

## Lecture #2: Functions, Expressions

### Administrative

- Reader with discussion and other materials available at Vick Copy (Euclid and Hearst).
- Sign yourself up on Piazza. See course web page:  
`http://inst.cs.berkeley.edu/~cs61a`
- Be sure to get an account form next week in lab, and provide registration data.

**Announcement:** We're trying to hire a new lecturer. There will be two candidates coming Jan. 27-28 (Josh Hug) and Feb. 3-4 (John DeNero), and you can help evaluate them! For both days:

- Mon 01:00pm-02:00pm "Big ideas" talk (in Woz)
- Tue 11:45am-12:45pm Undergrad student lunch on northside (meet in 777 Soda)
- Tue 01:00pm-02:00pm Demo Class talk (in 380 Soda for Josh, Woz for John)
- UG Tue 02:00pm-02:45pm Open Session after demo class (same rooms)

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## Recap

- From last lecture: *Values* are data we want to manipulate and in particular,
- *Functions* are values that perform computations on values.
- *Expressions* denote computations that produce values.
- Today, we'll look at them in some detail at how functions operate on data values and how expressions denote these operations.
- As usual, although our concrete examples all involve Python, the actual concepts apply almost universally to programming languages.

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## Functions

- Something like *abs* denotes or evaluates to a function.
- To depict the denoted function values, we sometimes use this notation:

`abs(x):`      `add(a, b)`

- Idea: The opening on the left takes in values and one on the right to delivers results.
- The (green) *formal parameter names*—such as *x*, *a*, *b*—show the number of parameters (inputs) to the function.
- The list of formal parameter names gives us the function's *signature*—in Python, this is the number of arguments.
- For our purposes, the blue name is simply a helpful comment to suggest what the function does.
- (Python actually maintains this *intrinsic name* and the parameter names internally, but this is not a universal feature of programming languages, and, as you'll see, can be confusing.)

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## Functions: Lambda

- I'm often going to use a more venerable notation for function values:

`λ x: << | x | >>`      `λ a, b: << the sum of a and b >>`

- Formal parameters go to the left of the colon.
- The part to the right of the colon is an expression that indicates what value is produced.
- I'll use `<< ... >>` expressions to indicate non-Python descriptions of values or computations.
- In Python, you can *denote* simple function values like this:

`lambda a, b : << the sum of a and b >>`

which evaluates to

`λ a, b: << the sum of a and b >>`

- (Well, OK: the `<< ... >>` isn't really Python, but I'll use it as a placeholder for some computation I'm not prepared to write.)

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## Calling Functions (I)

- The fundamental operation on function values is to *call* or *invoke* them, which means giving them one value for each formal parameter and having them produce the result of their computation on these values:

`-5 > abs(number):`      `> 5`

`(29, 13) > add(left, right)`      `> 42`

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## Call Expressions

- A call expression denotes the operation of calling a function.
- Consider `add(2, 3)`:

`add`      `( 2 , 3 )`  
*Operator*      *Operand 0*      *Operand 1*

- The operator and the operands are all themselves expressions (recursion again).
- To evaluate this call expression:
  - Evaluate the operator (let's call the value *C*). It must evaluate to a function.
  - Evaluate the operands (or *actual parameters* in the order they appear (let's call these values *P*<sub>0</sub> and *P*<sub>1</sub>))
  - Call *C* with parameters *P*<sub>0</sub> and *P*<sub>1</sub>.

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## Calling a Function (I): Substitution

- Once we have the values for the operator and operands, we must still actually evaluate the call.
- A simple way to understand this (which will work for simple expressions) is to think of the process as *substitution*.
- Once you have a value:
 
$$\lambda a, b: \ll \text{sum of } a \text{ and } b \gg$$
- and values for the operands (let's say 2 and 3),
- substitute* the operand values for the formal parameters, replacing the whole call with
 
$$\ll \text{sum of 2 and 3} \gg$$
- which in turn evaluates to 5.

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## Side Trip: Values versus Denotations

- Expressions such as 2 in a programming language are called *literals*.
- To evaluate them, we replace them with whatever values they are supposed to stand for.
- This is confusing:
  - Q: What is the value of the literal 2?
  - A: 2.
- ... and then you get into long, technical explanations about how the second "2" is really in a different language than the first, and actually is just another notation for some mystical Platonic "2" that is floating off somewhere.
- I'll just try to be practical and distinguish values from literals by surrounding values in a boxes: the value of 2 is 2.
- One way to see the distinction between literals and values: the literals 0x10 and 16 are obviously different, but both denote the same value: 16.

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## Example: From Expression to Value

Let's evaluate the expression `mul(add(2, mul(0x4, 0x6)), add(0x3, 005))`. In the following sequence, values are shown in boxes. Everything outside a box is an expression.

- `mul(add(2, mul(0x4, 0x6)), add(0x3, 005))`
- $\lambda a, b: \ll a \times b \gg$  (`add(2, mul(0x4, 0x6)), add(0x3, 005)`)
- $\lambda a, b: \ll a \times b \gg$  ( $\lambda a, b: \ll a + b \gg$  (2,  $\lambda a, b: \ll a \times b \gg$  (4, 6)), `add(0x3, 005)`)
- $\lambda a, b: \ll a \times b \gg$  ( $\lambda a, b: \ll a + b \gg$  (2,  $\ll 4 \times 6 \gg$ , `add(0x3, 005)`))
- $\lambda a, b: \ll a \times b \gg$  ( $\lambda a, b: \ll a + b \gg$  (2, 24), `add(0x3, 005)`))
- $\lambda a, b: \ll a \times b \gg$  ( $\ll 2 + 24 \gg$ , `add(0x3, 005)`)
- $\lambda a, b: \ll a \times b \gg$  (26, `add(0x3, 005)`)
- $\lambda a, b: \ll a \times b \gg$  (26,  $\lambda a, b: \ll a + b \gg$  (3, 5))
- ...  $\lambda a, b: \ll a \times b \gg$  (26, 8)
- ... 208.

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## Puzzle I

Evaluate

`(lambda a: lambda b: a + b)(1)(3)`

- First, must understand how it's grouped:

$(\lambda a: \lambda b: a + b)(1)(3)$

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## Puzzle I (contd.)

- `(lambda a: lambda b: a + b)(1)(3)`
- $\lambda a: \lambda b: a + b$  (1)(3)
- $\lambda b: \lambda a: a + b$  (1 + b)(3)
- $\lambda b: \lambda a: a + b$  (1 + 3)
- 1 + 3
- 4

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## Impure Functions

- The functions so far have been *pure*: their output depends only on their input parameters' values, and they do nothing in response to a call but compute a value.
- Functions may do additional things when called besides returning a value.
- We call such things *side effects*.
- Example: the built-in `print` function:

```
-5 > print('• • •')
      > None
      display text '-5'
```

- Displaying text is `print`'s side effect. It's value, in fact, is generally useless (always the null value).
- For this lecture (at least), I'll use  $\lambda!$  ("lambda bang") to denote function values with side effects.

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## Example: Print

What about an expression with side effects?

1. `print(print(1), print(2))`
2. `λ! x: << print x >> ( λ! x: << print x >> (1), print(2) )`
3. `λ! x: << print x >> (None, print(2))`  
*and print '1'.*
4. `λ! x: << print x >> (None, λ! x: << print x >> (2))`
5. `λ! x: << print x >> (None, None)`  
*and print '2'.*
6. `None`  
*and print 'None None'.*