Ecosystem models A model of intermediate complexity for ecosystems for anchovy and sardine

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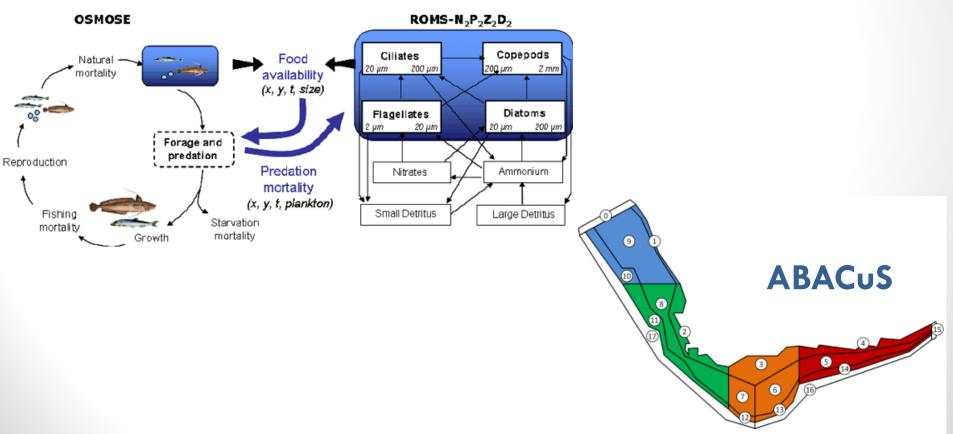
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Ecosystem models



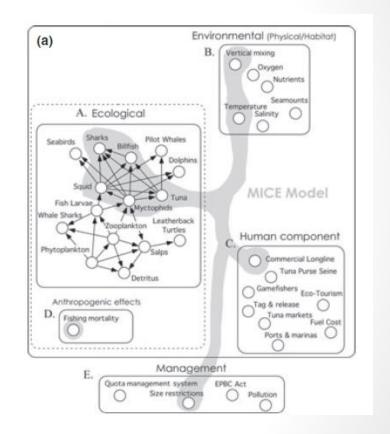
Ecopath with Ecosim

No fish is an island



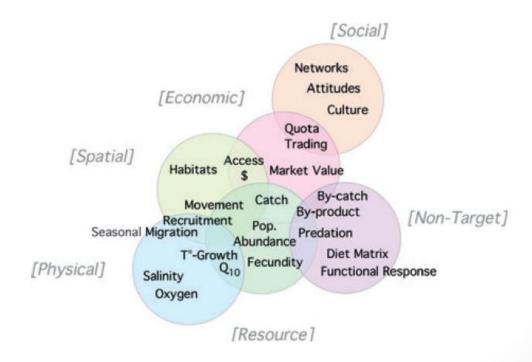
Model of Intermediate Complexity for Ecosystems (MICE)

- Represent ecological processes for a limited group of species (typically <10) and include at least one explicit representation of an ecological process (e.g. interspecific interaction or spatial habitat use).
- MICE can have linked physical models.
- Provide the ability to address tactical questions. Strategic (what-if scenarios) purposes.



Model of Intermediate Complexity for Ecosystems (MICE)

- Designed based on data available to parameterize the model.
- Context and question-driven.
- Estimate parameters through fitting to data, use statistical diagnostic tools to evaluate model performance and account for uncertainty.

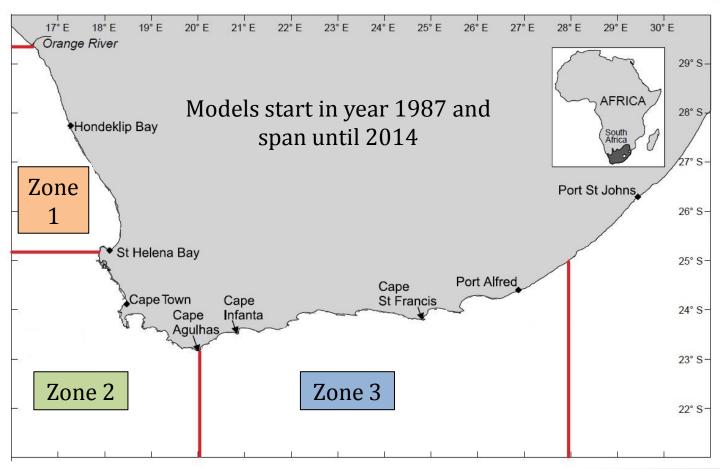


MICE - anchovy and sardine

 Explore the dynamics of anchovy and sardine in a spatially disaggregated model that would allow for consideration of the impacts of environmental variability and possible effects of climate change on movements between zones and on other key population dynamics processes.

