$$\begin{split} \text{Ek} &:= \frac{m_{k} \cdot vx^{2}}{2} + \frac{m_{k} \cdot vy^{2}}{2} + \frac{J_{c} \cdot \omega \alpha^{2}}{2} + \frac{\left(J_{c1} + J_{w1} + J_{s1}\right) \cdot \left(\omega \varphi_{1}\right)^{2}}{2} + \frac{\left(J_{c1} + J_{w1} + J_{s1}\right) \cdot \left(\omega \varphi_{2}\right)^{2}}{2} + \frac{1}{2} \cdot \dots \\ &+ m_{1} \cdot \frac{\left(vx_{c1}\right)^{2}}{2} + m_{1} \cdot \frac{\left(vy_{c1}\right)^{2}}{2} + m_{1} \cdot \frac{\left(vx_{c2}\right)^{2}}{2} + m_{1} \cdot \frac{\left(vy_{c2}\right)^{2}}{2} \end{split}$$

$$\mathbf{U} := \mathbf{m_k} \! \cdot \! \mathbf{g} \! \cdot \! \mathbf{y} + \mathbf{m_1} \! \cdot \! \mathbf{g} \! \cdot \! \mathbf{y} \mathbf{c_1} + \mathbf{m_1} \! \cdot \! \mathbf{g} \! \cdot \! \mathbf{y}_{\mathbf{c}2} \dots$$

$$+ 1 + \frac{k_{y} \cdot (y + 1 \cdot \alpha)^{2}}{2} + \frac{k_{y} \cdot (y - 1 \cdot \alpha)^{2}}{2} + \frac{k_{x} \cdot (x + H \cdot \alpha)^{2}}{2} + \frac{k_{x} \cdot (-x - H \cdot \alpha)^{2}}{2}$$

$$+ 1 + \frac{k_{y} \cdot (y + 1 \cdot \alpha)^{2}}{2} + \frac{k_{y} \cdot (y - 1 \cdot \alpha)^{2}}{2} + \frac{k_{x} \cdot (x + H \cdot \alpha)^{2}}{2} + \frac{k_{x} \cdot (-x - H \cdot \alpha)^{2}}{2}$$

$$+ 1 + \frac{k_{y} \cdot (y + 1 \cdot \alpha)^{2}}{2} + \frac{k_{y} \cdot (y - 1 \cdot \alpha)^{2}}{2} + \frac{k_{x} \cdot (x + H \cdot \alpha)^{2}}{2} + \frac{k_{x} \cdot (-x - H \cdot \alpha)^{2}}{2}$$

$$D := \frac{\frac{\textbf{b}_y \cdot \left(vy + l \cdot \omega \alpha\right)^2}{2} + \frac{\textbf{b}_y \cdot \left(vy - l \cdot \omega \alpha\right)^2}{2} + \frac{\textbf{b}_x \cdot \left(-vx - H \cdot \omega \alpha\right)^2}{2} + \frac{\textbf{b}_x \cdot \left(vx + H \cdot \omega \alpha\right)^2}{2}$$

$$x_{c1} := -a \cdot \cos(\beta - \alpha) - e \cdot \cos(\phi_1) + x$$

$$y_{c1} := a \cdot \sin(\beta - \alpha) + e \cdot \sin(\phi_1) + y$$

$$\mathbf{x}_{c2} := \mathbf{a} \cdot \cos(\beta - \alpha) + \mathbf{e} \cdot \cos(\phi_2) + \mathbf{x}$$

$$y_{c2} := -a \cdot \sin(\beta - \alpha) + e \cdot \sin(\phi_2) + y$$

$$vx_{c1} := vx - a \cdot \omega \alpha \cdot \sin(\beta - \alpha) + \omega \phi_1 \cdot e \cdot \sin(\phi_1)$$

$$vy_{c1} := vy - a \cdot \omega \alpha \cdot \cos(\beta - \alpha) + \omega \phi_1 \cdot e \cdot \cos(\phi_1)$$

