# COMP6248 Differentiable Programming

(and some Deep Learning)

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All credit for this slide goes to Niranjan

Data

$$\{x_n, y_n\}_{n=1}^N \qquad \{x_n\}_{n=1}^N$$

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Prediction	$\hat{\mathbf{y}}_{N+1} = f(\mathbf{x}_{N+1}, \hat{\boldsymbol{\theta}})$

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Regularisation

Modelling Uncertainty  $p(\theta | \{x_n, y_n\}_{n=1}^N)$ 

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Sequence Modelling 
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In the early days the focus of deep learning was on learning functions for classification. Nowadays the functions are much more general in their inputs and outputs.

 Differentiable programming is a term coined by Yann Lecun<sup>1</sup> to describe a superset of Deep Learning.

<sup>&</sup>lt;sup>1</sup>https://www.facebook.com/yann.lecun/posts/10155003011462143

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  - The implication is that we need to be able to compute gradients with respect to the parameters of these functional blocks. We'll start explore this in detail next week...
  - The idea of Differentiable Programming also opens up interesting possibilities:
    - The functional blocks don't need to be direct functions in a mathematical sense; more generally they can be algorithms.
    - What if the functional block we're learning parameters for is itself an algorithm that optimises the parameters of an internal algorithm using a gradient based optimiser?!<sup>2</sup>

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- Not necessarily!
  - Most deep learning systems are trained using first order gradient-based optimisers, but there is an active body of research on gradient-free methods.

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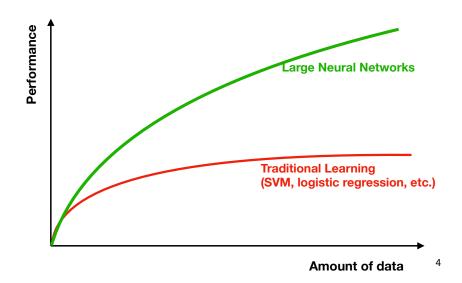
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- There is an increasing interest in methods that use different styles of learning, such as Hebbian learning, within deep networks. More broadly there are a number of us<sup>3</sup> who are interested in biologically motivated models and learning methods.
- This course will primarily focus on differentiable methods, but we'll look at how relaxations can be made to make non-differentiable operators learnable with gradient-based optimisers.

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# Why should we care about this?



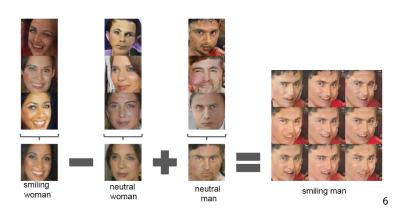
<sup>&</sup>lt;sup>4</sup>Reference: Andrew Ng

# Success stories - Object detection and segmentation



<sup>&</sup>lt;sup>5</sup>Pinheiro, Pedro O., et al. "Learning to refine object segments." European Conference on Computer Vision. Springer, Cham, 2016.

# Success stories - Image generation



<sup>&</sup>lt;sup>6</sup>Radford, Alec, Luke Metz, and Soumith Chintala. "Unsupervised representation learning with deep convolutional generative adversarial networks." arXiv preprint arXiv:1511.06434 (2015).

#### Success stories - Translation

- ENGLISH TEXT
- The reason Boeing are doing this is to cram more seats in to make their plane more competitive with our products," said Kevin Keniston, head of passenger comfort at Europe's Airbus.
- TRANSLATED TO FRENCH
- La raison pour laquelle Boeing fait cela est de creer plus de sieges pour rendre son avion plus competitif avec nos produits", a declare Kevin Keniston, chef du confort des passagers chez Airbus.

9 / 18

<sup>&</sup>lt;sup>7</sup>Wu, Yonghui, et al. "Google's neural machine translation system: Bridging the gap between human and machine translation." arXiv preprint arXiv:1609.08144 (2016).

A word of warning: This is not a module about how to apply someone else's deep network architecture to a task, or how to train existing models!

You will learn some of that along the way of course, but the real objective is for you to graduate knowing how to understand, critique and implement new and recent research papers on deep learning and associated topics.

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- Gain facility in working with deep learning libraries in order to create and evaluate network architectures.
- Oritically appraise the merits and shortcomings of model architectures on specific problems.

### What will we cover in the module?

http://comp6248.ecs.soton.ac.uk/

### How is this module going to be delivered?

- Lectures
  - Note: I am refreshing some material from last year, but the website still has links to the old slides.
  - You need to read the suggested papers/links before the lectures!
- 2 Labs

# Lab session plan

Lab	Date	Topic
Lab 1	05/02/20	Introducing PyTorch
Lab 2	12/02/20	Automatic Differentiation
Lab 3	19/02/20	Optimisation
Lab 4	26/02/20	NNs with PyTorch and Torchbearer
	04/03/20	NO LAB
Lab 5	11/03/20	CNNs with PyTorch and Torchbearer
Lab 6	18/03/20	Transfer Learning
Lab 7	18/03/20	RNNs, Sequence Prediction and Embeddings
	Break	
Lab 7	22/04/20	RNNs, Sequence Prediction and Embeddings
Lab 8	29/04/19	Deep Generative Models
	06/05/19	Coursework Help and Advice
	13/05/19	Coursework Help and Advice

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- Programming in Python

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- How to perform differentiable sampling of a Multivariate Normal Distribution?

#### Assessment Structure

- 1 Lab work 40%
- Final project 40% Handin in Week 12 (15th May, 4PM)
- Online quizzes 20% Planned for Thursdays in Weeks 6 (5th-Mar) and 10 (30-Apr)

# The Main Assignment

The ICLR Reproducibility Challenge

http://comp6248.ecs.soton.ac.uk/coursework.html