```
LinksPlatform's Platform Numbers Class Library
     ./csharp/Platform.Numbers/Arithmetic.cs
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
6
        /// <summary>
       /// Each function performs the simplest arithmetic operation on the type specified as a
           parameter
        /// 	ilde{K}аждая функция выполняет простейшую арифметическую операцию над типом, указанным в
9
           качестве параметра.
        /// </summary>
10
       public static class Arithmetic
12
13
            /// <summary>
14
            /// Adding the x and y arguments
15
            /// Сложение аргументов х и у
            /// </summary>
17
            /// <returns>
18
            /// Sum of x and y
19
            /// Сумма х и у
            /// </returns>
21
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
22
           public static T Add<T>(T x, T y) => Arithmetic<T>.Add(x, y);
24
            /// <summary>
25
            /// Subtracting x from y
26
            /// Вычитание х из у
27
            /// </summary>
28
            /// <returns>
            /// Difference of x and y
30
            /// Разность х и у
31
            /// </returns>
32
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            public static T Subtract<T>(T x, T y) => Arithmetic<T>.Subtract(x, y);
34
            /// <summary>
36
            /// Multiplication the x and y
37
            /// Умножение х и у
38
            /// </summary>
39
            /// <returns>
40
            /// <returns>
41
            /// Product of x and y
            /// Произведение х и у
43
            /// </returns>
44
45
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Multiply<T>(T x, T y) => Arithmetic<T>.Multiply(x, y);
46
47
            /// <summary>
            /// Dividing x by y
49
            /// Деление х на у
50
            /// </summary>
            /// <returns>
52
            /// Quoitent of x and y
53
            /// Частное х и у
            /// </returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
56
            public static T Divide<T>(T x, T y) => Arithmetic<T>.Divide(x, y);
57
58
            /// <summary>
59
            /// Increasing the parameter x by one
61
            /// Увеличение параметра х на единицу
            /// </summary>
62
            /// <returns>
63
            /// Increase by one x
64
            /// Увеличенное на единицу х
65
            /// </returns>
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Increment<T>(T x) => Arithmetic<T>.Increment(x);
69
            /// <summary>
70
            /// Increase the parameter x passed by reference by one
71
            /// Увеличение переданного по ссылке параметра х на единицу
            /// </summary>
            /// <returns>
```

```
/// Increase by one x with returning the value to the original variable
7.5
             /// Увеличенное на единицу х с возвратом значения в исходную переменную
             /// </returns>
77
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
             public static T Increment<T>(ref T x) => x = Arithmetic<T>.Increment(x);
80
             /// <summary>
81
             /// Decrease parameter x by one
82
             /// Уменьшение параметра х на единицу
83
             /// </summary>
84
             /// <returns>
85
             /// Reduced by one x
             /// Уменьшенное на единицу х
87
             /// </returns>
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public static T Decrement<T>(T x) => Arithmetic<T>.Decrement(x);
90
             /// <summary>
92
             /// Decreasing the parameter x passed by reference by one
93
             /// Уменьшение переданного по ссылке параметра х на единицу
94
             /// </summary>
95
             /// <returns>
96
             /// Reduced by one x with returning the value to the original variable
97
             /// Уменьшенное на единицу х с воз вратом значения в исходную переменную
             /// </returns>
99
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
100
             public static T Decrement<T>(ref T x) => x = Arithmetic<T>.Decrement(x);
101
        }
102
103
     ./csharp/Platform.Numbers/ArithmeticExtensions.cs
1.2
   using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 3
    namespace Platform.Numbers
        public static class ArithmeticExtensions
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
 9
             public static T Decrement<T>(this ref T x) where T : struct => x =
10
                Arithmetic<T>.Decrement(x);
11
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
             public static T Increment<T>(this ref T x) where T : struct => x =
13
             → Arithmetic<T>.Increment(x);
        }
15
1.3
     ./csharp/Platform.Numbers/Arithmetic[T].cs
   using System;
    using System.Reflection.Emit;
 2
    using System.Runtime.CompilerServices;
    using Platform. Exceptions;
    using Platform.Reflection;
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform. Numbers
10
11
        public static class Arithmetic<T>
12
13
             public static readonly Func<T, T, T> Add = CompileAddDelegate();
            public static readonly Func<T, T, T> Subtract = CompileSubtractDelegate();
15
            public static readonly Func<T, T, T> Multiply = CompileMultiplyDelegate()
public static readonly Func<T, T, T> Divide = CompileDivideDelegate();
public static readonly Func<T, T> Increment = CompileIncrementDelegate();
                                                  T> Multiply = CompileMultiplyDelegate();
16
17
18
             public static readonly Func<T, T> Decrement = CompileDecrementDelegate();
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             private static Func<T, T, T> CompileAddDelegate()
22
23
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
24
25
                      Ensure.Always.IsNumeric<T>();
26
                      emiter.LoadArguments(0, 1);
                      emiter.Add();
28
                      emiter.Return();
```

```
});
30
             }
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T, T> CompileSubtractDelegate()
34
35
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
37
                     Ensure.Always.IsNumeric<T>();
38
                     emiter.LoadArguments(0, 1);
39
                     emiter.Subtract();
40
                     emiter.Return();
41
                 });
42
43
             }
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            private static Func<T, T, T> CompileMultiplyDelegate()
46
47
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
48
49
                     Ensure.Always.IsNumeric<T>();
50
                     emiter.LoadArguments(0, 1);
5.1
                     emiter.Emit(OpCodes.Mul);
52
                     emiter.Return();
                 });
54
             }
55
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            private static Func<T, T, T> CompileDivideDelegate()
58
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
60
61
62
                     Ensure.Always.IsNumeric<T>();
63
                     emiter.LoadArguments(0, 1);
                     if(NumericType<T>.IsSigned)
64
                     {
65
                          emiter.Emit(OpCodes.Div);
                     }
67
                     else
68
                     {
69
                          emiter.Emit(OpCodes.Div_Un);
7.0
7.1
                     emiter.Return();
72
                 });
73
             }
74
75
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
76
            private static Func<T, T> CompileIncrementDelegate()
77
78
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
79
80
                     Ensure.Always.IsNumeric<T>();
                     emiter.LoadArgument(0);
82
                     emiter.Increment<T>();
83
                     emiter.Return();
                 });
85
86
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
88
            private static Func<T, T> CompileDecrementDelegate()
89
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
