# **Assignment t-test**

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t-test test the null hypothesis  $H_0$  against the alternative hypothesis  $H_1$ .

For univariate samples, t-test performs a Student t test. The test statistic is assumed to follow a Student t-Distribution [df].

For multivariate samples, t-test performs Hotelling's  $t^2$  test. The test statistic is assumed to follow a Hotelling t-square distribution [p, df] where p is the dimension of data.

The degrees of freedom df, used to specify the distribution of the test statistic, depend on the sample size, number of samples, and in the case of two univariate samples, the results of a test for equal variances.

For the t-test, a cutoff  $\alpha$  is chosen such that  $H_0$  is rejected only if  $p < \alpha$ . The value of  $\alpha$  used for the "Test Conclusion" and "Short Test Conclusion" properties is controlled by the Significance Level option. This value  $\alpha$  is also used in diagnostic tests of assumptions, including tests for normality, equal variance, and symmetry. By default,  $\alpha$  is set to 0.05.

1. Certain refined edible oil is packed in tins holding 16 kg each. The filling machine can maintain this but with a standard deviation of 0.5 kg. Samples of 25 are taken from the production line. If a sample means are (i) 16.35 kg, (ii) 15.8 kg. Can we be 95 per cent sure that the sample has come from a population of 16 kg tins?

# **Solution:**

Null hypothesis:  $H_0: \mu = 16$ 

Alternative hypothesis:  $H_1: \mu \neq 16$  (two tailed test)

(i) given, 
$$\bar{x} = 16.35$$
,  $s = 0.5$  and  $n = 25$ 

t-statistic:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{16.35 - 16}{0.5/\sqrt{25}} = 3.5$$

degrees of freedom:

$$d.o.f = n - 1 = 25 - 1 = 24$$

The critical value for t (from t-distribution table) with degrees of freedom = 24 and  $\alpha = 0.05$  is 2.064

Standard Error:

$$S.E = \frac{s}{\sqrt{n}} = \frac{0.5}{\sqrt{25}} = 0.1$$

**Conclusion:**  $|t| > t_{0.05}$ , we reject the Null hypothesis. That is the sample mean is differ from the intended weight and hence does not come from a population of 16 kg tins.

(ii) given,  $\bar{x}=15.8, s=0.5$  and n=25

t-statistic:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{15.8 - 16}{0.5/\sqrt{25}} = -2.0$$

degrees of freedom:

$$d.o.f = n - 1 = 25 - 1 = 24$$

The critical value for t (from t-distribution table) with degrees of freedom = 24 and  $\alpha = 0.05$  is 2.064

Standard Error:

$$S.E = \frac{s}{\sqrt{n}} = \frac{0.5}{\sqrt{25}} = 0.1$$

**Conclusion:**  $|t| < t_{0.05}$ , we fail to reject the Null hypothesis. That is the sample mean is not differ from the intended weight and hence come from a population of 16 kg tins.

