

Bachelor Proposals

Logic and Semantics & Programming Languages

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AARHUS UNIVERSITY

LS & PL Members

Logic and Semantics



Programming Languages



All Things Programming Languages, Analysis and Verification

- Programming languages
 - Logic, compilers
 - Type systems, type inference
 - Security, Coq
 - ...
- Automata and formal languages
 - Algorithmic verification
 - Symbolic model checking
 - Static program analysis
 - ...



How do I check that my program is correct?

- Program logics
- Static analysis
- ...
- **Property Based Testing**
- Random testing



How do I check that my program is correct?

- Program logics
 - Static analysis
 - ...
 - **Property Based Testing**
 - Random testing
-
- Instead of a full program spec, test a few key properties $\phi = \psi_1 \rightarrow \psi_2$
 - If input satisfies ψ_1 , program execution satisfies ψ_2

Property Based Testing



```
// Transitivity
def LessThan(x:a, y:b): Bool={
  ...
}
```

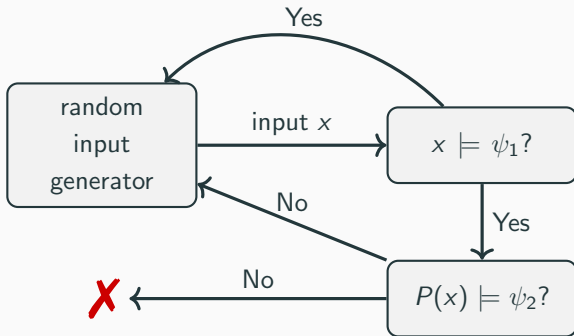
$$\text{LessThan}(x, y) \wedge \text{LessThan}(y, z) \implies \text{LessThan}(x, z)$$

```
// Idempotence
def SetUnion(x:Set[a], y:Set[a]): Set[a]={
  ...
}
```

$$x = y \implies \text{SetUnion}(x, y) = x$$



Testing program P for property $\phi = \psi_1 \rightarrow \psi_2$





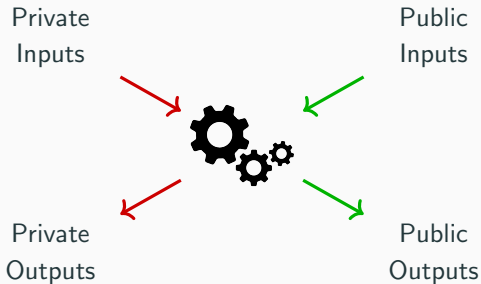
Unique combination of features:

- Algebraic data types
- Polymorphic effects
- First-class Datalog constraints
- ...

```
// The purity of 'map' depends on the purity of 'f'
def map(f: a→b \ ef, l: List[a]): List[b] \ ef =
  match l {
    case Nil      => Nil
    case x :: xs => f(x) :: map(f, xs)
  }
```

