Financial Econometrics

Lecture 1: Introduction to MATLAB

Adapted from
Introduction to Programming in MATLAB lecture notes,
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Getting Started

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MATLAB Basics

- MATLAB can be thought of as a super-powerful graphing calculator
  - Remember the TI-83 from calculus?
  - With many more buttons (built-in functions)
- In addition it is a programming language
  - MATLAB is an interpreted language, like Java
  - Commands executed line by line

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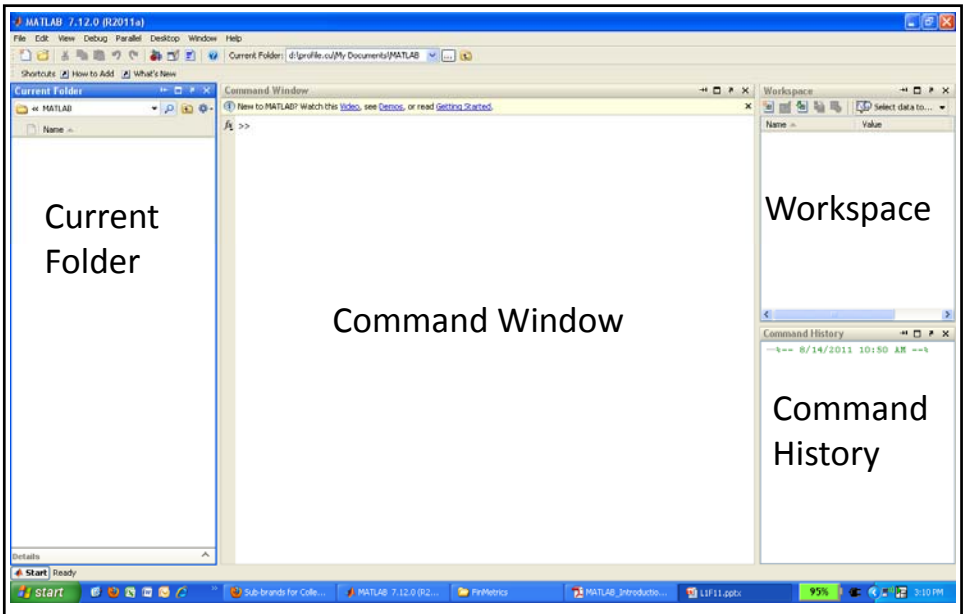

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Help/Docs

- `help`
  - **The most** important function for learning MATLAB on your own
- To get info on how to use a function:

```
» help sin
```

  - Help lists related functions at the bottom and links to the doc
- To get a nicer version of help with examples and easy-to-read descriptions:

```
» doc sin
```

- To search for a function by specifying keywords:

```
» doc
```

+ Search tab

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Scripts

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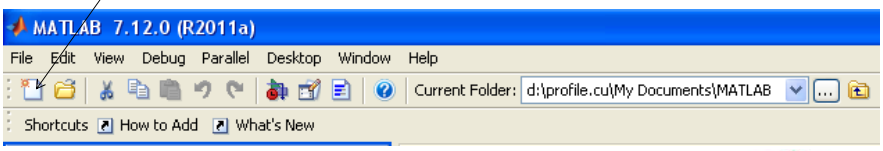
Scripts: Overview

- Scripts are
  - collection of commands executed in sequence
  - written in the MATLAB editor
  - saved as MATLAB files (.m extension)
- To create an MATLAB file from command-line

```
» edit helloWorld.m
```