# Program:

```
#!/usr/bin/env python3
import numpy as np
from scipy.stats import t
import matplotlib.pyplot as plt
plt.style.use('seaborn-darkgrid')
print ("_____T-test____")
p_mean = float(input("\nPopulation mean: "))
s_mean = float(input("Sample mean: "))
s_stdv = float(input("Sample stand_dev: "))
n = float(input("Sample length: "))
# degrees of freedom, level of significance, confidence level
dof = n - 1; los = 0.05; cnl = 1 - los
# calculation of T-statistics
tstatistics = (s_mean - p_mean)/(s_stdv/np.sqrt(n))
tstatistics = -tstatistics if tstatistics > 0 else tstatistics
print("\nT-statistics: {:.5f}".format(tstatistics))
# calculation of Critical values
tcritical_l = t.ppf(q = los/2, df = dof)
tcritical_u = -tcritical_l
print("\nCritical values are {:.5f}, {:.5f}".format(tcritical_l, tcritical_u))
# decision making - using T-statistics and Critical values
if tstatistics < tcritical_l or tstatistics > tcritical_u:
   print("Reject the Null hypothesis.")
else: print("Fail to reject the Null hypothesis.")
# calculation of p-value
pvalue = 2*t.cdf(tstatistics, df = dof)
print("\np-value: {:.5f}".format(pvalue))
# decision making - using p-value
if pvalue < los: print("Reject the Null hypothesis.")</pre>
else: print("Fail to reject the Null hypothesis.")
# standard error
std_err = s_stdv/np.sqrt(n)
print("\nStandard Error: {:.5f}".format(std_err))
# confidence interval
cnf_int = s_mean + std_err * np.array([tcritical_l, tcritical_u])
print("Confidence Interval: {}".format(cnf_int))
# plot script
x1=np.linspace(-10,tcritical_1,1000); y1=t.pdf(x1,df=dof)
x2=np.linspace(tcritical_u,10,1000); y2=t.pdf(x2,df=dof)
x3=np.linspace(-4,4,1000); y3=t.pdf(x3,df=dof)
ax=plt.figure().add_subplot(111); ax.plot(x3,y3,color='brown')
ax.fill_between(x1,y1,0,alpha=0.5,color='brown',label='Rejection Region')
ax.fill_between(x2,y2,0,alpha=0.5,color='brown'); ax.set(xlabel='X',ylabel='P(X)')
ax.axvline(x=tstatistics,ls='--',c='b',label='T statistics = {:.5f}'.format(tstatistics))
```

ax.set(xlim=[-4,4],title="T Distribution (degrees of freedom = {:.0f})".format(dof))
plt.legend(); plt.show()

# Output:

\_\_\_\_\_T-test\_\_\_\_\_

Population mean: 16 Sample mean: 16.35 Sample stand\_dev: 0.5 Sample length: 25

T-statistics: -3.50000

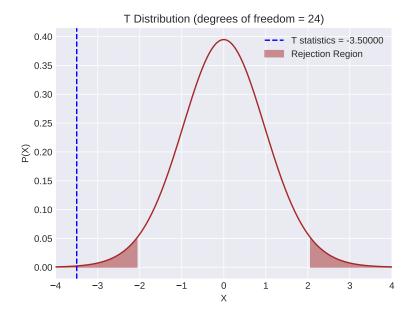
Critical values are -2.06390, 2.06390 Reject the Null hypothesis.

p-value: 0.00184

Reject the Null hypothesis.

Standard Error: 0.10000

Confidence Interval: [16.14361014 16.55638986]



\_\_\_\_\_T-test\_\_\_\_\_

Population mean: 16 Sample mean: 15.8 Sample stand\_dev: 0.5 Sample length: 25

T-statistics: -2.00000

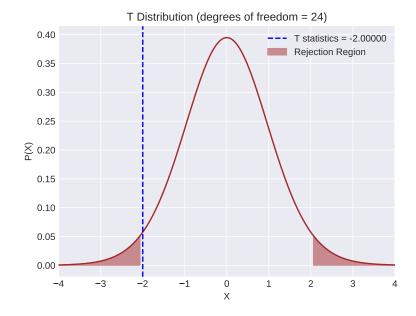
Critical values are -2.06390, 2.06390 Fail to reject the Null hypothesis.

p-value: 0.05694

Fail to reject the Null hypothesis.

Standard Error: 0.10000

Confidence Interval: [15.59361014 16.00638986]



2. A filling machine is expected to fill 5 Kg of powder into bags. A sample of 10 bags gave the weighs 4.7, 4.9, 5.0, 5.1, 5.4, 5.2, 4.6, 5.1, 4.6 and 4.7 Test whether the machine is working properly.

