





WARSAW UNIVERSITY OF TECHNOLOGY

# Sparse Autoencoders Do Not Find Canonical Units of Analysis

ICLR 2025 Poster

# About the Paper

- On ArXiv: 07.02.2025

- ICLR 2025 Poster: 22.01.2025



Streamlit



OpenReview

- Reviewers scores: two 8 and two 6
- Very long conversations with both 6 reviewers
- <sub>-</sub> 8 Authors

YEAR

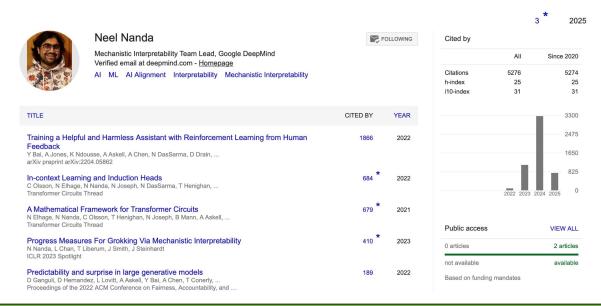
2025

2025

## About the Authors - Neel Nanda

Runs the Google DeepMind mechanistic interpretability team

<sub>-</sub> 80% of SAE papers are his (just kidding)



#### The three of them just do SAE



arXiv preprint arXiv:2502.04878

index with machine learning

Ecological Informatics 82, 102730

TITLE

Bart Bussmann Independent Verified email at student.uva.nl Artificial Intelligence

Sparse Autoencoders Do Not Find Canonical Units of Analysis

P Leask, B Bussmann, M Pearce, J Bloom, C Tigges, NA Moubayed, ...

S Mortier, A Hamedpour, B Bussmann, RPT Wandji, S Latré, ...

Showing sae latents are not atomic using meta-saes



YEAR

2025

2024

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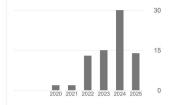
2023

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Public access



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0 articles	4 articles
not available	available
Based on funding mandates	
Co-authors	

Mechanistic Interpretability Team.

Jannes Nys ETH Zürich

VIEW ALL



#### Patrick Leask

**Durham University** Verified email at durham.ac.uk Artificial Intelligence

B Bussmann, M Pearce, P Leask, J Bloom, L Sharkey, N N https://www.alignmentforum.org/posts/TMAmHh4DdMr4n0	landa	n-sae-latents
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Inferring the relationship between soil temperature and the normalized difference vegetation

P Leask, B Bussmann, JI Bloom, C Tigges, N Al Moubayed, N Nanda NeurIPS 2024 Workshop on Scientific Methods for Understanding Deep Learning

TITLE

Sparse Autoencoders Do Not Find Canonical Units of Analysis

NeurIPS 2024 Workshop on Scientific Methods for Understanding Deep Learning

P Leask, B Bussmann, M Pearce, J Bloom, C Tigges, NA Moubayed, ... ICLR 2025

Stitching sparse autoencoders of different sizes

BatchTopK Sparse Autoencoders B Bussmann, P Leask, N Nanda

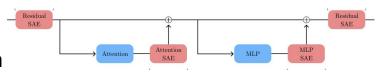
# TL;DR - SAEs May Not Provide Canonical Features in LLMs

Mechanistic interpretability aims to decompose neural network activations into interpretable features. Authors **challenge** the belief that SAEs **find canonical units** in LLMs:

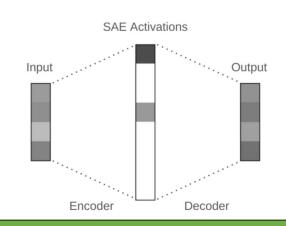
- SAE Stitching: Reveals incompleteness by showing larger SAEs contain novel latents that improve smaller SAEs' performance.
- Meta-SAEs: Demonstrates non-atomicity by decomposing SAE latents into combinations of smaller SAE latents (Use SAE on SAE).

# Recap on Sparse Autoencoders (SAEs)

 SAE is a technique for transforming a dense representation (with superposition) into a sparse monosemantic representation



- SAE decompose the activations of a model into more interpretable pieces.
- Can be applied to any activation representation
- It is simply an autonencoder with some proxy enforcing sparsity:
  - TopK
  - L1 regularization
  - JumpReLU



