1.1 ./Platform.Numbers/Arithmetic.cs

```
using System;
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class Arithmetic
    {
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Add<T>(T x, T y) => Arithmetic<T>.Add(x, y);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Subtract<T>(T x, T y) => Arithmetic<T>.Subtract(x, y);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        [Obsolete]
        public static T Subtract<T>(Integer<T> x, Integer<T> y) => Arithmetic<T>.Subtract(x, y);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Increment<T>(T x) => Arithmetic<T>.Increment(x);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Decrement<T>(T x) => Arithmetic<T>.Decrement(x);
    }
}
```

1.2 ./Platform.Numbers/ArithmeticExtensions.cs

```
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class ArithmeticExtensions
    {
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Decrement<T>(this ref T x) where T : struct => x =
        ↪  Arithmetic<T>.Decrement(x);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Increment<T>(this ref T x) where T : struct => x =
        ↪  Arithmetic<T>.Increment(x);
    }
}
```

1.3 ./Platform.Numbers/Arithmetic[T].cs

```
using System;
using System.Runtime.CompilerServices;
using Platform.Exceptions;
using Platform.Reflection;

// ReSharper disable StaticFieldInGenericType
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class Arithmetic<T>
    {
        public static readonly Func<T, T, T> Add = CompileAddDelegate();
        public static readonly Func<T, T, T> Subtract = CompileSubtractDelegate();
        public static readonly Func<T, T> Increment = CompileIncrementDelegate();
        public static readonly Func<T, T> Decrement = CompileDecrementDelegate();

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T, T> CompileAddDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0, 1);
                emiter.Add();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

```
        private static Func<T, T, T> CompileSubtractDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0, 1);
                emiter.Subtract();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T> CompileIncrementDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArgument(0);
                emiter.Increment<T>();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T> CompileDecrementDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArgument(0);
                emiter.Decrement<T>();
                emiter.Return();
            });
        }
    }
}
```

1.4 ./Platform.Numbers/Bit.cs

```
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class Bit
    {
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static long Count(long x)
        {
            long n = 0;
            while (x != 0)
            {
                n++;
                x &= x - 1;
            }
            return n;
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static int GetLowestPosition(ulong value)
        {
            if (value == 0)
            {
                return -1;
            }
            var position = 0;
            while ((value & 1UL) == 0)
            {
                value >>= 1;
                ++position;
            }
            return position;
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Not<T>(T x) => Bit<T>.Not(x);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Or<T>(T x, T y) => Bit<T>.Or(x, y);
```

```

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T And<T>(T x, T y) => Bit<T>.And(x, y);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T ShiftLeft<T>(T x, int y) => Bit<T>.ShiftLeft(x, y);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T ShiftRight<T>(T x, int y) => Bit<T>.ShiftRight(x, y);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T PartialWrite<T>(T target, T source, int shift, int limit) =>
        ↪  Bit<T>.PartialWrite(target, source, shift, limit);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T PartialRead<T>(T target, int shift, int limit) =>
        ↪  Bit<T>.PartialRead(target, shift, limit);
    }
}
```

1.5 ./Platform.Numbers/BitExtensions.cs

```
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class BitwiseExtensions
    {
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Not<T>(this ref T target) where T : struct => target = Bit.Not(target);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T PartialWrite<T>(this ref T target, T source, int shift, int limit) where
        ↪  T : struct => target = Bit<T>.PartialWrite(target, source, shift, limit);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T PartialRead<T>(this T target, int shift, int limit) =>
        ↪  Bit<T>.PartialRead(target, shift, limit);
    }
}
```

1.6 ./Platform.Numbers/Bit[T].cs

```
using System;
using System.Runtime.CompilerServices;
using Platform.Exceptions;
using Platform.Reflection;

