```
LinksPlatform's Platform Numbers Class Library
     ./csharp/Platform.Numbers/Arithmetic.cs
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
6
        public static class Arithmetic
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
9
            public static T Add<T>(T x, T y) => Arithmetic<T>.Add(x, y);
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            public static T Subtract<T>(T x, T y) => Arithmetic<T>.Subtract(x, y);
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            public static T Multiply<T>(T x, T y) => Arithmetic<T>.Multiply(x, y);
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Divide<T>(T x, T y) => Arithmetic<T>.Divide(x, y);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            public static T Increment<T>(T x) => Arithmetic<T>.Increment(x);
22
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
            public static T Increment<T>(ref T x) => x = Arithmetic<T>.Increment(x);
25
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            public static T Decrement<T>(T x) => Arithmetic<T>.Decrement(x);
28
29
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            public static T Decrement<T>(ref T x) => x = Arithmetic<T>.Decrement(x);
        }
32
33
     ./csharp/Platform.Numbers/ArithmeticExtensions.cs
1.2
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
   {
        public static class ArithmeticExtensions
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Decrement<T>(this ref T x) where T : struct => x =
10
             → Arithmetic<T>.Decrement(x);
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Increment<T>(this ref T x) where T : struct => x =
13
                Arithmetic<T>.Increment(x);
14
   }
15
    ./csharp/Platform.Numbers/Arithmetic[T].cs
1.3
   using System;
using System.Reflection.Emit;
   using System.Runtime.CompilerServices;
   using Platform. Exceptions;
   using Platform.Reflection;
   // ReSharper disable StaticFieldInGenericType
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform. Numbers
10
   {
11
        public static class Arithmetic<T>
12
13
            public static readonly Func<T, T, T> Add = CompileAddDelegate();
public static readonly Func<T, T, T> Subtract = CompileSubtractDelegate();
public static readonly Func<T, T, T> Multiply = CompileMultiplyDelegate();
14
16
            public static readonly Func<T, T, T> Divide = CompileDivideDelegate();
17
            public static readonly Func<T, T> Increment = CompileIncrementDelegate();
            public static readonly Func<T, T> Decrement = CompileDecrementDelegate();
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T, T> CompileAddDelegate()
22
```

```
return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.Add();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T, T> CompileSubtractDelegate()
    return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.Subtract();
        emiter.Return();
    });
[{\tt MethodImpl}({\tt MethodImpl}{\tt Options}. {\tt AggressiveInlining}) \, ]
private static Func<T, T, T> CompileMultiplyDelegate()
    return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.Emit(OpCodes.Mul);
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T, T> CompileDivideDelegate()
    return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1)
        if(NumericType<T>.IsSigned)
            emiter.Emit(OpCodes.Div);
        else
            emiter.Emit(OpCodes.Div_Un);
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T> CompileIncrementDelegate()
    return DelegateHelpers.Compile<Func<T, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArgument(0);
        emiter.Increment<T>();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T> CompileDecrementDelegate()
    return DelegateHelpers.Compile<Func<T, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArgument(0);
        emiter.Decrement<T>();
        emiter.Return();
    });
}
```

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93 94

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99

100

}

```
./csharp/Platform.Numbers/Bit.cs
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
4
   namespace Platform.Numbers
6
       public static class Bit
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
9
10
            public static long Count(long x)
11
                long n = 0;
12
                while (x != 0)
14
                    n++;
                    x &= x - 1;
16
17
                return n;
18
            }
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            public static int GetLowestPosition(ulong value)
23
                if (value == 0)
24
25
                    return -1;
26
27
                var position = 0;
28
                while ((value & 1UL) == 0)
29
                    value >>= 1;
31
                    ++position;
33
34
                return position;
            }
35
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
37
            public static T Not<T>(T x) => Bit<T>.Not(x);
38
39
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
40
            public static T Or<T>(T x, T y) => Bit<T>.Or(x, y);
41
42
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
43
            public static T And<T>(T x, T y) => Bit<T>.And(x, y);
44
45
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
46
            public static T ShiftLeft<T>(T x, int y) => Bit<T>.ShiftLeft(x, y);
48
49
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T ShiftRight<T>(T x, int y) => Bit<T>.ShiftRight(x, y);
50
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T PartialWrite<T>(T target, T source, int shift, int limit) =>
5.3
            \rightarrow Bit<T>.PartialWrite(target, source, shift, limit);
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
55
            public static T PartialRead<T>(T target, int shift, int limit) =>
56
            → Bit<T>.PartialRead(target, shift, limit);
        }
     ./csharp/Platform.Numbers/BitExtensions.cs
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
4
   namespace Platform. Numbers
   {
6
        public static class BitwiseExtensions
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Not<T>(this ref T target) where T : struct => target = Bit.Not(target);
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            public static T PartialWrite<T>(this ref T target, T source, int shift, int limit) where
13
               T : struct => target = Bit<T>.PartialWrite(target, source, shift, limit);
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