$$vx_{c2} := vx + a \cdot \omega \alpha \cdot \sin(\beta - \alpha) - \omega \phi_2 \cdot e \cdot \sin(\phi_2)$$

$$vy_{c2} := vy + a \cdot \omega \alpha \cdot \cos(\beta - \alpha) + \omega \phi_2 \cdot e \cdot \cos(\phi_2)$$
 Rownanie Alfa

$$\begin{aligned} \text{rown1} &:= J_c \cdot \omega \omega \alpha + 2 \cdot H \cdot b_x \cdot vx + 2 \cdot H \cdot k_x \cdot x + 2 \cdot H^2 \cdot \alpha \cdot k_x + 2 \cdot H^2 \cdot b_x \cdot \omega \alpha + 2 \cdot \alpha \cdot k_y \cdot l^2 + 2 \cdot b_y \cdot l^2 \cdot \omega \alpha + \blacksquare \dots \\ &+ 2 \cdot a^2 \cdot m_1 \cdot \omega \omega \alpha - a \cdot m_1 \cdot \left(\omega \varphi_1\right)^2 \cdot \sin \left(\beta - \alpha - \varphi_1\right) \cdot e + a \cdot m_1 \cdot \omega \omega \varphi_2 \cdot e \cdot \cos \left(\beta - \alpha + \varphi_2\right) - \blacksquare \dots \\ &+ a \cdot m_1 \cdot \omega \omega \varphi_1 \cdot \cos \left(\beta - \alpha - \varphi_1\right) \cdot e - a \cdot m_1 \cdot \left(\omega \varphi_2\right)^2 \cdot e \cdot \sin \left(\beta - \alpha + \varphi_2\right) \end{aligned}$$

$$\boldsymbol{M}_{\mbox{el1}} \coloneqq 2 \cdot \boldsymbol{M}_{ut} \cdot \left(\boldsymbol{\omega}_s - \boldsymbol{\omega}_{ut}\right) \cdot \frac{\left(\boldsymbol{\omega}_s - \boldsymbol{\omega} \boldsymbol{\varphi}_1\right)}{\left(\boldsymbol{\omega}_s - \boldsymbol{\omega}_{ut}\right)^2 + \left(\boldsymbol{\omega}_s - \boldsymbol{\omega} \boldsymbol{\varphi}_1\right)^2}$$

$$\boldsymbol{M}_{\text{el2}} \coloneqq 2 \cdot \boldsymbol{M}_{ut} \cdot \left(\boldsymbol{\omega}_s - \boldsymbol{\omega}_{ut}\right) \cdot \frac{\left(\boldsymbol{\omega}_s - \boldsymbol{\omega} \boldsymbol{\varphi}_2\right)}{\left(\boldsymbol{\omega}_s - \boldsymbol{\omega}_{ut}\right)^2 + \left(\boldsymbol{\omega}_s - \boldsymbol{\omega} \boldsymbol{\varphi}_2\right)^2}$$

$$\mathbf{Q}_{\alpha} \coloneqq \mathbf{M}_{el1} - \mathbf{M}_{el2}$$

$$Q_x := -T_{r,1}$$

$$Q_y := -F_{r,1}$$

$$Q_{\phi 1} := \mathbf{M}_{el1}$$

$$Q_{\phi 2} := \mathbf{M}_{el2}$$

## Rownianie X

$$\begin{split} &m_1 \cdot e \cdot \cos\left(\varphi_1\right) \cdot \left(\omega \varphi_1\right)^2 - m_1 \cdot e \cdot \cos\left(\varphi_2\right) \cdot \left(\omega \varphi_2\right)^2 + 2 \cdot b_x \cdot vx + 2 \cdot k_x \cdot x + 2 \cdot m_1 \cdot vvx + m_k \cdot vvx + 2 \cdot H \cdot \alpha \cdot k_x \\ &+ \textbf{1} + 2 \cdot H \cdot b_x \cdot \omega \alpha + m_1 \cdot \omega \omega \varphi_1 \cdot e \cdot \sin\left(\varphi_1\right) - m_1 \cdot \omega \omega \varphi_2 \cdot e \cdot \sin\left(\varphi_2\right) \end{split}$$

