```
mod ::=
                      {}
                      [val exp]
                      [val:typ]
                       [type typ]
                       [type : kind]
                       [data typ]
                       [\mathtt{data}:typ]
                       [unit mod]
                      [unit : sig]
                      {\tt new} \ mod
                      \{module \ l = mod\}
                      mod.l
                      \mathtt{link}\ x = mod_1\ \mathtt{with}\ mod_2
                      link x = mod_1 seals mod_2
                      mod :> sig
                       (mod)
                       [val exp:typ]
                                                                                             \rightsquigarrow [val exp] with [val : typ]
                       [type]
                                                                                             → [type : #]
                       [type typ:kind]
                                                                                             \rightsquigarrow [type typ] with [type : kind]
                                                                                             \rightsquigarrow [data typ] with [type : kind]
                       [data typ:kind]
                       [data:typ:kind]
                                                                                             \rightsquigarrow [data : typ] with [type : kind]
                       [unit mod:sig]
                                                                                             \leadsto [unit mod] with [unit :sig]
                       [module mod]
                                                                                             \leadsto mod
                       [module : mod]
                                                                                             \leadsto ! mod
                       [module mod_1: mod_2]
                                                                                             \leadsto mod_1 \text{ with } !mod_2
                                                                                             \rightsquigarrow link x = \{dec_1\} with \cdots link x = \{dec_n[x.x_i/x_i]\} with \{\}
                       \{dec_1\langle , \rangle \cdots \langle , \rangle dec_n\}
                                                                                            \leadsto \mathtt{new}\ mod
                      ! mod
                      mod_1 with mod_2
                                                                                            \rightsquigarrow link x = mod_1 with mod
                      mod_1 seals mod_2
                                                                                             \leadsto link x = mod_1 seals mod
                                                                                             \leadsto link x = ! mod_1 with mod
                      {\tt link}\;x\;:\;mod_1\;{\tt with}\;mod_2
                                                                                             \leadsto link x = ! mod_1 seals mod
                      link x : mod_1 seals mod_2
                                                                                             \leadsto \{ dec_1 \langle \mbox{,} \rangle \ldots \langle \mbox{,} \rangle dec_n \mbox{, module } l = mod \} . l
                      let dec_1\langle , \rangle \ldots \langle , \rangle dec_n in mod
                      let x = mod_1 in mod_2
                                                                                             \leadsto let module x = mod_1 in mod_2
                                                                                             \rightsquigarrow [unit link x = \{\text{module Arg} = mod_1\} with \{\text{module Res} = mod_2[x.\text{Arg}/x]\}
                      \mathtt{fn}\ x = mod_1\ \mathtt{in}\ mod_2
                      \mathtt{fn}\;x\;\colon mod_1\;\mathtt{in}\;mod_2
                                                                                             \leadsto fn x = ! mod_1 in mod_2
                      mod_1 \ mod_2
                                                                                             \rightsquigarrow ({module Arg = mod_2} with ! mod_1). Res
  dec ::=
                      val p \langle [\alpha_1, \dots, \alpha_n] \rangle (x_1 : typ_1) \cdots (x_m : typ_m) : typ
                                                                                             \leadsto p = [\text{val} : \langle \text{forall } [\alpha_1, \dots, \alpha_n] \rightarrow \rangle \ typ_1 \rightarrow \cdots \rightarrow typ_m \rightarrow typ]
                      val p \langle [\alpha_1, \dots, \alpha_n] \rangle (x_1:typ_1) \cdots (x_m:typ_m) \langle : typ \rangle = exp
                                                                                             \leadsto p = \texttt{[val } \langle \texttt{fn } \texttt{[} \alpha_1 \texttt{,} \dots \texttt{,} \alpha_n \texttt{]} \texttt{ ->} \rangle \texttt{ fn } x_1 \colon typ_1 \texttt{ ->} \dots \texttt{fn } x_m \colon typ_m \texttt{ ->} \ exp
                                                                                                             \langle : \langle \text{forall } [\alpha_1, \dots, \alpha_n] \rightarrow \rangle \ typ_1 \rightarrow \cdots \rightarrow typ_m \rightarrow typ \rangle]
                                                                                             \leadsto p = \texttt{[type } \langle \texttt{: \#} n \text{ -> \#} \rangle \texttt{]}
                      type p \langle [\alpha_1, \ldots, \alpha_n] \rangle
                      type p \langle [\alpha_1, \ldots, \alpha_n] \rangle : kind
                                                                                             \rightsquigarrow p = [type : \langle \#n \rightarrow \rangle \ kind]
