

# Recurrent Neural Networks

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## Batch Normalization

- ▶ Batch normalization (BN) is a technique for improving the performance of ANNs
- ▶ It improves the stability of ANNs by adjusting and scaling the activations
- ▶ BN makes your ANN more robust to the choice of hyperparameters (larger range of parameters that will work well)
- ▶ It was introduced by Sergey Ioffe and Christian Szegedy in 2015 <sup>1</sup>

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<sup>1</sup><https://arxiv.org/pdf/1502.03167.pdf>

## Batch Normalization

**Input:** Values of  $x$  over a mini-batch:  $\mathcal{B} = \{x_1 \dots x_m\}$ ;

Parameters to be learned:  $\gamma, \beta$

**Output:**  $\{y_i = \text{BN}_{\gamma, \beta}(x_i)\}$

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \quad // \text{ mini-batch mean}$$

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \quad // \text{ mini-batch variance}$$

$$\hat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \quad // \text{ normalize}$$

$$y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \text{BN}_{\gamma, \beta}(x_i) \quad // \text{ scale and shift}$$

**Algorithm 1:** Batch Normalizing Transform, applied to activation  $x$  over a mini-batch.

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## Batch Normalization

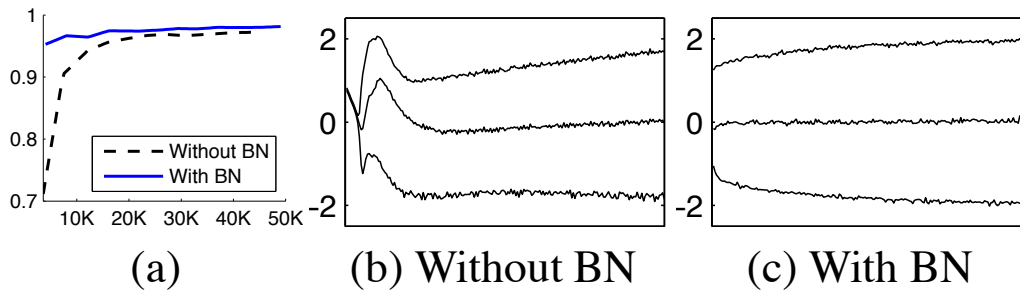


Figure 1: (a) *The test accuracy of the MNIST network trained with and without Batch Normalization, vs. the number of training steps. Batch Normalization helps the network train faster and achieve higher accuracy.* (b, c) *The evolution of input distributions to a typical sigmoid, over the course of training, shown as  $\{15, 50, 85\}$ th percentiles. Batch Normalization makes the distribution more stable and reduces the internal covariate shift.*

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## Batch Normalization

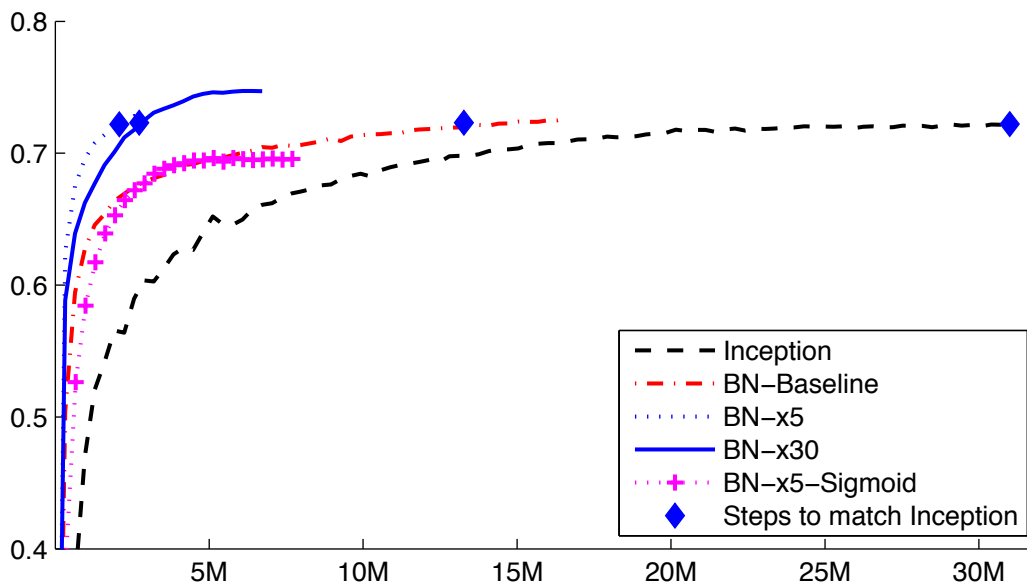


Figure 2: *Single crop validation accuracy of Inception and its batch-normalized variants, vs. the number of training steps.*