As a preprocessing step we apply a scalar normalization to the model activations so their average squared L2 norm is the residual stream dimension, D. We denote the normalized activations as  $\mathbf{x} \in \mathbb{R}^D$ , and attempt to decompose this vector using F features as follows:

$$\hat{\mathbf{x}} = \mathbf{b}^{dec} + \sum_{i=1}^F f_i(\mathbf{x}) \mathbf{W}^{dec}_{\cdot,i}$$

where  $W^{dec} \in \mathbb{R}^{D \times F}$  are the learned SAE decoder weights,  $\mathbf{b}^{dec} \in \mathbb{R}^D$  are learned biases, and  $f_i$  denotes the activity of feature *i*. Feature activations are given by the output of the encoder:

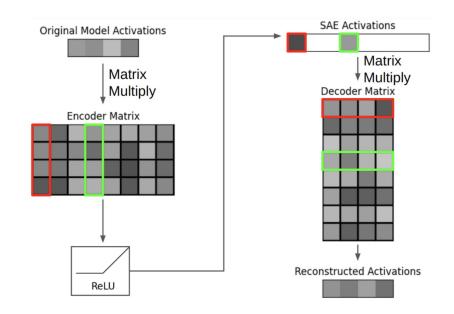
$$f_i(x) = ext{ReLU}\left(\mathbf{W}_{i,\cdot}^{enc} \cdot \mathbf{x} + b_i^{enc}
ight)$$

where  $W^{enc} \in \mathbb{R}^{F \times D}$  are the learned SAE encoder weights, and  $\mathbf{b}^{enc} \in \mathbb{R}^F$  are learned biases.

The loss function  $\mathcal L$  is the combination of an L2 penalty on the reconstruction loss and an L1 penalty on feature activations.

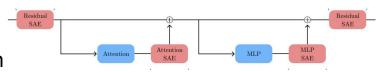
$$\mathcal{L} = \mathbb{E}_{\mathbf{x}} \left[ \|\mathbf{x} - \hat{\mathbf{x}}\|_2^2 + \lambda \sum_i f_i(\mathbf{x}) \cdot \|\mathbf{W}_{\cdot,i}^{dec}\|_2 
ight]$$

Including the factor of  $\|\mathbf{W}_{,i}^{dec}\|_2$  in the L1 penalty term allows us to interpret the unit-normalized decoder vectors  $\frac{\mathbf{W}_{,i}^{dec}}{\|\mathbf{W}_{,i}^{dec}\|_2}$  as "feature vectors" or "feature directions," and the product  $f_i(\mathbf{x}) \cdot \|\mathbf{W}_{,i}^{dec}\|_2$  as the feature activations  $^2$ . Henceforth we will use "feature activation" to refer to this quantity.

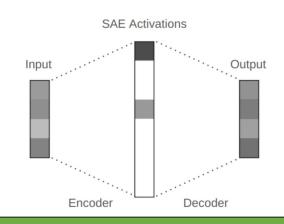


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#### How to interpret SAE features

#### Just use LLM!

For each feature draw:

- 5 highest activating examples20 random, non-activating examples



The model based on the k highest and n random samples suggest the description

Autointerpretable score is calculated by giving example and description and asking model to predict the magnitude of the feature.

Finally the correlation is calculated between ground truth and LLM prediction

# The Shady Part

- Authors introduce BatchTopK in paper published on arXiv: 07.02.2025
- The same authors published paper BatchTopK on arXiv:
   09.12.2024; and on ICLR: 22.01.2025



In summary, our contributions are:

- 1. **SAE stitching**, as a method for comparing latents across different sizes of SAE. Latents in a larger SAE are either novel latents, missing in smaller SAEs, or reconstruction latents, similar to some latents in smaller SAEs.
- 2. **Meta-SAEs**, as an approach for decomposing the decoder directions of SAEs into interpretable, monosemantic meta-latents.
- 3. We also introduce **BatchTopK SAEs**, the state-of-the-art SAE architecture for sparse dictionary learning on language model activations at a fixed average sparsity.



**BatchTopK Sparse Autoencoders** 

Bart Bussmann, Patrick Leask, Neel Nanda

#### **Stitching Sparse Autoencoders of Different Sizes**

Patrick Leask, Bart Bussmann, Joseph Isaac Bloom, Curt Tigges, Noura Al Moubayed, Neel Nanda

math Published: 10 Oct 2024, Last Modified: 09 Nov 2024 of SciForDL Poster Severyone Revisions BibTeX CC BY 4.0

# SAE Stitching

$$\hat{\mathbf{x}} := \alpha \mathbf{b}_0^{\text{dec}} + (1 - \alpha) \mathbf{b}_1^{\text{dec}} + \sum_{l_0 \in L_0} \mathbf{W}_{0, l_0}^{\text{dec}} f_{0, l_0}(\mathbf{x}) + \sum_{l_1 \in L_1} \mathbf{W}_{1, l_1}^{\text{dec}} f_{1, l_1}(\mathbf{x})$$
(5)

where  $\alpha = \frac{|L_0|}{|L_0|+|L_1|}$ ,  $\mathbf{W}_{0,l_0}^{\text{dec}}$  and  $\mathbf{W}_{1,l_1}^{\text{dec}}$  represent individual decoder directions and  $L_0$  and  $L_1$  are the set of latents we include from the respective SAEs. Unlike with model stitching (Bansal et al., 2021), SAE decoder directions are privileged and require no transformations to stitch.

