# Air Quality and Comfort Constrained Energy Efficient Operation of Multi-Unit Buildings Syed A.R. Naqvi, Koushik Kar, James Onyejizu

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#### Overview

Maintaining optimum indoor air quality (IAQ) through effective ventilation is critical for the well-being and productivity of building occupants. Control strategies aimed at improving the efficiency of heating, ventilation and air conditioning (HVAC) systems must jointly operate ventilation as well as heating and cooling processes. To this end, we propose a framework for minimizing energy consumption of the HVAC system in a multi-unit building, while meeting thermal comfort and IAQ requirements.

#### Introduction

- Air quality impacts wellness and occupants' productivity.
- Research in the area of building HVAC control has mostly focused on ensuring the occupants' thermal comfort.

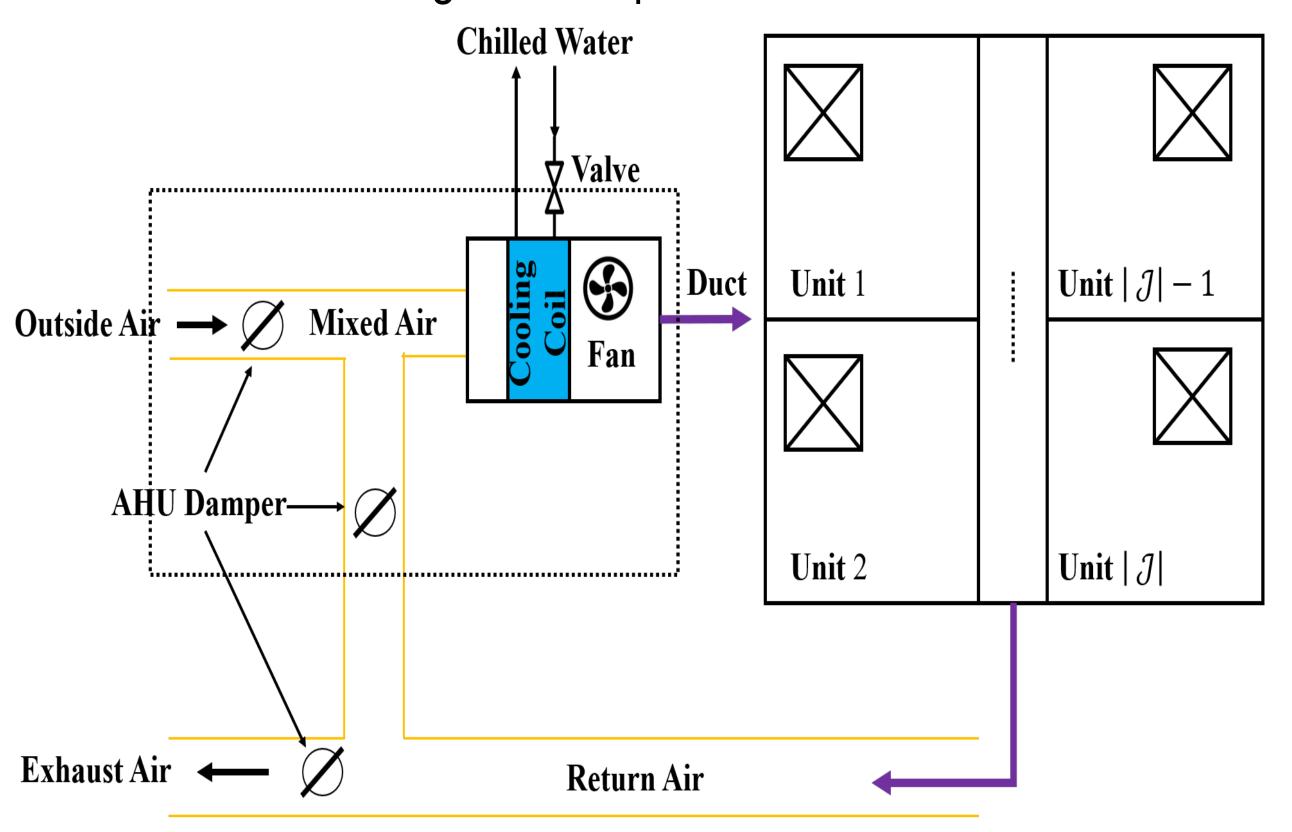


Fig 1: Overall HVAC system (Air handling unit, Cooling/heating coil, VAV boxes, Fan ) in our multi-unit building model

A need to develop a holistic approach for concurrently managing IAQ and indoor temperatures optimally.