**Solution:** 

Null hypothesis:  $H_0: \mu = 5$ 

**Alternative hypothesis:**  $H_1: \mu \neq 5$  (two tailed test)

Sample mean:

$$\bar{x} = \frac{\sum_{i=1}^{n} x_i}{n} = \frac{4.7 + 4.9 + 5.0 + 5.1 + 5.4 + 5.2 + 4.6 + 5.1 + 4.6 + 4.7}{10} = 4.93$$

Sample variance:

$$s^{2} = \frac{\sum_{i=1}^{n} (x_{i} - \bar{x})^{2}}{n-1} = \frac{\sum_{i=1}^{10} (x_{i} - 4.93)^{2}}{10-1} = 0.07567$$

Sample standard deviation:

$$s = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{\sum_{i=1}^{10} (x_i - 4.93)^2}{10-1}} = \sqrt{0.07567} = 0.275076$$

t-statistic:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{4.93 - 5}{0.275076/\sqrt{10}} = -0.80472$$

degrees of freedom:

$$d.o.f = n - 1 = 10 - 1 = 9$$

The critical value for t for a two-tailed test at 5% level of significane with 10 - 1 = 9 degrees of freedom is 2.262

Standard Error:

$$S.E = \frac{s}{\sqrt{n}} = \frac{0.275076}{\sqrt{10}} = 0.08699$$

**Conclusion:**  $|t| < t_{0.05}$ , we fail to reject the Null hypothesis. That is the sample data are consistent with the assumption of mean 5 kg in the population.

# Program:

```
#!/usr/bin/env python3
import numpy as np
from scipy.stats import t, ttest_1samp
import matplotlib.pyplot as plt
plt.style.use('seaborn-darkgrid')
print("_____T-test (One Sample)_____")
p_mean = float(input("\nPopulation mean: "))
n = int(input("Sample length: "))
sample = [float(value) for value in input("Sample values: ").split()]
s_mean = np.mean(sample); s_stdv = np.std(sample, ddof=1)
# degrees of freedom, level of significance, confidence level
dof = n - 1; los = 0.05; cnl = 1 - los
# calculation of T-statistics and p-value
tstatistics, pvalue = ttest_1samp(sample, p_mean)
print("\nT statistics: {:.5f}".format(tstatistics))
# calculation of Critical values
tcritical_l = t.ppf(q = los/2, df = dof)
tcritical_u = -tcritical_l
print("\nCritical values are {:.5f}, {:.5f}".format(tcritical_l, tcritical_u))
# decision making - using T-statistics and Critical values
if tstatistics < tcritical_l or tstatistics > tcritical_u:
   print("Reject the Null hypothesis.")
else: print("Fail to reject the Null hypothesis.")
print("\np-value: {:.5f}".format(pvalue))
# decision making - using p-value
if pvalue < los: print("Reject the Null hypothesis.")</pre>
else: print("Fail to reject the Null hypothesis.")
# standard error
std_err = s_stdv/np.sqrt(n)
print("\nStandard Error: {:.5f}".format(std_err))
# confidence interval
cnf_int = s_mean + std_err * np.array([tcritical_l, tcritical_u])
print("Confidence Interval: {}".format(cnf_int))
# plot script
x1=np.linspace(-10,tcritical_l,1000); y1=t.pdf(x1,df=dof)
x2=np.linspace(tcritical_u,10,1000); y2=t.pdf(x2,df=dof)
x3=np.linspace(-4,4,1000); y3=t.pdf(x3,df=dof)
ax=plt.figure().add_subplot(111); ax.plot(x3,y3,color='brown')
ax.fill_between(x1,y1,0,alpha=0.5,color='brown',label='Rejection Region')
ax.fill_between(x2,y2,0,alpha=0.5,color='brown'); ax.set(xlabel='X',ylabel='P(X)')
ax.axvline(x=tstatistics,ls='--',c='b',label='T statistics = {:.5f}'.format(tstatistics))
ax.set(xlim=[-4,4],title="T Distribution (degrees of freedom = {:.0f})".format(dof))
plt.legend(); plt.savefig('tscript2.pdf',dpi=72,bbox_inches='tight'); plt.show()
```

