                                                 ake_adder
                                                  compose1
      4 def make_adder(n):
                                                                 func compose1(f, g)
            def adder(k)
                                                                                                     iter_improve(golden_update, golden_test)
                return k + n
                                                                                                  1.618033988749895
            return adder
                                                                  func h(x) [parent=f2]
                                                    adder
      9 def compose1(f, g):
                                                                                                  while not done(guess) and k < max\_updates:
           def h(x):
                                                                                                     guess = update(guess)
k = k + 1
     11
                return f(g(x))
            return h
                                                                                                  return guess
                                              2
     14 compose1(square, (make_adder(2)))(3)
                                                                                             def newton_update(f):
                                                                                                 """Return an update function for f using Newton's method."""
def update(x):
    return x - f(x) / approx_derivative(f, x)

    Every user-defined function has a

                                              [par
                                                  ent=f2] 🚄
                                                                                                  return update
 • The parent of a function is the
                                             1
                                                       x 3 -
 frame in which it was defined
• Every local frame has a parent
                                                                                            def approx_derivative(f, x, delta=1e-5):
"""Return an approximation to the derivative of f at x."""
df = f(x + delta) - f(x)
                                                  [parent=f1]
                                                              A function's signature
                                                             has all the information
to create a local frame
 • The parent of a frame is the parent of the function called
                                                 o
                                                      k 3
                                                                                                  return df/delta
                                                                                             def find_root(f, guess=1):

    Compound objects combine objects together
    An abstract data type lets us manipulate compound objects as units

                                                                                                    "Return a guess of a zero of the function f, near guess.
                                                                                                 >>> from math import sin
>>> find_root(lambda y: sin(y), 3)
3.141592653589793
 Programs that use data isolate two aspects of programming:

    How data are represented (as parts)
    How data are manipulated (as units)
    Data abstraction: A methodology by which functions enforce an

                                                                                                  return iter_improve(newton_update(f), lambda x: f(x) == 0, guess)
   abstraction barrier between representation and use
                                                                                            def mul_rational(x, y):
    return(rational(numer(x) * numer(y), denom(x) * denom(y))
                            def sum_squares(x, y):
    return square(x)+square(y)
  def square(x):
       return mul(x, x)
 What does sum_squares need to know about square?
                                                                                                        Constructor
                                                                                                                                         Selectors
 · Square takes one argument. Yes
                                                                                            def add_rational(x, y):
    nx, dx = numer(x), denom(x)
    ny, dy = numer(y), denom(y)
 • Square has the intrinsic name square. No
  Square computes the square of a number. Yes
 • Square computes the square by calling mul. No
                                                                                                  return rational(nx * dy + ny * dx, dx * dy)
                                                                                            def eq_rational(x, y):
    return numer(x) * denom(y) == numer(y) * denom(x)
                  tuple
                               tuple
                                              tuple
                                                           tuple
                                                                               None
                   0
                                0
                                              0
                                                           0
                                                                                             def rational(n, d):
                                                                            represents
                                                                                                    "Construct
                                                                                                                  a rational number x that represents n/d."""
                                                                            the empty
                                               3
                    1
                                 2
                                                            4
                                                                 None
                                                                                                  return (n, d)
                                                                                list
                                                                                             from operator import getitem
 recursive
                                                                                            def numer(x):
    """Return the numerator of rational number x."""
 list is a
                  The first element of
                                                   The second element of
    pair
                 the pair is the first element of the list
                                                   the pair is the rest of the list
                                                                                                  return getitem(x, 0)
                                                                                            def denom(x):
    """Return the denominator of rational number x."""
empty_rlist = None
def rlist(first, rest):
    """Make a recursive list from its first element and the rest."""
    return (first, rest)
                                                                                                  return getitem(x, 1)
                                                                                             def pair(x, y):
                                                                                                    "Return a functional pair."""
    first(s):
"""Return
                                                                                                  def dispatch(m):
                the first element of a recursive list s."""
     return s[0]
                                                                                                       if m == 0:
                                                                                                                              This function
                                                                                                            return x
                                                                                                                            represents a pair
        "Return the rest of the elements of a recursive list s."""
                                                                                                       elif m == 1:
     return s[1]
                                                                                                            return y
        If a recursive list s is constructed from a first element f and
                                                                                                  return dispatch
        a recursive list r, then
                                                                                            def getitem_pair(p, i):
    """Return the element at index i of pair p."""
       • first(s) returns f, and

    rest(s) returns r, which is a recursive list.

                                                                                                  return p(i)
def len_rlist(s):
    """Return the length of recursive list s."""
                                                            Length. A sequence has
                                                                                             from operator import floordiv, mod
                                                            a finite length.
                                                                                             def divide_exact(n, d):
    length = 0
while s != empty_rlist:
                                                                                                      Return the quotient and remainder of dividing N by D.
     s, length = rest(s), length + 1 return length
                                                            Element selection. A
                                                            sequence has an
                                                                                                  >>>(q, r = divide_exact(2012, 10))<
                                                                                                                                                Multiple assignment
                                                            element corresponding
                                                                                                  >>> q
                                                                                                                                                     to two names
                                                            to any non-negative integer index less
def getitem_rlist(s, i):
                                                                                                  201
    while i > 0:
    s, i = rest(s), i - 1
                                                                                                            Multiple return values,
                                                            than its length,
                                                                                                               separated by commas
     s, i = rest
return first(s)
                                                            starting at 0 for the
                                                            first element.
                                                                                                  return floordiv(n, d), mod(n, d)
```