91
92
                     Ensure.Always.IsNumeric<T>();
93
                     emiter.LoadArgument(0);
94
                     emiter.Decrement<T>();
95
                     emiter.Return();
96
                 });
            }
98
        }
99
100
     ./csharp/Platform.Numbers/Bit.cs
    using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 4
```

```
namespace Platform. Numbers
7
10
        public static class Bit
11
            /// <summary>
12
            /// <returns>the number of ones in the bit representation of a numberss</returns>
13
            /// </summary>
14
            /* the number of ones in the bit representation of a number */
15
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
16
            public static long Count(long x)
17
18
                long n = 0;
19
                while (x != 0)
20
21
                    n++:
22
                    x \&= x - 1;
24
                return n;
            }
27
            /// <summary>
            /// <returns>first bit set</returns>
29
            /// </summary>
30
            /* first bit set */
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
32
            public static int GetLowestPosition(ulong value)
33
34
                if (value == 0)
35
                {
36
                    return -1;
                }
38
                var position = 0;
39
                while ((value & 1UL) == 0)
40
41
                    value >>= 1;
                    ++position;
43
44
                return position;
45
            }
46
47
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
48
            public static T Not<T>(T x) => Bit<T>.Not(x);
50
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Or<T>(T x, T y) => Bit<T>.Or(x, y);
52
53
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T And<T>(T x, T y) => Bit<T>.And(x, y);
55
57
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T ShiftLeft<T>(T x, int y) => Bit<T>.ShiftLeft(x, y);
58
59
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
60
            public static T ShiftRight<T>(T x, int y) => Bit<T>.ShiftRight(x, y);
62
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
63
            public static T PartialWrite<T>(T target, T source, int shift, int limit) =>

→ Bit<T>.PartialWrite(target, source, shift, limit);
65
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
66
            public static T PartialRead<T>(T target, int shift, int limit) =>

→ Bit<T>.PartialRead(target, shift, limit);
68
69
    ./csharp/Platform.Numbers/BitExtensions.cs
1.5
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
        /// <summary>
7
        /// <returns> bit operations </returns>
8
        /// </summary>
        /* bit operations */
10
       public static class BitwiseExtensions
11
12
        {
```

```
14
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public static T Not<T>(this ref T target) where T : struct => target = Bit.Not(target);
16
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public static T PartialWrite<T>(this ref T target, T source, int shift, int limit) where
19
             T: struct => target = Bit<T>.PartialWrite(target, source, shift, limit);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             public static T PartialRead<T>(this T target, int shift, int limit) =>
22
             → Bit<T>.PartialRead(target, shift, limit);
        }
    }
^{24}
1.6
     ./csharp/Platform.Numbers/Bit[T].cs
   using System;
   using System.Runtime.CompilerServices;
   using Platform. Exceptions;
3
   using Platform. Reflection;
   // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Numbers
9
    {
10
        public static class Bit<T>
11
12
            public static readonly Func<T, T> Not = CompileNotDelegate();
public static readonly Func<T, T, T> Or = CompileOrDelegate();
public static readonly Func<T, T, T> And = CompileAndDelegate();
13
14
1.5
             public static readonly Func<T, int, T> ShiftLeft = CompileShiftLeftDelegate();
16
            public static readonly Func<T, int, T> ShiftRight = CompileShiftRightDelegate();
public static readonly Func<T, T, int, int, T> PartialWrite =
18

→ CompilePartialWriteDelegate();

             public static readonly Func<T, int, int, T> PartialRead = CompilePartialReadDelegate();
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             private static Func<T, T> CompileNotDelegate()
23
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
24
25
                      Ensure.Always.IsNumeric<T>();
26
                      emiter.LoadArguments(0);
27
                      emiter.Not();
28
                      emiter.Return();
                 });
30
             }
31
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
             private static Func<T, T, T> CompileOrDelegate()
34
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
37
                      Ensure.Always.IsNumeric<T>();
38
                      emiter.LoadArguments(0, 1);
39
                      emiter.Or();
40
                      emiter.Return();
41
                 });
             }
43
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
             private static Func<T, T, T> CompileAndDelegate()
46
47
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
49
                      Ensure.Always.IsNumeric<T>();
50
                      emiter.LoadArguments(0, 1);
51
                      emiter.And();
52
                      emiter.Return();
53
                 });
54
             }
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             private static Func<T, int, T> CompileShiftLeftDelegate()
58
59
                 return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
60
                      Ensure.Always.IsNumeric<T>();
62
                      emiter.LoadArguments(0, 1);
63
```

```
emiter.ShiftLeft();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, int, T> CompileShiftRightDelegate()
    return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
    {
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.ShiftRight();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T, int, int, T> CompilePartialWriteDelegate()
    return DelegateHelpers.Compile<Func<T, T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        var constants = GetConstants();
        var bitsNumber = constants.Item1:
        var numberFilledWithOnes = constants.Item2;
        ushort shiftArgument = 2;
        ushort limitArgument = 3
        var checkLimit = emiter.DefineLabel();
        var calculateSourceMask = emiter.DefineLabel();
        // Check shift
        emiter.LoadArgument(shiftArgument);
        emiter.LoadConstant(0);
        emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
        // Fix shift
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(shiftArgument);
        emiter.Add();
        emiter.StoreArgument(shiftArgument);
        emiter.MarkLabel(checkLimit);
        // Check limit
        emiter.LoadArgument(limitArgument);
        emiter.LoadConstant(0)
        emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
        // Fix limit
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(limitArgument);
        emiter.Add();
        emiter.StoreArgument(limitArgument);
        emiter.MarkLabel(calculateSourceMask);
        var sourceMask = emiter.DeclareLocal<T>();
        var targetMask = emiter.DeclareLocal<T>();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.LoadArgument(limitArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.And();
        emiter.StoreLocal(sourceMask);
        emiter.LoadLocal(sourceMask);
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.StoreLocal(targetMask);
        emiter.LoadArgument(0); // target
        emiter.LoadLocal(targetMask);
        emiter.And();
        emiter.LoadArgument(1); // source
        emiter.LoadLocal(sourceMask);
        emiter.And():
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Or();
        emiter.Return();
    });
[MethodImpl(MethodImplOptions.AggressiveInlining)]
```