- or click



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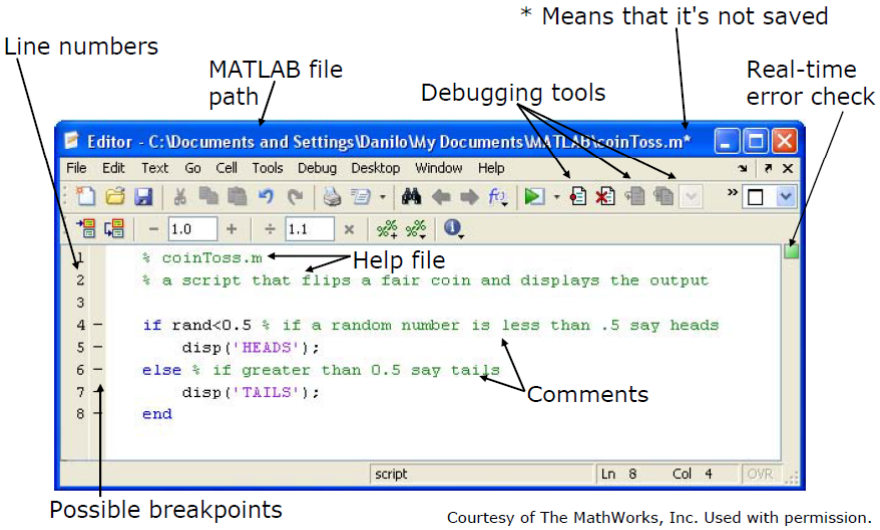
Scripts: the Editor



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Scripts: Some Notes

- **COMMENT!**
  - Anything following a % is seen as a comment
  - The first contiguous comment becomes the script's help file
  - Comment thoroughly to avoid wasting time later
- Note that scripts are somewhat static, since there is no input and no explicit output
- All variables created and modified in a script exist in the workspace even after it has stopped running

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Exercise: Scripts

Make a `helloWorld` script

- When run, the script should display the following text:

  Hello World!
  I am going to learn MATLAB!

- **Hint:** use `disp` to display strings. Strings are written between single quotes, like `'This is a string'`
- Open the editor and save a script as helloWorld.m. This is an easy script, containing two lines of code:

```
» % helloWorld.m
» % my first hello world program in MATLAB

» disp('Hello World!');
» disp('I am going to learn MATLAB!');
```

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Defining & Manipulating Variables

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Naming variables

- To create a variable, simply assign a value to a name:
  - » `var1=3.14`
  - » `myString='hello world'`
- Variable names
  - first character must be a LETTER
  - after that, any combination of letters, numbers and _
  - CASE SENSITIVE! (`var1` is different from `Var1`)
- Built-in variables. Don't use these names!
  - `i` and `j` can be used to indicate complex numbers
  - `pi` has the value 3.1415926…
  - `ans` stores the last unassigned value (like on a calculator)
  - `Inf` and `-Inf` are positive and negative infinity
  - `NaN` represents 'Not a Number'

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Scalars

- A variable can be given a value explicitly
  ```
  » a = 10
  ```
  - shows up in workspace!
- Or as a function of explicit values and existing variables
  ```
  » c = 1.3*45-2*a
  ```
- To suppress output, end the line with a semicolon
  ```
  » cooldude = 13/3;
  ```

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Arrays

- Like other programming languages, arrays are an important part of MATLAB
- Two types of arrays

  (1) matrix of numbers (either double or complex)

  (2) cell array of objects (more advanced data structure)

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Row Vectors

- Row vector: comma or space separated values between brackets

```
» row = [1 2 5.4 -6.6]
» row = [1, 2, 5.4, -6.6];
```

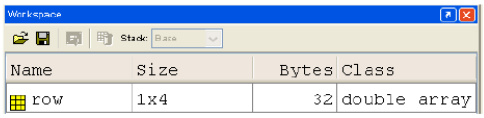
- Command window:

```
>> row=[1 2 5.4 -6.6]

row =

    1.0000    2.0000    5.4000   -6.6000
```

- Workspace:



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Column Vectors

- Column vector: semicolon separated values between brackets

```
» column = [4;2;7;4]
```

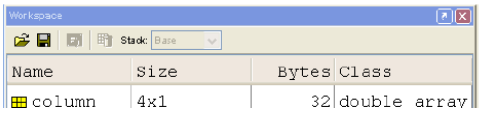
- Command window:

```
>> column=[4;2;7;4]

column =

     4
     2
     7
     4
```