// ReSharper disable StaticFieldInGenericType
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class Bit<T>
    {
        public static readonly Func<T, T> Not = CompileNotDelegate();
        public static readonly Func<T, T, T> Or = CompileOrDelegate();
        public static readonly Func<T, T, T> And = CompileAndDelegate();
        public static readonly Func<T, int, T> ShiftLeft = CompileShiftLeftDelegate();
        public static readonly Func<T, int, T> ShiftRight = CompileShiftRightDelegate();
        public static readonly Func<T, T, int, int, T> PartialWrite =
        ↪  CompilePartialWriteDelegate();
        public static readonly Func<T, int, int, T> PartialRead = CompilePartialReadDelegate();

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T> CompileNotDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0);
                emiter.Not();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T, T> CompileOrDelegate()
        {
```

```
            return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0, 1);
                emiter.Or();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T, T> CompileAndDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0, 1);
                emiter.And();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, int, T> CompileShiftLeftDelegate()
        {
            return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0, 1);
                emiter.ShiftLeft();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, int, T> CompileShiftRightDelegate()
        {
            return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArguments(0, 1);
                emiter.ShiftRight();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T, int, int, T> CompilePartialWriteDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T, int, int, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                var constants = GetConstants();
                var bitsNumber = constants.Item1;
                var numberFilledWithOnes = constants.Item2;
                ushort shiftArgument = 2;
                ushort limitArgument = 3;
                var checkLimit = emiter.DefineLabel();
                var calculateSourceMask = emiter.DefineLabel();
                // Check shift
                emiter.LoadArgument(shiftArgument);
                emiter.LoadConstant(0);
                emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
                // Fix shift
                emiter.LoadConstant(bitsNumber);
                emiter.LoadArgument(shiftArgument);
                emiter.Add();
                emiter.StoreArgument(shiftArgument);
                emiter.MarkLabel(checkLimit);
                // Check limit
                emiter.LoadArgument(limitArgument);
                emiter.LoadConstant(0);
                emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
                // Fix limit
                emiter.LoadConstant(bitsNumber);
                emiter.LoadArgument(limitArgument);
                emiter.Add();
                emiter.StoreArgument(limitArgument);
                emiter.MarkLabel(calculateSourceMask);
```

```
                var sourceMask = emiter.DeclareLocal<T>();
                var targetMask = emiter.DeclareLocal<T>();
                emiter.LoadConstant(typeof(T), numberFilledWithOnes);
                emiter.LoadArgument(limitArgument);
                emiter.ShiftLeft();
                emiter.Not();
                emiter.LoadConstant(typeof(T), numberFilledWithOnes);
                emiter.And();
                emiter.StoreLocal(sourceMask);
                emiter.LoadLocal(sourceMask);
                emiter.LoadArgument(shiftArgument);
                emiter.ShiftLeft();
                emiter.Not();
                emiter.StoreLocal(targetMask);
                emiter.LoadArgument(0); // target
                emiter.LoadLocal(targetMask);
                emiter.And();
                emiter.LoadArgument(1); // source
                emiter.LoadLocal(sourceMask);
                emiter.And();
                emiter.LoadArgument(shiftArgument);
                emiter.ShiftLeft();
                emiter.Or();
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, int, int, T> CompilePartialReadDelegate()
        {
            return DelegateHelpers.Compile<Func<T, int, int, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                var constants = GetConstants();
                var bitsNumber = constants.Item1;
                var numberFilledWithOnes = constants.Item2;
                ushort shiftArgument = 1;
                ushort limitArgument = 2;
                var checkLimit = emiter.DefineLabel();
                var calculateSourceMask = emiter.DefineLabel();
                // Check shift
                emiter.LoadArgument(shiftArgument);
                emiter.LoadConstant(0);
                emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
                // Fix shift
                emiter.LoadConstant(bitsNumber);
                emiter.LoadArgument(shiftArgument);
                emiter.Add();
                emiter.StoreArgument(shiftArgument);
                emiter.MarkLabel(checkLimit);
                // Check limit
                emiter.LoadArgument(limitArgument);
                emiter.LoadConstant(0);
                emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
                // Fix limit
                emiter.LoadConstant(bitsNumber);
                emiter.LoadArgument(limitArgument);
                emiter.Add();
                emiter.StoreArgument(limitArgument);
                emiter.MarkLabel(calculateSourceMask);
                var sourceMask = emiter.DeclareLocal<T>();
                var targetMask = emiter.DeclareLocal<T>();
                emiter.LoadConstant(typeof(T), numberFilledWithOnes);
                emiter.LoadArgument(limitArgument); // limit
                emiter.ShiftLeft();
                emiter.Not();
                emiter.LoadConstant(typeof(T), numberFilledWithOnes);
                emiter.And();
                emiter.StoreLocal(sourceMask);
                emiter.LoadLocal(sourceMask);
                emiter.LoadArgument(shiftArgument);
                emiter.ShiftLeft();
                emiter.StoreLocal(targetMask);
                emiter.LoadArgument(0); // target
                emiter.LoadLocal(targetMask);
                emiter.And();
                emiter.LoadArgument(shiftArgument);
                emiter.ShiftRight();
```