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69

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72

73

76

77 78

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81

82 83

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118

119

120

121

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123

125

126 127

128

129

130

131 132

133

134

135

136

137

139 140

141

```
private static Func<T, int, int, T> CompilePartialReadDelegate()
142
                 return DelegateHelpers.Compile<Func<T, int, int, T>>(emiter =>
144
145
                     Ensure.Always.IsNumeric<T>();
146
                     var constants = GetConstants()
147
                      var bitsNumber = constants.Item1
148
                     var numberFilledWithOnes = constants.Item2;
149
                     ushort shiftArgument = 1;
                     ushort limitArgument = 2
151
152
                      var checkLimit = emiter.DefineLabel();
                     var calculateSourceMask = emiter.DefineLabel();
153
                     // Check shift
154
                     emiter.LoadArgument(shiftArgument);
155
                     emiter.LoadConstant(0)
                     emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
157
                      // Fix shift
158
                     emiter.LoadConstant(bitsNumber);
                     emiter.LoadArgument(shiftArgument);
160
                     emiter.Add()
161
                     emiter.StoreArgument(shiftArgument);
162
                     emiter.MarkLabel(checkLimit);
                     // Check limit
164
                     emiter.LoadArgument(limitArgument);
165
                      emiter.LoadConstant(0)
166
                     emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
167
                     // Fix limit
168
                     emiter.LoadConstant(bitsNumber);
169
                     emiter.LoadArgument(limitArgument);
171
                     emiter.Add()
                     emiter.StoreArgument(limitArgument)
172
                     emiter.MarkLabel(calculateSourceMask)
173
                     var sourceMask = emiter.DeclareLocal<T>();
174
                     var targetMask = emiter.DeclareLocal<T>();
175
                     emiter.LoadConstant(typeof(T), numberFilledWithOnes);
176
                     emiter.LoadArgument(limitArgument); // limit
177
                     emiter.ShiftLeft();
178
                     emiter.Not();
179
                      emiter.LoadConstant(typeof(T), numberFilledWithOnes);
180
                     emiter.And()
                     emiter.StoreLocal(sourceMask);
182
                     emiter.LoadLocal(sourceMask);
183
                     emiter.LoadArgument(shiftArgument);
185
                     emiter.ShiftLeft();
                     emiter.StoreLocal(targetMask);
186
                     emiter.LoadArgument(0); // target
                     emiter.LoadLocal(targetMask);
188
                     emiter.And();
189
                     emiter.LoadArgument(shiftArgument);
190
                     emiter.ShiftRight();
191
                     emiter.Return();
192
                 });
193
             }
195
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
196
             private static Tuple<int, T> GetConstants()
197
198
                 var type = typeof(T);
199
                 if (type == typeof(ulong))
201
                     return new Tuple<int, T>(64, (T)(object)ulong.MaxValue);
202
                 if (type == typeof(uint))
204
205
                     return new Tuple<int, T>(32, (T)(object)uint.MaxValue);
206
                    (type == typeof(ushort))
                 if
208
                 {
209
210
                     return new Tuple<int, T>(16, (T)(object)ushort.MaxValue);
211
                    (type == typeof(byte))
212
213
                     return new Tuple<int, T>(8, (T)(object)byte.MaxValue);
215
                 throw new NotSupportedException();
216
             }
217
        }
218
219
```

```
./csharp/Platform.Numbers/Math.cs
   using System;
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
4
   namespace Platform. Numbers
6
        /// <remarks>
8
        /// Resizable array (FileMappedMemory) for values cache may be used. or cached oeis.org
9
           </remarks>
10
        public static class Math
11
12
            /// <remarks>
13
            /// <para>Source: https://oeis.org/A000142/list </para>
14
            /// <para>Источник: https://oeis.org/A000142/list </para>
15
            /// </remarks>
16
17
            private static readonly ulong[] _factorials =
18
                1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800, 39916800, 479001600, 6227020800, 87178291200, 1307674368000, 20922789888000
20
21
                355687428096000, 6402373705728000, 121645100408832000, 2432902008176640000
            };
23
24
            /// <remarks>
25
            /// <para>Source: https://oeis.org/A000108/list </para>
26
            /// <para>Источник: https://oeis.org/A000108/list </para>
27
            /// </remarks>
            private static readonly ulong[] _catalans =
29
30
                                 14, 42, 132, <del>1</del>22,
0. 9694845, 35357670,
                                                         1430,