- Workspace:



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size & length

- You can tell the difference between a row and a column vector by:
  - Looking in the workspace
  - Displaying the variable in the command window
  - Using the size function

```
>> size(row)
ans =
     1     4

>> size(column)
ans =
     4     1
```

- To get a vector's length, use the length function

```
>> length(row)
ans =
     4

>> length(column)
ans =
     4
```

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Matrices

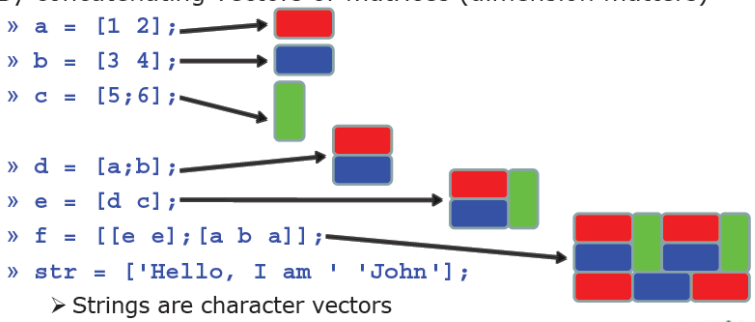
- Make matrices like vectors
- Element by element

```
» a= [1 2;3 4];
```

$$a = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

- By concatenating vectors or matrices (dimension matters)

```
» a = [1 2];
» b = [3 4];
» c = [5;6];
» d = [a;b];
» e = [d c];
» f = [[e e];[a b a]];
» str = ['Hello, I am ' 'John'];
```



  - Strings are character vectors

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save/clear/load

- Use **save** to save variables to a file
  - » `save myFile a b`
    - saves variables a and b to the file myfile.mat
    - myfile.mat file is saved in the current directory
    - Default working directory is
  - » `\MATLAB`
    - Make sure you're in the desired folder when saving files. Right now, we should be in:
  - » `MATLAB\IAPMATLAB\day1`

- Use **clear** to remove variables from environment
  - » `clear a b`
    - look at workspace, the variables a and b are gone

- Use **load** to load variable bindings into the environment
  - » `load myFile`
    - look at workspace, the variables a and b are back

- Can do the same for entire environment
  - » `save myenv; clear all; load myenv;`

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Basic Scalar Operations

- Arithmetic operations (+,-,*,/)
  - » `7/45`
  - » `(1+i)*(2+i)`
  - » `1 / 0`
  - » `0 / 0`

- Exponentiation (^)
  - » `4^2`
  - » `(3+4*j)^2`

- Complicated expressions, use parentheses
  - » `((2+3)*3)^0.1`

- Multiplication is NOT implicit given parentheses
  - » `3(1+0.7) gives an error`

- To clear command window
  - » `clc`

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Built-in Functions

- MATLAB has an **enormous** library of built-in functions
- Call using parentheses – passing parameter to function

```
» sqrt(2)
» log(2), log10(0.23)
» cos(1.2), atan(-.8)
» exp(2+4*i)
» round(1.4), floor(3.3), ceil(4.23)
» angle(i); abs(1+i);
```

Transpose

- The transpose operators turns a column vector into a row vector and vice versa

```
» a = [1 2 3 4+i]
» transpose(a)
» a'
» a.'
```

- The `'` gives the Hermitian-transpose, i.e. transposes and conjugates all complex numbers
- For vectors of real numbers `.'` and `'` give same result

Addition and Subtraction

- Addition and subtraction are element-wise; sizes must match (unless one is a scalar):

$$\begin{array}{r} [12 \quad 3 \quad 32 \quad -11] \\ +[2 \quad 11 \quad -30 \quad 32] \\ \hline =[14 \quad 14 \quad 2 \quad 21] \end{array} \qquad \begin{bmatrix} 12 \\ 1 \\ -10 \\ 0 \end{bmatrix} - \begin{bmatrix} 3 \\ -1 \\ 13 \\ 33 \end{bmatrix} = \begin{bmatrix} 9 \\ 2 \\ -23 \\ -33 \end{bmatrix}$$