# Optimization Framework/Method

Objective function

$$\min \int P(t) dt = \frac{C_p}{\eta COP} \int \dot{m}_j(t) [U] dt \begin{cases} V_j : \text{ volume of zone } j, \\ \rho \text{ is the density of air } R_j^o : \text{ thermal resistance of } I, \\ U = \beta(t) T_j(t) + (1 - \beta(t)) T_\infty(t) - T_s \end{cases}$$

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Constraints

$$0 \le \dot{m}_j(t) \le \overline{m} \ \forall j, \qquad 0 \le \beta(t) \le 1,$$
  
 $O_j(t) \le O_j^{max} \ \forall j, \qquad \left| T_j(t) - \Delta_j \right| \le \delta_j \ \forall_j$ 

Evolution of CO<sub>2</sub> concentration

$$V_{j} \frac{dO_{j}(t)}{dt} = \frac{\dot{m}_{j}(t)}{\rho} (O_{mix}(t) - O_{j}(t)) + Z_{j}(t) \sigma$$

$$O_{mix}(t) = [1 - \beta(t)] O_{out}(t) + N(t)$$

$$N(t) = \beta(t) \frac{\sum_{j \in J} O_{j}(t) \dot{m}_{j}(t)}{\sum_{j \in J} \dot{m}_{j}(t)}]$$

Zonal temperature dynamics

$$C_{j} \frac{dT_{j}(t)}{dt} = \frac{T_{\infty} - T_{j}(t)}{R_{j}^{\circ}} + c_{p} \dot{m}_{j}(t) (T_{S} - T_{j}(t))$$

 $C_i$ : thermal capacitance of zone j,

 $R_i^o$ : thermal resistance of zone j with ambient

 $O_i(t)$ : zonal  $CO_2$  concentration

 $T_S$ : supply air temperature (constant)

 $T_i(t)$ : temperature of zone j at time t

 $O_{mix}(t):CO_2$  concentration in the mixed air

 $\sigma$ : per-person  $CO_2$  contribution

 $Z_i(t)$ : occupancy in zone j at time t

 $T_{\infty}(t)$ : ambient temperature,

 $\dot{m}_i(t)$ : mass flow rate of air to zone j at time

P(t): energy consumed by the cooling coil

 $\eta$ : efficiency of the cooling coil

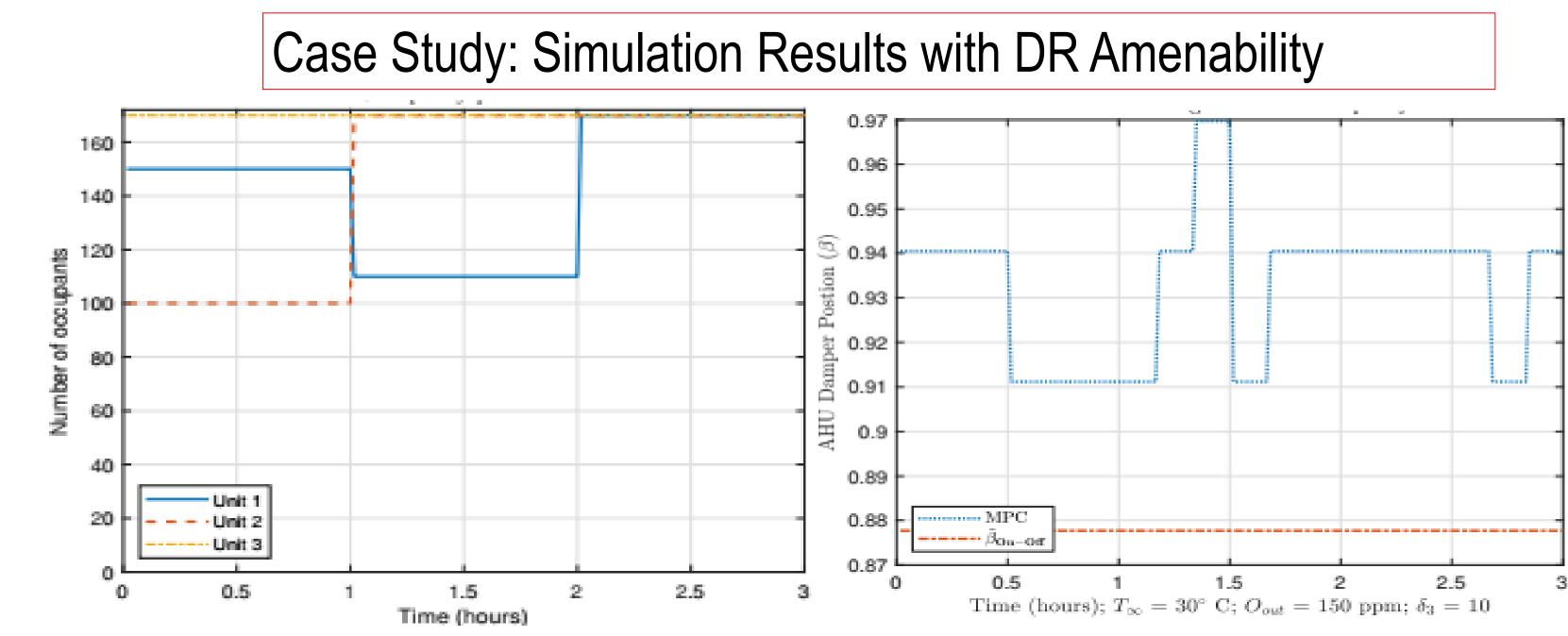
 $C_{v}$ : specific heat capacity of air