```
public static T PartialRead<T>(this T target, int shift, int limit) =>
16

→ Bit<T>.PartialRead(target, shift, limit);
        }
17
    }
18
1.6
    ./csharp/Platform.Numbers/Bit|T|.cs
   using System;
   using System.Runtime.CompilerServices;
using Platform.Exceptions;
3
   using Platform. Reflection;
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform. Numbers
9
10
        public static class Bit<T>
11
12
             public static readonly Func<T, T> Not = CompileNotDelegate();
13
             public static readonly Func<T, T, T> Or = CompileOrDelegate()
             public static readonly Func<T, T, T> And = CompileAndDelegate();
15
            public static readonly Func<T, int, T> ShiftLeft = CompileShiftLeftDelegate();
public static readonly Func<T, int, T> ShiftRight = CompileShiftRightDelegate();
16
            public static readonly Func<T, int, T> ShiftRight = CompileSh
public static readonly Func<T, T, int, int, T> PartialWrite =
18
                 CompilePartialWriteDelegate();
             public static readonly Func<T, int, int, T> PartialRead = CompilePartialReadDelegate();
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             private static Func<T, T> CompileNotDelegate()
22
23
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
2.4
                      Ensure.Always.IsNumeric<T>();
                      emiter.LoadArguments(0);
27
                      emiter.Not();
28
                      emiter.Return();
                 });
30
             }
31
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
             private static Func<T, T, T> CompileOrDelegate()
34
35
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
37
                      Ensure.Always.IsNumeric<T>();
38
39
                      emiter.LoadArguments(0, 1);
                      emiter.Or();
40
                      emiter.Return();
41
                 });
42
             }
43
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
             private static Func<T, T, T> CompileAndDelegate()
46
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
                 {
49
                      Ensure.Always.IsNumeric<T>();
50
                      emiter.LoadArguments(0, 1);
                      emiter.And();
52
                      emiter.Return();
53
                 });
54
             }
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
58
             private static Func<T, int, T> CompileShiftLeftDelegate()
59
                 return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
60
61
                      Ensure.Always.IsNumeric<T>();
62
                      emiter.LoadArguments(0, 1);
63
                      emiter.ShiftLeft();
                      emiter.Return();
65
                 });
66
68
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
             private static Func<T, int, T> CompileShiftRightDelegate()
71
                 return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
```

```
Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.ShiftRight();
        emiter.Return();
    });
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T, int, int, T> CompilePartialWriteDelegate()
    return DelegateHelpers.Compile<Func<T, T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>()
        var constants = GetConstants();
        var bitsNumber = constants.Item1;
        var numberFilledWithOnes = constants.Item2;
        ushort shiftArgument = 2
        ushort limitArgument = 3
        var checkLimit = emiter.DefineLabel();
        var calculateSourceMask = emiter.DefineLabel();
        // Check shift
        emiter.LoadArgument(shiftArgument);
        emiter.LoadConstant(0)
        emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
        // Fix shift
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(shiftArgument);
        emiter.Add()
        emiter.StoreArgument(shiftArgument);
        emiter.MarkLabel(checkLimit);
        // Check limit
        emiter.LoadArgument(limitArgument);
        emiter.LoadConstant(0);
        emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
        // Fix limit
        emiter.LoadConstant(bitsNumber)
        emiter.LoadArgument(limitArgument);
        emiter.Add()
        emiter.StoreArgument(limitArgument);
        emiter.MarkLabel(calculateSourceMask);
        var sourceMask = emiter.DeclareLocal<T>();
        var targetMask = emiter.DeclareLocal<T>();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.LoadArgument(limitArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.And();
        emiter.StoreLocal(sourceMask);
        emiter.LoadLocal(sourceMask);
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.StoreLocal(targetMask);
        emiter.LoadArgument(0); // target
        emiter.LoadLocal(targetMask);
        emiter.And();
        emiter.LoadArgument(1); // source
        emiter.LoadLocal(sourceMask);
        emiter.And();
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Or();
        emiter.Return();
    });
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, int, int, T> CompilePartialReadDelegate()
    return DelegateHelpers.Compile<Func<T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        var constants = GetConstants();
        var bitsNumber = constants.Item1;
        var numberFilledWithOnes = constants.Item2;
        ushort shiftArgument = 1;
```

7.3

7.5

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136 137

139 140

141

142 143

145

146

148

149

150