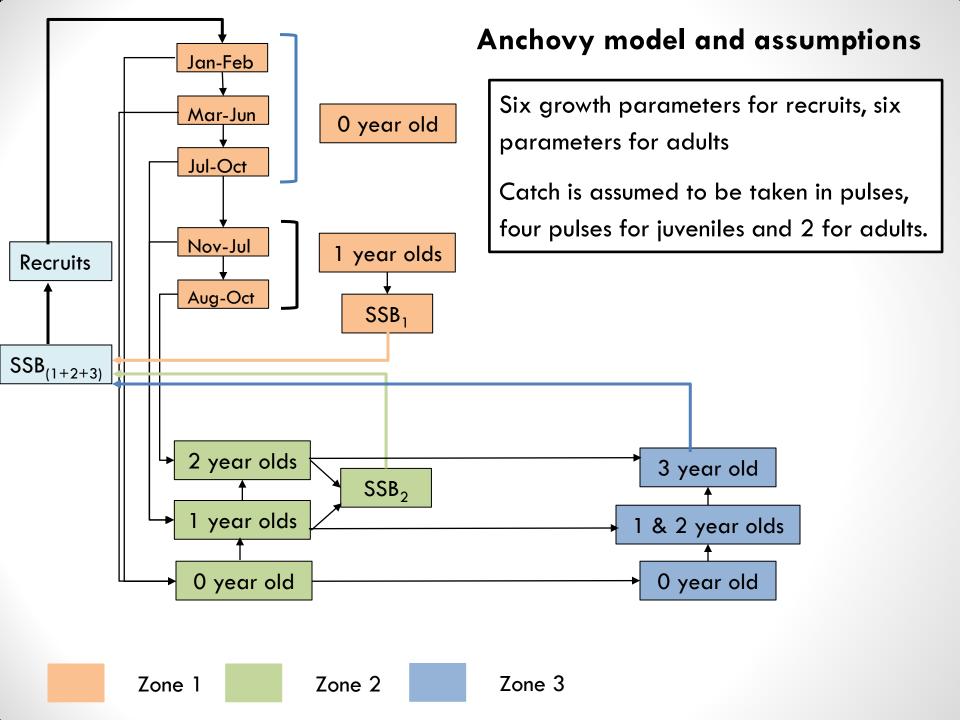
MICE: anchovy and sardine

- Age-structured, biomass-based spatial model.
- Model equations account for juvenile and adult movement between zones, growth, recruitment, natural and fishing mortality.