```
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Tuple<int, T> GetConstants()
        {
            var type = typeof(T);
            if (type == typeof(ulong))
            {
                return new Tuple<int, T>(64, (T)(object)ulong.MaxValue);
            }
            if (type == typeof(uint))
            {
                return new Tuple<int, T>(32, (T)(object)uint.MaxValue);
            }
            if (type == typeof(ushort))
            {
                return new Tuple<int, T>(16, (T)(object)ushort.MaxValue);
            }
            if (type == typeof(byte))
            {
                return new Tuple<int, T>(8, (T)(object)byte.MaxValue);
            }
            throw new NotSupportedException();
        }
    }
}
```

1.7 ./Platform.Numbers/Integer.cs

```
using System;
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    [Obsolete]
    public struct Integer : IEquatable<Integer>
    {
        public readonly ulong Value;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public Integer(ulong value) => Value = value;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(ulong integer) => new Integer(integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(long integer) => unchecked((ulong)integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(uint integer) => new Integer(integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(int integer) => unchecked((ulong)integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(ushort integer) => new Integer(integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(short integer) => unchecked((ulong)integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(byte integer) => new Integer(integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(sbyte integer) => unchecked((ulong)integer);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(bool integer) => integer ? 1UL : 0UL;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator ulong(Integer integer) => integer.Value;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator long(Integer integer) => unchecked((long)integer.Value);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator uint(Integer integer) => unchecked((uint)integer.Value);
```

```

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator int(Integer integer) => unchecked((int)integer.Value);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator ushort(Integer integer) =>
        ↪  unchecked((ushort)integer.Value);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator short(Integer integer) =>
        ↪  unchecked((short)integer.Value);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator byte(Integer integer) => unchecked((byte)integer.Value);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator sbyte(Integer integer) =>
        ↪  unchecked((sbyte)integer.Value);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator bool(Integer integer) => integer.Value != OUL;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public bool Equals(Integer other) => Value == other.Value;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public override string ToString() => Value.ToString();
    }
}
```

1.8 ./Platform.Numbers/Integer[T].cs

```
using System;
using System.Runtime.CompilerServices;
using System.Collections.Generic;
using Platform.Exceptions;
using Platform.Reflection;

// ReSharper disable StaticFieldInGenericType
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
#pragma warning disable RECS0108 // Warns about static fields in generic types

namespace Platform.Numbers
{
    [Obsolete]
    public struct Integer<T> : IEquatable<Integer<T>>
    {
        private static readonly EqualityComparer<T> _equalityComparer =
        ↪  EqualityComparer<T>.Default;
        private static readonly Func<ulong, Integer<T>> _create;

        public static readonly T Zero;
        public static readonly T One;
        public static readonly T Two;

        public readonly T Value;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        static Integer()
        {
            _create = CompileCreateDelegate();
            try
            {
                Zero = default;
                One = Arithmetic.Increment(Zero);
                Two = Arithmetic.Increment(One);
            }
            catch (Exception exception)
            {
                exception.Ignore();
            }
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public Integer(T value) => Value = value;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static implicit operator Integer(Integer<T> integer)
        {
            if (typeof(T) == typeof(Integer))
            {
```

