en jaune, éléments pas clairs/à préciser

# **HEART: HiErarchical Abstraction for Real-Time partial order planning**

## Paper #1788

Préciser en footnote ce que c'est: In diverse planning the objective is to find a set of plans m that are at least d distance away from each other.

soft constraints: touiours pas clair ...

#### Abstract

When asked about the biggest issues with automated planning, the answer often consists of speed, quality, and expressivity. However, certain applications need a mix of these criteria. Most existing solutions focus on one area while not addressing the others. We aim to present a new method to compromise on these aspects in respect to demanding domains like assistive robotics, intent recognition, and real-time computations. The HEART planner is an anytime planner based on a hierarchical version of Partial Order Planning (POP). Its principle is to retain a partial plan at each abstraction level in the hierarchy of actions. While the intermediary plans are not solutions, they meet criteria for usages ranging from explanation to goal inference. This paper also evaluates the variations of speed/quality combinations of the abstract plan in relation to the complete planning process.

Our research project on intent recognition using assistive robots requires being able to execute complex human-related tasks on robots with limited processing power and to give answers in real time (within a polling period).

Planners are not meant to solve recognition problems. However, several works extended what is called in psychology as the theory of mind. That theory supposes that to recognize the intents and goals of others we simply transpose our own. It is equivalent to ask "what would I do I was them?" when observing the behavior of other agents. This leads to new ways to use inverted planning as an inference tool. One of the first to propose that idea was Baker et al. [Baker, Tenenbaum, & Saxe, 2007] that uses Bayesian planning to infer intentions. Another one was Ramirez et al. [Ramirez & Geffner, 2009] that found an elegant way to transform a plan recognition problem into classical planning. This is done simply by encoding observation constraints into the planning domain [Baioletti, Marcugini, & Milani, 1998] to ensure the selection of actions in the order that they were observed. A cost comparison will then give us a probability of the goal to be pursued made the observations.

Some works extended this with multi-goal recognition [J. Chen, Chen, Xu, Huang, & Chen, 2013] and even robotic applications [Talamadupula, Briggs, Chakraborti, Scheutz, & Kambhampati, 2014]. A new method, proposed by Sohrabi et al. [Sohrabi, Riabov, & Udrea, 2016], makes the recognition fluent centric. It assigns costs to missing or noisy observed fluents by using soft constraints. This method also uses a meta-goal that combines each possible goal and is realized when at least one of them is satisfied. Sohrabi et al. state that the quality of the recognition is directly linked to the quality and properties of the generated plans. This is why guided diverse planning was preferred along with the ability to infer several probable goals at once.

Obviously, extensive problems need more computation time in order for a solution to be found. This is especially true in automated planning as it has been proven to be a P-SPACE problem if not harder[Weld, 1994]. Sizable problems are usually intractable within the tight constraints of real-time robotics. The problem of dealing with unsolvability has already been addressed in [Göbelbecker, Keller, Eyerich, Brenner, & Nebel, 2010] where "excuses" are being investigated as potential explanations for when a problem has no solutions. The closest way to address time una problem has no solutions. The closest way to address time unsolvability is by using explainability [Fox, Long, & Magazzeni, solvability is by using explainability [Fox, Long, & Magazzeni, and the complete solution as defined by the complete solution as a problem has no solutions. The closest way to address time unsolvability is by using explainability [Fox, Long, & Magazzeni, and the complete solution as a problem has no solutions. The closest way to address time unsolvability is by using explainability [Fox, Long, & Magazzeni, and the complete solution as a problem has no solutions. The closest way to address time unsolvability is by using explainability [Fox, Long, & Magazzeni, and the complete solution as a problem has no solutions. The closest way to address time unsolvability is by using explainability [Fox, Long, & Magazzeni, and the complete solution as a problem has no solutions. The closest way to address time unsolvability is by using explainability [Fox, Long, & Magazzeni, and the complete solution as a problem has no solutions. solvability is by using explainability [Fox, Long, & Magazzeni, much as an explanation of the plan.