- The following would give an error

```
» c = row + column
```

- Use the transpose to make sizes compatible

```
» c = row' + column
» c = row + column'
```

- Can sum up or multiply elements of vector

```
» s=sum(row);
» p=prod(row);
```

Element-Wise Functions

- All the functions that work on scalars also work on vectors

```
» t = [1 2 3];
» f = exp(t);
```

  - is the same as

```
» f = [exp(1) exp(2) exp(3)];
```

- If in doubt, check a function's help file to see if it handles vectors elementwise

- Operators (* / ^) have two modes of operation
  - element-wise
  - standard

Operators: element-wise

- To do element-wise operations, use the dot: `.` (`.*`, `./`, `.^`). BOTH dimensions must match (unless one is scalar)!
  - `» a=[1 2 3];b=[4;2;1];`
  - `» a.*b, a./b, a.^b → all errors`
  - `» a.*b', a./b', a.^(b') → all valid`

$$\begin{bmatrix}1 & 2 & 3\end{bmatrix} .* \begin{bmatrix}4\\2\\1\end{bmatrix} = ERROR$$

$$\begin{bmatrix}1\\2\\3\end{bmatrix} .* \begin{bmatrix}4\\2\\1\end{bmatrix} = \begin{bmatrix}4\\4\\3\end{bmatrix}$$

$$3\times 1 .* 3\times 1 = 3\times 1$$

$$\begin{bmatrix}1 & 1 & 1\\2 & 2 & 2\\3 & 3 & 3\end{bmatrix} .* \begin{bmatrix}1 & 2 & 3\\1 & 2 & 3\\1 & 2 & 3\end{bmatrix} = \begin{bmatrix}1 & 2 & 3\\2 & 4 & 6\\3 & 6 & 9\end{bmatrix}$$

$$3\times 3 .* 3\times 3 = 3\times 3$$

$$\begin{bmatrix}1 & 2\\3 & 4\end{bmatrix} .\hat{} 2 = \begin{bmatrix}1^2 & 2^2\\3^2 & 4^2\end{bmatrix}$$

Can be any dimension

Operators: standard

- Multiplication can be done in a standard way or element-wise
- Standard multiplication (*) is either a dot-product or an outer-product
  - Remember from linear algebra: inner dimensions must MATCH!!
- Standard exponentiation (^) can only be done on square matrices or scalars
- Left and right division (/ \) is same as multiplying by inverse
  - Our recommendation: just multiply by inverse (more on this later)

$$\begin{bmatrix}1 & 2 & 3\end{bmatrix} * \begin{bmatrix}4\\2\\1\end{bmatrix} = 11$$

$$1\times 3 * 3\times 1 = 1\times 1$$

$$\begin{bmatrix}1 & 2\\3 & 4\end{bmatrix} \hat{} 2 = \begin{bmatrix}1 & 2\\3 & 4\end{bmatrix} * \begin{bmatrix}1 & 2\\3 & 4\end{bmatrix}$$

Must be square to do powers

$$\begin{bmatrix}1 & 1 & 1\\2 & 2 & 2\\3 & 3 & 3\end{bmatrix} * \begin{bmatrix}1 & 2 & 3\\1 & 2 & 3\\1 & 2 & 3\end{bmatrix} = \begin{bmatrix}3 & 6 & 9\\6 & 12 & 18\\9 & 18 & 27\end{bmatrix}$$

$$3\times 3 * 3\times 3 = 3\times 3$$

Automatic Initialization

- Initialize a vector of **ones**, **zeros**, or **rand**om numbers
  - » `o=ones(1,10)`
    - row vector with 10 elements, all 1
  - » `z=zeros(23,1)`
    - column vector with 23 elements, all 0
  - » `r=rand(1,45)`
    - row vector with 45 elements (uniform [0,1])
  - » `n=nan(1,69)`
    - row vector of NaNs (useful for representing uninitialized variables)