```
            return (Integer)(object)integer.Value;
        }
        return Convert.ToUInt64(integer.Value);
    }

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator ulong(Integer<T> integer) => ((Integer)integer).Value;

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator T(Integer<T> integer) => integer.Value;

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(T integer) => new Integer<T>(integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(ulong integer) => _create(integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(Integer integer) => _create(integer.Value);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(long integer) => unchecked((ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(uint integer) => new Integer(integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(int integer) => unchecked((ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(ushort integer) => new Integer(integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(short integer) => unchecked((ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(byte integer) => new Integer(integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(sbyte integer) => unchecked((ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator Integer<T>(bool integer) => integer ? 1UL : 0UL;

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator long(Integer<T> integer) =>
    ↪  unchecked((long)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator uint(Integer<T> integer) =>
    ↪  unchecked((uint)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator int(Integer<T> integer) =>
    ↪  unchecked((int)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator ushort(Integer<T> integer) =>
    ↪  unchecked((ushort)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator short(Integer<T> integer) =>
    ↪  unchecked((short)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator byte(Integer<T> integer) =>
    ↪  unchecked((byte)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator sbyte(Integer<T> integer) =>
    ↪  unchecked((sbyte)(ulong)integer);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public static implicit operator bool(Integer<T> integer) => integer != 0UL;

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public bool Equals(Integer<T> other) => _equalityComparer.Equals(Value, other.Value);

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

```
        public override string ToString() => Value.ToString();

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<ulong, Integer<T>> CompileCreateDelegate()
        {
            return DelegateHelpers.Compile<Func<ulong, Integer<T>>>(emiter =>
            {
                if (typeof(T) != typeof(Integer))
                {
                    Ensure.Always.CanBeNumeric<T>();
                }
                emiter.LoadArgument(0);
                if (typeof(T) != typeof(ulong) && typeof(T) != typeof(Integer))
                {
                    emiter.UncheckedConvert<ulong, T>();
                    //emiter.Call(typeof(To).GetMethod(typeof(T).Name, Types<ulong>.Array));
                }
                if (NumericType<T>.IsNullable)
                {
                    emiter.NewObject(typeof(T), NumericType<T>.UnderlyingType);
                }
                if (typeof(T) == typeof(Integer))
                {
                    emiter.NewObject(typeof(Integer), typeof(ulong));
                }
                emiter.NewObject(typeof(Integer<T>), typeof(T));
                emiter.Return();
            });
        }
    }
}
```