> For intent recognition, an important metric is the number of correct fluents. So if finding a complete solution is impossible, a partial solution can meet enough criteria to give a good approximation of the goal probability. One of the main approaches to automated planning is called Partial Order Planning (POP). It works by refining partial plans into a solution. Another approach is Hierarchical Task Networks (HTN) that are meant to process the problem using composite actions in order to define hierarchical tasks within the plan. These two approaches are not exclusive and have been combined in several works [Pellier & Fiorino, 2007, Gerevini, Kuter, Nau, Saetti, & Waisbrot [2008]]. Our work is complet based on HiPOP [Bechon, Barbier, Infantes, Lesire, & Vidal, Hierarchical POF 2014], that is expanding the classical POP algorithm with new (HiPOP) flaws in order to make it solves HTN problems. Planning with solve? HTN makes for high-level plans which have been found to be quite effective when applied to intent recognition [Höller, Bercher, Behnke, & Biundo, 2018]. cf biblio, la ref n'est pas complète

In the rest of the paper, we will describe how HiErarchical Abstraction for Real-Time partial order planning (HEART) can create abstract intermediary plans that can be used for intent recognition within our time constraints.

planS

Table 1: Most of the symbols used in the paper.

Symbol	Description
pre(a), eff(a)	Preconditions and effects of the action $a$ .
methods(a)	Methods of the action $a$ .
$\mathcal{D}, \mathcal{P}$	Planning domain and problem.
$lv(a), lv(\mathcal{D})$	Abstraction level of the action or domain.
$\phi^{\pm}(l)$	Signed incidence function for partial order plans.
• • •	$\phi^-$ gives the source and $\phi^+$ the target step of l.
	No sign gives a pair corresponding to link <i>l</i> .
causes(l)	Gives the causes of a causal link $l$ .
$a_a > a_s$	Step $a_a$ is anterior to the successor step $a_p$ .
$L^{\pm}(a)$	Set of incoming $(L^{-})$ and
	outgoing $(L^+)$ links of step $a$ .
	No sign gives all adjacent links.
$l \downarrow a$	Link $l$ participates in the partial support of step $a$ .
$\downarrow_f a$	Fluent $f$ isn't supported in step $a$ .
$\pi \downarrow a$	Plan $\pi$ fully supports $a$ .
	If no left side, it means just full support.
$A_{r}^{n}$	Proper actions set of x down n levels.
	$A_x$ for $n = 1$ and $A_x^*$ for $n = lv(x)$ .
[exp]	Iverson brackets: 0 if $exp = false$ , 1 otherwise.

#### 1 Definitions

In this paper, we use the notations defined in table 1. Our notations are adapted from the ones used in [Ghallab, Nau, & Traverso, 2004], [Göbelbecker et al., 2010], graph theory, and propositional logic. The symbol  $\pm$  is only used to signify that the notation has signed variants. All related notions will be defined later.

Planners often work in two phases: first we compile the planning domain then we give the planner an instance of a corresponding planning problem to solve.

## 1.1 Domain

The domain specifies the allowed operators that can be used to plan and all the fluents they use for preconditions and effects.

**Definition 1** (Domain). A domain is a tuple  $\mathcal{D} = \langle C_{\mathcal{D}}, R, F, O \rangle$  where :

- $C_{\mathcal{D}}$  is the set of **domain constants**.
- *R* is the set of **relations** (also called *properties*) of the domain. These relations are similar to quantified predicates in first order logic.
- F is the set of **fluents** used in the domain to describe operators
- O is the set of **operators** which are fully lifted *actions*.

*Example*: The example domain in listing 1 is inspired from the kitchen domain of [Ramirez & Geffner, 2010].

```
9 infuse(extract,liquid,container) ::
    Action;
10 make(drink) :: Action;
```

Listing 1: Domain file used in our planner. Composite actions have been truncated for lack of space.

**Definition 2** (Fluent). A fluent is a parameterized relation  $f = r(arg_1, arg_2, ..., arg_n)$  where :

- *r* is the relation of the fluent under the form of a boolean predicate.
- $arg_i | i \in [1, n]$  are the arguments (possibly quantified).
- n = |r| is the arity of r.

Fluents are signed. Negative fluents are noted  $\neg f$  and behave as a logical complement. The quantifiers are affected by the sign of the fluents. We don't use the closed world hypothesis: fluents are not satisfied until provided whatever their sign.

*Example*: When we want to describe an item not being held we can use the fluent  $\neg taken(item)$ . If the cup contains water in(water, cup) is true.

