

Parte II. Como Metas

$$\Theta = C_3 e^{mz} + C_4 e^{-mz}$$

$$\Theta = T(z) - T_{\infty}$$

$$T(z) = T_{\infty} + C_3 e^{mz} + C_4 e^{-mz}$$

$$m = \sqrt{\frac{h_0}{K A_c}}$$

$$m = \sqrt{\frac{4 h \cdot L}{K D}}$$

$$\rho = \pi D L$$

$$A_c = \frac{\pi D^2}{4}$$

$$\frac{dT^I}{dz} = m C_3 e^{mz} + m C_4 e^{-mz}$$

B.C. 1

$$z = -L/2$$

$$-K A_s \frac{dT^I}{dz} = h A_s (T_{\infty} - T^I(-L/2))$$

esto se cambia por el 4º

B.C. 2

$$z = 0$$

$$T^I = T^{II}$$

B.C. 3

$$z = 0$$

$$-K \frac{dT^I}{dz} = -K \frac{dT^{II}}{dz} \Rightarrow \frac{dT^I}{dz} = \frac{dT^{II}}{dz}$$

B.C. 4

$$z = L/2$$

$$-K \frac{dT^{II}}{dz} = h (T^{II}(L/2) - T_{\infty})$$

$$-K A_1 \left(C_1 - \frac{e_{gen} z}{K} \right) = h A_1 (T_{\infty} - T^I(-L/2))$$

$$A \cdot C = b$$

$$C = A^{-1} \cdot b$$

$$\begin{aligned} -K C_1 + \frac{e_{gen}(-L)}{K} &= h T_{\infty} - h \left(-\frac{e_{gen}(-L/2)^2}{2K} + C_1(-L/2) + C_2 \right) \\ -K C_1 + \frac{e_{gen}(-L)}{K} &= h T_{\infty} - h \left(-\frac{e_{gen}(-L/2)^2}{2K} + C_1(-L/2) + C_2 \right) \\ -K C_1 + \frac{e_{gen}(-L)}{K} &= h T_{\infty} - h \left(-\frac{e_{gen}(-L/2)^2}{2K} + C_1(-L/2) + C_2 \right) \end{aligned} \quad \Rightarrow \quad h T_{\infty} + \frac{h e_{gen}(-L/2)^2}{2K} - e_{gen}(-L/2)$$

$$-\frac{e_{gen} z^2}{2K} + C_1 z + C_2 = T_{\infty} + C_3 e^{mz} + C_4 e^{-mz}$$

$$z=0 \Rightarrow$$

$$0 + 0 + C_2 = T_{\infty} + C_3 + C_4$$

$$C_2 - C_3 - C_4 = T_{\infty} \quad \} \quad (2)$$

$$* \quad \left(C_1 - \frac{e_{gen} z}{K} \right) = m C_3 e^{mz} - m C_4 e^{-mz}$$

$$C_1 - m C_3 + m C_4 = 0 \quad \} \quad (3)$$

$$* \quad -K(m C_3 e^{mz} + m C_4 e^{-mz}) = h(T^I(L/2) - T_{\infty})$$

$$-K(m C_3 e^{mz} + m C_4 e^{-mz}) = h(T^I(L/2) - T_{\infty}) \quad \} \quad (4)$$

$$-K m C_3 e^{mz} - K m C_4 e^{-mz} = h(T_{\infty} + C_3 e^{mz} + C_4 e^{-mz} - T_{\infty})$$

$$-K m C_3 e^{mz} - h C_3 e^{mz} - K m C_4 e^{-mz} - h C_4 e^{-mz}$$

$$C_3(-K m e^{mz} - h e^{mz}) - C_4(K m e^{-mz} + h e^{-mz}) = 0$$