```
LinksPlatform's Platform Numbers Class Library
    ./csharp/Platform.Numbers/Arithmetic.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
6
        /// <summary>
       /// <para> Each function performs the simplest arithmetic operation on the type specified as
           a parameter </para>
        /// <para> Каждая функция выполняет простейшую арифметическую операцию над типом, указанным
        → в качестве параметра </para>
        /// </summary>
       public static class Arithmetic
11
12
13
            /// <summary>
            /// <para> Adding the x and y arguments </para>
15
            /// <para> Сложение аргументов х и у </para>
16
            /// </summary>
17
            /// <returns>
            /// <para> Sum of x and y </para>
19
            /// <para> Сумма х и у </para>
20
            /// </returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
22
            public static T Add\langle T \rangle (T x, T y) \Rightarrow Arithmetic \langle T \rangle . Add(x, y);
23
^{24}
            /// <summary>
25
            /// <para> Subtracting x from y </para>
26
            /// <para> Вычитание х из у </para>
            /// </summary>
28
            /// <returns>
29
            /// <para> Difference of x and y </para>
30
            /// <para> Разность х и у </para>
31
            /// </returns>
32
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            public static T Subtract<T>(T x, T y) => Arithmetic<T>.Subtract(x, y);
35
36
            /// <summary>
            /// <para> Multiplication the x and y </para>
37
            /// <para> Умножение х и у </para>
38
            /// </summary>
39
            /// <returns>
            /// <returns>
41
            /// <para> Product of x and y </para>
42
            /// <para> Произведение х и ў </para>
43
            /// </returns>
44
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            public static T Multiply<T>(T x, T y) => Arithmetic<T>.Multiply(x, y);
46
47
            /// <summary>
48
            /// <para> Dividing x by y </para>
49
            /// <para> Деление х на у </para>
50
            /// </summary>
51
            /// <returns>
            /// <para> Quoitent of x and y </para>
            /// <para> Частное х и у </para>
54
            /// </returns>
55
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Divide<T>(T x, T y) => Arithmetic<T>.Divide(x, y);
57
            /// <summary>
59
            /// <para> Increasing the parameter x by one </para>
60
            /// <para> Увеличение параметра х на единицу </para>
61
            /// </summary>
62
            /// <returns>
63
            /// <para> Increase by one x </para>
64
            /// <para> Увеличенное на единицу х </para>
            /// </returns>
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
67
            public static T Increment<T>(T x) => Arithmetic<T>.Increment(x);
68
69
70
            /// <para> Increase the parameter x passed by reference by one </para>
71
            /// <para> Увеличение переданного по ссылке параметра х на единицу </para>
72
            /// </summary>
73
            /// <returns>
```

```
/// <para> Increase by one x with returning the value to the original variable </para>
7.5
             /// <para> Увеличенное на единицу х с возвратом значения в исходную переменную </para>
             /// </returns>
77
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
            public static T Increment<T>(ref T x) => x = Arithmetic<T>.Increment(x);
80
             /// <summary>
81
             /// <para> Decrease parameter x by one </para>
82
             /// <para> Уменьшение параметра х на единицу </para>
83
             /// </summary>
84
             /// <returns>
85
             /// <para> Reduced by one x </para>
             /// <para> Уменьшенное на единицу х </para>
87
             /// </returns>
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Decrement<T>(T x) => Arithmetic<T>.Decrement(x);
90
             /// <summary>
92
             /// <para> Decreasing the parameter x passed by reference by one </para>
93
             /// <para> Уменьшение переданного по ссылке параметра х на единицу </para>
94
             /// </summary>
95
            /// <returns>
96
             /// <para> Reduced by one x with returning the value to the original variable </para>
97
             /// <para> Уменьшенное на единицу х с воз вратом значения в исходную переменную </para>
             /// </returns>
99
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
100
            public static T Decrement<T>(ref T x) => x = Arithmetic<T>.Decrement(x);
101
        }
102
103
     ./csharp/Platform.Numbers/ArithmeticExtensions.cs
   using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 3
    namespace Platform.Numbers
        public static class ArithmeticExtensions
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
 9
            public static T Decrement<T>(this ref T x) where T : struct => x =
10
             → Arithmetic<T>.Decrement(x);
11
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            public static T Increment<T>(this ref T x) where T : struct => x =
13
             → Arithmetic<T>.Increment(x);
        }
15
     ./csharp/Platform.Numbers/Arithmetic[T].cs
   using System;
    using System.Reflection.Emit;
 2
    using System.Runtime.CompilerServices;
    using Platform. Exceptions;
    using Platform.Reflection;
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform. Numbers
10
11
        public static class Arithmetic<T>
12
13
            public static readonly Func<T, T, T> Add = CompileAddDelegate();
            public static readonly Func<T, T, T> Subtract = CompileSubtractDelegate();
15
            public static readonly Func<T, T, T> Multiply = CompileMultiplyDelegate()
public static readonly Func<T, T, T> Divide = CompileDivideDelegate();
public static readonly Func<T, T> Increment = CompileIncrementDelegate();
                                                  T> Multiply = CompileMultiplyDelegate();
16
17
18
            public static readonly Func<T, T> Decrement = CompileDecrementDelegate();
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             private static Func<T, T, T> CompileAddDelegate()
22
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
24
25
                     Ensure.Always.IsNumeric<T>();
26
                     emiter.LoadArguments(0, 1);
                     emiter.Add();
28
                     emiter.Return();
```

```
});
30
             }
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T, T> CompileSubtractDelegate()
34
35