# Output:

\_\_\_\_\_T-test (One Sample)\_\_\_\_\_

Population mean: 5 Sample length: 10

Sample values: 4.7 4.9 5.0 5.1 5.4 5.2 4.6 5.1 4.6 4.7

T statistics: -0.80472

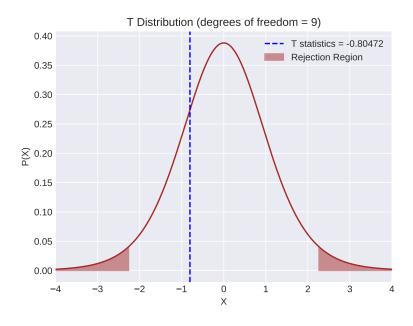
Critical values are -2.26216, 2.26216 Fail to reject the Null hypothesis.

p-value: 0.44172

Fail to reject the Null hypothesis.

Standard Error: 0.08699

Confidence Interval: [4.73322266 5.12677734]



3. Two sets of ten students selected at random from a college were taken. One set was given memory test as they were and the other was given the memory test after two weeks of training and the scores are given below.

Set A: 10 8 7 9 8 10 9 6 7 8 Set B: 12 8 8 10 8 11 9 8 9 9

Do you think there is a significant effect due to training?

## **Solution:**

**Null hypothesis:**  $H_0: \mu_1 = \mu_2$ , No significant effect due to training **Alternative hypothesis:**  $H_1: \mu_1 \neq \mu_2$ , Significant effect due to training

### Set A:

Mean:

$$\bar{x}_1 = \frac{\sum_{i=1}^{n_1} x_{1i}}{n_1} = \frac{10 + 8 + 7 + 9 + 8 + 10 + 9 + 6 + 7 + 8}{10} = 8.2$$

Variance:

$$s_1^2 = \frac{\sum_{i=1}^{n_1} (x_{1i} - \bar{x}_1)^2}{n_1 - 1} = \frac{\sum_{i=1}^{n_2} (x_{1i} - 8.2)^2}{10 - 1} = 1.73333$$

Standard Deviation:

$$s_1 = \sqrt{\frac{\sum_{i=1}^{n_1} (x_{1i} - \bar{x_1})^2}{n_1 - 1}} = \sqrt{\frac{\sum_{i=1}^{10} (x_{1i} - 8.2)^2}{10 - 1}} = \sqrt{1.73333} = 1.31656$$

Set B:

Mean:

$$\bar{x}_2 = \frac{\sum_{i=1}^{n_2} x_{2i}}{n_2} = \frac{12 + 8 + 8 + 10 + 8 + 11 + 9 + 8 + 9 + 9}{10} = 9.2$$

Variance:

$$s_2^2 = \frac{\sum_{i=1}^{n^2} (x_{2i} - \bar{x_2})^2}{n^2 - 1} = \frac{\sum_{i=1}^{10} (x_{2i} - 9.2)^2}{10 - 1} = 1.95556$$

Standard Deviation:

$$s_2 = \sqrt{\frac{\sum_{i=1}^{n^2} (x_{2i} - \bar{x}_2)^2}{n^2 - 1}} = \sqrt{\frac{\sum_{i=1}^{10} (x_{2i} - 9.2)^2}{10 - 1}} = \sqrt{1.95556} = 1.39841$$

Calculation of s1/s2:

$$\frac{s_1}{s_2} = \frac{1.31656}{1.39841} = 0.94147$$

Test statistic:

$$t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{s_1^2/n1 + s_2^2/n2}}$$

where n1 and n2 are the sample sizes,  $\bar{x}_1$  and  $\bar{x}_2$  are the sample means, and  $s_1^2$  and  $s_2^2$  are the sample variances. If equal variances are assumed (0.5 < s1/s2 < 2), then the formula reduces to:

$$t = \frac{\bar{x}_1 - \bar{x}_2}{s_p \sqrt{1/n1 + 1/n2}}$$

where

$$s_p^2 = \frac{(n1-1)s_1^2 + (n2-1)s_2^2}{n1 + n2 - 2}$$

Calculation of  $s_p$ :