The general function call is:

```
var=zeros(M,N);
```

Number of rows Number of columns

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Vector Indexing

- MATLAB indexing starts with **1**, not **0**
  - We will not respond to any emails where this is the problem.
- a(n) returns the n^{th} element

$a = [13 \quad 5 \quad 9 \quad 10]$

a(1) a(2) a(3) a(4)

- The index argument can be a vector. In this case, each element is looked up individually, and returned as a vector of the same size as the index vector.

```
» x=[12 13 5 8];
» a=x(2:3);  ------> a=[13 5];
» b=x(1:end-1);  ------> b=[12 13 5];
```

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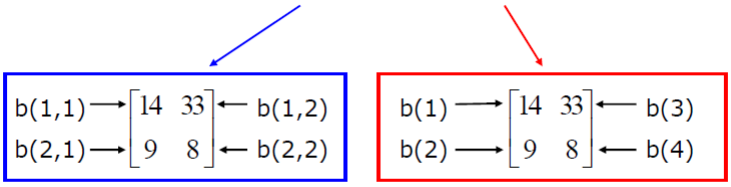
Matrix Indexing

- Matrices can be indexed in two ways
  - using **subscripts** (row and column)
  - using linear **indices** (as if matrix is a vector)
- Matrix indexing: subscripts or linear indices



- Picking submatrices

```
» A = rand(5) % shorthand for 5x5 matrix
» A(1:3,1:2) % specify contiguous submatrix
» A([1 5 3], [1 4]) % specify rows and columns
```

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Advanced Indexing 1

- To select rows or columns of a matrix, use the **:**

$$c = \begin{bmatrix} 12 & 5 \\ -2 & 13 \end{bmatrix}$$

```
» d=c(1,:);  ⟶  d=[12 5];
» e=c(:,2);  ⟶  e=[5;13];
» c(2,:)=[3 6];  %replaces second row of c
```

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Advanced Indexing 2

- MATLAB contains functions to help you find desired values within a vector or matrix

```
» vec = [5 3 1 9 7]
```

- To get the minimum value and its index:

```
» [minVal,minInd] = min(vec);
```

  - `max` works the same way

- To find any the indices of specific values or ranges

```
» ind = find(vec == 9);
» ind = find(vec > 2 & vec < 6);
```

  - **find** expressions can be very complex, more on this later

- To convert between subscripts and indices, use **ind2sub**, and **sub2ind**. Look up **help** to see how to use them.

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Making Figures

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Plotting

- Example

```
» x=linspace(0,4*pi,10);
» y=sin(x);
```

- Plot values against their index

```
» plot(y);
```

- Usually we want to plot y versus x

```
» plot(x,y);
```

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What does plot do?

- **plot** generates dots at each (x,y) pair and then connects the dots with a line
- To make plot of a function look smoother, evaluate at more points

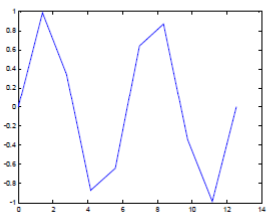
```
» x=linspace(0,4*pi,1000);
» plot(x,sin(x));
```

- x and y vectors must be same size or else you'll get an error

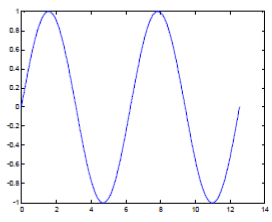
```
» plot([1 2], [1 2 3])
```

  - error!!