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
37
                     Ensure.Always.IsNumeric<T>();
38
                     emiter.LoadArguments(0, 1);
39
                     emiter.Subtract();
40
                     emiter.Return();
41
                 });
42
43
             }
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            private static Func<T, T, T> CompileMultiplyDelegate()
46
47
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
48
49
                     Ensure.Always.IsNumeric<T>();
50
                     emiter.LoadArguments(0, 1);
5.1
                     emiter.Emit(OpCodes.Mul);
52
                     emiter.Return();
                 });
54
             }
55
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            private static Func<T, T, T> CompileDivideDelegate()
58
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
60
61
62
                     Ensure.Always.IsNumeric<T>();
63
                     emiter.LoadArguments(0, 1);
                     if(NumericType<T>.IsSigned)
64
                     {
65
                          emiter.Emit(OpCodes.Div);
                     }
67
                     else
68
                     {
69
                          emiter.Emit(OpCodes.Div_Un);
7.0
7.1
                     emiter.Return();
72
                 });
73
             }
74
75
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
76
            private static Func<T, T> CompileIncrementDelegate()
77
78
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
79
80
                     Ensure.Always.IsNumeric<T>();
                     emiter.LoadArgument(0);
82
                     emiter.Increment<T>();
83
                     emiter.Return();
                 });
85
86
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
88
            private static Func<T, T> CompileDecrementDelegate()
89
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
91
92
                     Ensure.Always.IsNumeric<T>();
93
                     emiter.LoadArgument(0);
94
                     emiter.Decrement<T>();
95
                     emiter.Return();
96
                 });
            }
98
        }
99
100
     ./csharp/Platform.Numbers/Bit.cs
    using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 4
```

```
namespace Platform. Numbers
7
        /// <summary>
9
        /// <para> Various operations on the set number bits </para>
10
        /// <para> Различные операции над установленными ьитами числа </para>
        /// </summary>
12
        /// <returns>
13
        /// <para> Data on the established beta numbers </para>
14
        /// <para> Данные об установленных бетах числа </para>
15
16
        public static class Bit
17
18
19
            /// <summary>
            /// <para> Counts the number of bits set in a number </para>
20
            /// <para> Подсчитывает количество установленных бит в числе </para>
21
            /// </summary>
22
            /// <returns>
            /// <para> Number of bits set in a number </para>
            /// <para> Количество установленных бит в числе </para>
25
            /// </returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            public static long Count(long x)
28
29
                long n = 0;
30
                while (x != 0)
31
32
                    n++;
33
                    x &= x - 1;
35
                return n;
36
37
            /// <summary>
38
            /// <para> Searches for the first bit set in a number </para>
            /// <para> Ищет первый установленный бит в числе </para>
            /// </summary>
41
            /// <returns>
42
            /// <para> First bit set </para>
43
            /// <para> Первый установленный бит </para>
44
            /// </returns>
45
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
47
            public static int GetLowestPosition(ulong value)
48
                if (value == 0)
49
                    return -1;
51
                var position = 0;
53
54
                while ((value & 1UL) == 0)
                     value >>= 1;
56
57
                     ++position;
58
59
                return position;
            }
60
            ///<summary>
62
            ///<para> </para>
///<para> </para>
63
64
            ///</summary>
65
            ///<returns>
66
            ///<para> </para>
            ///<para> </para>
            ///</returns>
69
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
70
            public static T Not<T>(T x) => Bit<T>.Not(x);
72
            ///<summary>
            ///<para> </para>
74
            ///<para> </para>
7.5
            ///</summary>
76
            ///<returns>
77
            ///<para> </para>
78
            ///<para> </para>
79
            ///</returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
81
            public static T Or<T>(T x, T y) => Bit<T>.Or(x, y);
82
83
            ///<summary>
84
            ///<para> </para>
```

```
///<para> </para>
86
             ///</summary>
             ///<returns>
88
             ///<para>
                        </para>
89
             ///<para>
                        </para>
             ///</returns>
91
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
92
            public static T And<T>(T x, T y) => Bit<T>.And(x, y);
93
94
             ///<summary>
95
             ///<para>
                        </para>
             ///<para>
                        </para>
             ///</summary>
98
             ///<returns>
99
             ///<para>
                        </para>
             ///<para> </para>
101
             ///</returns>
102
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T ShiftLeft<T>(T x, int y) => Bit<T>.ShiftLeft(x, y);
105
             ///<summary>
106
            ///<para>
                        </para>
107
            ///<para> </para>
108
             ///</summary>
             ///<returns>
110
             ///<para>
                        </para>
111
             ///<para>
                        </para>
112
             ///</returns>
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
114
            public static T ShiftRight<T>(T x, int y) => Bit<T>.ShiftRight(x, y);
115
116
             ///<summary>
117
             ///<para>
                        </para>
118
             ///<para>
                       </para>
119
            ///</summary>
120
            ///<returns>
121
             ///<para>
                        </para>
                        </para>
             ///<para>
123
             ///</returns>
124
125
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T PartialWrite<T>(T target, T source, int shift, int limit) =>