                      type p \langle [\alpha_1, \ldots, \alpha_n] \rangle \langle : kind \rangle = typ
                                                                                            \rightsquigarrow p = [\text{type } \langle \text{fn } [\alpha_1, \dots, \alpha_n] \rightarrow \rangle \ typ \ \langle : \langle \#n \rightarrow \rangle \ kind \rangle]
                      data p \langle [\alpha_1, \ldots, \alpha_n] \rangle \langle : kind \rangle = typ
                                                                                            \rightsquigarrow p = [\text{data } \langle \text{fn } [\alpha_1, \dots, \alpha_n] \rightarrow \rangle \ typ \ \langle : \langle \#n \rightarrow \rangle \ kind \rangle]
                      data p \langle [\alpha_1, \ldots, \alpha_n] \rangle \langle : kind \rangle : typ
                                                                                            \leadsto p = [\text{data} : \langle \text{fn} [\alpha_1, \dots, \alpha_n] \rightarrow \rangle \ typ \ \langle : \langle \#n \rightarrow \rangle \ kind \rangle]
                      \mathtt{unit}\ p\ :\ sig
                                                                                             \leadsto p = [\mathtt{unit} : sig]
                      unit p \langle : sig \rangle = mod
                                                                                             \rightsquigarrow p = [\text{unit } mod \langle : sig \rangle]
                      module p : mod
                                                                                             \leadsto p = [module : mod]
                      module p \ \langle : mod_1 \rangle = mod_2
                                                                                             \rightsquigarrow p = [\text{module } mod_2 \langle : mod_1 \rangle]
                      \verb|module| x.ls = mod|
                                                                                             \rightsquigarrow x = \{ \text{module } l_1 = \cdots \{ \text{module } l_n = mod \} \cdots \}
                                                                                             \leadsto val x = exp
                      {\tt do}\ exp
```

```
prog ::=
                   dec_1\langle , \rangle \ldots \langle , \rangle dec_n
                                                                                 \leadsto unit it = mod
  sig
        ::=
                   mod import (ls_1, ..., ls_n)
                   mod export (ls_1, \ldots, ls_n)
                                                                                 \rightsquigarrow mod \text{ import ()}
                   \epsilon \mid ls.l
                   x \mid x . ls
         ::=
kind ::=
                   #n -> #
                                                                                 # -> #
 typ
        ::=
                   ! mod
                   int
                   string
                   (\mathit{typ}_1,\ldots,\mathit{typ}_n)
                   (typ_1 | \dots | typ_n)
                   typ_1 \rightarrow typ_2
                   forall [\alpha_1, \ldots, \alpha_n] \rightarrow typ
                   fn [\alpha_1, \ldots, \alpha_n] \rightarrow typ
                   typ [typ_1, \dots, typ_n]
                   (typ)
                                                                                 \rightsquigarrow !p
\rightsquigarrow (() | ())
                   p
                   bool
 exp ::=
                   !\,mod
                   n
                   s
                   exp_1 + exp_2
                   exp_1 - exp_2
                   exp_1 == exp_2
                   \exp_1 < \exp_2
                   exp_1 ++ exp_2
                   (exp_1, \ldots, exp_n)
                   exp#n
                   exp@n[typ]
                   case exp of x_1 \rightarrow exp_1 \mid \ldots \mid x_n \rightarrow exp_n
                   \verb"fn $x\!:\!typ -> exp"
                   exp_1 exp_2
                   fn [\alpha_1,...,\alpha_n] -> exp
                   exp\ [typ_1, \dots, typ_n]
                   in mod\ [typ_1,\ldots,typ_n]\ exp
                   out mod\ [typ_1, \ldots, typ_n]\ exp
                   let module x = mod in exp
                   \mathtt{print}\ exp
                   (exp)
                                                                                 \leadsto !p
                   @n[typ]
                                                                                 \rightsquigarrow ()@n[typ]
                   false
                                                                                 \rightsquigarrow @1[bool]
                                                                                 \rightsquigarrow @2[boo1]
                   true
                                                                                 \leadsto \mathtt{case}\ exp_1\ \mathtt{of}\ x\hbox{--}\!\!\!\!>\!\! exp_3\ |\ x\hbox{--}\!\!\!\!>\!\! exp_2
                   \hbox{if $exp_1$ then $exp_2$ else $exp_3$}\\
                   let dec_1\langle , \rangle \ldots \langle , \rangle dec_n in exp
                                                                                 \leadsto let dec_1 in ... let dec_n in exp
                                                                                 \leadsto let x = [val exp_1] in exp_2
                   \mathtt{let}\ x = exp_1\ \mathtt{in}\ exp_2
                                                                                 \rightsquigarrow let x = [val \ exp:typ] \ in \ x
                   (exp: typ)
                   exp_1 ; exp_2
                                                                                 \leadsto \mathtt{let}\ x = exp_1\ \mathtt{in}\ exp_2
```