```
LinksPlatform's Platform Numbers Class Library
    ./csharp/Platform.Numbers/Arithmetic.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform. Numbers
5
6
        /// <summary>
       /// <para> Each function performs the simplest arithmetic operation on the type specified as
           a parameter </para>
        /// <para> Каждая функция выполняет простейшую арифметическую операцию над типом, указанным
        → в качестве параметра </para>
        /// </summary>
       public static class Arithmetic
11
12
13
            /// <summary>
            /// <para> Adding the x and y arguments </para>
15
            /// <para> Сложение аргументов х и у </para>
16
            /// </summary>
17
            /// <returns>
            /// <para> Sum of x and y </para>
19
            /// <para> Сумма х и у </para>
20
            /// </returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
22
            public static T Add\langle T \rangle (T x, T y) \Rightarrow Arithmetic \langle T \rangle . Add(x, y);
23
^{24}
            /// <summary>
25
            /// <para> Subtracting x from y </para>
26
            /// <para> Вычитание х из у </para>
            /// </summary>
28
            /// <returns>
29
            /// <para> Difference of x and y </para>
30
            /// <para> Разность х и у </para>
31
            /// </returns>
32
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            public static T Subtract<T>(T x, T y) => Arithmetic<T>.Subtract(x, y);
35
36
            /// <summary>
            /// <para> Multiplication the x and y </para>
37
            /// <para> Умножение х и у </para>
38
            /// </summary>
39
            /// <returns>
            /// <returns>
41
            /// <para> Product of x and y </para>
42
            /// <para> Произведение х и ў </para>
43
            /// </returns>
44
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            public static T Multiply<T>(T x, T y) => Arithmetic<T>.Multiply(x, y);
46
47
            /// <summary>
48
            /// <para> Dividing x by y </para>
49
            /// <para> Деление х на у </para>
50
            /// </summary>
51
            /// <returns>
            /// <para> Quoitent of x and y </para>
            /// <para> Частное х и у </para>
54
            /// </returns>
55
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Divide<T>(T x, T y) => Arithmetic<T>.Divide(x, y);
57
            /// <summary>
59
            /// <para> Increasing the parameter x by one </para>
60
            /// <para> Увеличение параметра х на единицу </para>
61
            /// </summary>
62
            /// <returns>
63
            /// <para> Increase by one x </para>
64
            /// <para> Увеличенное на единицу х </para>
            /// </returns>
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
67
            public static T Increment<T>(T x) => Arithmetic<T>.Increment(x);
68
69
70
            /// <para> Increase the parameter x passed by reference by one </para>
71
            /// <para> Увеличение переданного по ссылке параметра х на единицу </para>
72
            /// </summary>
73
            /// <returns>
```

```
/// <para> Increase by one x with returning the value to the original variable </para>
7.5
             /// <para> Увеличенное на единицу х с возвратом значения в исходную переменную </para>
             /// </returns>
77
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
            public static T Increment<T>(ref T x) => x = Arithmetic<T>.Increment(x);
80
             /// <summary>
81
             /// <para> Decrease parameter x by one </para>
82
             /// <para> Уменьшение параметра х на единицу </para>
83
             /// </summary>
84
             /// <returns>
85
             /// <para> Reduced by one x </para>
             /// <para> Уменьшенное на единицу х </para>
87
             /// </returns>
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T Decrement<T>(T x) => Arithmetic<T>.Decrement(x);
90
             /// <summary>
92
             /// <para> Decreasing the parameter x passed by reference by one </para>
93
             /// <para> Уменьшение переданного по ссылке параметра х на единицу </para>
94
             /// </summary>
95
            /// <returns>
96
             /// <para> Reduced by one x with returning the value to the original variable </para>
97
             /// <para> Уменьшенное на единицу х с воз вратом значения в исходную переменную </para>
             /// </returns>
99
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
100
            public static T Decrement<T>(ref T x) => x = Arithmetic<T>.Decrement(x);
101
        }
102
103
     ./csharp/Platform.Numbers/ArithmeticExtensions.cs
   using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 3
    namespace Platform.Numbers
        public static class ArithmeticExtensions
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
 9
            public static T Decrement<T>(this ref T x) where T : struct => x =
10
             → Arithmetic<T>.Decrement(x);
11
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            public static T Increment<T>(this ref T x) where T : struct => x =
13
             → Arithmetic<T>.Increment(x);
        }
15
     ./csharp/Platform.Numbers/Arithmetic[T].cs
   using System;
    using System.Reflection.Emit;
 2
    using System.Runtime.CompilerServices;
    using Platform. Exceptions;
    using Platform.Reflection;
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform. Numbers
10
11
        public static class Arithmetic<T>
12
13
            public static readonly Func<T, T, T> Add = CompileAddDelegate();