126
             → Bit<T>.PartialWrite(target, source, shift, limit);
127
             ///<summary>
                        </para>
129
            ///<para>
                        </para>
             ///<para>
130
             ///</summary>
            ///<returns>
132
            ///<para> </para>
133
            ///<para>
                       </para>
134
             ///</returns>
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
136
            public static T PartialRead<T>(T target, int shift, int limit) =>
137
             → Bit<T>.PartialRead(target, shift, limit);
        }
138
139
     ./csharp/Platform.Numbers/BitExtensions.cs
1.5
    using System.Runtime.CompilerServices;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Numbers
 5
 6
        /// <summary>
        /// <returns> bit operations </returns>
        /// </summary>
        /* bit operations */
10
        public static class BitwiseExtensions
11
12
13
14
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            public static T Not<T>(this ref T target) where T : struct => target = Bit.Not(target);
17
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            public static T PartialWrite<T>(this ref T target, T source, int shift, int limit) where
                T : struct => target = Bit<T>.PartialWrite(target, source, shift, limit);
```

```
[MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             public static T PartialRead<T>(this T target, int shift, int limit) =>
                Bit<T>.PartialRead(target, shift, limit);
23
24
    ./csharp/Platform.Numbers/Bit[T].cs
1.6
   using System;
   using System.Runtime.CompilerServices;
   using Platform. Exceptions;
3
   using Platform.Reflection;
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform. Numbers
9
10
        public static class Bit<T>
11
12
            public static readonly Func<T, T> Not = CompileNotDelegate()
            public static readonly Func<T, T, T> Or = CompileOrDelegate()
14
            public static readonly Func<T, T, T> And = CompileAndDelegate();
public static readonly Func<T, int, T> ShiftLeft = CompileShiftLeftDelegate();
public static readonly Func<T, int, T> ShiftRight = CompileShiftRightDelegate();
15
16
17
            public static readonly Func<T, T, int, int, T> PartialWrite =
18
                 CompilePartialWriteDelegate();
            public static readonly Func<T, int, int, T> PartialRead = CompilePartialReadDelegate();
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            private static Func<T, T> CompileNotDelegate()
22
2.3
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
25
                      Ensure.Always.IsNumeric<T>();
26
                      emiter.LoadArguments(0);
27
                      emiter.Not();
                      emiter.Return();
29
                 });
30
             }
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            private static Func<T, T, T> CompileOrDelegate()
34
35
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
                      Ensure.Always.IsNumeric<T>();
38
                      emiter.LoadArguments(0, 1);
39
                      emiter.Or();
40
41
                      emiter.Return();
                 });
42
             }
43
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            private static Func<T, T, T> CompileAndDelegate()
46
47
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
48
49
                      Ensure.Always.IsNumeric<T>();
                      emiter.LoadArguments(0, 1);
51
                      emiter.And();
52
                      emiter.Return();
53
                 });
             }
55
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            private static Func<T, int, T> CompileShiftLeftDelegate()
58
                 return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
60
                 {
61
                      Ensure.Always.IsNumeric<T>();
62
                      emiter.LoadArguments(0, 1);
63
                      emiter.ShiftLeft();
64
                      emiter.Return();
65
                 });
66
             }
67
68
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             private static Func<T, int, T> CompileShiftRightDelegate()
70
71
```

```
return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.ShiftRight();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T, int, int, T> CompilePartialWriteDelegate()
    return DelegateHelpers.Compile<Func<T, T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>()
        var constants = GetConstants();
        var bitsNumber = constants.Item1;
        var numberFilledWithOnes = constants.Item2;
        ushort shiftArgument = 2;
        ushort limitArgument = 3;
        var checkLimit = emiter.DefineLabel();
        var calculateSourceMask = emiter.DefineLabel();
        // Check shift
        emiter.LoadArgument(shiftArgument);
        emiter.LoadConstant(0);
        emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
        // Fix shift
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(shiftArgument);
        emiter.Add()
        emiter.StoreArgument(shiftArgument);
        emiter.MarkLabel(checkLimit);
        // Check limit
        emiter.LoadArgument(limitArgument);
        emiter.LoadConstant(0)
        emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
        // Fix limit
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(limitArgument);
        emiter.Add()
        emiter.StoreArgument(limitArgument);
        emiter.MarkLabel(calculateSourceMask)
        var sourceMask = emiter.DeclareLocal<T>();
        var targetMask = emiter.DeclareLocal<T>();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.LoadArgument(limitArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.And():
        emiter.StoreLocal(sourceMask);
        emiter.LoadLocal(sourceMask)
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.StoreLocal(targetMask);
        emiter.LoadArgument(0); // target
        emiter.LoadLocal(targetMask);
        emiter.And();
        emiter.LoadArgument(1); // source
        emiter.LoadLocal(sourceMask);
        emiter.And():
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Or();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, int, int, T> CompilePartialReadDelegate()
    return DelegateHelpers.Compile<Func<T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        var constants = GetConstants()
        var bitsNumber = constants.Item1;
        var numberFilledWithOnes = constants.Item2;
```