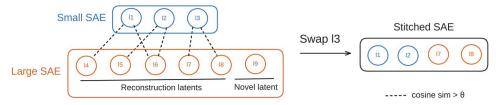
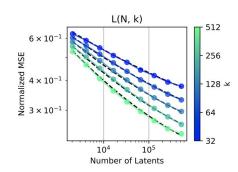


Figure 3: SAE stitching operation: connected subgraphs of latents can be swapped between SAEs based on cosine similarity

two categories, i.e. for an SAE decoder direction  $\mathbf{W}_{1,i}^{\text{dec}}$ , the feature is assigned to the novel group if

$$\max_{j} \left( \frac{\mathbf{W}_{1,i}^{\text{dec}} \cdot \mathbf{W}_{0,j}^{\text{dec}}}{\|\mathbf{W}_{1,i}^{\text{dec}}\| \|\mathbf{W}_{0,j}^{\text{dec}}\|} \right) < \theta$$
 (6)

where  $\mathbf{W}_{0,j}^{\text{dec}}$  represents any decoder direction in  $\mathbf{W}_0^{\text{dec}}$ . If the maximum cosine similarity is larger than the threshold, it is assigned to the reconstruction group. Figure 4 shows the relationship between



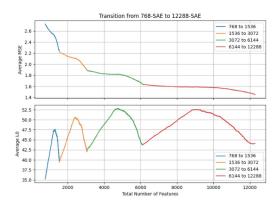


Figure 5: Interpolating between SAE pairs of increasing dictionary size  $(768 \rightarrow 1536 \rightarrow 3072 \rightarrow 6144 \rightarrow 12288)$  through two steps per phase: adding novel latents (increasing L0) then swapping groups of reconstruction latents (decreasing L0 on average). Both steps on average improve reconstruction (MSE). The L0 and MSE are averages over input samples.

# SAE Stitching

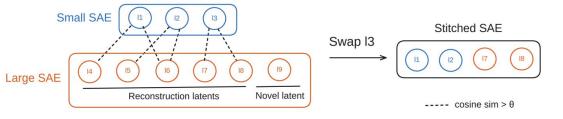


Figure 3: SAE stitching operation: connected subgraphs of latents can be swapped between SAEs based on cosine similarity

The existence of the novel group of latents demonstrates that smaller SAEs are incomplete, and that larger SAE learn features that are missed by the smaller SAE."

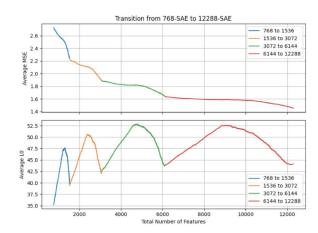


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### Meta-SAE

To decompose the latents of larger SAEs, we introduce meta-SAEs. Meta-SAEs are SAEs trained to reconstruct the decoder directions  $\mathbf{W}_{i}^{\text{dec}}$  of a standard SAE using a dictionary of meta-latents, rather

SAE Latent Description   Meta-Latent Descriptions	
Albert Einstein	Science & Scientists, Famous People, Space & Astronomy, Germany,
	Electricity, Words starting with a capital E
Rugby	Sports activities, Words starting with 'R', References to Ireland, Refer-
70000 50	ences to sports leagues, activities & actions
Android Operating System	Mobile phones, operating systems, Californian cities

"some reconstruction group latents have high decoder cosine similarity to multiple latents in the smaller SAE, suggesting the large SAE latent is an interpolation or composition of the smaller SAE latents"

"The latents of meta-SAEs have similar decoder directions to those found in SAEs of comparable size trained directly on the same network activations. This observation further supports the hypothesis that larger SAE latents are not entirely new features but may be compositions of features already learned, albeit less precisely, by smaller models."

#### A.8 METASAE ADDITIONAL FIGURES

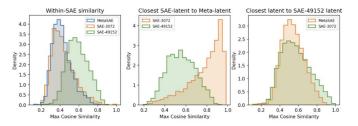


Figure 22: Cosine similarity between SAE latents and meta-SAE latents. Note the high maximum cosine similarity between latents from a meta-SAE with 2304 latents, and a standard SAE with 3072 latents.