            public static readonly Func<T, T, T> Subtract = CompileSubtractDelegate();
15
            public static readonly Func<T, T, T> Multiply = CompileMultiplyDelegate()
public static readonly Func<T, T, T> Divide = CompileDivideDelegate();
public static readonly Func<T, T> Increment = CompileIncrementDelegate();
                                                  T> Multiply = CompileMultiplyDelegate();
16
17
18
            public static readonly Func<T, T> Decrement = CompileDecrementDelegate();
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             private static Func<T, T, T> CompileAddDelegate()
22
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
24
25
                     Ensure.Always.IsNumeric<T>();
26
                     emiter.LoadArguments(0, 1);
                     emiter.Add();
28
                     emiter.Return();
```

```
});
30
             }
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T, T> CompileSubtractDelegate()
34
35
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
37
                     Ensure.Always.IsNumeric<T>();
38
                     emiter.LoadArguments(0, 1);
39
                     emiter.Subtract();
40
                     emiter.Return();
41
                 });
42
43
             }
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            private static Func<T, T, T> CompileMultiplyDelegate()
46
47
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
48
49
                     Ensure.Always.IsNumeric<T>();
50
                     emiter.LoadArguments(0, 1);
5.1
                     emiter.Emit(OpCodes.Mul);
52
                     emiter.Return();
                 });
54
             }
55
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            private static Func<T, T, T> CompileDivideDelegate()
58
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
60
61
62
                     Ensure.Always.IsNumeric<T>();
63
                     emiter.LoadArguments(0, 1);
                     if(NumericType<T>.IsSigned)
64
                     {
65
                          emiter.Emit(OpCodes.Div);
                     }
67
                     else
68
                     {
69
                          emiter.Emit(OpCodes.Div_Un);
7.0
7.1
                     emiter.Return();
72
                 });
73
             }
74
75
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
76
            private static Func<T, T> CompileIncrementDelegate()
77
78
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
79
80
                     Ensure.Always.IsNumeric<T>();
                     emiter.LoadArgument(0);
82
                     emiter.Increment<T>();
83
                     emiter.Return();
                 });
85
86
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
88
            private static Func<T, T> CompileDecrementDelegate()
89
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
91
92
                     Ensure.Always.IsNumeric<T>();
93
                     emiter.LoadArgument(0);
94
                     emiter.Decrement<T>();
95
                     emiter.Return();
96
                 });
            }
98
        }
99
100
     ./csharp/Platform.Numbers/Bit.cs
    using System.Runtime.CompilerServices;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 4
```

```
namespace Platform. Numbers
7
        public static class Bit
10
11
            /// <summary>
12
            /// <para> Counts the number of bits set in a number </para>
13
            /// <para> Подсчитывает количество установленных бит в числе </para>
14
            ///</summary>
15
            /// <returns>
16
            /// <para> Number of bits set in a number </para>
17
            /// <para> Количество установленных бит в числе </para>
18
            /// </returns>
19
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static long Count(long x)
21
22
                long n = 0;
                while (x != 0)
24
                    n++:
26
                    x &= x - 1;
28
29
                return n;
            }
30
            /// <summary>
31
            /// <para> Searches for the first bit set in a number </para>
            /// <para> Ищет первый установленный бит в числе </para>
            /// </summary>
34
            /// <returns>
35
            /// <para> First bit set </para>
36
            /// <para> Первый установленный бит </para>
37
            /// </returns>
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static int GetLowestPosition(ulong value)
41
                if (value == 0)
42
                {
                    return -1;
44
                var position = 0;
46
                while ((value & 1UL) == 0)
47
                    value >>= 1;
49
50
                    ++position;
51
52
                return position;
5.3
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
55
            public static T Not<T>(T x) => Bit<T>.Not(x);
56
57
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
58
            public static T Or<T>(T x, T y) => Bit<T>.Or(x, y);
60
61
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T And<T>(T x, T y) => Bit<T>.And(x, y);
63
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public static T ShiftLeft<T>(T x, int y) => Bit<T>.ShiftLeft(x, y);
65
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
67
            public static T ShiftRight<T>(T x, int y) => Bit<T>.ShiftRight(x, y);
68
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
70
            public static T PartialWrite<T>(T target, T source, int shift, int limit) =>
71
            → Bit<T>.PartialWrite(target, source, shift, limit);