```
ushort limitArgument = 2;
151
                      var checkLimit = emiter.DefineLabel();
                     var calculateSourceMask = emiter.DefineLabel();
153
                     // Check shift
154
                     emiter.LoadArgument(shiftArgument);
                     emiter.LoadConstant(0)
156
                     emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
157
                      // Fix shift
158
                     emiter.LoadConstant(bitsNumber);
                     emiter.LoadArgument(shiftArgument);
160
                     emiter.Add():
161
                     emiter.StoreArgument(shiftArgument);
162
                     emiter.MarkLabel(checkLimit);
163
                      // Check limit
164
                     emiter.LoadArgument(limitArgument);
165
                      emiter.LoadConstant(0)
                     emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
167
                     // Fix limit
168
                     emiter.LoadConstant(bitsNumber);
169
                     emiter.LoadArgument(limitArgument);
170
                     emiter.Add()
171
                     emiter.StoreArgument(limitArgument)
172
                     emiter.MarkLabel(calculateSourceMask)
                     var sourceMask = emiter.DeclareLocal<T>();
174
                     var targetMask = emiter.DeclareLocal<T>();
175
                     emiter.LoadConstant(typeof(T), numberFilledWithOnes);
                     emiter.LoadArgument(limitArgument); // limit
177
                     emiter.ShiftLeft();
178
                     emiter.Not();
179
                      emiter.LoadConstant(typeof(T), numberFilledWithOnes);
180
                     emiter.And();
181
                     emiter.StoreLocal(sourceMask);
182
                     emiter.LoadLocal(sourceMask);
183
                     emiter.LoadArgument(shiftArgument);
184
                     emiter.ShiftLeft();
185
                     emiter.StoreLocal(targetMask);
186
                     emiter.LoadArgument(0); // target
                     emiter.LoadLocal(targetMask);
188
                     emiter.And();
189
                     emiter.LoadArgument(shiftArgument);
                     emiter.ShiftRight();
191
                     emiter.Return();
192
                 });
193
             }
195
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             private static Tuple<int, T> GetConstants()
197
198
                 var type = typeof(T);
199
                 if (type == typeof(ulong))
201
                     return new Tuple<int, T>(64, (T)(object)ulong.MaxValue);
202
                 }
                 if (type == typeof(uint))
204
205
                     return new Tuple<int, T>(32, (T)(object)uint.MaxValue);
206
                 }
207
                 if
                    (type == typeof(ushort))
208
                 {
209
                     return new Tuple<int, T>(16, (T)(object)ushort.MaxValue);
210
211
                    (type == typeof(byte))
212
213
                     return new Tuple<int, T>(8, (T)(object)byte.MaxValue);
214
215
                 throw new NotSupportedException();
216
             }
217
        }
218
219
      ./csharp/Platform.Numbers/Math.cs
1.7
    using System;
          System.Collections.Generic;
    using
    using System.Linq;
 3
    using System.Runtime.CompilerServices;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
```