The central notion of planning is operators. Instanciated operators are called *actions*. In our framework, actions can be partially instantiated and therefore we consider operators as a special case of actions.

**Definition 3** (Action). An action a is an instantiated operator of the domain. It can have instantiation parameters. We note it  $a = \langle name, pre, eff, methods \rangle$  where :

- name is the name of the action.
- pre and eff are sets of fluents that are respectively the preconditions and effects of the action.
- methods is a set of methods (partial order plans) that can realize the action.

*Example*: The precondition of the operator take(item) is simply a single negative fluent noted  $\neg taken(item)$  ensuring the variable item isn't already taken.

*Composite* actions are represented using methods. Each method is a partial order plan used in Partial-Order Planning (POP). An action without methods is called *atomic*.

**Definition 4** (Plan). A partially ordered plan is an *acyclic* directed graph  $\pi = (S, L)$  with :

- *S* the set of **steps** of the plan as vertices. A step is an action belonging in the plan.
- L the set of causal links of the plan as edges. We note
   l: a<sub>s</sub> → a<sub>t</sub> the link between its source a<sub>s</sub> and target a<sub>t</sub> caused by c.

In our representation, ordering constraints are defined as the transitive cover of causal links over the set of steps. We note ordering constraints like this:  $a_a > a_s$  with  $a_a$  being anterior to its successor  $a_s$ . Ordering constraints can't form cycles meaning that the steps must be different and that the successor can't also be anterior to its anterior steps:  $a_a \neq a_s \land a_s \not\succ a_a$ .

If we need to enforce order, we simply add a causal link without cause. This graph representation along with the implicit ordering constraints makes for a simplified framework that still retains classical properties needed for POP.

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Our representation in files for methods is very simplified and only give causeless causal links. The causes of each links to the preconditions and effects of the composite action are inferred. This inference is done by running an instance of POP on the method (keeping the composite action as intended) while compiling the domain. We use the following formula to compute the final result:  $pre(a) = \bigcup_{a_s \in L^+(a)} causes(a_s)$  and  $eff(a) = \bigcup_{a_s \in L^-(a)} causes(a_s)$ . Errors are reported if POP cannot be completed or if one of the two following rules are not met:

- Methods must contain an initial and goal step along with a guarantee of the respect of order constraints between the two  $(I_m > G_m)$ 
  - and they must not contain their parent action as a step or as a step of any composite actions within them (a ∉ A<sub>a</sub>\*, see section 3.1).

#### 1.2 Problem

The other part of the input of most planners is the problem instance. This problem is often most simply described by two components: the initial state and the goal of the problem.

**Definition 5** (Problem). The planning problem is defined as a tuple  $\mathcal{P} = \langle \mathcal{D}, \mathcal{C}_{\mathcal{P}}, \Omega \rangle$  where :

- $\mathcal{D}$  is a planning domain.
- C<sub>p</sub> is the set of **problem constants** disjoint from the domain constants.
- Ω is the problem's root operator which methods are solutions of the problem.

The root operator contains the initial state and goal specifications (noted respectively I and G) of the problem.

*Example*: We use a simple problem for our example domain. The initial state provides that nothing is ready, taken or hot and all containers are empty (all using quantifiers). The goal is to have everything needed to have tea ready. For reference, here is the problem as stated in our file:

```
1 init eff (hot(~), taken(~), placed(~), ~
    in ~);
2 goal pre (hot(water), tea in cup, water
    in cup, placed(spoon), placed(cup));
```

Listing 2: Example problem instance for the kitchen domain.

In all cases, the root operator is initialized to  $\Omega = \langle ", s_0, s^*, \{\pi\} \rangle$  with  $s_0$  being the initial state and  $s^*$  the goal specifications

The method  $\pi$  is a partial order plan with only the initial and goal steps linked together. Partial order plans are at the heart of Partial Order Planning (POP).

*Example*: The initial partial order plan is  $\pi = (\{I, G\}, \{I \rightarrow G\})$  with :

```
• I = \langle "init", \varnothing, s_0, \varnothing \rangle and
• G = \langle "goal", \varnothing, s^*, \varnothing \rangle.
```

The goal of the planner is to refine the plan  $\pi$  until it becomes a solution to the problem.