72
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
73
            public static T PartialRead<T>(T target, int shift, int limit) =>
            → Bit<T>.PartialRead(target, shift, limit);
        }
   }
76
    ./csharp/Platform.Numbers/BitExtensions.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Numbers
```

```
{
6
        /// <summary>
        /// <returns> bit operations </returns>
        /// </summary>
q
        /* bit operations */
        public static class BitwiseExtensions
11
12
        ₹
13
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
             public static T Not<T>(this ref T target) where T : struct => target = Bit.Not(target);
16
17
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            public static T PartialWrite<T>(this ref T target, T source, int shift, int limit) where
19
                T : struct => target = Bit<T>.PartialWrite(target, source, shift, limit);
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            public static T PartialRead<T>(this T target, int shift, int limit) =>
             → Bit<T>.PartialRead(target, shift, limit);
23
    }
24
16
     ./csharp/Platform.Numbers/Bit[T].cs
   using System;
   using System.Runtime.CompilerServices;
2
    using Platform. Exceptions;
3
   using Platform. Reflection;
4
6
    // ReSharper disable StaticFieldInGenericType
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
7
   namespace Platform. Numbers
10
        public static class Bit<T>
11
12
            public static readonly Func<T, T> Not = CompileNotDelegate();
13
            public static readonly Func<T, T, T> Or = CompileOrDelegate();
14
            public static readonly Func<T, T, T> And = CompileAndDelegate();
            public static readonly Func<T, int, T> ShiftLeft = CompileShiftLeftDelegate();
public static readonly Func<T, int, T> ShiftRight = CompileShiftRightDelegate();
public static readonly Func<T, T, int, int, T> PartialWrite =
16
17
                CompilePartialWriteDelegate();
            public static readonly Func<T, int, int, T> PartialRead = CompilePartialReadDelegate();
19
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            private static Func<T, T> CompileNotDelegate()
22
23
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
24
25
                     Ensure.Always.IsNumeric<T>();
26
                     emiter.LoadArguments(0);
                     emiter.Not();
28
                      emiter.Return();
29
                 });
30
             }
31
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T, T> CompileOrDelegate()
34
35
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
36
37
                     Ensure.Always.IsNumeric<T>();
38
39
                     emiter.LoadArguments(0, 1);
                     emiter.Or();
41
                     emiter.Return();
                 });
42
             }
43
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            private static Func<T, T, T> CompileAndDelegate()
46
47
                 return DelegateHelpers.Compile<Func<T, T, T>>(emiter =>
48
49
                     Ensure.Always.IsNumeric<T>();
50
                     emiter.LoadArguments(0, 1);
51
                      emiter.And();
                      emiter.Return();
                 });
54
             }
```

```
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, int, T> CompileShiftLeftDelegate()
    return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
    {
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.ShiftLeft();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, int, T> CompileShiftRightDelegate()
    return DelegateHelpers.Compile<Func<T, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        emiter.LoadArguments(0, 1);
        emiter.ShiftRight();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, T, int, int, T> CompilePartialWriteDelegate()
    return DelegateHelpers.Compile<Func<T, T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>();
        var constants = GetConstants()
        var bitsNumber = constants.Item1;
        var numberFilledWithOnes = constants.Item2;
        ushort shiftArgument = 2;
        ushort limitArgument = 3
        var checkLimit = emiter.DefineLabel();
        var calculateSourceMask = emiter.DefineLabel();
        // Check shift
        emiter.LoadArgument(shiftArgument);
        emiter.LoadConstant(0)
        emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
        // Fix shift
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(shiftArgument);
        emiter.Add():
        emiter.StoreArgument(shiftArgument);
        emiter.MarkLabel(checkLimit);
        // Check limit
        emiter.LoadArgument(limitArgument);
        emiter.LoadConstant(0)
        emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
        // Fix limit
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(limitArgument);
        emiter.Add()
        emiter.StoreArgument(limitArgument);
        emiter.MarkLabel(calculateSourceMask);
        var sourceMask = emiter.DeclareLocal<T>();
        var targetMask = emiter.DeclareLocal<T>();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.LoadArgument(limitArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.And();
        emiter.StoreLocal(sourceMask);
        emiter.LoadLocal(sourceMask);
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Not();
        emiter.StoreLocal(targetMask);
        emiter.LoadArgument(0); // target
        emiter.LoadLocal(targetMask);
        emiter.And();
        emiter.LoadArgument(1); // source
        emiter.LoadLocal(sourceMask);
        emiter.And();
```