7.4

7.5

77

78

79 80

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139 140

141

 $\frac{142}{143}$

144 145

146

147

148

149

```
ushort shiftArgument =
150
                     ushort limitArgument = 2;
151
                     var checkLimit = emiter.DefineLabel();
152
                     var calculateSourceMask = emiter.DefineLabel();
                      // Check shift
154
                     emiter.LoadArgument(shiftArgument);
155
                     emiter.LoadConstant(0)
156
                      emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
157
                     // Fix shift
158
                     emiter.LoadConstant(bitsNumber);
159
                     emiter.LoadArgument(shiftArgument);
160
                     emiter.Add();
161
                     emiter.StoreArgument(shiftArgument);
162
                      emiter.MarkLabel(checkLimit);
163
                        Check limit
                     emiter.LoadArgument(limitArgument);
165
                     emiter.LoadConstant(0)
166
                     emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
167
                      // Fix limit
168
                     emiter.LoadConstant(bitsNumber);
169
                     emiter.LoadArgument(limitArgument);
170
                     emiter.Add()
171
                     emiter.StoreArgument(limitArgument);
172
                     emiter.MarkLabel(calculateSourceMask):
173
                     var sourceMask = emiter.DeclareLocal<T>();
                     var targetMask = emiter.DeclareLocal<T>()
175
                     emiter.LoadConstant(typeof(T), numberFilledWithOnes);
176
                      emiter.LoadArgument(limitArgument); // limit
177
                      emiter.ShiftLeft();
                     emiter.Not();
179
                     emiter.LoadConstant(typeof(T), numberFilledWithOnes);
180
                     emiter.And();
182
                     emiter.StoreLocal(sourceMask);
                     emiter.LoadLocal(sourceMask);
183
                     emiter.LoadArgument(shiftArgument);
184
                     emiter.ShiftLeft();
                     emiter.StoreLocal(targetMask);
186
                     emiter.LoadArgument(0); // target
187
                     emiter.LoadLocal(targetMask);
                     emiter.And();
189
                     emiter.LoadArgument(shiftArgument);
190
                      emiter.ShiftRight();
191
192
                      emiter.Return();
                 });
193
             }
194
195
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
196
             private static Tuple<int, T> GetConstants()
197
198
                 var type = typeof(T);
199
                 if (type == typeof(ulong))
200
                     return new Tuple<int, T>(64, (T)(object)ulong.MaxValue);
202
                 }
203
                    (type == typeof(uint))
204
                 {
205
                     return new Tuple<int, T>(32, (T)(object)uint.MaxValue);
206
207
                    (type == typeof(ushort))
208
209
                     return new Tuple<int, T>(16, (T)(object)ushort.MaxValue);
210
211
                    (type == typeof(byte))
212
213
                     return new Tuple<int, T>(8, (T)(object)byte.MaxValue);
214
                 throw new NotSupportedException();
216
             }
217
        }
    }
219
      ./csharp/Platform.Numbers/Math.cs
    using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 4
    namespace Platform. Numbers
```

```
7
        /// <remarks>
        /// Resizable array (FileMappedMemory) for values cache may be used. or cached oeis.org
9
        /// </remarks>
10
        public static class Math
11
12
             /// <remarks>
13
             /// <para>Source: https://oeis.org/A000142/list </para>
14
             /// <para>Источник: https://oeis.org/A000142/list </para>
15
             /// </remarks>
16
17
            private static readonly ulong[] _factorials =
18
19
                 1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800, 39916800, 479001600, 6227020800, 87178291200, 1307674368000, 20922789888000, 355687428096000, 6402373705728000, 121645100408832000, 2432902008176640000
20
22
24
             /// <remarks>
25
             /// <para>Source: https://oeis.org/A000108/list </para>
             /// <para>Источник: https://oeis.org/A000108/list </para>
27
             /// </remarks>
28
29
            private static readonly ulong[] _catalans =
30
                 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 742900, 2674440, 9694845, 35357670, 129644790, 6564120420, 24466267020, 91482563640, 343059613
                                                                   4862,
                                                                                             208012,
                                                                           16796,
                                                                                    58786,
                                                                           477638700, 1767263190,
32
                                                              343059613650, 1289904147324,
33
                     4861946401452
                                    69533550916004,
                 18367353072152,
                                                      263747951750360, 1002242216651368,