COP: coefficient of performance of the chiller •

 $\beta(t) = 1$ : the AHU damper is OFF

 $\beta(t) = 0$ : the AHU damper is ON

## Summary of Results



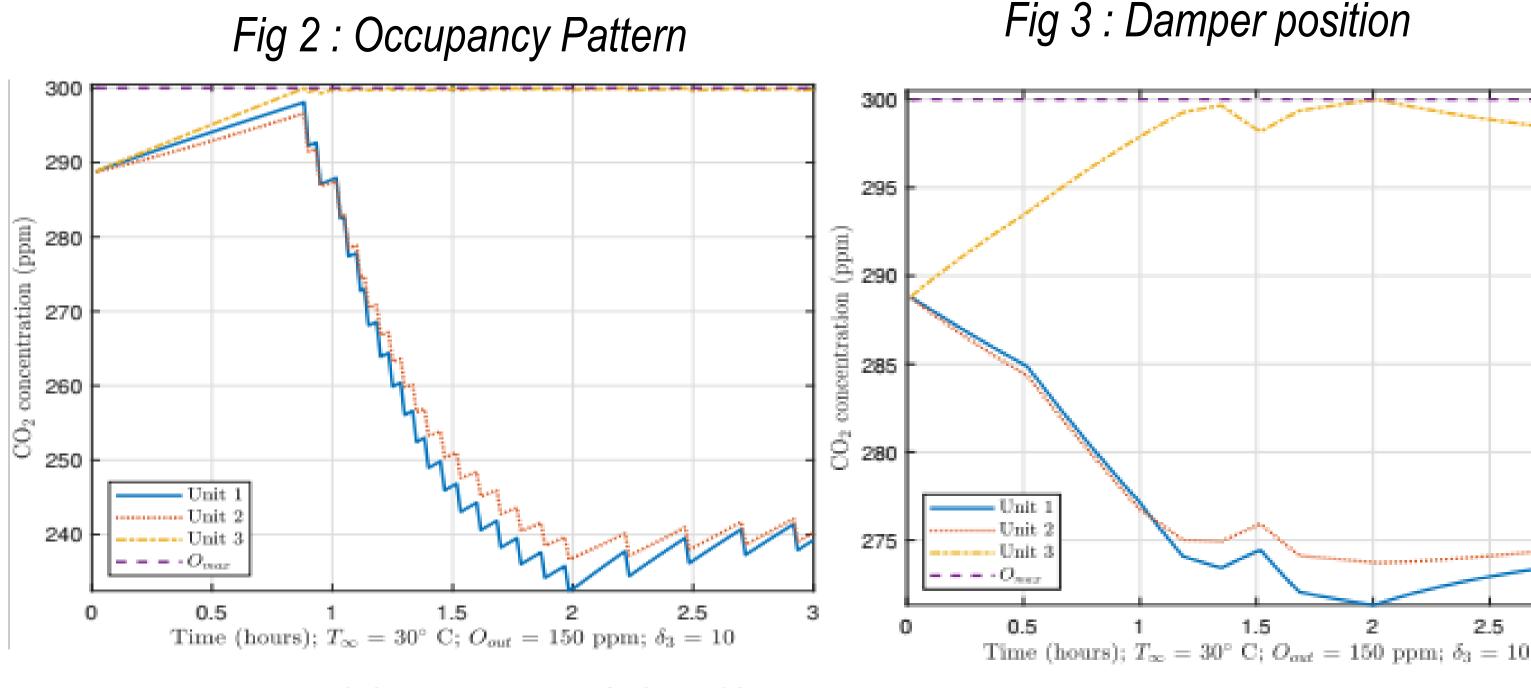


Fig 4 : CO<sub>2</sub> dynamics (JOTAC)

Fig 5 : CO<sub>2</sub> dynamics (MPC)

Table 1: Energy savings difference between JOTAC and MPC

Scenerio	Energy (MJ)		% Energy Savings
	JOTAC	MPC	
A	9.091	9.322	2.48
A'	6.646	7.094	6.32
В	9.267	9.506	2.51
B'	7.156	7.837	8.69
С	9.091	9.265	1.88
C'	6.530	6.876	5.03

Our proposed control strategy (JOTAC) could potentially result in energy savings of nearly 8.69% when compared to the MPC-based approach.

#### Future Work

- Formal Proof of near-optimality of the dynamic versions
- Validation using real building data sets
- ML/RL driven approach-based on the bilinear structure to develop PIML models

# Acknowledgements

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occupancy patterns: with DR-amenability without DR-amenability  $O_{\infty}$  = 150 ppm

Outdoor temperature,  $T_{\infty}$  = 30°c Outdoor air  $CO_2$  Concentration,

Simulation Setup

Zonal temperature setpoint =  $20^{\circ}c$ Target indoor  $CO_2$  concentration,  $O_{\infty}$  = 300 ppm

### Benefits

- Provides optimum indoor air quality for occupants' wellness and productivity
- Maintains thermal comfort conditions within acceptable limits
- \* Reduces power consumption of variable air volume HVAC systems which can subsequently lead to a reduction in energy prices