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## Recurrent Neural Networks - Motivation

x: Kate Farrahi and Jonathon Hare teach deep learning

y: 1 1 0 1 1 0 0 0

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# Recurrent Neural Networks - Motivation

x:  $x^{<1>}$     $x^{<2>}$    ...    $x^{<t>}$    ...    $x^{<T_x>}$   
x:   Kate   Farrahi   ...   Hare   ...   learning

y:  $y^{<1>}$     $y^{<2>}$    ...    $y^{<t>}$    ...    $y^{<T_y>}$   
y:   1   1   ...   1   ...   0

In this example,  $T_x = T_y = 8$  but  $T_x$  and  $T_y$  can be different.

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## One Hot Encoding

How can we represent individual words?

"a"	"abbreviations"		"zoology"	"zoom"
1	0		0	0
0	1		0	1
0	0		0	0
.	.		.	.
.	.	...	.	.
.	.		.	.
0	0		0	0
0	0		1	0
0	0		0	1

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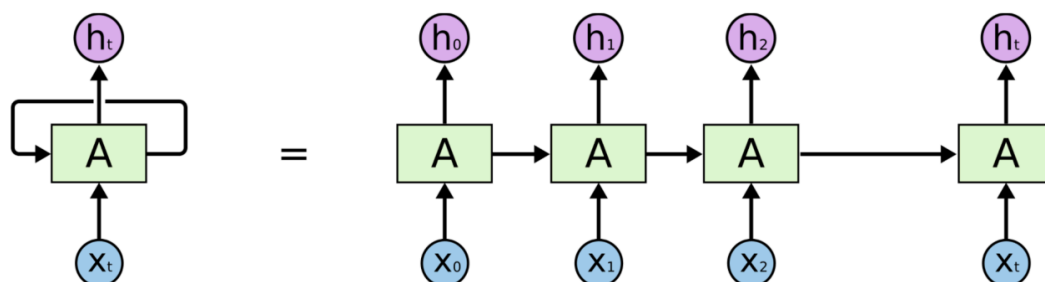
<sup>2</sup><https://ayearofai.com>

# Why Not a Standard Feed Forward Network?

- ▶ For a task such as "Named Entity Recognition" a feed forward network would have several disadvantages
- ▶ The inputs and outputs may have varying lengths
- ▶ The features wouldn't be shared across different positions in the network

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## Recurrent Neural Networks



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- ▶ RNNs are a family of ANNs for processing sequential data
- ▶ RNNs have directed cycles in their computational graphs
- ▶ They can have complicated dynamics, difficult to train
- ▶ They are more biologically realistic

<sup>3</sup>Image taken from <https://towardsdatascience.com>

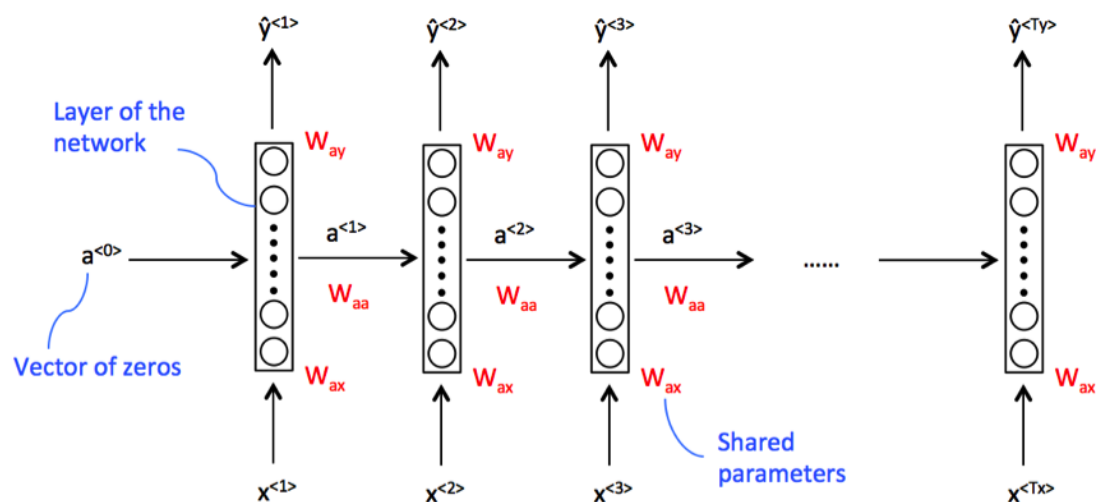
# Recurrent Neural Networks

RNNs combine two properties which make them very powerful.