                     3814986502092304
                 14544636039226909, 55534064877048198, 212336130412243110, 812944042149730764,
35
                  → 3116285494907301262, 11959798385860453492
             };
36
            public static readonly ulong MaximumFactorialNumber = 20;
38
39
            public static readonly ulong MaximumCatalanIndex = 36;
40
41
             /// <summary>
42
             /// <para>Returns the product of all positive integers less than or equal to the number
43
                 specified as an argument.</para>
             /// <para>Возвращает произведение всех положительных чисел меньше или равных указанному
44
                в качестве аргумента числу.</para>
             /// </summary>
45
             /// <param name="n"><para>The maximum positive number that will participate in
46
             _{
ightarrow} factorial's product.</para><para>Максимальное положительное число, которое будет
                 участвовать в произведение факториала. </para> </param>
             /// <returns><para>The product of all positive integers less than or equal to the number
             specified as an argument.</para><para>Произведение всех положительных чисел меньше
                или равных указанному в качестве аргумента числу.</para></returns>
             public static ulong Factorial(ulong n)
48
49
                 if (n >= 0 && n <= MaximumFactorialNumber)</pre>
50
                 {
                     return factorials[n];
52
                 }
53
                 else
54
55
                      throw new ArgumentOutOfRangeException($\"Only numbers from 0 to
56
                          {MaximumFactorialNumber} are supported by unsigned integer with 64 bits
                          length.");
                 }
             }
             /// <summary>
60
             /// <para>Returns the Catalan Number with the number specified as an argument.</para>
61
             /// <para>Возвращает Каталановое число с номером указанным в качестве аргумента.</para>
62
             /// </summary>
             /// <param name="n"><para>The number of Catalan number.</para>+Номер Каталанового
64
                числа.</para></param>
             /// <returns><para>The Catalan Number with the number specified as an
65
                argument.</para><para>Каталановое число с номером указанным в качестве
                аргумента.</para></returns>
            public static ulong Catalan(ulong n)
67
                 if (n >= 0 && n <= MaximumCatalanIndex)</pre>
68
69
                     return _catalans[n];
```

```
else
72
7.3
                    throw new ArgumentOutOfRangeException($\sigma"Only numbers from 0 to
                        {MaximumCatalanIndex} are supported by unsigned integer with 64 bits
                     → length.");
                }
            }
76
77
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static bool IsPowerOfTwo(ulong x) => (x & x - 1) == 0;
79
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
81
            public static T Abs<T>(T x) => Math<T>.Abs(x);
82
83
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
84
            public static T Negate<T>(T x) => Math<T>.Negate(x);
   }
87
    ./csharp/Platform.Numbers/MathExtensions.cs
1.8
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform. Numbers
        /// <summary>
7
       /// <para> Additional mathematical transformations </para>
8
       /// <para> Дополнительные математические преобразования </para>
       /// </summary>
10
       /// <returns>
11
       /// <para> The converted value in the original variable </para>
12
       /// <para> Преобразованное значение в исходной переменной </para>
13
       /// </returns>
14
       public static class MathExtensions
15
            /// <summary>
17
            /// <para> Takes a module from a number </para>
18
            /// <para> Берёт модуль от числа </para>
19
            /// </summary>
20
            /// <returns>
2.1
            /// <para> The absolute value of a number </para>
            /// <para> Абсолютное значение числа </para>
23
            /// </returns>
^{24}
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
25
            public static T Abs<T>(this ref T x) where T : struct => x = Math<T>.Abs(x);
            /// <summary>
            /// <para> Makes a number negatory </para>
29
            /// <para> Делает число отрицательным </para>
30
            /// </summary>
31
            /// <returns>
32
            /// <para> Negatory number </para>
33
            /// <para> Отрицательное число </para>
            /// </returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            public static T Negate<T>(this ref T x) where T : struct => x = Math<T>.Negate(x);
37
       }
38
   }
39
     ./csharp/Platform.Numbers/Math[T].cs
1.9
   using System;
   using System.Runtime.CompilerServices;
   using Platform. Exceptions;
3
   using Platform.Reflection;
   // ReSharper disable StaticFieldInGenericType
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
7
   namespace Platform. Numbers
9
       public static class Math<T>
11
12
            public static readonly Func<T, T> Abs = CompileAbsDelegate();
13
            public static readonly Func<T, T> Negate = CompileNegateDelegate();
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
16
            private static Func<T, T> CompileAbsDelegate()
```

```
18