1.9 ./Platform.Numbers/Math.cs

```
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    /// <remarks>
    /// Resizable array (FileMappedMemory) for values cache may be used. or cached oeis.org
    /// </remarks>
    public static class Math
    {
        /// <remarks>
        /// <para>Source: https://oeis.org/A000142/list </para>
        /// <para>Источник: https://oeis.org/A000142/list </para>
        /// </remarks>
        private static readonly double[] _factorials =
        {
            1D, 1D, 2D, 6D, 24D, 120D, 720D, 5040D, 40320D, 362880D, 3628800D, 39916800D,
            479001600, 6227020800, 87178291200, 1307674368000D, 20922789888000D,
            355687428096000D, 6402373705728000D, 121645100408832000D, 2432902008176640000D,
            51090942171709440000D, 1124000727777607680000D
        };

        /// <remarks>
        /// <para>Source: https://oeis.org/A000108/list </para>
        /// <para>Источник: https://oeis.org/A000108/list </para>
        /// </remarks>
        private static readonly double[] _catalans =
        {
            1D,   1D,   2D,   5D,   14D,   42D,   132D,   429D,   1430D,   4862D,   16796D,   58786D,
            ↪  208012D,
            742900D,   2674440D,   9694845D,   35357670D,   129644790D,   477638700D,   1767263190D,
            6564120420D,   24466267020D,   91482563640D,   343059613650D,   1289904147324D,
            ↪  4861946401452D,
            18367353072152D,   69533550916004D,   263747951750360D,   1002242216651368D,
            ↪  3814986502092304D
        };

        public static double Factorial(double n)
        {
            if (n <= 1)
            {
                return 1;
            }
            if (n < _factorials.Length)
            {
```

```
                return _factorials[(int)n];
            }
            return n * Factorial(n - 1);
        }

        public static double Catalan(double n)
        {
            if (n <= 1)
            {
                return 1;
            }
            if (n < _catalans.Length)
            {
                return _catalans[(int)n];
            }
            return Factorial(2 * n) / (Factorial(n + 1) * Factorial(n));
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static bool IsPowerOfTwo(ulong x) => (x & x - 1) == 0;

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Abs<T>(T x) => Math<T>.Abs(x);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Negate<T>(T x) => Math<T>.Negate(x);
    }
}
```

1.10 ./Platform.Numbers/MathExtensions.cs

```
using System.Runtime.CompilerServices;

#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class MathExtensions
    {
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Abs<T>(this ref T x) where T : struct => x = Math<T>.Abs(x);

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public static T Negate<T>(this ref T x) where T : struct => x = Math<T>.Negate(x);
    }
}
```

1.11 ./Platform.Numbers/Math[T].cs

```
using System;
using System.Runtime.CompilerServices;
using Platform.Exceptions;
using Platform.Reflection;

// ReSharper disable StaticFieldInGenericType
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

namespace Platform.Numbers
{
    public static class Math<T>
    {
        public static readonly Func<T, T> Abs = CompileAbsDelegate();
        public static readonly Func<T, T> Negate = CompileNegateDelegate();

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T> CompileAbsDelegate()
        {
            return DelegateHelpers.Compile<Func<T, T>>(emiter =>
            {
                Ensure.Always.IsNumeric<T>();
                emiter.LoadArgument(0);
                if (NumericType<T>.IsSigned)
                {
                    emiter.Call(typeof(System.Math).GetMethod("Abs", Types<T>.Array));
                }
                emiter.Return();
            });
        }

        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        private static Func<T, T> CompileNegateDelegate()
```

```
        {
            return DelegateHelpers.Compile<Func<T, T>>(emiter =>
            {
                emiter.LoadArgument(0);
                emiter.Negate();
                emiter.Return();
            });
        }
    }
}
```

1.12 ./Platform.Numbers.Tests/ArithmeticExtensionsTests.cs

```
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class ArithmeticExtensionsTests
    {
        [Fact]
        public static void IncrementTest()
        {
            var number = 0UL;
            var returnValue = number.Increment();
            Assert.Equal(1UL, returnValue);
            Assert.Equal(1UL, number);
        }

        [Fact]
        public static void DecrementTest()
        {
            var number = 1UL;
            var returnValue = number.Decrement();
            Assert.Equal(0UL, returnValue);
            Assert.Equal(0UL, number);
        }
    }
}
```

1.13 ./Platform.Numbers.Tests/ArithmeticTests.cs

```
using System;
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class ArithmeticTests
    {
        [Fact]
        public static void CompiledOperationsTest()
        {
            Assert.True(Arithmetic<short>.Add(1, 2) == 3);
            Assert.True(Arithmetic<short>.Subtract(2, 1) == 1);
            Assert.True(Arithmetic<byte>.Increment(1) == 2);
            Assert.True(Arithmetic<ulong>.Decrement(2) == 1);
            Assert.Throws<NotSupportedException>(() => Arithmetic<string>.Subtract("1", "2"));
        }
    }
}
```