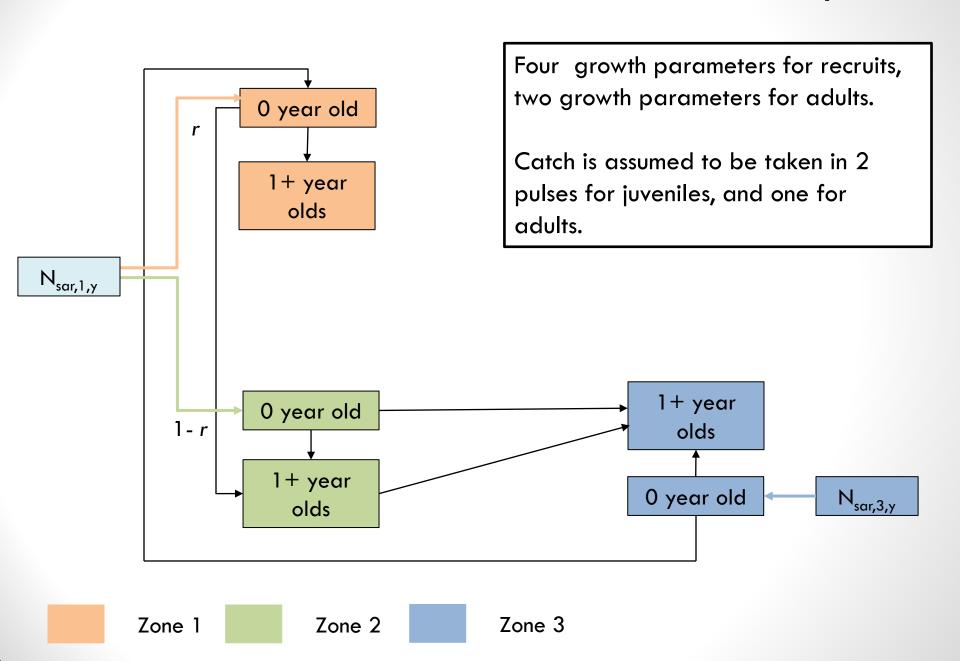


MICE: Catch data

- Monthly length frequencies from the commercial landings and monthly cut-off lengths (from de Moor et al., 2012) were used to determine monthly catch of 0-year-olds and 1+ fish (in numbers).
- The monthly catch (in tons) for juveniles and adults was determined using length-weight relationships for sardine and anchovy (de Moor & Butterworth, 2015a, 2015b).
- Both models assumed that these catches are taken in pulses throughout the year, monthly catch data were then grouped among months to fit the model structure.

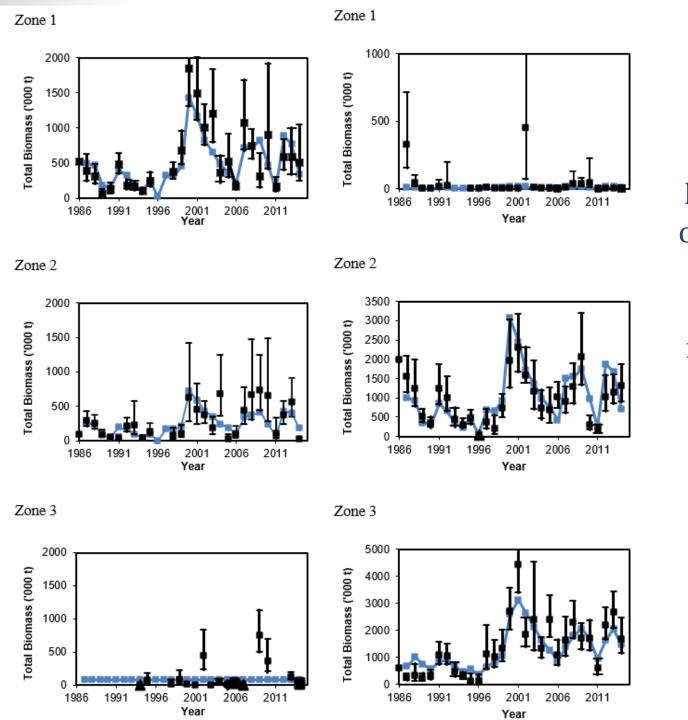


Sardine model and assumptions



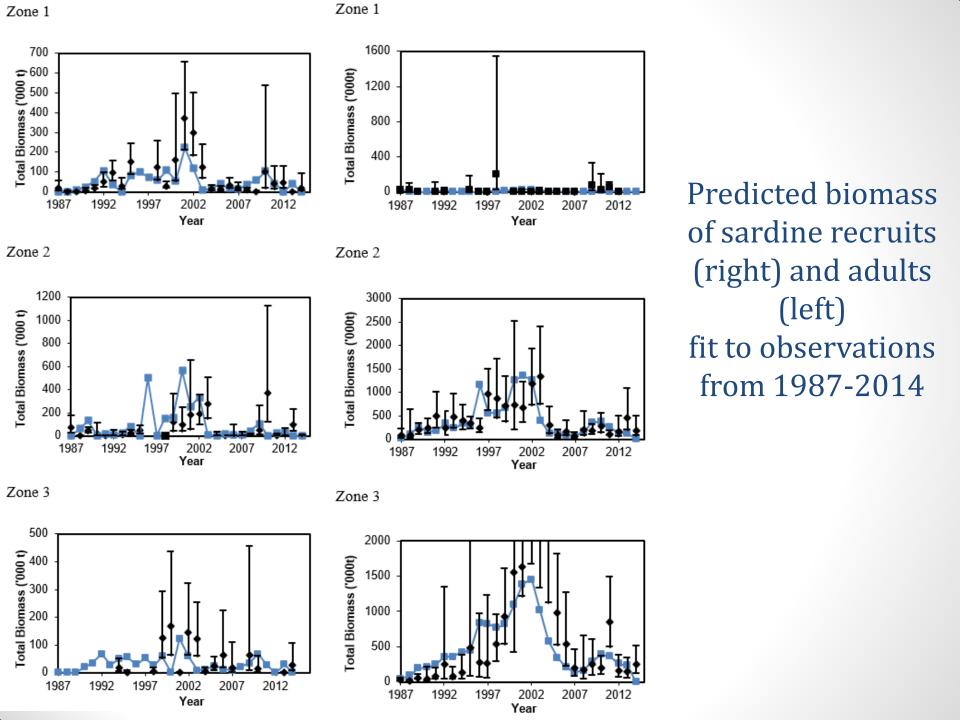
Relationship with environmental parameters