                                                                 4862,
                        2, 5, 14
2674440,
                                                                         16796.
                                                                                  58786,
                                                                                           208012,
31
                742900
                                                          129644790,
                                                                         477638700,
                                                                                      1767263190,
32
                6564120420, 24466267020, 91482563640,
                                                            343059613650, 1289904147324,
33
                → 4861946401452,
18367353072152, 69533550916004,
                                                    263747951750360, 1002242216651368,
34
                 → 3814986502092304.
                14544636039226909, 55534064877048198, 212336130412243110, 812944042149730764,
                 \  \, \rightarrow \  \, 3116285494907301262 \, , \  \, 11959798385860453492 \, \, \,
            };
36
37
            public static readonly ulong MaximumFactorialNumber = 20;
39
            public static readonly ulong MaximumCatalanIndex = 36;
40
41
            /// <summary>
            /// <para>Returns the product of all positive integers less than or equal to the number
43
                specified as an argument.</para>
            /// <para>Возвращает произведение всех положительных чисел меньше или равных указанному
44
                в качестве аргумента числу.</para>
            /// </summary>
45
            /// <param name="n"><para>The maximum positive number that will participate in
             🛶 factorial's product.</para><pаra>Максимальное положительное число, которое будет
                участвовать в произведение факториала.</para></param>
            /// <returns><para>The product of all positive integers less than or equal to the number
47
             specified as an argument.</para><para>Произведение всех положительных чисел меньше
               или равных указанному в качестве аргумента числу.</para></returns>
            public static ulong Factorial(ulong n)
48
                if (n >= 0 && n <= MaximumFactorialNumber)</pre>
50
51
                     return _factorials[n];
52
                }
53
                else
54
                {
                     throw new ArgumentOutOfRangeException($"Only numbers from 0 to
56
                     {MaximumFactorialNumber} are supported by unsigned integer with 64 bits
                     → length.");
                }
57
            }
58
59
            /// <summary>
60
            /// <para>Returns the Catalan Number with the number specified as an argument.</para>
61
            /// <para>Возвращает Каталановое число с номером указанным в качестве аргумента.</para>
62
            /// </summary>
63
            /// <param name="n"><para>The number of Catalan number.</para><para>Номер Каталанового
64

¬ числа.</para></param>
```

```
/// <returns><para>The Catalan Number with the number specified as an
65
             → argument.</para>Каталановое число с номером указанным в качестве
                аргумента.</para></returns>
            public static ulong Catalan(ulong n)
                if (n >= 0 && n <= MaximumCatalanIndex)</pre>
68
                     return _catalans[n];
70
                }
7.1
                else
72
                {
73
                     throw new ArgumentOutOfRangeException($"Only numbers from 0 to
74
                        {MaximumCatalanIndex} are supported by unsigned integer with 64 bits
                         length.");
                }
75
            }
77
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
            public static bool IsPowerOfTwo(ulong x) => (x & x - 1) == 0;
79
80
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Abs<T>(T x) => Math<T>.Abs(x);
82
83
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
84
            public static T Negate<T>(T x) => Math<T>.Negate(x);
85
86
     ./csharp/Platform.Numbers/MathExtensions.cs
1.8
   using System.Runtime.CompilerServices;
1
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
        public static class MathExtensions
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
9
            public static T Abs<T>(this ref T x) where T : struct => x = Math<T>.Abs(x);
1.0
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            public static T Negate<T>(this ref T x) where T : struct => x = Math<T>.Negate(x);
13
        }
   }
15
1.9
    ./csharp/Platform.Numbers/Math[T].cs
   using System;
using System.Runtime.CompilerServices;
2
   using Platform. Exceptions;
   using Platform.Reflection;
   // ReSharper disable StaticFieldInGenericType
6
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
9
   namespace Platform.Numbers
   {
10
        public static class Math<T>
11
            public static readonly Func<T, T> Abs = CompileAbsDelegate();
public static readonly Func<T, T> Negate = CompileNegateDelegate();
13
14
15
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
16
