Going Deep

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February 21, 2019

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$$|F(x) - f(x)| < \epsilon$$
 for all $x \in I_m$.

Then Why Go Deep?

- There are functions you can compute with a deep neural network that shallow networks require exponentially more hidden units to compute.
- ▶ The following function is more efficient to implement using a deep neural network: $y = x_1 \oplus x_2 \oplus x_3 \oplus \cdots \oplus x_n$

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- In training, the gradient may become vanishingly small (or large), effectively preventing the weight from changing its value (or exploding in value).
- ▶ This leads to the neural network not being able to train.
- ► This issue affects many-layered networks (feed-forward), as well as recurrent networks.

➤ One of the most effective ways to resolve the vanishing gradient problem is with residual neural networks (ResNets)¹.

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- ResNets are artificial neural networks that use skip connections to jump over layers.
- ► The vanishing gradient problem is mitigated in ResNets by reusing activations from a previous layer.

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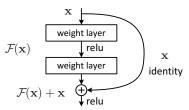


Figure 2. Residual learning: a building block.².

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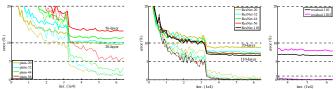


Figure 6. Training on CIFAR-10. Dashed lines denote training error, and bold lines denote testing error. Left: plain networks. The error of plain-110 is higher than 60% and not displayed. Middle: ResNets. Right: ResNets with 110 and 1202 layers.

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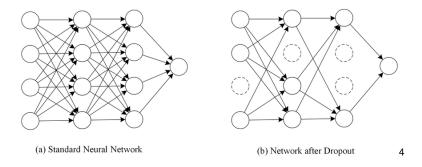
Regularization in Deep Networks

- ▶ L1 and L2 norm
- ► Dropout

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- The key idea in dropout is to randomly drop neurons, including all of the connections, from the neural network during training.



⁴Image from: https://www.researchgate.net/figure/ Dropout-neural-network-model-a-is-a-standard-neural-network-b-is-the-sfig3_309206911

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- ▶ Neurons cannot co-adapt to other units (they cannot assume that all of the other units will be present)
- By breaking co-adaptation, each unit will ultimately find more general features