- Investigate whether any relationships can currently be detected between model parameters and environmental indices.
- Environmental indices spanning from 1980-2050 from the NEMO-MEDUSA 2.0 model: Sea surface salinity, temperature (SST) and pH, primary production (PP) and wind speed.
- Relationship between SST (seasonal averages)/PP and recruitment residuals for a given year has been analysed. Average of the monthly primary production from September_(y-1) to April_(y) was used. The relationship between $PP_{(y-1)}$ and recruitment residuals of year y was investigated.

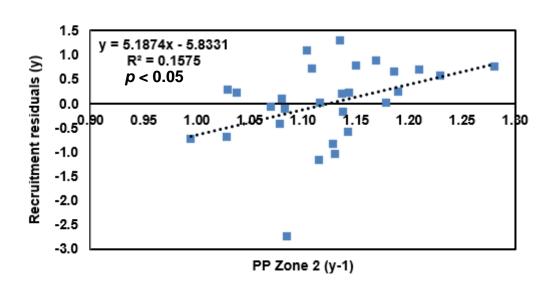


Results

Predicted biomass of anchovy recruits (right) and adults (left) fit to observations from 1987-2014

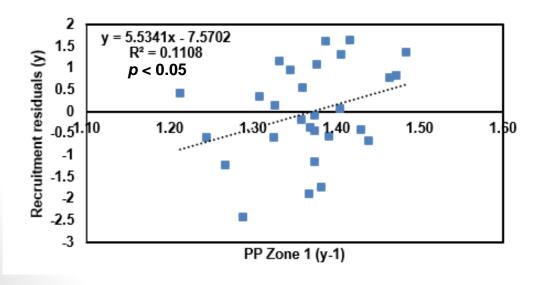


Zone 2



Recruitment residuals for the anchovy single stock and PP (g C m² d⁻¹)

Zone 1



Recruitment residuals for the west stock of sardine and PP(g C m² d⁻¹)

Future direction: what-if scenarios

- Estimate movement parameters annually, and link them to SST or PP in each zone.
- Link sardine and anchovy recruitment to variations in SST or PP.
- Use time series of environmental parameters to evaluate future changes in biomass, recruitment and movement of sardine and anchovy.
- Evaluate scenarios of increases or decreases in SST/upwelling accounting for spatial differences along the South African coast.



Appendix: A1. Anchovy equations. Definitions of parameters and variables provided in Table A1.

0-year-old biomass at the time of the survey (1 June)

$$B_{y,0,1}^{anSURVEY} = (1 - move_s^{0-1})((f^{-1}(SSB_{y-1,1}^{an} + SSB_{y-1,2}^{an}))G_0^{-1}e^{-2M_0^{an}/12} - C_{y,0,1}^{anJF})G_0^{-3}e^{-3M_0^{an}/12} - C_{y,0,1}^{anMM}$$

$$B_{y,0,2}^{anSURVEY} = \left(1 - move_s^{0-4}\right) move_s^{0-1} \left(\left(f^{-1}\left(SSB_{y-1,1}^{an} + SSB_{y-1,2}^{an}\right)\right) G_0^{-1} e^{-2M_0^{an}/12} - C_{y,0,1}^{anJF} \right) G_0^{-3} e^{-3M_0^{an}/12} - C_{y,0,2}^{anMM}$$

1-year-old biomass in November

$$B_{y,1,1}^{an} = \left(1 - move_{s}^{0-3}\right) \left(\left(1 - move_{s}^{0-2}\right) \left(B_{y,0,1}^{anSURVEY}G_{0}^{5}e^{-M_{0}^{an}/12} - C_{y,0,1}^{anJJ}\right)G_{0}^{6}e^{-M_{0}^{an}/12}\right)G_{0}^{7}e^{-M_{0}^{an}/12} - C_{y,0,1}^{anAO}G_{0}^{8}e^{-2M_{0}^{an}/12}$$

$$\boldsymbol{B}_{y,1,3}^{an} = \left(\left(B_{y,0,3}^{anSURVEY} \boldsymbol{G}_{0}^{5} e^{-M_{0}^{an}/12} - \boldsymbol{C}_{y,0,3}^{anJJ} \right) \boldsymbol{G}_{0}^{6} e^{-M_{0}^{an}/12} \right) \boldsymbol{G}_{0}^{7} e^{-M_{0}^{an}/12} - \boldsymbol{C}_{y,0,3}^{anAO} \right) \boldsymbol{G}_{0}^{8} e^{-2M_{0}^{an}/12}$$