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### 1.3 Partial Order Planning

Our method is based on the classical POP algorithm which works by refining a partial plan into a solution by removing all its flaws recursively.

**Definition 6** (Flaws). Flaws have a *proper fluent* f and a related step often called the *needer*  $a_n$ . Flaws in a partial plan are either :

- Subgoals are *open conditions* that are yet to be supported by another step  $a_n$  often called *provider*.
- Threats are caused by steps that can break a causal link with their effects. They are called *breakers* of the threatened link.

A step  $a_b$  is threatening a causal link  $a_p \xrightarrow{f} a_n$  if and only if  $\neg f \in eff(a_b) \land a_p > a_b > a_n$ . Said otherwise, the breaker can cancel an effect of a providing step before it gets used by its needer.

*Example*: In our initial plan, there are two unsupported subgoals: one to make the tea ready and another to put sugar in it. In this case, the needer is the goal step and the proper fluents are each of its preconditions.

These flaws need fixing before the plan can become a solution. In POP it is done by finding resolvers.

**Definition 7** (Resolvers). Classical resolvers are additional causal links. It is a kind of mirror image of flaws.

- For subgoals, the resolvers are a set of potential causal links containing the proper fluent f in their causes while taking the needer step a<sub>n</sub> as their target.
- For threats, there are usually only two resolvers: demotion and promotion of the breaker relative to the threatened link.

Example: the subgoal for sugar in our example can be solved by using the action pour(water, cup) as the source of a causal link carrying the proper fluent as its only cause. The application of a resolver is not necessarily a step in the right direction. It can have consequences that may require reverting its application in order to be able to solve the problem.

**Definition 8** (Side effects). Flaws that arise because of the application of a resolver are called *related flaws*. They are inserted in the *agenda* (a set of flaws supporting flaw selection) with each application of a resolver:

- Related subgoals are all the new open conditions inserted by new steps.
- Related threats are the causal links threatened by the insertion of a new step or the deletion of a guarding link.

Flaws can also become irrelevant when a resolver is applied. It is always the case of the targeted flaw but this can also affect other flaws. Those *invalidated flaws* are removed from the agenda upon detection:

- *Invalidated subgoals* are subgoals satisfied by the new causal links or the removal of their needer.
- Invalidated threats happen when the breaker no longer threatens the causal link because the order guards the threatened causal link or either of them has been removed.

related sibgoal

Example: adding the action pour(water, cup) causes another subgoal with each of the action's preconditions which are that the cup and the water must be taken and water not already in the cup.

In that last, definition we mentioned effects that aren't present in classical POP, namely *negative effects*. All classical resolvers only add elements to the partial plan. Our method needs to occasionally remove steps so we plan ahead accordingly.

In algorithm 1 we present our generic version of POP based on [Ghallab et al., 2004, sec. 5.4.2].

### Algorithm 1 Partial Order Planner

```
1 function pop(Agenda \alpha, Problem \mathcal{P})
                               > Populated agenda of flaws needs to be
 2
       if a = \emptyset then
   provided
 3
            return Success
                                                      ▶ Stops all recursion
 4
        Flaw f \leftarrow \text{choose}(a)
                                   ▶ Chosen flaw removed from agenda
 5
        Resolvers R \leftarrow \text{solve}(f, \mathcal{P})
 6
        for all r \in R do
                                   ▶ Non-deterministic choice operator
 7
                                         > Apply resolver to partial plan
            apply(r, \pi)
 8
            Agenda a' \leftarrow \text{update}(a)
 9
            if pop(a', \mathcal{P}) = Success then
                                                     ▶ Refining recursively
10
                return Success
11
                                    ▶ Failure, undo resolver application
            revert(r, \pi)
12
                                                   ▶ Flaw wasn't resolved
        a \leftarrow a \cup \{f\}
                            ▶ Revert to last non-deterministic choice of
13
        return Failure
   resolver
```

# 2 Approach

Our method is using POP with HTN. In this section, we explain how our method combines both approaches and how they are used to generate intermediary abstract plans.

### 2.1 Abstraction in POP

In order to handle abstraction with POP, there are a couple of ways. The most straightforward way is illustrated in another planner called Duet [Gerevini et al., 2008] by simply managing hierarchical actions separately from a regular planner. We chose another way strongly inspired by the works of Bechon *et al.* on a planner called HiPOP [Bechon et al., 2014]. This planner is adapting HTN notions for POP by extending it and modifying its behavior. For that, we need to introduce new flaws and resolvers.