58 59

61

62

63

65

66

68

69 70

7.1

72

74

7.5

76

77

78

79 80

81

82 83

84 85

87

88

89

91

93

94

95

96

97

98

100

101

102

103

104

105

107

108

109

110

111

112

113

114

115

117

118

119

120

121

122

124

125

126

127

128

129

131

```
emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft();
        emiter.Or();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Func<T, int, int, T> CompilePartialReadDelegate()
    return DelegateHelpers.Compile<Func<T, int, int, T>>(emiter =>
        Ensure.Always.IsNumeric<T>()
        var constants = GetConstants();
        var bitsNumber = constants.Item1;
        var numberFilledWithOnes = constants.Item2;
        ushort shiftArgument =
        ushort limitArgument = 2;
        var checkLimit = emiter.DefineLabel();
        var calculateSourceMask = emiter.DefineLabel();
        // Check shift
        emiter.LoadArgument(shiftArgument);
        emiter.LoadConstant(0)
        emiter.BranchIfGreaterOrEqual(checkLimit); // Skip fix
        // Fix shift
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(shiftArgument);
        emiter.Add();
        emiter.StoreArgument(shiftArgument);
        emiter.MarkLabel(checkLimit);
          Check limit
        emiter.LoadArgument(limitArgument);
        emiter.LoadConstant(0);
        emiter.BranchIfGreaterOrEqual(calculateSourceMask); // Skip fix
        // Fix limit
        emiter.LoadConstant(bitsNumber);
        emiter.LoadArgument(limitArgument);
        emiter.Add()
        emiter.StoreArgument(limitArgument);
        emiter.MarkLabel(calculateSourceMask);
        var sourceMask = emiter.DeclareLocal<T>();
        var targetMask = emiter.DeclareLocal<T>();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.LoadArgument(limitArgument); // limit
        emiter.ShiftLeft();
        emiter.Not();
        emiter.LoadConstant(typeof(T), numberFilledWithOnes);
        emiter.And();
        emiter.StoreLocal(sourceMask);
        emiter.LoadLocal(sourceMask);
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftLeft()
        emiter.StoreLocal(targetMask);
        emiter.LoadArgument(0); // target
        emiter.LoadLocal(targetMask);
        emiter.And();
        emiter.LoadArgument(shiftArgument);
        emiter.ShiftRight();
        emiter.Return();
    });
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
private static Tuple<int, T> GetConstants()
    var type = typeof(T);
    if (type == typeof(ulong))
        return new Tuple<int, T>(64, (T)(object)ulong.MaxValue);
    if (type == typeof(uint))
        return new Tuple<int, T>(32, (T)(object)uint.MaxValue);
       (type == typeof(ushort))
    {
        return new Tuple<int, T>(16, (T)(object)ushort.MaxValue);
```