            private static Func<T, T> CompileAbsDelegate()
17
                return DelegateHelpers.Compile<Func<T, T>>(emiter =>
19
20
                     Ensure.Always.IsNumeric<T>();
21
                     emiter.LoadArgument(0);
22
                     if (NumericType<T>.IsSigned)
23
24
                         emiter.Call(typeof(System.Math).GetMethod("Abs", Types<T>.Array));
25
26
27
                     emiter.Return();
                });
            }
29
30
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T> CompileNegateDelegate()
32
```

```
return DelegateHelpers.Compile<Func<T, T>>(emiter =>
34
                     emiter.LoadArgument(0);
36
                     emiter.Negate();
37
                     emiter.Return();
                });
39
            }
40
        }
41
42
      ./csharp/Platform.Numbers.Tests/ArithmeticExtensionsTests.cs
1.10
   using Xunit;
   namespace Platform.Numbers.Tests
4
5
        public static class ArithmeticExtensionsTests
6
            [Fact]
            public static void IncrementTest()
                var number = OUL;
10
                var returnValue = number.Increment();
11
                Assert.Equal(1UL, returnValue);
12
                Assert.Equal(1UL, number);
13
            }
14
15
            [Fact]
16
            public static void DecrementTest()
                var number = 1UL;
19
                var returnValue = number.Decrement();
20
                Assert.Equal(OUL, returnValue);
21
                Assert.Equal(OUL, number);
22
            }
23
        }
24
   }
25
      ./csharp/Platform.Numbers.Tests/ArithmeticTests.cs
1.11
   using System;
   using Xunit;
3
   namespace Platform.Numbers.Tests
4
5
        public static class ArithmeticTests
            [Fact]
            public static void CompiledOperationsTest()
10
                Assert.Equal(3, Arithmetic.Add(1, 2));
11
                Assert.Equal(1, Arithmetic.Subtract(2, 1));
12
                Assert Equal(8, Arithmetic Multiply(2, 4));
                Assert.Equal(4, Arithmetic.Divide(8, 2));
14
                Assert.Equal(2, Arithmetic.Increment(1))
15
16
                Assert.Equal(1UL, Arithmetic.Decrement(2UL));
                Assert.Throws<NotSupportedException>(() => Arithmetic<string>.Subtract("1", "2"));
17
            }
18
        }
19
   }
1.12
      ./csharp/Platform.Numbers.Tests/BitTests.cs
   using System;
2
   using Xunit;
   namespace Platform.Numbers.Tests
4
        public static class BitTests
6
7
            [Theory]
            [InlineData(00, -1)] // 0000 0000 (none, -1)
            [InlineData(01, 00)] // 0000 0001 (first, 0)
10
            [InlineData(08, 03)] // 0000 1000 (forth, 3)
            [InlineData(88, 03)] // 0101 1000 (forth, 3)
12
            public static void GetLowestBitPositionTest(ulong value, int expectedPosition)
13
14
                Assert.True(Bit.GetLowestPosition(value) == expectedPosition);
16
17
            [Fact]
18
```

```
public static void ByteBitwiseOperationsTest()
    Assert.True(Bit<byte>.Not(2) == unchecked((byte)~2));
    Assert.True(Bit<byte>.Or(1, 2) == (1 | 2));
    Assert.True(Bit\langle byte \rangle.And(1, 2) == (1 & 2));
    Assert.True(Bit<byte>.ShiftLeft(1, 2) == (1 << 2))
    Assert.True(Bit<byte>.ShiftRight(1, 2) == (1 >> 2));
[Fact]
public static void UInt16BitwiseOperationsTest()
    Assert.True(Bit<ushort>.Not(2) == unchecked((ushort)~2));
    Assert.True(Bit<ushort>.Or(1, 2) == (1 | 2));Assert.True(Bit<ushort>.And(1, 2) == (1 & 2));
    Assert.True(Bit<ushort>.ShiftLeft(1, 2) == (1 << 2));
    Assert.True(Bit<ushort>.ShiftRight(1, 2) == (1 >> 2));
}
[Fact]
public static void UInt32BitwiseOperationsTest()
    Assert.True(Bit<uint>.Not(2) == unchecked((uint)~2));
    Assert.True(Bit\langle uint \rangle.Or(1, 2) == (1 | 2));
    Assert.True(Bit<uint>.And(1, 2) == (1 & 2));

Assert.True(Bit<uint>.ShiftLeft(1, 2) == (1 << 2));

Assert.True(Bit<uint>.ShiftRight(1, 2) == (1 >> 2));
}
[Fact]
public static void UInt64BitwiseOperationsTest()
    Assert.True(Bit<ulong>.Not(2) == unchecked((ulong)~2));
    Assert.True(Bit<ulong>.Or(1, 2) == (1 | 2));
    Assert.True(Bit\langle ulong \rangle.And(1, 2) == (1 & 2));
    Assert.True(Bit<ulong>.ShiftLeft(1, 2) == (1 << 2))
    Assert.True(Bit<ulong>.ShiftRight(1, 2) == (1 >> 2));
[Fact]
public static void PartialReadWriteTest()
    {
         uint firstValue = 1;
        uint secondValue = 1543;
         // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
         Assert.True(firstValue == unpackagedFirstValue);
         Assert.True(secondValue == unpackagedSecondValue);
         // Using universal functions:
         Assert.True(PartialRead(value, 0, 1) == firstValue);
         Assert.True(PartialRead(value, 1, -1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = PartialWrite(value, firstValue, 0, 1);
         value = PartialWrite(value, secondValue, 1, -1);
         Assert.True(PartialRead(value, 0, 1) == firstValue)
         Assert.True(PartialRead(value, 1, -1) == secondValue);
    }
    {
         uint firstValue = 1;
         uint secondValue = 1543;
         // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
         uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
         Assert.True(firstValue == unpackagedFirstValue);
```

