

# Unsupervised Clustering Algorithms Comparison for On-line Sensor Clustering

*Steven Lowette & Kristof Van Laerhoven*

## Characteristics overview

Algorithm	Implemented	Online	Learning Kind	Number of Clusters	Visualisation	Network Topology	Speed	Performance on Clustered Data	Performance on Spread Data	Remarks
<a href="#">Self Organising Map</a>	Yes	Yes	Soft competitive	Variable	All dim.	Fixed	++	++	--	
<a href="#">Recurrent Self Organising Map</a>	Yes	Yes	Soft Competitive	Variable	All dim.	Fixed	+	++	-	The same as the SOM, but with a 'memory' for Temporal Sequence Processing
<a href="#">K-Means Clustering</a>	Yes	Yes	Hard competitive	Fixed	2 dim. only	Variable	+	-	+	Learning rule 1/n gives mean over all input in cluster so far
<a href="#">Sequential Leader Clustering</a>	No	Yes	Hard competitive	Variable	2 dim. only	Variable	+	+/-	+/-	Low accuracy and flexibility, because the clusters are static
<a href="#">Growing K-Means Clustering</a>	Yes	Yes	Hard competitive	Variable	2 dim. only	Variable	+	+	+/-	Because of the movement of the clusters, old inputs can get out of it's cluster's radius
<a href="#">Growing K-means Clustering with Maximum Cluster Size (using FIFO)</a>	Yes	No	Hard competitive	Variable	2 dim. only	Variable	--	+	+/-	The gain of flexibility on the input data is overshadowed by the loss of on-line processing
<a href="#">Neural Gas</a>	Yes	Yes	Soft competitive	Fixed	2 dim. only	Variable	+	+/-	+	
<a href="#">Neural Gas with Competitive Hebbian Learning</a>	Yes	Yes	Soft competitive	Fixed	2 dim. only	Variable	+	+/-	+	The addition of the edges between the neurones has no influence on the learning
<a href="#">Growing Neural Gas</a>	Yes	Yes	Soft competitive	Variable	2 dim. only	Variable	++	-	+	

## Algorithm overview

### Self Organizing Map (SOM)

#### Parameters

- Number of X-Neurons: Horizontal number of neurons.
- Number of Y-Neurons: Vertical number of neurons.
- [Metric Function](#): Function used to calculate the distance between the input vector and the neurons.
- [Neighbor Metric Function](#): Function used to calculate the distance between the neighboring neurons.

- Neighbor Radius: Value of the excitation radius around the winning neuron.
- [Update Function](#): Function used to calculate the learning rate  $\text{Eta}$ , depending on the number of times a neuron was triggered.
- Initial Learning Rate: Starting value of the learning rate  $\text{Eta}$ .
- Torus: Whether or not the 2-dimensional network should be treated as a torus.

**Description of the Algorithm**

1. Read new input
1. Find winning neuron:
  - select distance function to be used
  - find neuron with minimal distance to input
1. Update neurons. For each neuron and component i:
  - select the neighbor distance function
  - calculate the neighbor value: NbrVal (centered around winning neuron)
  - select the update function for the learning rate
  - calculate the learning rate: Eta
  - update:  $\text{NewNeur}(i) = \text{OldNeur}(i) + \text{NbrVal} * \text{Eta} * (\text{Input}(i) - \text{OldNeur}(i))$

**Recurrent Self Organising Map (RSOM)****Parameters**

- Number of X-Neurons: Horizontal number of neurons.
- Number of Y-Neurons: Vertical number of neurons.
- [Metric Function](#): Function used to calculate the distance between the inputvector and the neurons.
- [Neighbor Metric Function](#): Function used to calculate the distance between the neighboring neurons.
- Neighbor Radius: Value of the excitation radius around the winning neuron.
- [Update Function](#): Function used to calculate the learning rate  $\text{Eta}$ , depending on the number of times a neuron was triggered.
- Initial Learning Rate: Starting value of the learning rate  $\text{Eta}$ .
- Alfa: Memory Value indicating the amount of memory of previous steps. If Alfa=1, then the RSOM is equivalent to the SOM.
- Torus: Whether or not the 2-dimensional network should be treated as a torus.

**Description of the Algorithm**

1. Read new input
2. Update the difference vectors. For each neuron and component i:
  - $\text{NewDiff}(i) = (1 - \text{Alfa}) * \text{OldDiff}(i) + \text{Alfa} * (\text{Input}(i) - \text{OldNeur}(i))$
1. Find winning neuron:
  - select distance function to be used
  - find difference vector with minimal distance to the origin
  - the winning neuron is the neuron which corresponds to this winning difference vector
1. Update neurons. For each neuron and component i:
  - select the neighbor distance function
  - calculate the neighbor value: NbrVal (centered around winning neuron)
  - select the update function for the learning rate
  - calculate the learning rate: Eta
  - update:  $\text{NewNeur}(i) = \text{OldNeur}(i) + \text{NbrVal} * \text{Eta} * \text{NewDiff}(i)$

**K-Means Clustering (KMC)****Parameters**

- Number of Clusters.
- [Metric Function](#): Function used to calculate the distance between the inputvector and the clusters.
- [Adaptation Rule](#): Function used to calculate the adaptation value  $\text{Eta}$

, depending on the number of inputs in the cluster.