136

137

139 140

141

 $\frac{142}{143}$ 

144

146

147

148

150

151

152

153

155

156

158

159

160

162

163 164

165

166

168

169

170 171

172

173

174

176

177

179

180

182

183

184

186

187

188

189

190

191

193

194 195

196

197 198

199

 $\frac{200}{201}$ 

 $\frac{202}{203}$ 

 $\frac{204}{205}$ 

 $\frac{206}{207}$ 

209

```
if (type == typeof(byte))
212
213
                      return new Tuple<int, T>(8, (T)(object)byte.MaxValue);
214
215
                  throw new NotSupportedException();
             }
217
         }
218
219
1.7
     ./csharp/Platform.Numbers/Math.cs
    using System;
    using System.Runtime.CompilerServices;
 3
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 4
    namespace Platform. Numbers
         /// <remarks>
         /// Resizable array (FileMappedMemory) for values cache may be used. or cached oeis.org
 9
         /// </remarks>
 10
         public static class Math
11
             /// <remarks>
13
             /// <para>Source: https://oeis.org/A000142/list </para>
14
             /// <para>Источник: https://oeis.org/A000142/list </para>
15
             /// </remarks>
17
             private static readonly ulong[] _factorials =
18
19
                 1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 362880, 39916800, 479001600, 6227020800, 87178291200, 1307674368000, 20922789888000
20
21
                  355687428096000, 6402373705728000, 121645100408832000, 2432902008176640000
             };
23
             /// <remarks>
25
             /// <para>Source: https://oeis.org/A000108/list </para>
26
             /// <para>Источник: https://oeis.org/A000108/list </para>
             /// </remarks>
             private static readonly ulong[] _catalans =
29
30
                 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, 20 742900, 2674440, 9694845, 35357670, 129644790, 477638700, 176726 6564120420, 24466267020, 91482563640, 343059613650, 1289904147324,
                                                                                             208012.
31
                                                                           477638700, 1767263190,
33
                      4861946401452
                                    69533550916004,
                  18367353072152,
                                                      263747951750360, 1002242216651368,
34
                      3814986502092304
                  14544636039226909, 55534064877048198, 212336130412243110, 812944042149730764,
35
                  → 3116285494907301262, 11959798385860453492
36
37
             public static readonly ulong MaximumFactorialNumber = 20;
39
             public static readonly ulong MaximumCatalanIndex = 36;
40
             /// <summary>
42
             /// <para>Returns the product of all positive integers less than or equal to the number
43

→ specified as an argument.
             /// <para>Возвращает произведение всех положительных чисел меньше или равных указанному
44
                 в качестве аргумента числу.</para>
             /// </summary>
             /// <param name="n"><para>The maximum positive number that will participate in
              🛶 factorial's product.</para><pаra>Максимальное положительное число, которое будет
                 участвовать в произведение факториала. </para></param>
             /// <returns><para>The product of all positive integers less than or equal to the number
47
                specified as an argument.</para><para>Произведение всех положительных чисел меньше
                 или равных указанному в качестве аргумента числу. </para></returns>
             public static ulong Factorial(ulong n)
                  if (n >= 0 && n <= MaximumFactorialNumber)</pre>
50
                  {
51
                      return _factorials[n];
                  }
53
                  else
                  {
                      throw new ArgumentOutOfRangeException($"Only numbers from 0 to
56
                       {MaximumFactorialNumber} are supported by unsigned integer with 64 bits
                       → length.");
                  }
57
             }
```

```
5.9
                      /// <summary>
                      /// <para>Returns the Catalan Number with the number specified as an argument.</para>
61
                      /// <para>Возвращает Каталановое число с номером указанным в качестве аргумента.</para>
62
                      /// </summary>
                      /// <param name="n"><para>The number of Catalan number.</para><para>Номер Каталанового
64

¬ числа.</para></param>

                      \protect\ensuremath{///}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremath{<}\protect\ensuremat
                       🛶 argument.</para>Каталановое число с номером указанным в качестве
                            аргумента.</para></returns>
                      public static ulong Catalan(ulong n)
66
                              if (n >= 0 && n <= MaximumCatalanIndex)</pre>
                              {
69
                                     return _catalans[n];
70
                              }
                              else
72
73
                                     throw new ArgumentOutOfRangeException($"Only numbers from 0 to
74
                                             {MaximumCatalanIndex} are supported by unsigned integer with 64 bits
                                            length.");
                              }
7.5
                      }
76
77
                      [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
                      public static bool IsPowerOfTwo(ulong x) => (x & x - 1) == 0;
79
80
                      [MethodImpl(MethodImplOptions.AggressiveInlining)]
81
                      public static T Abs<T>(T x) => Math<T>.Abs(x);
83
                      [MethodImpl(MethodImplOptions.AggressiveInlining)]
                      public static T Negate<T>(T x) => Math<T>.Negate(x);
85
              }
86
      }
87
         ./csharp/Platform.Numbers/MathExtensions.cs
1.8
      using System.Runtime.CompilerServices;
      #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 3
      namespace Platform.Numbers
 5
              public static class MathExtensions
 7
                      [MethodImpl(MethodImplOptions.AggressiveInlining)]
 9