10 x values:



1000 x values:



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Plot Options

- Can change the line color, marker style, and line style by adding a string argument

```
» plot(x,y,'k.-');
```

color marker line-style

- Can plot without connecting the dots by omitting line style argument

```
» plot(x,y,'.')
```

- Look at **help plot** for a full list of colors, markers, and linestyles

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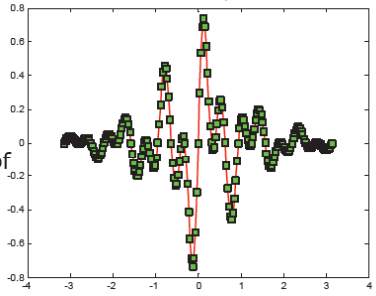
Line and Marker Options

- Everything on a line can be customized

```
» plot(x,y,'--s','LineWidth',2,...
       'Color', [1 0 0], ...
       'MarkerEdgeColor','k',...
       'MarkerFaceColor','g',...
       'MarkerSize',10)
```

You can set colors by using a vector of [R G B] values or a predefined color character like 'g', 'k', etc.



- See **doc line_props** for a full list of properties that can be specified

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Multiple Plots in one Figure

- To have multiple axes in one figure
  - » `subplot(2,3,1)`
    - ➢ makes a figure with 2 rows and three columns of axes, and activates the first axis for plotting
    - ➢ each axis can have labels, a legend, and a title
  - » `subplot(2,3,4:6)`
    - ➢ activating a range of axes fuses them into one
- To close existing figures
  - » `close([1 3])`
    - ➢ closes figures 1 and 3
  - » `close all`
    - ➢ closes all figures (useful in scripts/functions)

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Saving Figures

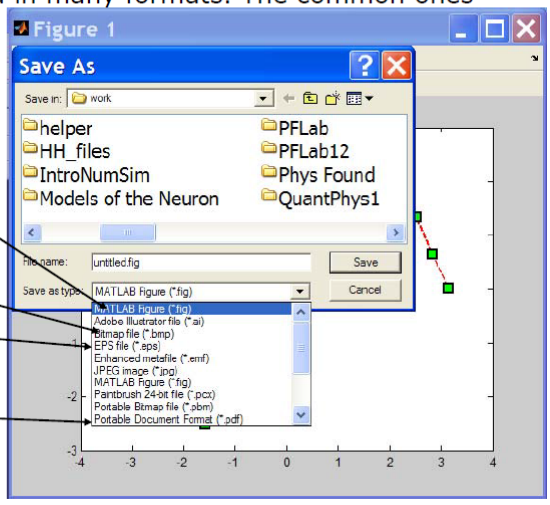
- Figures can be saved in many formats. The common ones are:

.fig preserves all information

.bmp uncompressed image

.eps high-quality scaleable format

.pdf compressed image



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Defining New Functions

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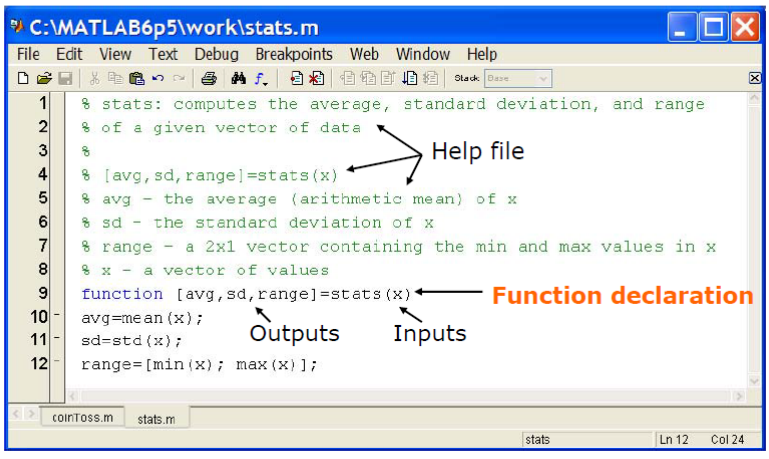
User-defined Functions

- Functions look exactly like scripts, but for **ONE** difference
  - Functions must have a function declaration