1.14 ./Platform.Numbers.Tests/BitTests.cs

```
using System;
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class BitTests
    {
        [Theory]
        [InlineData(00, -1)] // 0000 0000 (none, -1)
        [InlineData(01, 00)] // 0000 0001 (first, 0)
        [InlineData(08, 03)] // 0000 1000 (forth, 3)
        [InlineData(88, 03)] // 0101 1000 (forth, 3)
        public static void GetLowestBitPositionTest(ulong value, int expectedPosition)
        {
            Assert.True(Bit.GetLowestPosition(value) == expectedPosition);
        }

        [Fact]
        public static void ByteBitwiseOperationsTest()
```

```
        {
            Assert.True(Bit<byte>.Not(2) == unchecked((byte)~2));
            Assert.True(Bit<byte>.Or(1, 2) == (1 | 2));
            Assert.True(Bit<byte>.And(1, 2) == (1 & 2));
            Assert.True(Bit<byte>.ShiftLeft(1, 2) == (1 << 2));
            Assert.True(Bit<byte>.ShiftRight(1, 2) == (1 >> 2));
        }

        [Fact]
        public static void UInt16BitwiseOperationsTest()
        {
            Assert.True(Bit<ushort>.Not(2) == unchecked((ushort)~2));
            Assert.True(Bit<ushort>.Or(1, 2) == (1 | 2));
            Assert.True(Bit<ushort>.And(1, 2) == (1 & 2));
            Assert.True(Bit<ushort>.ShiftLeft(1, 2) == (1 << 2));
            Assert.True(Bit<ushort>.ShiftRight(1, 2) == (1 >> 2));
        }

        [Fact]
        public static void UInt32BitwiseOperationsTest()
        {
            Assert.True(Bit<uint>.Not(2) == unchecked((uint)~2));
            Assert.True(Bit<uint>.Or(1, 2) == (1 | 2));
            Assert.True(Bit<uint>.And(1, 2) == (1 & 2));
            Assert.True(Bit<uint>.ShiftLeft(1, 2) == (1 << 2));
            Assert.True(Bit<uint>.ShiftRight(1, 2) == (1 >> 2));
        }

        [Fact]
        public static void UInt64BitwiseOperationsTest()
        {
            Assert.True(Bit<ulong>.Not(2) == unchecked((ulong)~2));
            Assert.True(Bit<ulong>.Or(1, 2) == (1 | 2));
            Assert.True(Bit<ulong>.And(1, 2) == (1 & 2));
            Assert.True(Bit<ulong>.ShiftLeft(1, 2) == (1 << 2));
            Assert.True(Bit<ulong>.ShiftRight(1, 2) == (1 >> 2));
        }

        [Fact]
        public static void PartialReadWriteTest()
        {
            {
                uint firstValue = 1;
                uint secondValue = 1543;

                // Pack (join) two values at the same time
                uint value = secondValue << 1 | firstValue;

                uint unpackagedFirstValue = value & 1;
                uint unpackagedSecondValue = (value & 0xFFFFFFFE) >> 1;

                Assert.True(firstValue == unpackagedFirstValue);
                Assert.True(secondValue == unpackagedSecondValue);

                // Using universal functions:
                Assert.True(PartialRead(value, 0, 1) == firstValue);
                Assert.True(PartialRead(value, 1, -1) == secondValue);

                firstValue = 0;
                secondValue = 6892;

                value = PartialWrite(value, firstValue, 0, 1);
                value = PartialWrite(value, secondValue, 1, -1);

                Assert.True(PartialRead(value, 0, 1) == firstValue);
                Assert.True(PartialRead(value, 1, -1) == secondValue);
            }

            {
                uint firstValue = 1;
                uint secondValue = 1543;

                // Pack (join) two values at the same time
                uint value = secondValue << 1 | firstValue;

                uint unpackagedFirstValue = value & 1;
                uint unpackagedSecondValue = (value & 0xFFFFFFFE) >> 1;

                Assert.True(firstValue == unpackagedFirstValue);
                Assert.True(secondValue == unpackagedSecondValue);
```

```
100
101                 // Using universal functions:
102                 Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
103                 Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
104
105                 firstValue = 0;
106                 secondValue = 6892;
107
108                 value = Bit.PartialWrite(value, firstValue, 0, 1);
109                 value = Bit.PartialWrite(value, secondValue, 1, -1);
110
111                 Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
112                 Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
113             }
114
115             {
116                 uint firstValue = 1;
117                 uint secondValue = 1543;