$$\begin{aligned} &2 \cdot g \cdot m_1 - m_1 \cdot e \cdot \sin\left(\varphi_2\right) \cdot \left(\omega \varphi_2\right)^2 - m_1 \cdot e \cdot \sin\left(\varphi_1\right) \cdot \left(\omega \varphi_1\right)^2 + g \cdot m_k + 2 \cdot b_y \cdot vy + 2 \cdot m_1 \cdot vvy \dots \\ &+ \textbf{1} + m_k \cdot vvy + 2 \cdot k_y \cdot y + m_1 \cdot \omega \omega \varphi_1 \cdot e \cdot \cos\left(\varphi_1\right) + m_1 \cdot \omega \omega \varphi_2 \cdot e \cdot \cos\left(\varphi_2\right) \end{aligned} \qquad \text{Rownanie Y}$$

## Rowanie fi 1

$$\begin{split} &J_{c1}\cdot\omega\omega\varphi_1+J_{s1}\cdot\omega\omega\varphi_1+J_{w1}\cdot\omega\omega\varphi_1+m_1\cdot\omega\omega\varphi_1\cdot e^2+g\cdot m_1\cdot e\cdot \cos\left(\varphi_1\right)+m_1\cdot vvy\cdot e\cdot \cos\left(\varphi_1\right)+\blacksquare\ ...\\ &+m_1\cdot vvx\cdot e\cdot \sin\left(\varphi_1\right)-a\cdot m_1\cdot\omega\alpha\cdot \cos\left(\beta-\alpha-\varphi_1\right)\cdot e-a\cdot \alpha\cdot m_1\cdot\omega\alpha\cdot \sin\left(\beta-\alpha-\varphi_1\right)\cdot e-\blacksquare\ ...\\ &+a\cdot\alpha\cdot m_1\cdot\omega\varphi_1\cdot \sin\left(\beta-\alpha-\varphi_1\right)\cdot e+a\cdot m_1\cdot\omega\alpha\cdot\omega\varphi_1\cdot \sin\left(\beta-\alpha-\varphi_1\right)\cdot e-\blacksquare\ ... \end{split}$$

$$m_{n1} \cdot vvx_1 = \mathbf{I} \cdot T_{r,1} - T_{1,2}$$

$$\mathbf{m_{n1}} \cdot \mathbf{vvy_1} = \mathbf{v} \cdot \mathbf{F_{r,1}} - \mathbf{F_{1,2}} - \mathbf{m_{n1}} \cdot \mathbf{g}$$

$$m_{n2} \cdot vvx_2 = \mathbf{I} \cdot T_{1,2}$$

$$m_{n2} \cdot vvy_2 = \mathbf{I} \cdot F_{1,2} - m_{n2} \cdot g$$

$$F_{j,(j-1,k)} = \mathbf{I} \cdot \left( \mathbf{y}_{j-1,k} - \mathbf{y}_{j,k} \right)^{p} \cdot k \cdot \left[ 1 - \frac{\left(1 - R^{2}\right)}{2} \cdot \left(1 - sgn\left(\mathbf{y}_{j-1,k} - \mathbf{y}_{j,k}\right) \cdot sgn\left(\mathbf{v}\mathbf{x}_{j-1,k} - \mathbf{v}\mathbf{x}_{j,k}\right) \right) \right]$$

$$\boldsymbol{F}_{t(j\,,\,j-1\,,\,k)} = \boldsymbol{\text{\tiny 1}} \cdot -\boldsymbol{\mu} \cdot \boldsymbol{F}_{j\,(j-1\,,\,k)} \cdot sgn\!\!\left(\!\!\!\begin{array}{c} \boldsymbol{vx} \\ \boldsymbol{v}_{j\,,\,k} - \boldsymbol{vx}_{j-1\,,\,k} \end{array}\!\!\right)$$