**Definition 9** (Abstraction flaw). It occurs when a partial plan contains a step with a non-zero level. This step is the needer  $a_n$  of the flawon ne sait pas ce qu'est un level pour un step !!! préciser (cf. Def. 11)

- Resolvers: An abstraction flaw is solved with an **expansion resolver**. The resolver will replace the needer with one of its instantiated methods in the plan. This is done by linking all causal links to the initial and goal steps of the method as such:  $L^-(I_m) = L^-(a_n) \wedge L^+(G_m) = L^+(a_n)$  with  $m \notin methods(a_n)$ . This means that all incoming links will be redirected to the initial step of the method and all outgoing links will be linked from the goal of the method.
- *Side effects*: An abstraction flaw can be related to the introduction of a composite action in the plan by any resolver and invalidated by its removal.

Example: When adding the step make(tea) in the plan to solve the subgoal that needs tea being made, we also introduce

an abstraction flaw that will need the step replaced by its method using an expansion resolver.

One of the main focuses of HiPOP is to handle the issues caused by hierarchical domains when solved with POP. These issues are mostly linked to the way the expansion resolver might introduce new flaws and the optimal order in which solving these issues. One way this is handled is by always choosing to solve the abstraction flaws first. While this may arguably make the full resolution faster, it also loses opportunities to obtain abstract plans in the process.

### 2.2 Cycles

In order to simplify further expressions, we define two other notions:

**Definition 10** (Proper actions). Proper actions are actions that are "contained" within an entity: \* For a *domain* or a *problem* it is  $A_{\mathcal{D}|\mathcal{P}} = O$ . \* For a *plan* it is  $A_{\pi} = S_{\pi}$ . \* For an *action* it is  $A_a = \bigcup_{m \in methods(a)} S_m$ . That can be extended down several levels recursively:  $A_a^n = \bigcup_{a' \in A_a} A_{a'}^{n-1}$ .

We note  $A_a^* = A_a^{lv(a)}$  the complete set of all proper actions of the action a.

*Example*: The proper actions of make(drink) are the actions contained within its methods. Its complete set of proper actions is that plus all proper actions of its single proper composite action infuse(drink, water, cup).

**Definition 11** (Abstraction level). This is a measure of the maximum amount of abstraction an entity can hold:<sup>1</sup>

$$lv(x) = \left(\max_{a \in A_x} (lv(a)) + 1\right) [A_x \neq \emptyset]$$

Example: The abstraction level of any atomic action is 0 while it is 2 for the composite action make(drink). The example domain has an abstraction level of 3.

The main focus of our work is toward obtaining **abstract plans** which are plans that are completed while still containing abstract actions.

**Definition 12** (Cycle). During a cycle, all abstraction flaws are delayed. Each cycle has a designated *abstraction level* that limits the resolver selection for subgoals. Only operators of a level less than or equal to this level are allowed to be inserted in the plan. Once no more flaws other than abstraction flaws are present in the agenda, the current plan is saved and all remaining abstraction flaws are solved at once. Each cycle produces a more detailed abstract plan than the one before.

This allows the planner to do an approximative form of anytime execution. At anytime the planner is able to return a fully supported plan. Before the first cycle, the plan returned is the following  $I \xrightarrow{s_0} \Omega \xrightarrow{s^*} G$ . We use the root operator to indicate that no cycles have been completed.

*Example*: In our case using the method of intent recognition explained in [Sohrabi et al., 2016], we can already use this plan to find a likely goal explaining an observation (a set of temporally ordered fluents). That can make an early assessment of the probability of each goal of the recognition problem.

<sup>&</sup>lt;sup>1</sup>We use Iverson brackets here, see notations in table 1.

These intermediary plans are not solutions of the problem. However, they have some interesting properties that make them useful for several other applications. In order to find a solution, the HEART planner needs to reach the final cycle of abstraction level 0.

Example run: In the figure 1, we illustrate the way our example problem is progressively solved. Before the first cycle (level 3) all we have is the root operator. Then within the first cycle, we select the composite action make(tea) instanciated from the operator make(drink) along with its methods. All related flaws are fixed until all that is left is the abstract flaw. We save the partial plan for this cycle and expand make(tea) into a copy of the current plan for the next cycle.