```
namespace Platform. Numbers
8
9
        /// <remarks>
10
        /// Resizable array (FileMappedMemory) for values cache may be used. or cached oeis.org
11
        /// </remarks>
        public static class Math
13
14
             /// <remarks>
15
             /// <para>Source: https://oeis.org/A000142/list </para>
16
             /// <para>Источник: https://oeis.org/A000142/list </para>
17
             /// </remarks>
18
             private static readonly long[] _factorials =
19
20
                 1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800, 39916800, 479001600, 6227020800, 87178291200, 1307674368000, 20922789888000
21
22
                 355687428096000, 6402373705728000, 121645100408832000, 2432902008176640000,
23
             };
24
25
             /// <remarks>
26
             /// <para>Source: https://oeis.org/A000108/list </para>
             /// <para>Источник: https://oeis.org/A000108/list </para>
             /// </remarks>
29
             private static readonly long[] _catalans =
30
                                                                    4862,
                 1, 1, 2, 5, 14, 42, 132, 429, 1430, 742900, 2674440, 9694845, 35357670, 129 6564120420, 24466267020, 91482563640, 34
                                                                            16796,
                                                                                    58786,
32
                                                                           477638700,
                                                                                         1767263190,
                                                              129644790,
33
                                                               343059613650, 1289904147324,
34
                  \,\,\hookrightarrow\,\,\,4861946401452
                 18367353072152, 69533550916004, 263747951750360,
                                                                            1002242216651368,
35
                  → 3814986502092304
             };
37
             /// <summary>
             /// <para>Generate the factorial of the value "n".</para>
39
             /// <para>Генерация факториала из значения переменной "n".</para>
40
             /// </summary>
             /// <param name="n"><para>Factorial generation value.</para><para>Значение генерации
42

→ факториала.

/para></param>

             /// <returns><para>Result of factorial calculation.</para><para>Результат подсчета
43

→ факториала</para></returns>

             public static long Factorial(long n)
44
45
                 if (n <= 1)
46
                 {
47
                      return 1;
49
50
5.1
                    (n < 21)
53
                      return _factorials[n];
54
55
56
                 return n * Factorial(n - 1);
57
             }
59
             /// <summary>
60
             /// <para>Generate the factorial of the value "n".</para>
61
             /// <para>Генерация факториала из значения переменной "n".</para>
62
             /// </summary>
63
             /// <param name="n"><para>Factorial generation value.</para><para>Значение генерации
             → факториала.</para></param>
             /// <returns><para>Result of factorial calculation.</para><para>Результат подсчета
6.5
                 факториала</para></returns>
             public static long FactorialRecursionCountingArraylength(long n)
66
67
                 if (n <= 1)
                 {
69
                      return 1;
                 }
71
72
73
                 if (n < _factorials.Length)</pre>
74
75
                 {
                      return _factorials[n];
76
77
78
                 return n * Factorial(n - 1);
79
             }
```

```
81
             /// <summary>
             /// <para>Generate the factorial of the value "n".</para>
83
             /// <para>Генерация факториала из значения переменной "n".</para>
84
             /// </summary>
             /// <param name="n"><para>Factorial generation value.</para><para>Значение генерации
86
                 факториала.</para></param>
             /// <returns><para>Result of factorial calculation.</para><para>Результат подсчета
                 факториала</para></returns>
             public static long FactTree(int n)
88
89
                 if (n < 0)
90
                      return 0;
91
                 if (n == 0)
                      return 1;
93
                     (n == 1 | |
                                n == 2
                      return 1;
95
                 if (n == 3) return 2;
96
                 if (n == 4) return 6;
97
                     (n == 5) return 24
                 if
98
                     (n == 6) return 120;
                 if
99
                     (n == 7) return 720;
                 if
100
                     (n == 8) return 5040
                 i f
101
                     (n == 9) return 40320:
                 if
102
                 if (n == 10) return 362880;
                 if (n == 11) return 3628800;
104
                     (n == 12) return 39916800;
                 i f
105
                 if
                     (n == 13) return 479001600
106
107
                 if
                     (n == 14) return 6227020800
                 if (n == 15) return 87178291200;
108
                 if (n == 16) return 1307674368000;
109
                 if (n == 17) return 20922789888000;
110
                 if (n == 18) return 355687428096000;
                 if (n == 19) return 6402373705728000
112
                     (n == 20) return 121645100408832000;
                 if
113
                     (n == 21) return 2432902008176640000;
114
115
                 return n * Factorial(n - 1);
116
             }
117
118
             /// <summary>
119
             /// <para>Generate the factorial of the value "n".</para>
120
             /// <para>Генерация факториала из значения переменной "n".</para>
121
             /// </summary>
             /// <param name="n"><para>Factorial generation value.</para><para>Значение генерации
123
                 факториала.</para></param>
             /// <returns><para>Result of factorial calculation.</para><para>Результат подсчета
124
                 факториала</para></returns>
             public static long FactorialWhileWithArray(long n)
125
                 long[] _facts =
127
                 {
128
                               6, 24,
                                       120, 720, 5040, 40320, 362880, 3628800, 39916800
129
                      479001600, 6227020800, 87178291200, 1307674368000, 20922789888000, 355687428096000, 6402373705728000, 121645100408832000, 2432902008176640000,
130
131
                 };
132
                 if (n < _facts.Length) return _facts[n];</pre>
134
                 long r = n;
135
                 while (n > 1) r *= --n;
136
                 return r;
             }
138
139
             /// <summary>
140
             /// <para>Generate the factorial of the value "n".</para>
141
142
             /// <para>Генерация факториала из значения переменной "n".</para>
             /// </summary>
143
             /// <param name="n"><para>Factorial generation value.</para><para>Значение генерации
144
                факториала.</para></param>
             /// <returns><para>Result of factorial calculation.</para><para>Результат подсчета
145
                 факториала</para></returns>
             public static long FactorialWhileWithoutArray(long n)
146
147
                 if (n < _factorials.Length) return _factorials[n];</pre>
148
149
                 long r = n;
150
                 while (n > 1) r *= --n;
151
                 return r;
152
```