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```
Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = Bit.PartialWrite(value, firstValue, 0, 1);
        value = Bit.PartialWrite(value, secondValue, 1, -1);
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
    {
        uint firstValue = 1;
        uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        var readMasksAndShiftForOAnd1 = GetReadMaskAndShift(0, 1);
        var readMasksAndShiftFor1AndMinus1 = GetReadMaskAndShift(1,
        var writeMasksAndShiftForOAnd1 = GetWriteMasksAndShift(0, 1);
        var writeMasksAndShiftFor1AndMinus1 = GetWriteMasksAndShift(1, -1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
        firstValue = 0:
        secondValue = 6892;
        value = PartialWrite(value, firstValue, writeMasksAndShiftForOAnd1);
        value = PartialWrite(value, secondValue, writeMasksAndShiftFor1AndMinus1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
    }
}
// TODO: Can be optimized using precalculation of TargetMask and SourceMask
private static uint PartialWrite(uint target, uint source, int shift, int limit)
    if (shift < 0)</pre>
        shift = 32 + shift;
    }
    if (limit < 0)</pre>
    {
        limit = 32 + limit;
    }
    var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
    var targetMask = ~(sourceMask << shift);</pre>
    return target & targetMask | (source & sourceMask) << shift;</pre>
private static uint PartialRead(uint target, int shift, int limit)
    if (shift < 0)</pre>
    {
        shift = 32 + shift;
    }
    if (limit < 0)</pre>
    {
        limit = 32 + limit;
    var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
    var targetMask = sourceMask << shift;</pre>
    return (target & targetMask) >> shift;
}
```

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178

