

# Volatility

Historical Returns?

No

Implied Vol.

Yes, Historical

Forward-based  
Model-based

*How are historical returns weighted?*

**Equal (Un-)  
Weighted Returns**

Constant Volatility: GBM  $\rightarrow$  BSM.  
Does not model heavy tails.

Linda Allen STDEV & Jorion's Moving Average (MA)

**More Weight Given to Recent Returns**

ARCH(m)

Time-varying Volatility

**GARCH(1,1)**

Long-run Average

Lagged Variance

Lagged Return<sup>2</sup>

Time-vary variance =  
unconditional heavy tails

Forecasts Vol

**EWMA**

RiskMetrics<sup>TM</sup>

Does not forecast\*

- A-GARCH
- Non-normal GARCH

**Economic State (kernel function)**

Multivariate density  
estimation (MDE)

Was day like (not like) today?  
Give more (less) weight!