$$s_p = \sqrt{\frac{(10-1) \times 1.31656^2 + (10-1) \times 1.39841^2}{10+10-2}} = 1.35810$$

t-statistic:

$$t = \frac{8.2 - 9.2}{1.35810 \times \sqrt{1/10 + 1/10}} = -1.64646$$

degrees of freedom:

$$d.o. f = n_1 + n_2 - 2 = 10 + 10 - 2 = 18$$

The critical value for t (from t-distribution table) with degrees of freedom = 18 and  $\alpha = 0.05$  is 2.101

Standard Error:

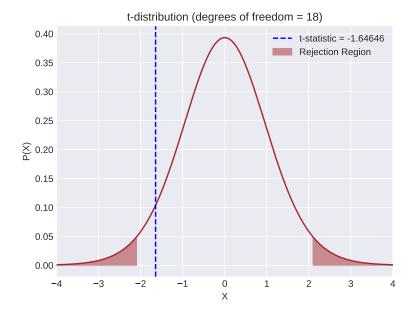
$$S.E = sp\sqrt{1/n1 + 1/n2} = 1.35810 \times \sqrt{1/10 + 1/10} = 0.60736$$

**Conclusion:**  $|t| < t_{0.05}$ , we fail to reject the Null hypothesis. That is there is no significant effect in the scores of the memeory test due to training.