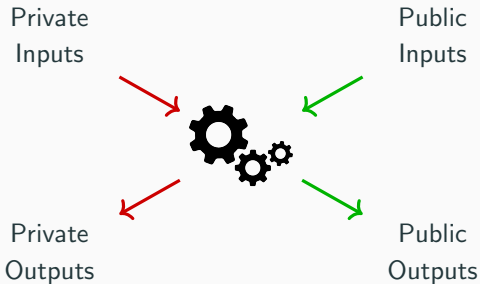



A language with runtime security monitoring



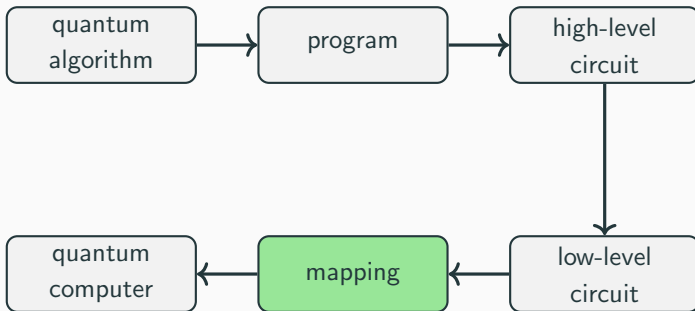


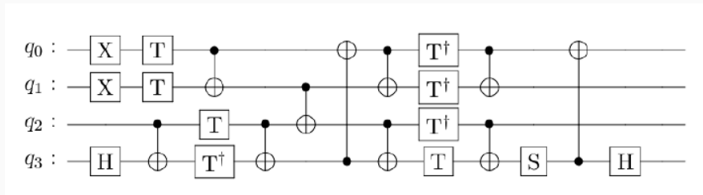
A language with runtime security monitoring



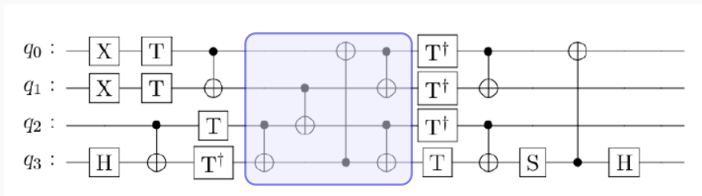
Non-interference

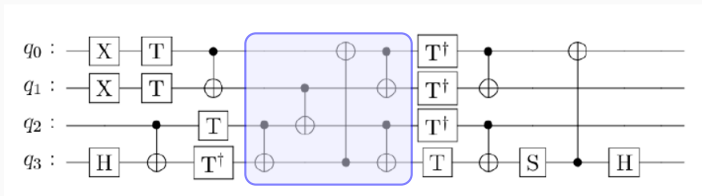
$$\forall x, y: (x.\text{public} = y.\text{public}) \implies (P(x).\text{public} = P(y).\text{public})$$



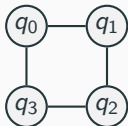


Quantum Layout Synthesis





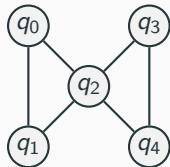
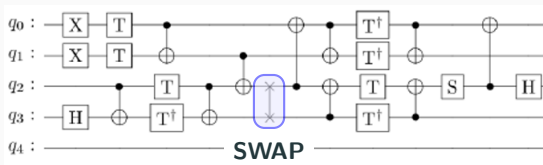
Requires

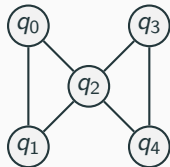
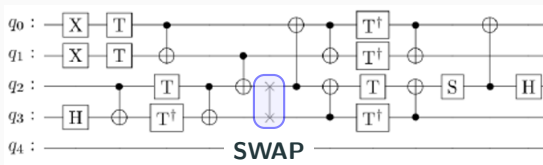


What if we only have?



Quantum Layout Synthesis





- Can a topology support a quantum circuit?
- What is the minimal number of **SWAP**s needed?
- What is the optimal circuit for a given topology?





“Well-typed programs cannot go wrong.” – Robin Milner

Well...

```
var x: Int;  
...  
//what if x is 0?  
println(42/x);
```

```
def get(a: Array[Int], i: Int): Int = {  
  return a(i);  
}  
var a: Array[Int];  
...  
//What if i >= a.len?  
println(get(a, i));
```



“Well-typed programs cannot go wrong.” – Robin Milner

Well...

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var x: Int;  
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println(42/x);
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```
def get(a: Array[Int], i: Int): Int = {  
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}  
var a: Array[Int];  
...  
//What if i >= a.len?  
println(get(a, i));
```

Q: How can we prevent such errors at compile time?



A: Dependent/Refinement Types!

```
var x: Int [v | v != 0];  
...  
//what if x is 0?  
println(42/x);
```

```
def get(a: Array[Int], i: Int [v | v < a.len]): Int = {  
  return a(i);  
}  
var a: Array[Int];  
...  
//What if i >= a.len?  
println(get(a, i));
```



A: Dependent/Refinement Types!

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```

- How do I design a sound type system around this concept?
- How do I typecheck programs (efficiently)?
- What kinds of type dependencies/refinements are allowed?