                      public static T Abs<T>(this ref T x) where T : struct => x = Math<T>.Abs(x);
1.0
11
                      [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
                      public static T Negate<T>(this ref T x) where T : struct => x = Math<T>.Negate(x);
13
              }
14
      }
15
         ./csharp/Platform.Numbers/Math[T].cs
19
      using System;
      using System.Runtime.CompilerServices;
      using Platform. Exceptions;
      using Platform. Reflection;
 4
      // ReSharper disable StaticFieldInGenericType
      #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
      namespace Platform. Numbers
 9
1.0
              public static class Math<T>
12
                      public static readonly Func<T, T> Abs = CompileAbsDelegate();
public static readonly Func<T, T> Negate = CompileNegateDelegate();
13
14
15
                      [MethodImpl(MethodImplOptions.AggressiveInlining)]
16
                      private static Func<T, T> CompileAbsDelegate()
18
                              return DelegateHelpers.Compile<Func<T, T>>(emiter =>
19
20
                                     Ensure.Always.IsNumeric<T>();
                                     emiter.LoadArgument(0);
22
                                     if (NumericType<T>.IsSigned)
                                     {
24
                                             emiter.Call(typeof(System.Math).GetMethod("Abs", Types<T>.Array));
25
```

```
26
                      emiter.Return();
27
                 });
28
             }
29
30
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
31
             private static Func<T, T> CompileNegateDelegate()
32
33
                 return DelegateHelpers.Compile<Func<T, T>>(emiter =>
34
                 {
35
                      emiter.LoadArgument(0);
36
                      emiter.Negate();
37
                      emiter.Return();
38
                 });
39
             }
40
        }
41
   }
42
1.10
      ./csharp/Platform.Numbers.Tests/ArithmeticExtensionsTests.cs
   using Xunit;
   namespace Platform.Numbers.Tests
3
4
        public static class ArithmeticExtensionsTests
5
             [Fact]
             public static void IncrementTest()
                 var number = OUL;
10
                 var returnValue = number.Increment();
11
                 Assert.Equal(1UL, returnValue);
12
                 Assert.Equal(1UL, number);
14
             [Fact]
16
             public static void DecrementTest()
17
18
                 var number = 1UL;
19
                 var returnValue = number.Decrement();
20
                 Assert.Equal(OUL, returnValue);
21
                 Assert.Equal(OUL, number);
22
             }
23
        }
   }
     ./csharp/Platform.Numbers.Tests/ArithmeticTests.cs
1.11
   using System;
   using Xunit;
2
   namespace Platform.Numbers.Tests
4
        public static class ArithmeticTests
6
             [Fact]
             public static void CompiledOperationsTest()
10
                 Assert.Equal(3, Arithmetic.Add(1, 2));
                 Assert.Equal(1, Arithmetic.Subtract(2, 1));
12
                 Assert.Equal(8, Arithmetic.Multiply(2, 4)
Assert.Equal(4, Arithmetic.Divide(8, 2));
Assert.Equal(2, Arithmetic.Increment(1));
                                                             4));
13
14
15
                 Assert.Equal(1UL, Arithmetic.Decrement(2UL));
16
                 Assert.Throws<NotSupportedException>(() => Arithmetic<string>.Subtract("1", "2"));
17
             }
        }
19
20
      ./csharp/Platform.Numbers.Tests/BitTests.cs
1.12
   using System;
using Xunit;
2
3
   namespace Platform.Numbers.Tests
4
5
6
        public static class BitTests
             [Theory]
             [InlineData(00, -1)] // 0000 0000 (none, -1)
             [InlineData(01, 00)] // 0000 0001 (first, 0)
10
```

```
[InlineData(08, 03)] // 0000 1000 (forth, 3)
[InlineData(88, 03)] // 0101 1000 (forth, 3)
public static void GetLowestBitPositionTest(ulong value, int expectedPosition)
    Assert.True(Bit.GetLowestPosition(value) == expectedPosition);
}
[Fact]
public static void ByteBitwiseOperationsTest()
    Assert.True(Bit<byte>.Not(2) == unchecked((byte)~2));
    Assert.True(Bit<byte>.Or(1, 2) == (1 | 2));
    Assert.True(Bit<byte>.And(1, 2) == (1 & 2));
Assert.True(Bit<byte>.ShiftLeft(1, 2) == (1 << 2));
Assert.True(Bit<byte>.ShiftRight(1, 2) == (1 >> 2));
}
[Fact]
public static void UInt16BitwiseOperationsTest()
    Assert.True(Bit<ushort>.Not(2) == unchecked((ushort)~2));
    Assert.True(Bit<ushort>.Or(1, 2) == (1 \mid 2));
    Assert.True(Bit<ushort>.And(1, 2) == (1 \& 2));
    Assert.True(Bit<ushort>.ShiftLeft(1, 2) == (1 << 2))
    Assert.True(Bit<ushort>.ShiftRight(1, 2) == (1 >> 2));
[Fact]
public static void UInt32BitwiseOperationsTest()
    Assert.True(Bit<uint>.Not(2) == unchecked((uint)~2));
    Assert. True(Bit<uint>.Or(1, 2) == (1 | 2));
    Assert.True(Bit\langle uint \rangle.And(1, 2) == (1 & 2));
    Assert.True(Bit<uint>.ShiftLeft(1, 2) == (1 << 2));
    Assert.True(Bit<uint>.ShiftRight(1, 2) == (1 >> 2));
}
[Fact]
public static void UInt64BitwiseOperationsTest()
    Assert.True(Bit<ulong>.Not(2) == unchecked((ulong)~2));
    Assert.True(Bit\langle ulong \rangle.Or(1, 2) == (1 | 2));
    Assert.True(Bit\langle ulong \rangle.And(1, 2) == (1 & 2));
    Assert.True(Bit<ulong>.ShiftLeft(1, 2) == (1 << 2))
    Assert.True(Bit<ulong>.ShiftRight(1, 2) == (1 >> 2));
[Fact]
public static void PartialReadWriteTest()
    {
         uint firstValue = 1;
         uint secondValue = 1543;
         // Pack (join) two values at the same time
         uint value = secondValue << 1 | firstValue;</pre>
         uint unpackagedFirstValue = value & 1;
         uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
         Assert.True(firstValue == unpackagedFirstValue);
         Assert.True(secondValue == unpackagedSecondValue);
         // Using universal functions:
         Assert.True(PartialRead(value, 0, 1) == firstValue);
         Assert.True(PartialRead(value, 1, -1) == secondValue);
         firstValue = 0
         secondValue = 6892;
         value = PartialWrite(value, firstValue, 0, 1);
         value = PartialWrite(value, secondValue, 1, -1);
         Assert.True(PartialRead(value, 0, 1) == firstValue);
         Assert.True(PartialRead(value, 1, -1) == secondValue);
    }
    {
         uint firstValue = 1;
```