#### Program:

```
#!/usr/bin/env python3
import numpy as np
from scipy.stats import t
import matplotlib.pyplot as plt
plt.style.use('seaborn-darkgrid')
def similar_variance(n1, s1_mean, n2, s2_mean):
    dof = n1+n2-2
    sp = np.sqrt(((n1-1)*s1_stdv**2+(n2-1)*s2_stdv**2)/(dof))
    return (s1_mean-s2_mean)/(sp * np.sqrt(1/n1 + 1/n2)), dof, sp
def non_similar_variance(n1,s1_mean,n2,s2_mean):
    sd = np.sqrt(s1_stdv**2/n1 + s2_stdv**2/n2)
    dof = (sd**4)/(((s1_std**2/n1)**2/(n1-1)) + ((s2_std**2/n2)**2/(n2-1)))
    return (s1_mean-s2_mean)/sd, dof, sd
def ttest_and_variance(s1_stdv, s2_stdv):
    if 0.5 < s1_stdv/s2_stdv < 2:</pre>
        return similar_variance(n1, s1_mean, n2, s2_mean)
    else:
        return non_similar_variance(n1,s1_mean,n2,s2_mean)
               __Two-sample t-test for unpaired data__
sample1 = [float(value) for value in input("Sample_1 values: ").split()]
sample2 = [float(value) for value in input("Sample_2 values: ").split()]
# Number of Observations
n1 = len(sample1); n2 = len(sample2)
# Mean and Standard Deviation
s1_mean = np.mean(sample1); s1_stdv = np.std(sample1, ddof=1)
s2_mean = np.mean(sample2); s2_stdv = np.std(sample2, ddof=1)
# level of significance, confidence level
los = 0.05; cnl = 1 - los
# standard error (SE) of mean of sample1
std_err1 = s1_stdv/np.sqrt(n1)
print("\nSample 1: \n\t Number of Observations = {} \n\t Mean = {:.5f}".format(n1,s1_mean))
print("\t Standard Deviation = {:.5f}".format(s1_stdv))
print("\t Standard Error of the Mean = {:.5f}".format(std_err1))
# standard error (SE) of mean of sample2
std_err2 = s2_stdv/np.sqrt(n2)
print("\nSample 2: \n\t Number of Observations = {} \n\t Mean = {:.5f}".format(n2,s2_mean))
print("\t Standard Deviation = {:.5f}".format(s2_stdv))
print("\t Standard Error of the Mean = {:.5f}".format(std_err2))
# calculation of t-statistic and degrees of freedom
tstatistic, dof, sp = ttest_and_variance(s1_stdv, s2_stdv)
print("\nt-statistic: {:.5f}".format(tstatistic))
# calculation of Critical values
tcritical_l = t.ppf(q = los/2, df = dof)
tcritical_u = -tcritical_l
print("\nCritical values are {:.5f}, {:.5f}".format(tcritical_l, tcritical_u))
```

```
# decision making: t-statistic and Critical values
if tstatistic < tcritical_l or tstatistic > tcritical_u:
   print("Reject the Null hypothesis.")
else: print("Fail to reject the Null hypothesis.")
# calculation of p-value
pvalue = 2*t.cdf(tstatistic, df = dof)
print("\np-value: {:.5f}".format(pvalue))
# decision making: p-value and level of significance
if pvalue < los: print("Reject the Null hypothesis.")</pre>
else: print("Fail to reject the Null hypothesis.")
# standard error
std_error = sp * np.sqrt(1/n1 + 1/n2)
print("\nStandard Error: {:.5f}".format(std_error))
# confidence interval
cnf_int = (s1_mean - s2_mean) + std_error * np.array([tcritical_1, tcritical_u])
print("Confidence Interval: {}".format(cnf_int))
x1=np.linspace(-10,tcritical_1,1000); y1=t.pdf(x1,df=dof)
x2=np.linspace(tcritical_u,10,1000); y2=t.pdf(x2,df=dof)
x3=np.linspace(-4,4,1000); y3=t.pdf(x3,df=dof)
ax=plt.figure().add_subplot(111); ax.plot(x3,y3,color='brown')
ax.fill_between(x1,y1,0,alpha=0.5,color='brown',label='Rejection Region')
ax.fill_between(x2,y2,0,alpha=0.5,color='brown'); ax.set(xlabel='X',ylabel='P(X)')
ax.axvline(x=tstatistic, ls='--', c='b', label='t-statistic = {:.5f}'.format(tstatistic))
ax.set(xlim=[-4,4],title="t-distribution (degrees of freedom = {:.0f})".format(dof))
plt.legend(); plt.savefig('tscript3.pdf',dpi=72,bbox_inches='tight'); plt.show()
Output:
         __Two-sample t-test for unpaired data__
Sample_1 values: 10 8 7 9 8 10 9 6 7 8
Sample_2 values: 12 8 8 10 8 11 9 8 9 9
Sample 1:
    Number of Observations = 10
     Mean = 8.20000
     Standard Deviation = 1.31656
     Standard Error of the Mean = 0.41633
Sample 2:
     Number of Observations = 10
     Mean = 9.20000
     Standard Deviation = 1.39841
     Standard Error of the Mean = 0.44222
t-statistic: -1.64646
Critical values are -2.10092, 2.10092
Fail to reject the Null hypothesis.
p-value: 0.11702
Fail to reject the Null hypothesis.
Standard Error: 0.60736
Confidence Interval: [-2.27602071 0.27602071]
```