                return DelegateHelpers.Compile<Func<T, T>>(emiter =>
19
20
                     Ensure.Always.IsNumeric<T>();
21
                     emiter.LoadArgument(0);
                     if (NumericType<T>.IsSigned)
23
24
                         emiter.Call(typeof(System.Math).GetMethod("Abs", Types<T>.Array));
25
                     }
                     emiter.Return();
27
                });
28
            }
30
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T> CompileNegateDelegate()
33
                return DelegateHelpers.Compile<Func<T, T>>(emiter =>
34
                     emiter.LoadArgument(0);
36
                     emiter.Negate();
37
                     emiter.Return();
38
                });
39
            }
40
        }
41
1.10
     ./csharp/Platform.Numbers.Tests/ArithmeticExtensionsTests.cs
   using Xunit;
   namespace Platform. Numbers. Tests
4
        public static class ArithmeticExtensionsTests
5
            [Fact]
            public static void IncrementTest()
                var number = OUL;
10
                var returnValue = number.Increment();
                Assert.Equal(1UL, returnValue);
                Assert.Equal(1UL, number);
13
            }
14
15
            [Fact]
16
            public static void DecrementTest()
                var number = 1UL;
19
                var returnValue = number.Decrement();
20
                Assert.Equal(OUL, returnValue);
21
                Assert.Equal(OUL, number);
22
            }
        }
24
25
      ./csharp/Platform.Numbers.Tests/ArithmeticTests.cs
1.11
1
   using System;
   using Xunit;
2
3
   namespace Platform.Numbers.Tests
5
        public static class ArithmeticTests
6
            [Fact]
            public static void CompiledOperationsTest()
10
                Assert.Equal(3, Arithmetic.Add(1, 2));
11
                Assert Equal(1, Arithmetic Subtract(2, 1));
12
                Assert.Equal(8, Arithmetic.Multiply(2,
                                                          4));
13
                Assert.Equal(4, Arithmetic.Divide(8, 2));
14
                Assert.Equal(2, Arithmetic.Increment(1));
15
                Assert.Equal(1UL, Arithmetic.Decrement(2UL));
16
                Assert.Throws<NotSupportedException>(() => Arithmetic<string>.Subtract("1", "2"));
17
            }
18
        }
19
     ./csharp/Platform.Numbers.Tests/BitTests.cs
1.12
   using System;
using Xunit;
```

```
namespace Platform. Numbers. Tests
    public static class BitTests
         [Theory]
         [InlineData(00, -1)] // 0000 0000 (none, -1)
        [InlineData(01, 00)] // 0000 0001 (first, 0)
        [InlineData(08, 03)] // 0000 1000 (forth, 3)
        [InlineData(88, 03)] // 0101 1000 (forth, 3)
        public static void GetLowestBitPositionTest(ulong value, int expectedPosition)
             Assert.True(Bit.GetLowestPosition(value) == expectedPosition);
        }
        [Fact]
        public static void ByteBitwiseOperationsTest()
             Assert.True(Bit<byte>.Not(2) == unchecked((byte)~2));
             Assert.True(Bit<br/>byte>.Or(1, 2) == (1 | 2))
             Assert.True(Bit<br/>byte>.And(1, 2) == (1 \& 2));
             Assert.True(Bit<byte>.ShiftLeft(1, 2) == (1 << 2));
             Assert.True(Bit<byte>.ShiftRight(1, 2) == (1 >> 2));
        }
        [Fact]
        public static void UInt16BitwiseOperationsTest()
             Assert.True(Bit<ushort>.Not(2) == unchecked((ushort)~2));
             Assert. True (Bit \langle ushort \rangle. Or (1, 2) == (1 | 2));
             Assert.True(Bit\langle ushort \rangle.And(1, 2) == (1 & 2));
             Assert.True(Bit<ushort>.ShiftLeft(1, 2) == (1 << 2));
             Assert.True(Bit<ushort>.ShiftRight(1, 2) == (1 >> 2));
        [Fact]
        public static void UInt32BitwiseOperationsTest()
             Assert.True(Bit<uint>.Not(2) == unchecked((uint)~2));
             Assert.True(Bit<uint>.Or(1, 2) == (1 | 2));
             Assert.True(Bit\langle uint \rangle.And(1, 2) == (1 & 2));
             Assert.True(Bit<uint>.ShiftLeft(1, 2) == (1 << 2))
             Assert.True(Bit<uint>.ShiftRight(1, 2) == (1 >> 2));
        }
        [Fact]
        public static void UInt64BitwiseOperationsTest()
             Assert.True(Bit<ulong>.Not(2) == unchecked((ulong)~2));
             Assert.True(Bit\langle ulong \rangle.Or(1, 2) == (1 | 2))
             Assert.True(Bit\langle ulong \rangle.And(1, 2) == (1 & 2));
             Assert.True(Bit<ulong>.ShiftLeft(1, 2) == (1 << 2));
             Assert.True(Bit<ulong>.ShiftRight(1, 2) == (1 >> 2));
        [Fact]
        public static void PartialReadWriteTest()
                 uint firstValue = 1;
                 uint secondValue = 1543;
                 // Pack (join) two values at the same time
                 uint value = secondValue << 1 | firstValue;</pre>
                 uint unpackagedFirstValue = value & 1;
                 uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
                 Assert.True(firstValue == unpackagedFirstValue);
                 Assert.True(secondValue == unpackagedSecondValue);
                 // Using universal functions:
                 Assert.True(PartialRead(value, 0, 1) == firstValue);
                 Assert.True(PartialRead(value, 1, -1) == secondValue);
                 firstValue = 0:
                 secondValue = 6892;
                 value = PartialWrite(value, firstValue, 0, 1);
```