```
153
154
            /// <summary>
155
            /// <para>Generate the factorial of the value "n".</para>
            /// <para>Генерация факториала из значения переменной "n".</para>
157
            /// </summary>
158
            /// <param name="n"><para>Factorial generation value.</para><para>Значение генерации
159
                факториала.</para></param>
            /// <returns><para>Result of factorial calculation.</para><para>Результат подсчета

→ факториала</para></returns>

            public static long FactorialWhileWithoutArrayAndCountingArrayLength(long n)
161
162
                 if (n < 21) return _factorials[n];</pre>
163
164
                 long r = n;
                 while (n > 1) r *= --n;
166
                 return r;
167
            }
168
169
170
            /// <summary>
171
            /// <para>Generating the Catalan Number of the value "n".</para>
            /// <para>Генерация числа Каталана из значения переменной "n".</para>
173
            /// </summary>
174
            /// <param name="n"><para>Catalan Number generation value.</para><para>Значение
175
                генерации Числа Каталана.</para></param>
            /// <returns><para>Result of Catalan Number calculation.</para><para>Результат подсчета
                Числа Каталана.</para></returns>
            public static long Catalan(int n)
177
178
179
180
                 if (n <= 1)
181
                 {
182
                     return 1;
184
                 if (n < _catalans.Length)</pre>
185
186
                     return _catalans[(int)n];
187
188
                return Factorial(2 * n) / (Factorial(n + 1) * Factorial(n));
189
            }
191
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static bool IsPowerOfTwo(ulong x) => (x & x - 1) == 0;
193
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
195
            public static T Abs<T>(T x) => Math<T>.Abs(x);
196
197
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
198
            public static T Negate<T>(T x) => Math<T>.Negate(x);
199
        }
200
201
1.8
     ./csharp/Platform.Numbers/MathExtensions.cs
   using System.Runtime.CompilerServices;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform. Numbers
 6
        public static class MathExtensions
 7
 8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Abs<T>(this ref T x) where T : struct => x = Math<T>.Abs(x);
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            public static T Negate<T>(this ref T x) where T : struct => x = Math<T>.Negate(x);
13
        }
14
15
     ./csharp/Platform.Numbers/Math[T].cs
1.9
    using System;
    using System.Runtime.CompilerServices;
         Platform.Exceptions;
    using
    using Platform.Reflection;
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
```