# Program: t-test with in-built scipy.stats.ttest

```
#!/usr/bin/env python3
import numpy as np
from scipy.stats import t, ttest_ind
import matplotlib.pyplot as plt
plt.style.use('seaborn-darkgrid')
                __Two-sample t-test for unpaired data___
print("
sample1 = [float(value) for value in input("Sample_1 values: ").split()]
sample2 = [float(value) for value in input("Sample_2 values: ").split()]
# Number of Observations
n1 = len(sample1); n2 = len(sample2)
# Mean and Standard Deviation
s1_mean = np.mean(sample1); s1_stdv = np.std(sample1, ddof=1)
s2_mean = np.mean(sample2); s2_stdv = np.std(sample2, ddof=1)
# calculation of degrees of freedom and pooled variance
if 0.5 < s1_stdv/s2_stdv < 2:</pre>
    dof = n1+n2-2
    sp = np.sqrt(((n1-1)*s1_stdv**2+(n2-1)*s2_stdv**2)/(dof))
else:
    sp = np.sqrt(s1_stdv**2/n1 + s2_stdv**2/n2)
    dof = (sp**4)/(((s1\_std**2/n1)**2/(n1-1)) + ((s2\_std**2/n2)**2/(n2-1)))
# level of significance, confidence level
los = 0.05; cnl = 1 - los
# standard error (SE) of mean of sample1
std_err1 = s1_stdv/np.sqrt(n1)
print("\nSample 1: \n\t Number of Observations = {} \n\t Mean = {:.5f}".format(n1,s1_mean))
print("\t Standard Deviation = {:.5f}".format(s1_stdv))
print("\t Standard Error of the Mean = {:.5f}".format(std_err1))
# standard error (SE) of mean of sample2
std_err2 = s2_stdv/np.sqrt(n2)
print("\nSample 2: \n\t Number of Observations = {} \n\t Mean = {:.5f}".format(n2,s2_mean))
print("\t Standard Deviation = {:.5f}".format(s2_stdv))
```

```
print("\t Standard Error of the Mean = {:.5f}".format(std_err2))
# calculation of t-statistic and p-value
tstatistic, pvalue = ttest_ind(sample1, sample2)
print("\nt-statistic: {:.5f}".format(tstatistic))
# calculation of Critical values
tcritical_l = t.ppf(q = los/2, df = dof)
tcritical_u = -tcritical_l
print("\nCritical values are {:.5f}, {:.5f}".format(tcritical_l, tcritical_u))
# decision making: t-statistic and Critical values
if tstatistic < tcritical_l or tstatistic > tcritical_u:
    print("Reject the Null hypothesis.")
else: print("Fail to reject the Null hypothesis.")
print("\np-value: {:.5f}".format(pvalue))
# decision making: p-value and level of significance
if pvalue < los: print("Reject the Null hypothesis.")</pre>
else: print("Fail to reject the Null hypothesis.")
# standard error
std_error = sp * np.sqrt(1/n1 + 1/n2)
print("\nStandard Error: {:.5f}".format(std_error))
# confidence interval
cnf_int = (s1_mean - s2_mean) + std_error * np.array([tcritical_l, tcritical_u])
print("Confidence Interval: {}".format(cnf_int))
x1=np.linspace(-10,tcritical_1,1000); y1=t.pdf(x1,df=dof)
x2=np.linspace(tcritical_u,10,1000); y2=t.pdf(x2,df=dof)
x3=np.linspace(-4,4,1000); y3=t.pdf(x3,df=dof)
ax=plt.figure().add_subplot(111); ax.plot(x3,y3,color='brown')
ax.fill_between(x1,y1,0,alpha=0.5,color='brown',label='Rejection Region')
ax.fill_between(x2,y2,0,alpha=0.5,color='brown'); ax.set(xlabel='X',ylabel='P(X)')
ax.axvline(x=tstatistic,ls='--',c='b',label='t-statistic = {:.5f}'.format(tstatistic))
ax.set(xlim=[-4,4],title="t-distribution (degrees of freedom = {:.0f})".format(dof))
plt.legend(); plt.savefig('ttest2.pdf',dpi=72,bbox_inches='tight'); plt.show()
```

### Output:

```
__Two-sample t-test for unpaired data__
Sample_1 values: 10 8 7 9 8 10 9 6 7 8
Sample_2 values: 12 8 8 10 8 11 9 8 9 9
Sample 1:
    Number of Observations = 10
    Mean = 8.20000
     Standard Deviation = 1.31656
    Standard Error of the Mean = 0.41633
Sample 2:
    Number of Observations = 10
    Mean = 9.20000
     Standard Deviation = 1.39841
     Standard Error of the Mean = 0.44222
t-statistic: -1.64646
Critical values are -2.10092, 2.10092
Fail to reject the Null hypothesis.
```

p-value: 0.11702

Fail to reject the Null hypothesis.

Standard Error: 0.60736

Confidence Interval: [-2.27602071 0.27602071]