13 14

16 17

19 20

22

 $\frac{23}{24}$ 

26

28

29 30

31

32

33

35 36 37

38

39

41

42

43

44

45

46

48

50

51

52

54

55

57

58

59 60 61

62

64

65

66

68

69 70

71

73

74

75

76

78

79 80

81

82 83

84

85

86 87

88

```
uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
        firstValue = 0:
        secondValue = 6892;
        value = Bit.PartialWrite(value, firstValue, 0, 1);
        value = Bit.PartialWrite(value, secondValue, 1, -1);
        Assert.True(Bit.PartialRead(value, 0, 1) == firstValue);
        Assert.True(Bit.PartialRead(value, 1, -1) == secondValue);
    {
        uint firstValue = 1:
        uint secondValue = 1543;
        // Pack (join) two values at the same time
        uint value = secondValue << 1 | firstValue;</pre>
        uint unpackagedFirstValue = value & 1;
        uint unpackagedSecondValue = (value & OxFFFFFFFE) >> 1;
        Assert.True(firstValue == unpackagedFirstValue);
        Assert.True(secondValue == unpackagedSecondValue);
        // Using universal functions:
        var readMasksAndShiftForOAnd1 = GetReadMaskAndShift(0, 1);
        var readMasksAndShiftFor1AndMinus1 = GetReadMaskAndShift(1,
        var writeMasksAndShiftForOAnd1 = GetWriteMasksAndShift(0, 1);
        var writeMasksAndShiftFor1AndMinus1 = GetWriteMasksAndShift(1, -1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
        firstValue = 0;
        secondValue = 6892;
        value = PartialWrite(value, firstValue, writeMasksAndShiftForOAnd1);
        value = PartialWrite(value, secondValue, writeMasksAndShiftFor1AndMinus1);
        Assert.True(PartialRead(value, readMasksAndShiftForOAnd1) == firstValue);
        Assert.True(PartialRead(value, readMasksAndShiftFor1AndMinus1) == secondValue);
    }
}
// TODO: Can be optimized using precalculation of TargetMask and SourceMask
private static uint PartialWrite(uint target, uint source, int shift, int limit)
    if (shift < 0)</pre>
        shift = 32 + shift:
    }
    if (limit < 0)</pre>
    {
        limit = 32 + limit;
    }
    var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
    var targetMask = ~(sourceMask << shift);</pre>
    return target & targetMask | (source & sourceMask) << shift;</pre>
private static uint PartialRead(uint target, int shift, int limit)
    if (shift < 0)</pre>
    {
        shift = 32 + shift;
```

