

# Isotope Tracking

## Applications

After a new product application at time  $t + 1$ , the top soil carbon isotope signature ( $\delta^{13}C$ ) for a soil layer  $k$ , is updated by balancing mass terms. Note that for pesticide applications only the first layer ( $k = z_0$ ) is considered, such that:

$$\delta^{13}C_{k(t+1)} = \frac{1}{M_{k,tot(t+1)}} \left( \delta^{13}C_{k(t)} \cdot M_{k(t)} + \delta^{13}C_{app(t+1)} \cdot M_{app(t+1)} \right)$$

$$M_{k,tot(t+1)} = M_{k(t)} + M_{app(t+1)}$$

where  $M_{k(t)}$  is the pesticide mass ( $\mu g$ ) for the layer  $k$  present before application  $app$ .

For each non-fractionating mass transfer process  $\delta^{13}C$  is updated also by balancing mass terms for each cell:

$$\delta^{13}C_{k(t+1)} = \frac{1}{M_{k,tot(t+1)}} \left( \delta^{13}C_{k(t)} \cdot M_{k(t)} + \delta^{13}C_{gain(t+1)} \cdot M_{gain(t+1)} - \delta^{13}C_{loss(t+1)} \cdot M_{loss(t+1)} \right)$$

$$M_{k,tot(t+1)} = M_{k(t)} + M_{gain(t+1)} - M_{loss(t+1)}$$

Update at each cell for each layer is computed by the following function, where the relevant layer and processes is selected:

```
def update_layer_delta(model, layer, process, mass_process, mass_before_transport):
    if layer == 0:
        delta_layer = model.delta_z0
        delta_layer_above = None
        mass_layer = model.pestmass_z0
    elif layer == 1:
        delta_layer = model.delta_z1
        delta_layer_above = model.delta_z0
        mass_layer = model.pestmass_z1
    elif layer == 2:
        delta_layer = model.delta_z2
        delta_layer_above = model.delta_z1
        mass_layer = model.pestmass_z2

    if process == "volat":
        pass
    elif process == "runoff":
        pass
    elif process == "leach":
        pass
    elif process == "latflux":
        pass
    else:
        raise NotImplementedError

    return "updated delta for delta_layer"
```

For volatilization, the process process="volat" is chosen,

```
def update_layer_delta(model, layer, process, mass_process, mass_before_transport):
    if layer == 0:
        delta_layer = model.delta_z0
        delta_layer_above = 0
        mass_layer = model.pestmass_z0
    elif layer == 1:
        delta_layer = model.delta_z1
        delta_layer_above = model.delta_z0
        mass_layer = model.pestmass_z1
    elif layer == 2:
        delta_layer = model.delta_z2
        delta_layer_above = model.delta_z1
        mass_layer = model.pestmass_z2

    if process == "volat":
        mass_loss = mass_process["mass_loss"]
        mass_gain = 0
        delta_gain = 0
        delta_loss = delta_layer

    elif process == "runoff":
        pass
    elif process == "leach":
        pass
    elif process == "latflux":
        pass
    else:
        raise NotImplementedError

    if process == "latflux":
        pass
    else:
        mass_tot = mass_before_transport + mass_gain - mass_loss
        delta_int = ((1/mass_tot) *
                     (delta_layer * mass_before_transport + # initial
                      delta_gain * mass_gain - # mass_in
                      delta_loss * mass_loss)) # mass_out

    return delta_int
```

Full function

```
def update_layer_delta(model, layer, process, mass_process, mass_before_transport):
    if layer == 0:
        delta_layer = model.delta_z0
        delta_layer_above = 0
        mass_layer = model.pestmass_z0
    elif layer == 1:
        delta_layer = model.delta_z1
        delta_layer_above = model.delta_z0
        mass_layer = model.pestmass_z1
    elif layer == 2:
        delta_layer = model.delta_z2
        delta_layer_above = model.delta_z1
```

```

    mass_layer = model.pestmass_z2
if process == "volat":
    mass_loss = mass_process["mass_loss"]
    mass_gain = 0
    delta_gain = 0
    delta_loss = delta_layer
elif process == "runoff":
    mass_loss = mass_process["mass_runoff"]
    mass_gain = 0
    delta_gain = 0
    delta_loss = delta_layer
elif process == "leach":
    mass_leached = mass_process["mass_leached"] # mg
    mass_loss = mass_leached
    mass_gain = 0
    delta_gain = delta_layer_above
    delta_loss = delta_layer
elif process == "latflux":
    mass_latflux = mass_process["net_mass_latflux"] # mg
    mass_loss = mass_process["cell_mass_loss_downstream"]
    mass_gain = mass_process["upstream_mass_inflow"]
    mass_tot = mass_before_transport + mass_gain - mass_loss
    # Proof of first fraction, i.e., f1 > 1
    f1 = mass_before_transport / mass_tot
    # Proof of 2nd (inflow) fraction, f2 < 1
    # f2 = accuflux(
    #     model.ldd, mass_gain)/accuflux(model.ldd, mass_tot)
    # Proof of third (leaving) mass fraction, f3 < 1
    f3 = mass_loss / mass_tot
else:
    raise NotImplementedError
if process == "latflux":
    delta2_f2 = accuflux(model.ldd_subs, mass_gain*delta_layer)/accuflux(model.ldd_subs, mass_tot)
    delta_int = (delta_layer * f1) + delta2_f2 - (delta_layer * f3)
else:
    mass_tot = mass_before_transport + mass_gain - mass_loss
    delta_int = ((1/mass_tot) *
        (delta_layer * mass_before_transport + # initial
         delta_gain * mass_gain - # mass_in
         delta_loss * mass_loss)) # mass_out
# return {"delta_int": delta_int, "mass_layer": mass_layer}
return delta_int

```

## References