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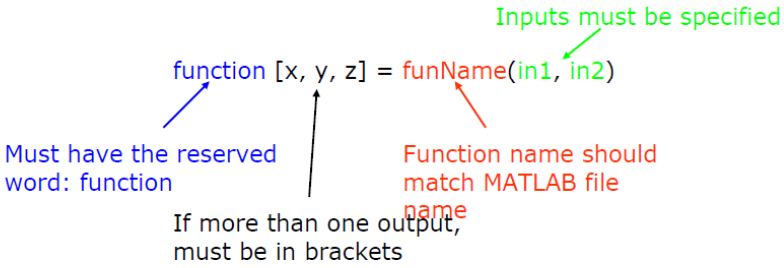
User-defined Functions

- Some comments about the function declaration



- No need for return: MATLAB 'returns' the variables whose names match those in the function declaration
- Variable scope: Any variables created within the function but not returned disappear after the function stops running

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Functions: overloading

- We're familiar with
  - `» zeros`
  - `» size`
  - `» length`
  - `» sum`
- Look at the help file for size by typing
  - `» help size`
- The help file describes several ways to invoke the function
  - D = SIZE(X)
  - [M,N] = SIZE(X)
  - [M1,M2,M3,...,MN] = SIZE(X)
  - M = SIZE(X,DIM)

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Functions: overloading

- MATLAB functions are generally overloaded
  - Can take a variable number of inputs
  - Can return a variable number of outputs
- What would the following commands return:

```
» a=zeros(2,4,8); %n-dimensional matrices are OK
» D=size(a)
» [m,n]=size(a)
» [x,y,z]=size(a)
» m2=size(a,2)
```

- You can overload your own functions by having variable input and output arguments (see `varargin`, `nargin`, `varargout`, `nargout`)

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Functions: Excercise

- Write a function with the following declaration:
  `function plotSin(f1)`
- In the function, plot a sin wave with frequency f1, on the range [0,2π]: $\sin(f_1 x)$
- To get good sampling, use 16 points per period.
- In an MATLAB file saved as plotSin.m, write the following:

```
» function plotSin(f1)

  x=linspace(0,2*pi,f1*16+1);
  figure
  plot(x,sin(f1*x))
```

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Program Flow Control

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Relational Operators

- MATLAB uses *mostly* standard relational operators
  - equal ==
  - **not** equal ~=
  - greater than >
  - less than <
  - greater or equal >=
  - less or equal <=
- Logical operators

	elementwise	short-circuit (scalars)
And	&	&&
Or	|	||
Not	~	
Xor	xor	
All true	all	
Any true	any	

- Boolean values: zero is false, nonzero is true
- See **help .** for a detailed list of operators

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if/else/elseif

- Basic flow-control, common to all languages
- MATLAB syntax is somewhat unique

IF

```
if cond
    commands
end
```

Conditional statement: evaluates to true or false

ELSE

```
if cond
    commands1
else
    commands2
end
```

ELSEIF

```
if cond1
    commands1
elseif cond2
    commands2
else
    commands3
end
```

- No need for parentheses: command blocks are between reserved words

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for

- **for** loops: use for a known number of iterations
- MATLAB syntax:

Loop variable

```
for n=1:100
    commands
end
```

Command block

- The loop variable
  - Is defined as a vector
  - Is a scalar within the command block
  - Does not have to have consecutive values (but it's usually cleaner if they're consecutive)
- The command block
  - Anything between the **for** line and the **end**

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while

- The while is like a more general for loop:
  - Don't need to know number of iterations

WHILE

```
while cond
   commands
end
```

- The command block will execute while the conditional expression is true
- Beware of infinite loops!