118
119                 // Pack (join) two values at the same time
120                 uint value = secondValue << 1 | firstValue;
121
122                 uint unpackagedFirstValue = value & 1;
123                 uint unpackagedSecondValue = (value & 0xFFFFFFFE) >> 1;
124
125                 Assert.True(firstValue == unpackagedFirstValue);
126                 Assert.True(secondValue == unpackagedSecondValue);
127
128                 // Using universal functions:
129                 var readMasksAndShiftFor0And1 = GetReadMaskAndShift(0, 1);
130                 var readMasksAndShiftFor1AndMinus1 = GetReadMaskAndShift(1, -1);
131                 var writeMasksAndShiftFor0And1 = GetWriteMasksAndShift(0, 1);
132                 var writeMasksAndShiftFor1AndMinus1 = GetWriteMasksAndShift(1, -1);
133
134                 Assert.True(PartialRead(value, readMasksAndShiftFor0And1) == firstValue);
135                 Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
136
137                 firstValue = 0;
138                 secondValue = 6892;
139
140                 value = PartialWrite(value, firstValue, writeMasksAndShiftFor0And1);
141                 value = PartialWrite(value, secondValue, writeMasksAndShiftFor1AndMinus1);
142
143                 Assert.True(PartialRead(value, readMasksAndShiftFor0And1) == firstValue);
144                 Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
145             }
146         }
147
148         // TODO: Can be optimized using precalculation of TargetMask and SourceMask
149         private static uint PartialWrite(uint target, uint source, int shift, int limit)
150         {
151             if (shift < 0)
152             {
153                 shift = 32 + shift;
154             }
155             if (limit < 0)
156             {
157                 limit = 32 + limit;
158             }
159             var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
160             var targetMask = ~(sourceMask << shift);
161             return target & targetMask | (source & sourceMask) << shift;
162         }
163
164         private static uint PartialRead(uint target, int shift, int limit)
165         {
166             if (shift < 0)
167             {
168                 shift = 32 + shift;
169             }
170             if (limit < 0)
171             {
172                 limit = 32 + limit;
173             }
174             var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
175             var targetMask = sourceMask << shift;
176             return (target & targetMask) >> shift;
177         }
178
179         private static Tuple<uint, uint, int> GetWriteMasksAndShift(int shift, int limit)
```

```
        {
            if (shift < 0)
            {
                shift = 32 + shift;
            }
            if (limit < 0)
            {
                limit = 32 + limit;
            }
            var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
            var targetMask = ~(sourceMask << shift);
            return new Tuple<uint, uint, int>(targetMask, sourceMask, shift);
        }

        private static Tuple<uint, int> GetReadMaskAndShift(int shift, int limit)
        {
            if (shift < 0)
            {
                shift = 32 + shift;
            }
            if (limit < 0)
            {
                limit = 32 + limit;
            }
            var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
            var targetMask = sourceMask << shift;
            return new Tuple<uint, int>(targetMask, shift);
        }

        private static uint PartialWrite(uint target, uint targetMask, uint source, uint
        ↪  sourceMask, int shift) => target & targetMask | (source & sourceMask) << shift;

        private static uint PartialWrite(uint target, uint source, Tuple<uint, uint, int>
        ↪  masksAndShift) => PartialWrite(target, masksAndShift.Item1, source,
        ↪  masksAndShift.Item2, masksAndShift.Item3);

        private static uint PartialRead(uint target, uint targetMask, int shift) => (target &
        ↪  targetMask) >> shift;

        private static uint PartialRead(uint target, Tuple<uint, int> masksAndShift) =>
        ↪  PartialRead(target, masksAndShift.Item1, masksAndShift.Item2);

        [Fact]
        public static void BugWithLoadingConstantOf8Test()
        {
            Bit<byte>.PartialWrite(0, 1, 5, -5);
        }
    }
}
```