4

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2.4

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```
value = PartialWrite(value, secondValue, 1, -1);
        Assert.True(PartialRead(value, 0, 1) == firstValue);
        Assert.True(PartialRead(value, 1, -1) == secondValue);
    }
    {
        uint firstValue = 1;
        uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = Bit.PartialWrite(value, firstValue, 0, 1);
        value = Bit.PartialWrite(value, secondValue, 1, -1);
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
    }
    {
        uint firstValue = 1;
        uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        var readMasksAndShiftForOAnd1 = GetReadMaskAndShift(0, 1);
        var readMasksAndShiftFor1AndMinus1 = GetReadMaskAndShift(1,
        var writeMasksAndShiftForOAnd1 = GetWriteMasksAndShift(0, 1);
        var writeMasksAndShiftFor1AndMinus1 = GetWriteMasksAndShift(1, -1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
        firstValue = 0:
        secondValue = 6892;
        value = PartialWrite(value, firstValue, writeMasksAndShiftForOAnd1);
        value = PartialWrite(value, secondValue, writeMasksAndShiftFor1AndMinus1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
    }
}
// TODO: Can be optimized using precalculation of TargetMask and SourceMask
private static uint PartialWrite(uint target, uint source, int shift, int limit)
    if (shift < 0)</pre>
    {
        shift = 32 + shift;
    if (limit < 0)</pre>
    {
        limit = 32 + limit;
    var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
    var targetMask = ~(sourceMask << shift);</pre>
    return target & targetMask | (source & sourceMask) << shift;</pre>
```

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117 118

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120 121

122

 $\frac{123}{124}$

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132 133

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135 136 137

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143

144

 $\frac{146}{147}$

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151

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153 154

155

157 158

160

161

```
162
163
             private static uint PartialRead(uint target, int shift, int limit)
164
                  if (shift < 0)</pre>
166
                  {
167
                      shift = 32 + shift;
169
                  if (limit < 0)</pre>
170
                  {
171
                      limit = 32 + limit;
172
173
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
174
                  var targetMask = sourceMask << shift;</pre>
175
                  return (target & targetMask) >> shift;
177
178
             private static Tuple<uint, uint, int> GetWriteMasksAndShift(int shift, int limit)
179
180
                  if (shift < 0)</pre>
181
                  {
                      shift = 32 + shift;
183
                  }
                  if (limit < 0)</pre>
185
                  {
186
                      limit = 32 + limit;
187
188
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
189
                  var targetMask = ~(sourceMask << shift);</pre>
190
                 return new Tuple<uint, uint, int>(targetMask, sourceMask, shift);
191
192
193
             private static Tuple<uint, int> GetReadMaskAndShift(int shift, int limit)
194
195
                  if (shift < 0)</pre>
                  {
197
                      shift = 32 + shift;
199
                  if (limit < 0)</pre>
200
201
                      limit = 32 + limit;
202
                  }
203
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
                  var targetMask = sourceMask << shift;</pre>
205
                  return new Tuple<uint, int>(targetMask, shift);
             }
207
             private static uint PartialWrite(uint target, uint targetMask, uint source, uint
209