2-year-old biomass in November

$$B_{y,2,1}^{an} = 0$$

$$\begin{split} B_{\mathbf{y},2,2}^{\mathit{an}} = & \left(\!\! \left(\!\! \left(\!\! \left(\!\! \left(\!\! 1 \!\! - \!\! move_{s}^{\scriptscriptstyle 1} \right) \!\! \left(\!\! B_{\mathbf{y},1,1}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,1}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,1}^{\mathit{anAO}} \right) \!\! G_{1}^{\scriptscriptstyle 4} e^{-2M_{i\cdot}^{\mathit{an}}/12} \\ & + \left(\!\! \left(\!\! 1 \!\! - \!\! move_{s}^{\scriptscriptstyle 1} \right) \!\! \left(\!\! \left(\!\! B_{\mathbf{y},1,1}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,1}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-M_{i\cdot}^{\mathit{an}}/12} + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,2}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 4} e^{-2M_{i\cdot}^{\mathit{an}}/12} \\ & + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,2}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 4} e^{-2M_{i\cdot}^{\mathit{an}}/12} \\ & + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,2}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 4} e^{-2M_{i\cdot}^{\mathit{an}}/12} \\ & + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,2}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 2} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,2}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\scriptscriptstyle 1} e^{-5M_{i\cdot}^{\mathit{an}}/12} - C_{\mathbf{y},1,2}^{\mathit{anNJ}} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} + \left(\!\! \left(\!\! B_{\mathbf{y},1,2}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} \right) \!\! G_{1}^{\scriptscriptstyle 3} e^{-4M_{i\cdot}^{\mathit{an}}/12} + \left(\!\! \left(\!\! B_{\mathbf{y},1,1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \right) \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an}} \!\! G_{1}^{\mathit{an$$

$$\begin{split} B_{_{y,2,3}}^{^{an}} &= move_{_E} \Big(move_{_S}^{^{1}} \Big(\Big(B_{_{y,1,1}}^{^{an}} G_{_{1}}^{^{1}} e^{^{-5M_{1+}^{an}/12}} - C_{_{y,1,1}}^{^{anNJ}} \Big) G_{_{1}}^{^{2}} e^{^{-4M_{1+}^{an}/12}} + \Big(\Big(B_{_{y,1,2}}^{^{an}} G_{_{1}}^{^{1}} e^{^{-5M_{1+}^{an}/12}} - C_{_{y,1,2}}^{^{anNJ}} \Big) G_{_{1}}^{^{2}} e^{^{-4M_{1+}^{an}/12}} + \Big(\Big(B_{_{y,1,2}}^{^{an}} G_{_{1}}^{^{1}} e^{^{-5M_{1+}^{an}/12}} - C_{_{y,1,2}}^{^{anNJ}} \Big) G_{_{1}}^{^{2}} e^{^{-4M_{1+}^{an}/12}} - C_{_{y,1,3}}^{^{anNJ}} \Big) G_{_{1}}^{^{2}} e^{^{-4M_{1+}^{an}/12}} - C_{_{y,1,3}}^$$

3+ biomass in November

$$B_{y,3+,1}^{an} = 0$$

$$B_{y,3+,2}^{an} = 0$$

$$B_{y,3+,3}^{an} = \left(B_{y-1,2,2}^{an} + B_{y-1,2,3}^{an}\right)G_{2}e^{-M_{1+}^{an}} + B_{y-1,3+,3}^{an}G_{3+}^{1}e^{-M_{1+}^{an}}$$

SSB in November

$$SSB_{y,1}^{an} = p_1 B_{y,1+,1}^{an}$$

$$SSB_{y,2}^{an} = p_2 B_{y,1+,2}^{an}$$

$$SSB_{y,3}^{an} = p_3 B_{y,1+,3}^{an}$$

Recruitment in January

$$f^{1}\left(SSB_{y-1,1}^{an} + SSB_{y-1,2}^{an}\right) = \begin{cases} a_{1}^{an} e^{\frac{\varepsilon_{y,1}^{an} - 0.5\left(\sigma_{1}^{an}\right)^{2}}{2}} & \text{if } SSB_{y-1,1}^{an} + SSB_{y-1,2}^{an} \ge b_{1}^{an} \\ a_{1}^{an} \frac{SSB_{y-1,1}^{an} + SSB_{y-1,2}^{an}}{b_{1}^{an}} e^{\frac{\varepsilon_{y,1}^{an} - 0.5\left(\sigma_{1}^{an}\right)^{2}}{2}} & \text{if } SSB_{y-1,1}^{an} + SSB_{y-1,2}^{an} \le b_{1}^{an} \end{cases}$$