92

94

95

96

98

99 100

101

102

103 104

105

107 108

109 110

111

112 113 114

115

116

117 118

119

121

122

123

125

126 127

128

129

131

132 133

134

136

137

138 139

140

142

143

145

146 147

148

150

151 152

153

154

156

157

158

159

160

 $\frac{162}{163}$ 

164 165

166

167

```
if (limit < 0)</pre>
170
171
                      limit = 32 + limit;
172
                  }
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
174
                  var targetMask = sourceMask << shift;</pre>
175
                  return (target & targetMask) >> shift;
176
177
             private static Tuple<uint, uint, int> GetWriteMasksAndShift(int shift, int limit)
179
180
                  if (shift < 0)</pre>
181
                  {
182
                      shift = 32 + shift;
183
                  if (limit < 0)</pre>
185
186
                      limit = 32 + limit;
187
                  }
188
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
189
                  var targetMask = ~(sourceMask << shift);</pre>
                  return new Tuple<uint, uint, int>(targetMask, sourceMask, shift);
191
192
193
             private static Tuple<uint, int> GetReadMaskAndShift(int shift, int limit)
194
                  if (shift < 0)</pre>
196
                  {
197
                      shift = 32 + shift;
198
199
                  if (limit < 0)</pre>
200
                      limit = 32 + limit;
202
                  }
203
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
                  var targetMask = sourceMask << shift;</pre>
205
                  return new Tuple<uint, int>(targetMask, shift);
207
208
             private static uint PartialWrite(uint target, uint targetMask, uint source, uint
209

→ sourceMask, int shift) => target & targetMask | (source & sourceMask) << shift;
</p>
210
             private static uint PartialWrite(uint target, uint source, Tuple<uint, uint, int>
              masksAndShift) => PartialWrite(target, masksAndShift.Item1, source,
                 masksAndShift.Item2, masksAndShift.Item3);
212
             private static uint PartialRead(uint target, uint targetMask, int shift) => (target &

    targetMask) >> shift;

214
             private static uint PartialRead(uint target, Tuple<uint, int> masksAndShift) =>
215
              PartialRead(target, masksAndShift.Item1, masksAndShift.Item2);
216
217
             public static void BugWithLoadingConstantOf8Test()
219
                  Bit<byte>.PartialWrite(0, 1, 5, -5);
220
             }
221
         }
222
223
       ./csharp/Platform.Numbers.Tests/MathExtensionsTests.cs
1.13
   using Xunit;
 1
    namespace Platform.Numbers.Tests
 3
 5
         public static class MathExtensionsTests
 6
             [Fact]
             public static void AbsTest()
                  var number = -1L;
10
                  var returnValue = number.Abs();
Assert.Equal(1L, returnValue);
1.1
12
                  Assert.Equal(1L, number);
             }
14
15
             [Fact]
             public static void NegateTest()
17
```

```
var number = 2L;
19
                var returnValue = number.Negate();
                Assert.Equal(-2L, returnValue);
21
                Assert.Equal(-2L, number);
22
            }
24
            [Fact]
25
            public static void UnsignedNegateTest()
26
27
                var number = 2UL;
                var returnValue = number.Negate();
29
                Assert.Equal(18446744073709551614, returnValue);
30
31
                Assert.Equal(18446744073709551614, number);
            }
32
       }
33
^{34}
1.14
     ./csharp/Platform.Numbers.Tests/MathTests.cs
using Xunit;
   namespace Platform. Numbers. Tests
3
        public static class MathTests
5
            [Fact]
            public static void CompiledOperationsTest()
9
                Assert.True(Math.Abs(Arithmetic < double > .Subtract(3D, 2D) - 1D) < 0.01);
10
            }
11
       }
12
   }
1.15 ./csharp/Platform.Numbers.Tests/SystemTests.cs
using Xunit;
   namespace Platform. Numbers. Tests
3
4
        public static class SystemTests
5
            public static void PossiblePackTwoValuesIntoOneTest()
{
                uint value = 0;
1.0
                // Set one to first bit
12
                value |= 1;
13
14
                Assert.True(value == 1);
15
                // Set zero to first bit
17
                value &= OxFFFFFFE;
19
                // Get first bit
                uint read = value & 1;
21
22
                Assert.True(read == 0);
23
                uint firstValue = 1;
25
                uint secondValue = 1543;
26
                // Pack (join) two values at the same time
28
                value = (secondValue << 1) | firstValue;</pre>
29
30
                uint unpackagedFirstValue = value & 1;
31
                uint unpackagedSecondValue = (value & OxFFFFFFE) >> 1;
33
                Assert.True(firstValue == unpackagedFirstValue)
                Assert.True(secondValue == unpackagedSecondValue);
35
                // Using universal functions:
37
38
                Assert.True(PartialRead(value, 0, 1) == firstValue);
39
                Assert.True(PartialRead(value, 1, -1) == secondValue);
40
                firstValue = 0
42
                secondValue = 6892;
43
44
                value = PartialWrite(value, firstValue, 0, 1);
                value = PartialWrite(value, secondValue, 1, -1);
46
```

```
Assert.True(PartialRead(value, 0, 1) == firstValue);
Assert.True(PartialRead(value, 1, -1) == secondValue);
48
49
              }
50
             private static uint PartialWrite(uint target, uint source, int shift, int limit)
52
53
                   if (shift < 0)</pre>
54
                   {
                       shift = 32 + shift;
56
                  if (limit < 0)</pre>
58
                   {
59
                       limit = 32 + limit;
60
                  }
61
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
62
                  var targetMask = ~(sourceMask << shift);</pre>
                  return (target & targetMask) | ((source & sourceMask) << shift);</pre>
64
65
66
             private static uint PartialRead(uint target, int shift, int limit)
67
68
                   if (shift < 0)</pre>
69
                   {
70
                       shift = 32 + shift;
                  }
72
                  if (limit < 0)</pre>
73
                   {
                       limit = 32 + limit;
75
                   }
76
                  var sourceMask = ~(uint.MaxValue << limit) & uint.MaxValue;</pre>
77
                  var targetMask = sourceMask << shift;</pre>
78
                  return (target & targetMask) >> shift;
             }
80
         }
81
    }
82
```

## Index

```
./csharp/Platform.Numbers.Tests/ArithmeticExtensionsTests.cs, 10
./csharp/Platform.Numbers.Tests/ArithmeticTests.cs, 10
./csharp/Platform.Numbers.Tests/BitTests.cs, 10
./csharp/Platform.Numbers.Tests/MathExtensionsTests.cs, 13
./csharp/Platform.Numbers.Tests/MathTests.cs, 14
./csharp/Platform.Numbers.Tests/SystemTests.cs, 14
./csharp/Platform.Numbers/Arithmetic.cs, 1
./csharp/Platform.Numbers/ArithmeticExtensions.cs, 2
./csharp/Platform.Numbers/Arithmetic[T].cs, 2
./csharp/Platform.Numbers/Bit.cs, 3
./csharp/Platform.Numbers/BitExtensions.cs, 4
./csharp/Platform.Numbers/Bit[T].cs, 5
./csharp/Platform.Numbers/Math.cs, 8
./csharp/Platform.Numbers/MathExtensions.cs, 9
./csharp/Platform.Numbers/Math[T].cs, 9
```