```
namespace Platform. Numbers
9
10
        public static class Math<T>
11
12
            public static readonly Func<T, T> Abs = CompileAbsDelegate();
public static readonly Func<T, T> Negate = CompileNegateDelegate();
13
14
15
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T> CompileAbsDelegate()
17
18
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
19
20
                     Ensure.Always.IsNumeric<T>();
21
                     emiter.LoadArgument(0);
22
                      if (NumericType<T>.IsSigned)
                      {
24
                          emiter.Call(typeof(System.Math).GetMethod("Abs", Types<T>.Array));
25
26
                     emiter.Return();
27
                 });
2.8
            }
29
30
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
31
            private static Func<T, T> CompileNegateDelegate()
32
33
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
34
35
                      emiter.LoadArgument(0);
                     emiter.Negate();
37
                      emiter.Return();
38
                 });
39
            }
40
        }
41
42
      ./csharp/Platform.Numbers.Tests/ArithmeticExtensionsTests.cs
1.10
   using Xunit;
   namespace Platform.Numbers.Tests
3
    {
5
        public static class ArithmeticExtensionsTests
6
             [Fact]
            public static void IncrementTest()
                 var number = OUL;
                 var returnValue = number.Increment();
11
                 Assert.Equal(1UL, returnValue);
12
13
                 Assert.Equal(1UL, number);
            }
14
15
             [Fact]
            public static void DecrementTest()
17
18
                 var number = 1UL;
19
                 var returnValue = number.Decrement();
20
                 Assert.Equal(OUL, returnValue);
21
22
                 Assert.Equal(OUL, number);
            }
23
        }
^{24}
      ./csharp/Platform.Numbers.Tests/ArithmeticTests.cs
1.11
   using System;
   using Xunit;
3
   namespace Platform.Numbers.Tests
4
5
        public static class ArithmeticTests
             [Fact]
            public static void CompiledOperationsTest()
9
10
                 Assert.Equal(3, Arithmetic.Add(1, 2));
11
                 Assert.Equal(1, Arithmetic.Subtract(2, 1));
                 Assert.Equal(8, Arithmetic.Multiply(2,
                                                            4));
                 Assert.Equal(4, Arithmetic.Divide(8, 2));
14
                 Assert.Equal(2, Arithmetic.Increment(1));
```

```
Assert.Equal(1UL, Arithmetic.Decrement(2UL));
16
                 Assert.Throws<NotSupportedException>(() => Arithmetic<string>.Subtract("1", "2"));
17
            }
18
        }
19
   }
     ./csharp/Platform.Numbers.Tests/BitTests.cs
1.12
using System;
   using Xunit;
   namespace Platform. Numbers. Tests
4
        public static class BitTests
6
             [Theory]
             [InlineData(00, -1)] // 0000 0000 (none, -1)
             [InlineData(01, 00)] // 0000 0001 (first, 0)
10
             [InlineData(08, 03)] // 0000 1000 (forth, 3)
11
            [InlineData(88, 03)] // 0101 1000 (forth, 3)
            public static void GetLowestBitPositionTest(ulong value, int expectedPosition)
13
14
                 Assert.True(Bit.GetLowestPosition(value) == expectedPosition);
15
            }
16
17
            [Fact]
            public static void ByteBitwiseOperationsTest()
19
20
21
                 Assert.True(Bit<byte>.Not(2) == unchecked((byte)~2));
                 Assert.True(Bit<br/>byte>.Or(1, 2) == (1 \mid 2));
22
                 Assert.True(Bit<br/>byte>.And(1, 2) == (1 \& 2));
23
                 Assert.True(Bit<byte>.ShiftLeft(1, 2) == (1 << 2));
                 Assert.True(Bit<byte>.ShiftRight(1, 2) == (1 >> 2));
26
27
            [Fact]
2.8
            public static void UInt16BitwiseOperationsTest()
29
                 Assert.True(Bit<ushort>.Not(2) == unchecked((ushort)~2));
31
                 Assert.True(Bit<ushort>.Or(1, 2) == (1 \mid 2));
32
                 Assert.True(Bit\langle ushort \rangle.And(1, 2) == (1 & 2));
33
                 Assert.True(Bit<ushort>.ShiftLeft(1, 2) == (1 << 2))
                 Assert.True(Bit<ushort>.ShiftRight(1, 2) == (1 >> 2));
35
            }
36
37
            [Fact]
38
            public static void UInt32BitwiseOperationsTest()
39
40
                 Assert.True(Bit<uint>.Not(2) == unchecked((uint)~2));
41
                 Assert.True(Bit\langle uint \rangle.Or(1, 2) == (1 | 2));
42
                 Assert.True(Bit\langle uint \rangle.And(1, 2) == (1 & 2));
43
                 Assert.True(Bit<uint>.ShiftLeft(1, 2) == (1 << 2))
44
                 Assert.True(Bit<uint>.ShiftRight(1, 2) == (1 >> 2));
45
            }
46
47
            [Fact]
48
            public static void UInt64BitwiseOperationsTest()
50
                 Assert.True(Bit<ulong>.Not(2) == unchecked((ulong)~2));
51
                 Assert.True(Bit\langle ulong \rangle.Or(1, 2) == (1 | 2));
                 Assert.True(Bit\langle ulong \rangle.And(1, 2) == (1 & 2));
53
                 Assert.True(Bit<ulong>.ShiftLeft(1, 2) == (1 << 2));
54
                 Assert.True(Bit<ulong>.ShiftRight(1, 2) == (1 >> 2));
5.5
            }
57
            [Fact]
            public static void PartialReadWriteTest()
59
60
                 {
61
                     uint firstValue = 1;
62
                     uint secondValue = 1543;
63
64
                     // Pack (join) two values at the same time
                     uint value = secondValue << 1 | firstValue;</pre>
66
67
                     uint unpackagedFirstValue = value & 1;
68
                     uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
69
70
                     Assert.True(firstValue == unpackagedFirstValue);
71
                     Assert.True(secondValue == unpackagedSecondValue);
```