→ sourceMask, int shift) => target & targetMask | (source & sourceMask) << shift;
</p>
210
             private static uint PartialWrite(uint target, uint source, Tuple<uint, uint, int>
                 masksAndShift) => PartialWrite(target, masksAndShift.Item1, source,
                 masksAndShift.Item2, masksAndShift.Item3);
212
             private static uint PartialRead(uint target, uint targetMask, int shift) => (target &
213

    targetMask) >> shift;

214
             private static uint PartialRead(uint target, Tuple<uint, int> masksAndShift) =>
215
              PartialRead(target, masksAndShift.Item1, masksAndShift.Item2);
216
             [Fact]
217
             public static void BugWithLoadingConstantOf8Test()
218
219
                  Bit<byte>.PartialWrite(0, 1, 5, -5);
220
             }
221
         }
223
       ./csharp/Platform.Numbers.Tests/MathExtensionsTests.cs
    using Xunit;
    namespace Platform.Numbers.Tests
 4
         public static class MathExtensionsTests
 5
             [Fact]
             public static void AbsTest()
                  var number = -1L;
```

```
var returnValue = number.Abs();
11
                Assert.Equal(1L, returnValue);
12
                Assert.Equal(1L, number);
13
14
            [Fact]
16
            public static void NegateTest()
17
                var number = 2L;
19
                var returnValue = number.Negate();
                Assert.Equal(-2L, returnValue);
21
                Assert.Equal(-2L, number);
22
23
            }
24
            [Fact]
25
            public static void UnsignedNegateTest()
27
                var number = 2UL;
                var returnValue = number.Negate();
29
                Assert.Equal(18446744073709551614, returnValue);
30
                Assert.Equal(18446744073709551614, number);
            }
        }
33
34
1.14
      ./csharp/Platform.Numbers.Tests/MathTests.cs
   using Xunit;
1
2
   namespace Platform.Numbers.Tests
4
        public static class MathTests
5
            [Fact]
            public static void CompiledOperationsTest()
                Assert.True(Math.Abs(Arithmetic < double > .Subtract(3D, 2D) - 1D) < 0.01);
10
11
        }
12
   }
13
      ./csharp/Platform.Numbers.Tests/SystemTests.cs
1.15
   using Xunit;
   namespace Platform. Numbers. Tests
3
4
        public static class SystemTests
5
            [Fact]
            public static void PossiblePackTwoValuesIntoOneTest()
10
                uint value = 0;
11
                // Set one to first bit
                value |= 1;
13
                Assert.True(value == 1);
15
16
                // Set zero to first bit
                value &= OxFFFFFFE;
18
19
                // Get first bit
20
                uint read = value & 1;
21
                Assert.True(read == 0);
23
24
                uint firstValue = 1:
25
                uint secondValue = 1543;
26
27
                // Pack (join) two values at the same time
                value = (secondValue << 1) | firstValue;</pre>
29
30
                uint unpackagedFirstValue = value & 1;
31
                uint unpackagedSecondValue = (value & OxFFFFFFE) >> 1;
32
33
                Assert.True(firstValue == unpackagedFirstValue)
34
                Assert.True(secondValue == unpackagedSecondValue);
36
                // Using universal functions:
38
                Assert.True(PartialRead(value, 0, 1) == firstValue);
```

```
Assert.True(PartialRead(value, 1, -1) == secondValue);
40
41
                  firstValue = 0;
42
                  secondValue = 6892;
43
44
                  value = PartialWrite(value, firstValue, 0, 1);
45
                  value = PartialWrite(value, secondValue, 1, -1);
46
47
                  Assert.True(PartialRead(value, 0, 1) == firstValue);
Assert.True(PartialRead(value, 1, -1) == secondValue);
48
             }
50
             private static uint PartialWrite(uint target, uint source, int shift, int limit)
52
53
                  if (shift < 0)</pre>
54
                       shift = 32 + shift;
56
57
                  if (limit < 0)</pre>
58
                  {
59
                       limit = 32 + limit;
60
                  }
61
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
62
                  var targetMask = ~(sourceMask << shift);</pre>
                  return (target & targetMask) | ((source & sourceMask) << shift);</pre>
64
             }
65
66
             private static uint PartialRead(uint target, int shift, int limit)
67
68
                  if (shift < 0)</pre>
                  {
70
                       shift = 32 + shift;
                  }
72
                  if (limit < 0)</pre>
73
                  {
74
                       limit = 32 + limit;
75
76
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
77
                  var targetMask = sourceMask << shift;</pre>
78
                  return (target & targetMask) >> shift;
79
             }
80
        }
81
   }
82
```

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