1. Distributed hidden state that allows them to store a lot of information about the past efficiently. This is because several different units can be active at once, allowing them to remember several things at once.
2. Non-linear dynamics that allows them to update their hidden state in complicated ways. They can however have complicated dynamics, making them difficult to train

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## Backpropagation Through Time (BPTT)



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<sup>4</sup>Image taken from Andrew Ng

## BPTT - Forward Pass

$$a^{<t>} = g(w_{aa}a^{<t-1>} + w_{ax}x^{<t>} + b_a) \quad (1)$$

$$\hat{y}^{<t>} = g(w_{ya}a^{<t>} + b_y) \quad (2)$$

$$\mathcal{L}^{<t>} = -y^{<t>} \log(\hat{y}^{<t>}) - (1 - y^{<t>}) \log(1 - \hat{y}^{<t>}) \quad (3)$$

$$\mathcal{L} = \sum_{t=1}^{T_y} \mathcal{L}^{<t>} \quad (4)$$

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## BPTT - Backwards Pass

$$\frac{\partial \mathcal{L}^{<3>}}{\partial w_{ya}} = \frac{\partial \mathcal{L}^{<3>}}{\partial \hat{y}^{<3>}} \frac{\partial \hat{y}^{<3>}}{\partial w_{ya}} \quad (5)$$

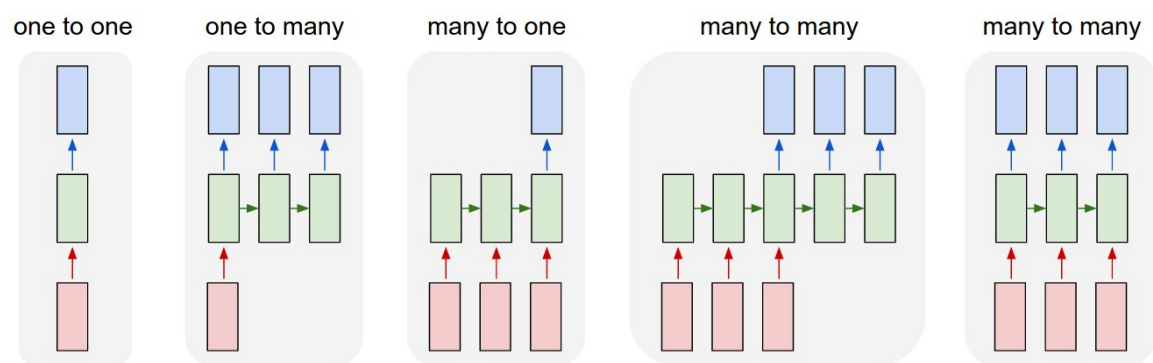
$$\frac{\partial \mathcal{L}^{<3>}}{\partial w_{aa}} = \frac{\partial \mathcal{L}^{<3>}}{\partial \hat{y}^{<3>}} \frac{\partial \hat{y}^{<3>}}{\partial a^{<3>}} \frac{\partial a^{<3>}}{\partial w_{aa}} \quad (6)$$

$$(7)$$

$$\begin{aligned} \text{Recall } a^{<3>} &= g(w_{aa}a^{<2>} + w_{ax}x^{<3>} + b_a) \\ \frac{\partial \mathcal{L}^{<3>}}{\partial w_{aa}} &= \frac{\partial \mathcal{L}^{<3>}}{\partial \hat{y}^{<3>}} \frac{\partial \hat{y}^{<3>}}{\partial a^{<3>}} \frac{\partial a^{<3>}}{\partial a^{<2>}} \frac{\partial a^{<2>}}{\partial a^{<1>}} \frac{\partial a^{<1>}}{\partial w_{aa}} \end{aligned} \quad (8)$$

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# Recurrent Neural Networks



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<sup>5</sup><http://karpathy.github.io/2015/05/21/rnn-effectiveness/>