```
// Using universal functions:
        Assert.True(PartialRead(value, 0, 1) == firstValue);
        Assert.True(PartialRead(value, 1, -1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = PartialWrite(value, firstValue, 0, 1);
        value = PartialWrite(value, secondValue, 1, -1);
        Assert.True(PartialRead(value, 0, 1) == firstValue);
        Assert.True(PartialRead(value, 1, -1) == secondValue);
    }
        uint firstValue = 1;
        uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = Bit.PartialWrite(value, firstValue, 0, 1);
        value = Bit.PartialWrite(value, secondValue, 1, -1);
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
    }
        uint firstValue = 1;
        uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & 0xFFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        var readMasksAndShiftForOAnd1 = GetReadMaskAndShift(0, 1);
        var readMasksAndShiftFor1AndMinus1 = GetReadMaskAndShift(1, -1);
        var writeMasksAndShiftForOAnd1 = GetWriteMasksAndShift(0, 1);
        var writeMasksAndShiftFor1AndMinus1 = GetWriteMasksAndShift(1, -1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = PartialWrite(value, firstValue, writeMasksAndShiftForOAnd1);
        value = PartialWrite(value, secondValue, writeMasksAndShiftFor1AndMinus1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
    }
// TODO: Can be optimized using precalculation of TargetMask and SourceMask
private static uint PartialWrite(uint target, uint source, int shift, int limit)
    if (shift < 0)</pre>
    {
        shift = 32 + shift;
```

7.3

7.5

76 77

78

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99 100

101

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103 104

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106 107

108

109 110

111

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116

117 118

119

120

122

 $\frac{123}{124}$ 

127

128

129

130

132 133

134

135

137

138 139

140

 $\frac{141}{142}$ 

143

144

146 147

148

149 150

152

```
154
                  if (limit < 0)</pre>
156
                      limit = 32 + limit;
                  }
158
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
159
                  var targetMask = ~(sourceMask << shift);</pre>
160
                  return target & targetMask | (source & sourceMask) << shift;</pre>
161
162
163
             private static uint PartialRead(uint target, int shift, int limit)
164
165
                  if (shift < 0)</pre>
166
                  {
167
                      shift = 32 + shift;
168
                  if (limit < 0)</pre>
170
171
                      limit = 32 + limit;
172
                  }
173
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
174
                  var targetMask = sourceMask << shift;</pre>
175
                  return (target & targetMask) >> shift;
176
             }
177
178
             private static Tuple<uint, uint, int> GetWriteMasksAndShift(int shift, int limit)
179
180
181
                  if (shift < 0)</pre>
                  {
182
                      shift = 32 + shift;
183
184
                  if (limit < 0)</pre>
                  {
186
                      limit = 32 + limit;
187
                  }
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
189
                  var targetMask = ~(sourceMask << shift);</pre>
190
                  return new Tuple<uint, uint, int>(targetMask, sourceMask, shift);
             }
192
193
             private static Tuple<uint, int> GetReadMaskAndShift(int shift, int limit)
194
195
                  if (shift < 0)</pre>
196
                      shift = 32 + shift;
198
199
                  if (limit < 0)</pre>
200
                  {
201
                      limit = 32 + limit;
202
203
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
204
                  var targetMask = sourceMask << shift;</pre>
205
                  return new Tuple<uint, int>(targetMask, shift);
206
             }
207
208
             private static uint PartialWrite(uint target, uint targetMask, uint source, uint
209
              → sourceMask, int shift) => target & targetMask | (source & sourceMask) << shift;
210
             private static uint PartialWrite(uint target, uint source, Tuple<uint, uint, int>
211
                 masksAndShift) => PartialWrite(target, masksAndShift.Item1, source,
                 masksAndShift.Item2, masksAndShift.Item3);
212
             private static uint PartialRead(uint target, uint targetMask, int shift) => (target &
213