### 3 Properties

First, we need to prove that our approach conserves the properties of classical POP when given enough time to complete.

#### 3.1 Soundness

For an algorithm to be sound, it needs to provide only *valid* solutions. Our approach can provide invalid plans but that happens only on interruptions and is clearly stated in the returned data. In order to prove soundness we first need to define the notion of support.

**Definition 13** (Support). An open condition f of a step a is supported in a partial order plan  $\pi$  if and only if  $\exists l \in L_{\pi}^{-}(a) \land \nexists a_b \in S_{\pi} : f \in causes(l) \land (\phi^{-}(l) \succ a_b \succ a \land \neg f \in eff(a_b))$ . This means that the fluent is provided by a causal link and isn't threatened by another step. We note this  $\pi \downarrow_f a$ .

**Full support** of a step is achieved when all its preconditions are supported:  $\pi \Downarrow a \equiv \forall f \in pre(a) : \pi \downarrow_f a$ .

We also need to define validity in order to derive all the equivalences of it:

**Definition 14** (Validity). A plan  $\pi$  is a valid solution of a problem  $\mathcal{P}$  if and only if  $\forall a \in S_{\pi} : \pi \Downarrow a \land lv(a) = 0$ .

It is reminded that  $G \in S_{\pi}$  by definition and that it is an atomic action

We can now start to prove the soundness of our approach. We base this proof upon the one done in [Erol, Hendler, & Nau, 1994]. It states that for classical POP if a plan doesn't contain any flaws it is fully supported. Our main difference being with abstraction flaws we need to prove that its resolution doesn't leave classical flaws unsolved in the resulting plan.

**Lemma** (Expansion with an empty method). If a composite action a is replaced by an empty method  $m = (\{I_m, G_m\}, \{I_m \to G_m\})$ , replace a with  $I_m$  in all needers of existing flaws and we add all open conditions of  $G_m$  as subgoals the resulting plan will not have any undiscovered flaws.

*Proof.* The initial and goal step of a method are *transparent* (pre(a) = eff(a)).

$$L^{-}(I_{m}) = L^{-}(a) \land pre(I_{m}) = pre(a) \implies (\pi \Downarrow a \equiv \pi \Downarrow I_{m})$$

If we do as stated, all subgoals are populated for  $I_m$  and  $G_m$ . For the threats, the order constraints are preserved and therefore can't cause another threat (the link between  $I_m$  and  $G_m$  is causeless).

**Lemma** (Expansion with an arbitrary method). If a composite action a is replaced by an arbitrary method m that contains the order constraint  $I_m > G_m$  and replace a with  $I_m$  in all needers of existing flaws and we add all open conditions contained within  $S_m$  as subgoals and all threatened links within  $L_m$  as threats, the resulting plan will not have any undiscovered flaws.

*Proof.* Adding to the previous proof, if a new method is inserted in an existing plan when replacing an action we actually do the following operation on steps:  $S'_{\pi} = (S_{\pi} \setminus a) \cup S_m$ . In the worst case, we will need to introduce one subgoal for each preconditions of the new steps. Using the same code as classical action insertion for all steps, all open conditions are provided.

Regarding the threats, we do the same operation for each link in the new plan than the one we do for new links. This guarantees that all threats are found in the new plan, therefore all classical flaws are discovered.

All new steps that are composite lead to an additional abstraction flaw so that all flaws are taken into account.

This proves that expansion does not introduce flaws that are not added to the POP agenda. Since POP must resolve all flaws in order to be successful and according to the proof of the soundness of POP, HEART is sound as well.

Another proven property is that intermediary plans are valid in the classical definition of the term (without abstraction flaws) and that when using only this definition, HEART is sound on its anytime results too.

### 3.2 Completeness

The completeness of POP has been proven in the same paper as for its soundness [Erol et al., 1994]. This proof states that the way POP handles flaws makes it explore all possible solutions. Since our method uses the same algorithm only the differences must be proven to respect the contract met by the classical flaws.