**Description of the Algorithm**

1. Read New Input
2. Find the winning cluster:
  - select distance function to be used
  - find cluster with minimal distance to input
1. Update:
  - select adaptation rule
  - calculate adaptation rate:  $\text{Eta}$
  - update each component  $i$  of the winning cluster:  $\text{NewClus}(i) = \text{OldClus}(i) + \text{Eta} * (\text{Input}(i) - \text{OldClus}(i))$

**Sequential Leader Clustering (SLC)****Parameters**

- [Metric Function](#): Function used to calculate the distance between the inputvector and the clusters.
- Threshold: Radius around a cluster's center, in which inputs must fall

**Description of the Algorithm**

1. Read New Input
2. Find the winning cluster
  - select distance function to be used
  - find cluster with minimal distance to input
1. If distance to winning cluster is under threshold then
  - input belongs to winning cluster
- Else
  - create new cluster = input
  - input belongs to new cluster

**Growing K-Means Clustering (GKMC)****Parameters**

- [Metric Function](#): Function used to calculate the distance between the inputvector and the clusters.
- [Adaptation Rule](#): Function used to calculate the adaptation value  $\text{Eta}$ , depending on the number of inputs in the cluster.
- Threshold: Radius around a cluster's center, in which inputs must fall

**Description of the Algorithm**

1. Read New Input
2. Find the winning cluster:
  - select distance function to be used
  - find cluster with minimal distance to input
1. If distance to winning cluster is under threshold then update:
  - select adaptation rule
  - calculate adaptation rate:  $\text{Eta}$
  - update winning cluster:  $\text{NewClus}(i) = \text{OldClus}(i) + \text{Eta} * (\text{Input}(i) - \text{OldClus}(i))$
- Else
  - create new cluster = input

**Growing K-means Clustering Algorithm with Maximum Cluster Size, using FIFO (GKMC\_FIFO)****Parameters**

- [Metric Function](#): Function used to calculate the distance between the inputvector and the clusters.
- Maximum Cluster Size: Maximal number of inputs in one cluster
- Threshold: Radius around a cluster's center, in which inputs must fall

**Description of the Algorithm**

1. Read New Input
2. Find the winning cluster:
  - select distance function to be used
  - find cluster with minimal distance to input
1. If distance to winning cluster is under threshold then update:
  - make input a 'member' of the winning cluster
  - update winning cluster:  $\text{WinClus} = \text{Mean}(\text{Last } N \times \text{Last Input in this Cluster})$
- Else
  - create new cluster
  - make input 'member' of new cluster

**Neural Gas Algorithm (NGA)****Parameters**

- Number of Neurons.
- [Metric Function](#): Function used to calculate the distance between the input vector and the clusters.
- Maximum Position: see Final Epsilon and Final Lambda.
- Initial Epsilon: Global learning rate at position 0.
- Final Epsilon: Global learning rate at the Maximum Position.
- Initial Lambda: Sequence learning rate at position 0 (see also Description of the Algorithm).
- Final Lambda: Sequence learning rate at the Maximum Position (see also Description of the Algorithm).

**Description of the Algorithm**

1. Read New Input
2. Calculate all the distances of the (fixed number of) clusters to the input
3. Make a list of the increasing distances and their corresponding clusternumber:  $\text{Sequence}()$
4. Update the clusters. For each cluster  $w$  and each component  $i$ :
  - calculate current learning rate:  $\text{EpsCur} = \text{Epsi} * (\text{Epsf}/\text{Epsi})^{(\text{Pos}/\text{MaxPos})}$
  - calculate current distance function:
 
$$\text{DistCur} = \text{Exp}(-\text{Sequence}(w) / (\text{Lmbi} * (\text{Lmbf}/\text{Lmbi})^{(\text{Pos}/\text{MaxPos})}))$$
  - update:  $\text{NewClus} = \text{OldClus} + \text{EpsCur} * \text{DistCur} * (\text{Input}(i) - \text{OldClus}(i))$

**Neural Gas Algorithm with Competitive Hebbian Learning (NGA\_CHL)****Parameters**

- Number of Neurons.
- [Metric Function](#): Function used to calculate the distance between the input vector and the clusters.
- Maximum Position: see Final Epsilon and Final Lambda.
- Initial Epsilon: Global learning rate at position 0.
- Final Epsilon: Global learning rate at the Maximum Position.
- Initial Lambda: Sequence learning rate at position 0 (see also Description of the Algorithm).
- Final Lambda: Sequence learning rate at the Maximum Position (see also Description of the Algorithm).
- Initial Maximum Edge Age: Maximal age for a non-refreshed edge at position 0.
- Final Maximum Edge Age: Maximal age for a non-refreshed edge at the Maximum Position.