→ targetMask) >> shift;
214
             private static uint PartialRead(uint target, Tuple<uint, int> masksAndShift) =>
215
              PartialRead(target, masksAndShift.Item1, masksAndShift.Item2);
             [Fact]
217
             public static void BugWithLoadingConstantOf8Test()
218
219
                  Bit<byte>.PartialWrite(0, 1, 5, -5);
220
             }
221
         }
222
```

```
namespace Platform.Numbers.Tests
3
        public static class MathExtensionsTests
5
            [Fact]
            public static void AbsTest()
                var number = -1L;
10
                var returnValue = number.Abs();
11
                 Assert.Equal(1L, returnValue);
                Assert.Equal(1L, number);
13
            }
14
15
            [Fact]
16
            public static void NegateTest()
17
                 var number = 2L;
19
                 var returnValue = number.Negate();
20
                Assert.Equal(-2L, returnValue);
21
                 Assert.Equal(-2L, number);
22
            }
23
24
            [Fact]
25
            public static void UnsignedNegateTest()
27
                 var number = 2UL;
                 var returnValue = number.Negate();
29
                  \texttt{Assert.Equal(18446744073709\bar{5}51614, returnValue);} \\
30
                 Assert.Equal(18446744073709551614, number);
31
            }
        }
33
34
1.14 ./csharp/Platform.Numbers.Tests/MathTests.cs
   using Xunit;
2
   namespace Platform. Numbers. Tests
4
        public static class MathTests
6
            [Fact]
            public static void CompiledOperationsTest()
                 Assert.True(Math.Abs(Arithmetic < double > .Subtract(3D, 2D) - 1D) < 0.01);
10
            }
11
        }
   }
13
     ./csharp/Platform.Numbers.Tests/SystemTests.cs
1.15
   using Xunit;
1
   namespace Platform. Numbers. Tests
3
        public static class SystemTests
5
            [Fact]
            public static void PossiblePackTwoValuesIntoOneTest()
                uint value = 0;
10
                 // Set one to first bit
12
                 value |= 1;
13
                 Assert.True(value == 1);
15
16
                 // Set zero to first bit
17
                 value &= OxFFFFFFE;
19
                 // Get first bit
20
                uint read = value & 1;
21
22
                 Assert.True(read == 0);
23
24
                 uint firstValue = 1;
^{25}
                 uint secondValue = 1543;
26
27
                 // Pack (join) two values at the same time
28
                 value = (secondValue << 1) | firstValue;</pre>
29
                 uint unpackagedFirstValue = value & 1;
```

```
uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
32
33
                 Assert.True(firstValue == unpackagedFirstValue);
34
                 Assert.True(secondValue == unpackagedSecondValue);
36
                 // Using universal functions:
37
38
                 Assert.True(PartialRead(value, 0, 1) == firstValue);
39
                 Assert.True(PartialRead(value, 1, -1) == secondValue);
41
                 firstValue = 0;
42
                 secondValue = 6892;
44
                 value = PartialWrite(value, firstValue, 0, 1);
value = PartialWrite(value, secondValue, 1, -1);
45
47
                 Assert.True(PartialRead(value, 0, 1) == firstValue);
                 Assert.True(PartialRead(value, 1, -1) == secondValue);
49
50
51
             private static uint PartialWrite(uint target, uint source, int shift, int limit)
52
53
                 if (shift < 0)</pre>
                 {
55
                      shift = 32 + shift;
56
57
                 if (limit < 0)</pre>
58
                 {
59
                      limit = 32 + limit;
60
                 }
61
                 var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
62
                 var targetMask = ~(sourceMask << shift);</pre>
63
                 return (target & targetMask) | ((source & sourceMask) << shift);</pre>
64
             }
65
66
             private static uint PartialRead(uint target, int shift, int limit)
67
                 if (shift < 0)</pre>
69
                 {
70
                      shift = 32 + shift;
71
                 }
72
                 if (limit < 0)</pre>
73
                      limit = 32 + limit;
75
                 var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
77
                 var targetMask = sourceMask << shift;</pre>
78
                 return (target & targetMask) >> shift;
79
             }
80
        }
81
   }
82
```

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