**Lemma** (Expansion solves the abstraction flaw). *The application of an expansion resolver invalidates the related abstraction flaw.* 

*Proof.* The expression of an abstraction flaw is the existence of its related composite step a in the plan. Since the application of an expansion resolver is of the form  $S'_{\pi} = (S_{\pi} \setminus a) \cup S_m$  unless  $a \in S_m$  (which is forbidden by definition),  $a \notin S'_{\pi}$ .

**Lemma** (Solved abstraction flaws cannot reoccur). The application of an expansion resolver guarantees that  $a \notin S_{\pi}$  for any other partial plan refined afterward without reverting the application of the resolver.

*Proof.* By definition of the methods:  $a \notin A_a^*$ . This means that a cannot be introduced by its expansion or the expansion of its proper actions. HEART restricts the selection of providers for an open condition to operators that have an abstraction level strictly inferior to the one currently being made. So once a is expanded the current level is decreased and a cannot be selected by subgoal resolvers. It cannot either be contained in another action's methods that are selected afterward because otherwise by definition its level would be at least lv(a) + 1.

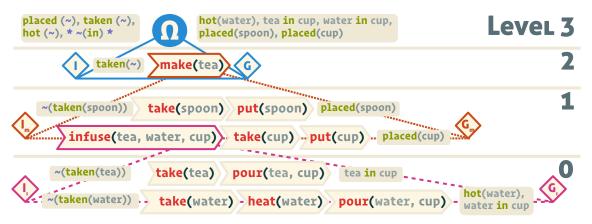


Figure 1: The cycle process on the example domain. All actions that are not expanded during a cycle are copied in the next plan. Some details have been omitted in order to be concise.

Since the implementation guarantees that the reversion is always done without side effects, all the aspects of completeness of POP are preserved in HEART.

#### 4 Results

In order to assess of its capabilities, our algorithm was tested on two different aspects: quality and complexity. All these tests were executed on an Intel® Core™ i7-7700HQ CPU clocked at 2.80GHz. The process used only one core and wasn't limited by time or memory. Each experiment was repeated between 10 000 and 700 times to ensure that variations in speed weren't impacting the results.

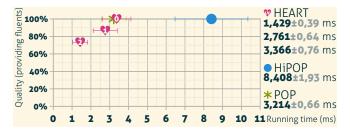


Figure 2: Evolution of the quality with computation time.

In figure 2, we show how the quality is affected by the abstraction in partial plans. The test is done in our example domain. The only variation when implementing our version of HiPOP was regarding the flaw selection and result representation, all the rest is identical. This shows that in some instances of hierarchical planning it may be more interesting to plan in a leveled fashion. It also exhibits a significative faster computation time for the first levels.

The quality is measured by counting the number of providing fluents in the plan  $\left|\bigcup_{a\in S_\pi} eff(a)\right|$ , which is actually used to compute the probability of a goal in intent recognition. We saw that a determining factor in speed for earlier levels was the number of preconditions of the composite actions. In these tests, we didn't reduce that number in order to get the fairest results possible.

In the second test, we used generated domains. These domains are extremely simple. They consist of an action of level 5 that

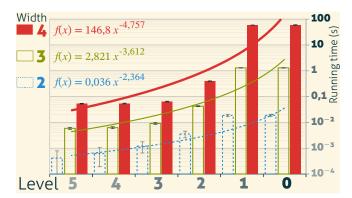


Figure 3: Impact of domain shape on the computation time by levels. The scale of the vertical axis is logarithmic.

has a method containing a number of other actions of a lower level. We call this number the width of the domain. Atomic actions are built with single fluent effects. The goal is the effect of the higher level action and the initial state is empty. There are no negative fluents in these domains. The figure 3 shows the computational profile of HEART for various levels and widths. It clearly behaves according to the exponential law with the exponent of the trend curves seemingly being correlated to the actual width. This means that computing the first cycles has a complexity that is close to being *linear* while computing the last cycles is of the same complexity as classical planning which is at least *P-SPACE* [Weld, 1994].

# **Conclusions**

We showed how HEART performs compared to complete planners in term of speed and quality. While the abstract plans generated during the planning process are complete solutions they are exponentially faster to generate while retaining significant quality over the final plans. By using these plans it is possible to find good approximations to intractable problems within tight time constraints. The applications of such a system, while including the targeted intent recognition, can range from explainable to multi-agent planning.

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