```
private static Tuple<uint, uint, int> GetWriteMasksAndShift(int shift, int limit)
179
                  if (shift < 0)</pre>
181
                  {
182
                      shift = 32 + shift;
183
184
                  if (limit < 0)</pre>
185
                  {
                      limit = 32 + limit;
187
                  }
188
                 var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
var targetMask = ~(sourceMask << shift);</pre>
189
190
                  return new Tuple<uint, uint, int>(targetMask, sourceMask, shift);
191
             }
192
193
             private static Tuple<uint, int> GetReadMaskAndShift(int shift, int limit)
195
                  if (shift < 0)</pre>
196
                      shift = 32 + shift:
198
199
                  if (limit < 0)</pre>
                  {
201
                      limit = 32 + limit;
202
                  }
203
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
204
                  var targetMask = sourceMask << shift;</pre>
205
206
                  return new Tuple<uint, int>(targetMask, shift);
207
208
             private static uint PartialWrite(uint target, uint targetMask, uint source, uint
209
              → sourceMask, int shift) => target & targetMask | (source & sourceMask) << shift;</p>
210
             private static uint PartialWrite(uint target, uint source, Tuple<uint, uint, int>
211
              masksAndShift) => PartialWrite(target, masksAndShift.Item1, source,
                 masksAndShift.Item2, masksAndShift.Item3);
             private static uint PartialRead(uint target, uint targetMask, int shift) => (target &
213

