Chapter 12 Non-parametric Test

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1	1 Questions:		
1.	1	What is V in the returned result of wilcox.test	
##	Wil	coxon signed rank exact test data: data\$air and data\$sulf.diox	

1.2 What is the definition of T in psignrank?

shift is not equal to 0

In the psignrank document(https://www.rdocumentation.org/packages/stats/versions/3.6. 2/topics/SignRank), the Wilcoxon signed rank statistic is "the sum of the ranks of the absolute values x[i] for which x[i] is positive". I am wondering if $T = T^+$ instead of $T = min(T^+, T^-)$? This appears to be correct when solving the example problem, where 2*(1 - psignrank(75.5, n=14)) = 0.135 but 2*psignrank(29.5, n=14) != 0.135

V = 21, p-value = 0.006653 alternative hypothesis: true location

I therefore wonder if $T = T^+$ should be the definition of psignrank in R.

Another question regarding this topic: when testing the two-tailed hypothesis, when should

we use 2*(1 - psignrank(T,n)) and 2*psignrank(T, n)? i.e. what is the mean for the wilcoxon signed rank distribution? Is it n(n+1)/4 as stated in the document?

This is right.

So when we calculate the p value, we determine whether to use 2*(1 - psignrank(T,n)) or 2*psignrank(T, n) based on if T > n(n+1)/4 or T < n(n+1)/4, right?

1.3 How can we decide which probability to calculate in one-sided Wilcoxon Rank Sum test?

In the Wilcoxon Rank Sum test, we always use $W = min(W_1, W_2)$ and $\mu_W = n_{min}*(n_{min} + n_{large} + 1)/2$ no matter if we want to know if $H_1: \mu_1 - \mu_2 < 0$ or $H_1: \mu_2 - \mu_1 < 0$, how to we determine if p-value $= 1 - Pr(z < z_W)$ or p-value $= Pr(z < z_W)$?

My understanding: it depends on which one you picked up for determining the W. In the example problem in the slides, H1 is about group 1 has less values, and W turns out to be W1, therefore p-value = Pr(z < 0).

1.4 Question about CTL

For sampling distribution, it can have sampling size n and sampling time m, what determines if it follows CLT? n or m? If we sample for 1 time and 100 times, each time with same size n, does that makes a difference? Another way to ask this question: if we sample for 3 times (m=3), but each time with sample size n=1000, does that follow CLT?

1.5 is it okay to share the Infererence cheat sheet raw file?

Willing to extend it.

2 Wilcoxon Signed Rank Test

- Only for paired sample.
- Evaluate the null hypothesis: $Z_T = (T \mu_T)/\sigma_T$
- Note:

$$\mu_T = 0$$

$$\sigma_T = \sqrt{\frac{n(n+1)(2n+1)}{6}}$$

• When n is large enough (n > 12), we get

$$Z_T \sim N(0,1)$$

- calculate the probability of getting Z_T when $\mu = 0$ is true.
- For two-sided test, follow what we do in the sampling distribution:
 - -2*p when z < 0
 - -2*(1 p) when z > 0
- if n > 12, you can just apply CLT, the R code is: wilcox.test(before, after, paired = T, exact = F, correct = F). exact = determines if the statistics follow normal distribution (exact = F) or exact distribution (exact = T).
- If $n \leq 12$, we cannot use the normal approximation. In that case, we use psignrank(T,n) in R to calculate the exact distribution.
 - R requires $T = T^+$ for this to work correctly!

3 Wilcoxon Rank-Sum test (also known as Mann-Whitney U test)

- nonparametric analog to the two-sample t-test
- get W_1 and W_2
- $\bullet \ \ W=\min(W_1,W_2)$
- $n_1 =$ sample size with the <u>smaller</u> sum of ranks.
- $n_2 = \text{sample size}$ with the <u>larger</u> sum of ranks.

$$\mu_W = \frac{n_1 \left(n_1 + n_2 + 1\right)}{2} \text{ and } \sigma_W = \sqrt{\frac{n_1 n_2 \left(n_1 + n_2 + 1\right)}{12}}$$

 $z_W = \frac{W - \mu_W}{\sigma_W}$

- $z_W \sim N(0,1)$ when n_1 and n_2 are large enough (n1, n2 > 10).
 - in R: wilcox.test(..., exact = F, correct = F, paired = F, alt = "")
- When n_1 and n_2 are very small (i.e. either is less than or equal to 10), we can use the exact distribution to calculate the p-values. In R: pwilcox(Wobs, n1, n2)
 - in this case, $W_{obs}=W-n_1(n_1+1)/2$
 - wilcox.test also works when exact = T
- correct: correct the data with continuity correction