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Exercise: Conditionals

- Modify your `plotSin(f1)` function to take two inputs: `plotSin(f1,f2)`
- If the number of input arguments is 1, execute the plot command you wrote before. Otherwise, display the line `'Two inputs were given'`
- Hint: the number of input arguments are in the built-in variable `nargin`

```
» function plotSin(f1,f2)

  x=linspace(0,2*pi,f1*16+1);
  figure

  if nargin == 1
      plot(x,sin(f1*x));
  elseif nargin == 2
      disp('Two inputs were given');
  end
```

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Random Numbers & Basic Statistics

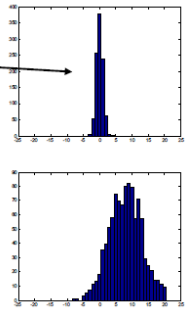
Random Numbers

- Many probabilistic processes rely on random numbers
- MATLAB contains the common distributions built in
  - » `rand`
    - draws from the uniform distribution from 0 to 1
  - » `randn`
    - draws from the standard normal distribution (Gaussian)
  - » `random`
    - can give random numbers from many more distributions
    - see **doc random** for help
    - the docs also list other specific functions
- You can also seed the random number generators

```
» rand('state',0); rand(1); rand(1);
  rand('state',0); rand(1);
```

Changing Mean and Variance

- We can alter the given distributions
  - » `y=rand(1,100)*10+5;`
    - gives 100 uniformly distributed numbers between 5 and 15
  - » `y=floor(rand(1,100)*10+6);`
    - gives 100 uniformly distributed integers between 10 and 15. floor or ceil is better to use here than round
  - » `y=randn(1,1000)`
  - » `y2=y*5+8`
    - increases std to 5 and makes the mean 8



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Statistics

- Whenever analyzing data, you have to compute statistics
  - » `scores = 100*rand(1,100);`
- Built-in functions
  - mean, median, mode
- To group data into a histogram
  - » `hist(scores,5:10:95);`
    - makes a histogram with bins centered at 5, 15, 25…95
  - » `N=histc(scores,0:10:100);`
    - returns the number of occurrences between the specified bin *edges* 0 to <10, 10 to <20…90 to <100. you can plot these manually:
  - » `bar(0:10:100,N,'r')`

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Exercise: Probability

- We will simulate Brownian motion in 1 dimension. Call the script 'brown'
- Make a 10,000 element vector of zeros
- Write a loop to keep track of the particle's position at each time
- Start at 0. To get the new position, pick a random number, and if it's <0.5, go left; if it's >0.5, go right. Store each new position in the k^{th} position in the vector
- Plot a 50 bin histogram of the positions.

```
» x=zeros(10000,1);
» for n=2:10000
»     if rand<0.5
»         x(n)=x(n-1)-1;
»     else
»         x(n)=x(n-1)+1;
»     end
» end
» figure;
» hist(x,50);
```

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I/O Operations

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Importing Data

- With `importdata`, you can also specify delimiters. For example, for comma separated values, use:
  - `» a=importdata('filename', ', ');`
    - The second argument tells matlab that the tokens of interest are separated by commas or spaces
- `importdata` is very robust, but sometimes it can have trouble. To read files with more control, use `fscanf` (similar to C/Java), `textread`, `textscan`. See **help** or **doc** for information on how to use these functions

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Reading Excel Files

- Reading excel files is equally easy
- To read from an Excel file, use `xlsread`
  - `» [num,txt,raw]=xlsread('randomNumbers.xls');`
    - Reads the first sheet
    - `num` contains numbers, `txt` contains strings, `raw` is the entire cell array containing everything
  - `» [num,txt,raw]=xlsread('randomNumbers.xls',...`
    `'mixedData');`
    - Reads the **mixedData** sheet
  - `» [num,txt,raw]=xlsread('randomNumbers.xls',-1);`
    - Opens the file in an Excel window and lets you click on the data you want!
- See `doc xlsread` for even more fancy options

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Writing Excel Files

- MATLAB contains specific functions for reading and writing Microsoft Excel files
- To write a matrix to an Excel file, use `xlswrite`

```
» [s,m]=xlswrite('randomNumbers',rand(10,4),...
  'Sheet1'); % we specify the sheet name
```

- You can also write a cell array if you have mixed data:

```
» C={'hello','goodbye';10,-2;-3,4};
» [s,m]=xlswrite('randomNumbers',C,'mixedData');
```

- `s` and `m` contain the 'success' and 'message' output of the write command
- See `doc xlswrite` for more usage options

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