1.15 ./Platform.Numbers.Tests/IntegerTests.cs

```
using System;
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class IntegerTests
    {
        [Fact]
        [Obsolete]
        public static void SignedIntegersTest()
        {
            var integer = -10;
            Assert.True(((Integer)integer) == -10L);
        }
    }
}
```

1.16 ./Platform.Numbers.Tests/MathExtensionsTests.cs

```
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class MathExtensionsTests
    {
        [Fact]
        public static void AbsTest()
        {
            var number = -1L;
```

```
            var returnValue = number.Abs();
            Assert.Equal(1L, returnValue);
            Assert.Equal(1L, number);
        }

        [Fact]
        public static void NegateTest()
        {
            var number = 2L;
            var returnValue = number.Negate();
            Assert.Equal(-2L, returnValue);
            Assert.Equal(-2L, number);
        }

        [Fact]
        public static void UnsignedNegateTest()
        {
            var number = 2UL;
            var returnValue = number.Negate();
            Assert.Equal(18446744073709551614, returnValue);
            Assert.Equal(18446744073709551614, number);
        }
    }
}
```

1.17 ./Platform.Numbers.Tests/MathTests.cs

```
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class MathTests
    {
        [Fact]
        public static void CompiledOperationsTest()
        {
            Assert.True(Math.Abs(Arithmetic<double>.Subtract(3D, 2D) - 1D) < 0.01);
        }
    }
}
```

1.18 ./Platform.Numbers.Tests/SystemTests.cs

```
using Xunit;

namespace Platform.Numbers.Tests
{
    public static class SystemTests
    {
        [Fact]
        public static void PossiblePackTwoValuesIntoOneTest()
        {
            uint value = 0;

            // Set one to first bit
            value |= 1;

            Assert.True(value == 1);

            // Set zero to first bit
            value &= 0xFFFFFFFE;

            // Get first bit
            uint read = value & 1;

            Assert.True(read == 0);

            uint firstValue = 1;
            uint secondValue = 1543;

            // Pack (join) two values at the same time
            value = (secondValue << 1) | firstValue;

            uint unpackagedFirstValue = value & 1;
            uint unpackagedSecondValue = (value & 0xFFFFFFFE) >> 1;

            Assert.True(firstValue == unpackagedFirstValue);
            Assert.True(secondValue == unpackagedSecondValue);

            // Using universal functions:

            Assert.True(PartialRead(value, 0, 1) == firstValue);
```

```
            Assert.True(PartialRead(value, 1, -1) == secondValue);

            firstValue = 0;
            secondValue = 6892;

            value = PartialWrite(value, firstValue, 0, 1);
            value = PartialWrite(value, secondValue, 1, -1);

            Assert.True(PartialRead(value, 0, 1) == firstValue);
            Assert.True(PartialRead(value, 1, -1) == secondValue);
        }

        private static uint PartialWrite(uint target, uint source, int shift, int limit)
        {
            if (shift < 0)
            {
                shift = 32 + shift;
            }
            if (limit < 0)
            {
                limit = 32 + limit;
            }
            var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
            var targetMask = ~(sourceMask << shift);
            return (target & targetMask) | ((source & sourceMask) << shift);
        }

        private static uint PartialRead(uint target, int shift, int limit)
        {
            if (shift < 0)
            {
                shift = 32 + shift;
            }
            if (limit < 0)
            {
                limit = 32 + limit;
            }
            var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;
            var targetMask = sourceMask << shift;
            return (target & targetMask) >> shift;
        }
    }
}
```

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