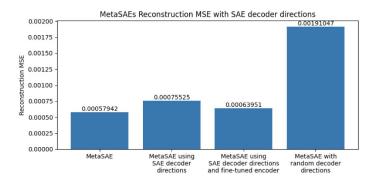


Figure 23: Change in reconstruction performance of a meta-SAE when its decoder directions are replaced with the most similar decoder direction from an SAE with a similar dictionary size.

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# BatchTopK

The training objective for BatchTopK SAEs is defined as:

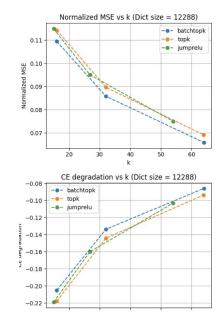
$$\mathcal{L}(\mathbf{X}) = \|\mathbf{X} - \text{BatchTopK}(\mathbf{W}^{\text{enc}}\mathbf{X} + \mathbf{b}^{\text{enc}})\mathbf{W}^{\text{dec}} + \mathbf{b}^{\text{dec}})\|_{2}^{2} + \alpha \mathcal{L}_{\text{aux}}$$
(7)

Here, X is the input data batch;  $W^{enc}$  and  $b^{enc}$  are the encoder weights and biases, respectively;  $W^{dec}$  and  $b^{dec}$  are the decoder weights and biases. The BatchTopK function sets all activation values to zero that are not among the top  $n \times k$  activations by value in the batch, not changing the other values. The term  $\mathcal{L}_{aux}$  is an auxiliary loss scaled by the coefficient  $\alpha$ , used to prevent dead latents, and is the same as in TopK SAEs.

BatchTopK introduces a dependency between the activations for the samples in a batch. We alleviate this during inference by using a threshold  $\theta$  that is estimated as the average of the minimum positive activation values across a number of batches:

$$\theta = \mathbb{E}_{\mathbf{X}}[\min\{z_{i,j}(\mathbf{X})|z_{i,j}(\mathbf{X}) > 0\}]$$
(8)

where  $z_{i,j}(\mathbf{X})$  is the jth latent activation of the ith sample in a batch  $\mathbf{X}$ . With this threshold, we use the JumpReLU activation function during inference instead of the BatchTopK activation function, zeroing out all activations under the threshold  $\theta$ .



Why is this better?
Because it lifts the constraint of **always using k** SAE latents

## **Discussion Time**

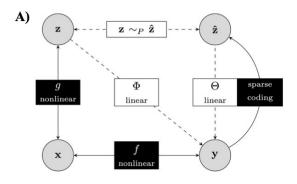
#### - is monosemanticity achievable at all?

2012). Assuming the setting described above, we know that  $f \circ g : \mathbb{R}^N \to \mathbb{R}^M$  is a linear function. Thus, there exists a matrix  $\Phi \in \mathbb{R}^{M \times N}$  (see Fig. 3A) such that

$$f \circ g(z) = \Phi z \quad \forall z \in \mathbb{R}^N. \tag{6}$$

Moreover, assuming the distribution over latent variables  $z \sim P(Z)$  is sparse (at most K active components) (Donoho, 2006), we can recover the latent variables with high probability if

$$M > \mathcal{O}\left(K\log\left(\frac{N}{K}\right)\right).$$
 (7)



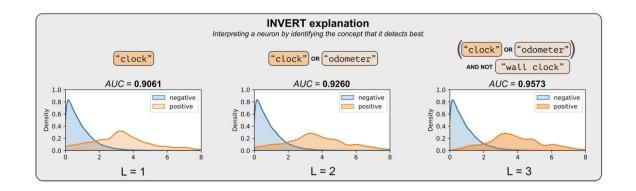
[Submitted on 3 Mar 2025]

From superposition to sparse codes: interpretable representations in neural networks

David Klindt, Charles O'Neill, Patrik Reizinger, Harald Maurer, Nina Miolane

## **Discussion Time**

- do we need monosemanticity to be able to explain NNs?



## **Discussion Time**

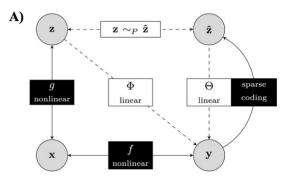
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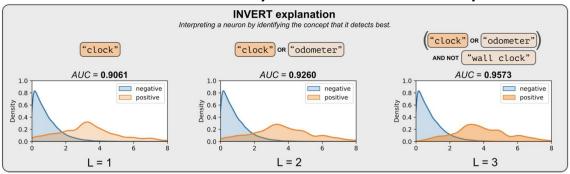
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