    targetMask) >> shift;

             private static uint PartialRead(uint target, Tuple<uint, int> masksAndShift) =>
              PartialRead(target, masksAndShift.Item1, masksAndShift.Item2);
216
             [Fact]
217
             public static void BugWithLoadingConstantOf8Test()
218
219
                  Bit<byte>.PartialWrite(0, 1, 5, -5);
             }
221
         }
222
223
1.13
       ./csharp/Platform.Numbers.Tests/MathExtensionsTests.cs
    using Xunit;
 2
    namespace Platform.Numbers.Tests
 3
 4
         public static class MathExtensionsTests
 6
             [Fact]
             public static void AbsTest()
                  var number = -1L;
10
                  var returnValue = number.Abs();
                  Assert.Equal(1L, returnValue);
12
                  Assert.Equal(1L, number);
13
             }
15
             [Fact]
16
             public static void NegateTest()
17
18
                 var number = 2L;
19
                  var returnValue = number.Negate();
20
                  Assert.Equal(-2L, returnValue);
21
                  Assert.Equal(-2L, number);
22
             }
23
             [Fact]
             public static void UnsignedNegateTest()
26
```

```
var number = 2UL;
28
                var returnValue = number.Negate();
                Assert.Equal(18446744073709551614, returnValue);
30
                Assert.Equal(18446744073709551614, number);
31
            }
       }
33
34
     ./csharp/Platform.Numbers.Tests/MathTests.cs
1.14
  using Xunit;
   namespace Platform.Numbers.Tests
3
        public static class MathTests
5
6
            [Fact]
            public static void CompiledOperationsTest()
                Assert.True(Math.Abs(Arithmetic<double>.Subtract(3D, 2D) - 1D) < 0.01);
10
            }
11
       }
12
13
     ./csharp/Platform.Numbers.Tests/SystemTests.cs
1.15
  using Xunit;
   namespace Platform.Numbers.Tests
3
        public static class SystemTests
5
6
            [Fact]
            public static void PossiblePackTwoValuesIntoOneTest()
                uint value = 0;
11
                // Set one to first bit
12
                value |= 1;
13
14
                Assert.True(value == 1);
16
                // Set zero to first bit
17
                value &= OxFFFFFFE;
18
19
                // Get first bit
20
                uint read = value & 1;
21
                Assert.True(read == 0);
23
24
                uint firstValue = 1;
25
                uint secondValue = 1543;
27
                // Pack (join) two values at the same time
                value = (secondValue << 1) | firstValue;</pre>
29
                uint unpackagedFirstValue = value & 1;
31
                uint unpackagedSecondValue = (value & 0xFFFFFFFE) >> 1;
32
33
                Assert.True(firstValue == unpackagedFirstValue);
34
                Assert.True(secondValue == unpackagedSecondValue);
36
                // Using universal functions:
38
                Assert.True(PartialRead(value, 0, 1) == firstValue);
39
                Assert.True(PartialRead(value, 1, -1) == secondValue);
41
                firstValue = 0;
42
                secondValue = 6892;
43
44
                value = PartialWrite(value, firstValue, 0, 1);
45
                value = PartialWrite(value, secondValue, 1, -1);
47
                Assert.True(PartialRead(value, 0, 1) == firstValue);
                Assert.True(PartialRead(value, 1, -1) == secondValue);
49
            }
50
51
            private static uint PartialWrite(uint target, uint source, int shift, int limit)
52
                if (shift < 0)</pre>
55
                    shift = 32 + shift;
```

```
57
                     if (limit < 0)</pre>
59
                           limit = 32 + limit;
                     }
61
                     var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
var targetMask = ~(sourceMask << shift);
return (target & targetMask) | ((source & sourceMask) << shift);</pre>
62
63
64
65
66
               private static uint PartialRead(uint target, int shift, int limit)
67
68
69
                     if (shift < 0)</pre>
                     {
70
                           shift = 32 + shift;
71
                     if (limit < 0)
{</pre>
73
74
                           limit = 32 + limit;
75
                     }
76
                     var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
77
                     var targetMask = sourceMask << shift;</pre>
78
                     return (target & targetMask) >> shift;
79
               }
80
          }
81
   }
82
```

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