**Description of the Algorithm**

1. Read New Input
2. Calculate distances
  - select distance function to be used
  - calculate all the distances of the (fixed number of) clusters to the input
1. Make an increasing list of the distances to the input and their corresponding clusternumber:  $\text{Sequence}()$
2. Update the clusters. For each cluster  $w$  and each component  $i$ :
  - calculate current learning rate:  $\text{EpsCur} = \text{Epsi} * (\text{Epsf}/\text{Epsi})^{(\text{Pos}/\text{MaxPos})}$
  - calculate current distance function:

```

    DistCur = Exp(-Sequence(w) / (Lmbi*(Lmbf/Lmbi)^(Pos/MaxPos)))
    o update: NewClus = OldClus + EpsCur * DistCur * (Input(i)-OldClus(i))

```

#### 1. Maintain edges:

- o detect two clusters nearest to input: Winner and Winner2
- o 'refresh' the edge between Winner and Winner2: set age=0 or create
- o increment all edges' age
- o for every edge: if age exceeds MaxAge then remove edge

## Growing Neural Gas (GNG)

### Parameters

- [Metric Function](#): Function used to calculate the distance between the input vector and the clusters.
- Maximal Edge Age: Maximal age for a non-refreshed edge.
- New Cluster Threshold: Number of steps after which a new cluster is to be created.
- Winning Learning Rate: Learning Rate for the winner.
- Neighbor Learning Rate: Learning rate for the clusters directly connected to the winning cluster with edges.
- Alfa: Fraction by which the local errors of the winning and the second best clusters are decreased, when creating a new cluster.
- Beta: Fraction by which all the clusters' local errors are decreased each step.

### Description of the Algorithm

1. Read New Input
2. Calculate distances:

- o select distance function to be used
- o find two clusters nearest to input: Winner and Winner2

1. Add squared distance between input and Winner to winner's 'error'
2. 'Refresh' the edge between Winner and Winner2: set age=0 or create
3. Adapt Clusters:

- o Adapt Winner:  $Winner(i) = Winner(i) + EpsWin * (Input(i) - Winner(i))$
- o Adapt Clusters connected to winner through edge:

```

    Nbr(i) = Nbr(i) + EpsNbr * (Input(i) - Nbr(i))

```

#### 1. Maintain edges:

- o increment all edges' age
- o for every edge: if age exceeds MaxAge then remove edge

1. Delete Clusters who are not connected any more
2. If Number of steps is the integer multiple of chosen Lambda Then

- o find cluster with biggest 'error': Winner
- o find neighboring cluster with second-biggest 'error': Winner2
- o decrease 'errors' of Winner and Winner2 by factor Alfa
- o create new cluster and interpolate place and 'error' between Winner and Winner2
- o connect new cluster to Winner and Winner2
- o delete edge between Winner and Winner2

#### 1. Decrease 'errors' of all clusters by factor Beta

## Definitions

### Metrics

- City Block Metric:  $d(\vec{a}, \vec{b}) = \sum_{i=1}^n |a_i - b_i|$
- Euclidean Metric:  $d(\vec{a}, \vec{b}) = \sqrt{\sum_{i=1}^n (a_i - b_i)^2}$
- Maximum Metric:  $d(\vec{a}, \vec{b}) = \max_i |a_i - b_i|$

**Neighbor Functions**

- Triangular:  $NeighFactor(\vec{a}) = \begin{cases} d(\vec{a}, Winner) < NeighRadius : \frac{NeighRadius - d(\vec{a}, Winner)}{NeighRadius} \\ d(\vec{a}, Winner) > NeighRadius : 0 \end{cases}$
- Gaussian:  $NeighFactor(\vec{a}) = e^{-\left(\frac{d(\vec{a}, Winner)}{NeighRadius}\right)^2}$
- Excitation/Inhibition:  $NeighFactor(\vec{a}) = \left[1 - \left(\frac{d(\vec{a}, Winner)}{NeighRadius}\right)^2\right] e^{-\left(\frac{d(\vec{a}, Winner)}{NeighRadius}\right)^2}$

Remark: If  $NeighFactor < 0$

, the adaptation is slightly modified to avoid overflow, by keeping the vector components between 0 and 255, as it should be.

**Adaptation Rules**

- Constant Learning Rate:  $EtaFactor = Eta_i$ ,

where  $Eta_i$  is the Initial Learning Rate.

- Linear decreasing Learning Rate:  $EtaFactor = \frac{Eta_i}{NrElements}$ ,

where  $NrElements$  is the number of elements associated with the current cluster or the number of times the current cluster has been triggered.

- Square Root Learning Rule:  $EtaFactor = \frac{Eta_i}{\sqrt{NrElements}}$
- Exponential Learning Rule:  $EtaFactor = \frac{Eta_i}{e^{NrElements}}$