Fitting the Model to Available Data

$$-\ln L = 0.5 \sum_{y=1987}^{2014} \sum_{z=1}^{3} \ln \left(2\pi \left(\sigma_{y,z}^{anMAY} \right)^{2} \right) + \left(\frac{\ln \left(B_{y,z}^{anMAY} \right) - \ln \left(k_{MAY,z}^{san} B_{y,0,z}^{anSURVEY} \right)}{\sigma_{y,z}^{anMAY}} \right)^{2}$$

$$+ 0.5 \sum_{y=1986}^{2014} \sum_{z=1}^{3} \ln \left(2\pi \left(\sigma_{y,z}^{anNOV} \right)^{2} \right) + \left(\frac{\ln \left(B_{y,z}^{anNOV} \right) - \ln \left(k_{NOV,z}^{an} \sum_{a=1}^{3+} B_{y,a,z}^{an} \right)}{\sigma_{y,z}^{anNOV}} \right)^{2}$$

$$+ 0.5 \sum_{y=1987}^{2014} \ln \left(2\pi \left(\sigma_{1}^{an} \right)^{2} \right) + \left(\frac{\varepsilon_{y,1}^{an}}{\sigma_{1}^{an}} \right)^{2}$$

Sardine equations.

0+ biomass at the time of the survey (1 June)

$$B_{y,0,1}^{sarSURVEY} = \left((r_y(e^{Nsar1,y}) + (move_w e^{Nsar3,y})) G_0^1 e^{-3M_0^{sar}/12} - C_{y,0,1}^{sarBS} \right) G_0^2 e^{-2M_0^{sar}/12}$$

$$B_{y,0,2}^{sarSURVEY} = \left(((1-r)(e^{Nsar1,y})) G_0^1 e^{-3M_0^{sar}/12} - C_{y,0,2}^{sarBS} \right) G_0^2 e^{-2M_0^{sar}/12}$$

$$B_{y,0,3}^{sarSURVEY} = \left(((1-move_w)(e^{Nsar3,y})) G_0^1 e^{-3M_0^{sar}/12} - C_{y,0,3}^{sarBS} \right) G_0^2 e^{-2M_0^{sar}/12}$$

1+ biomass in November

$$B_{y,1+,1}^{sar} = (1 - move_{s}) \left(B_{y,0,1}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,1}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + \left(B_{y-1,1+,1}^{sar} G_{1+}^{1} e^{-0.5M_{1+}^{sar}} - C_{y,1+,1}^{sar} \right) e^{-0.5M_{1+}^{sar}}$$

$$B_{y,1+,2}^{sar} = move_{s} \left(B_{y,0,1}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,1}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} + (1 - move_{e}) \left(B_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y,0,2}^{sarAS} \right) G_{0}^{4} e^{-3M_{0}^{sar}/12} - C_{y,0,2}^{sarSURVEY} G_{0}^{3} e^{-2M_{0}^{sar}/12} - C_{y$$

Fitting the Model to Available Data

$$-\ln L = 0.5 \sum_{y=1987}^{2014} \sum_{z=1}^{3} \ln \left(2\pi \left(\sigma_{y,z}^{sarMAY} \right)^{2} \right) + \left(\frac{\ln \left(B_{y,z}^{sarMAY} \right) - \ln \left(k_{MAY,z}^{sar} B_{y,0,z}^{sarSURVEY} \right) \right)^{2}}{\sigma_{y,z}^{sarMAY}} + 0.5 \sum_{y=1986}^{2014} \sum_{z=1}^{3} \ln \left(2\pi \left(\sigma_{y,z}^{sarNOV} \right)^{2} \right) + \left(\frac{\ln \left(B_{y,z}^{sarNOV} \right) - \ln \left(k_{NOV,z}^{sarNOV} B_{y,1+,z}^{sar} \right) \right)^{2}}{\sigma_{y,z}^{sarNOV}} \right)$$