

Lecture - 4

Non-linear devices

⇒ Why do we need them?

- To implement complex functions
- For logic operations

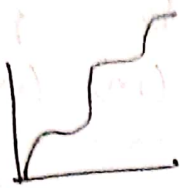
⇒  } There are linear

But what if we want to implement a function like this —

$$y = x^2 + 2x + 3y^2$$

Then the linear elements won't be enough.

In the non-linear devices, the input-output characteristics would be non-linear, for example



or

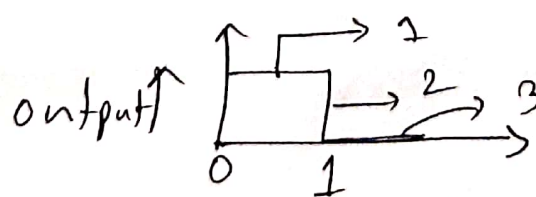


In a simple NOT gate, the input-output curve is a combination of two or more linear ones



When the input at node 'A' is 0 (LOW), then the output at 'B' is 1 (HIGH).

And when the input is 1, then the output is 0.



} more than one line

→ input

What about OR / AND

operations?

For OR gate —

A (in)	B (in)	Y (out)
0	0	0
0	1	1
1	0	1
1	1	1

For AND —

A (in)	B (in)	Y (out)
0	0	0
0	1	0
1	0	0
1	1	1

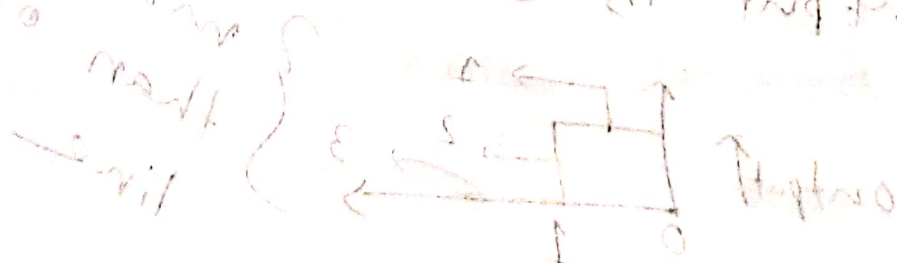
You can see, that the

outputs here are not

exactly linear in nature.

We would need several

lines to plot these



Now, what is the problem with Non-linear equations?

⇒ Well, they are non-linear.

They are harder to solve.

To Model Non-linear devices, you get Non-linear equations.

You need to solve those to design & analyze the device properly.

Now, for equations like these—

$$x + y = 2, \quad 2x + 3y = 5 \quad \left. \vphantom{\begin{matrix} x + y = 2 \\ 2x + 3y = 5 \end{matrix}} \right\} \text{linear}$$

you can solve them easily.

But when you have one

like these — can't

$$e^x + y = 1$$
$$x + 3ny = 5$$

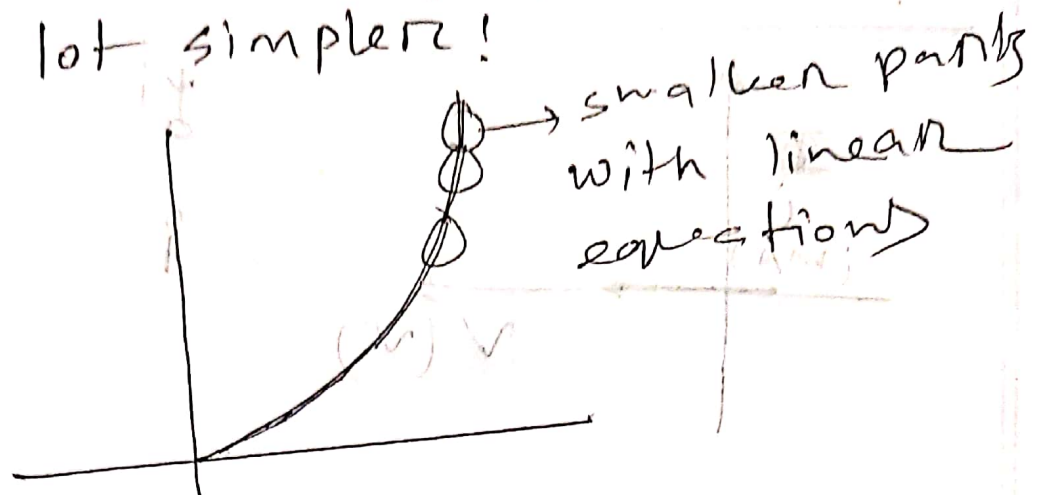
These
are solved
so easily

You can plot them and find an intersection point of the two lines (which is the solution). But that would be time consuming and computational load is heavier, if you want to solve it numerically. So what should we do?

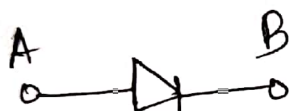
→ We divide and conquer!

We just divide the lines into small linear, straight

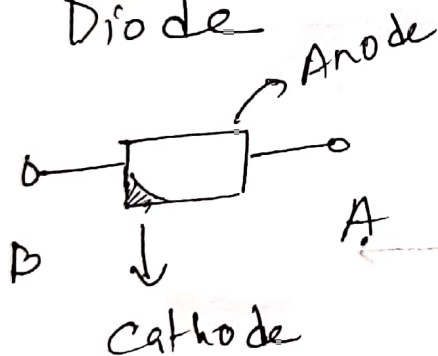
parts and solve the equations for individual parts, which would be a lot simpler!



Piecewise Linear Approximation:



Diode



'A' terminal: Anode

'B' terminal: Cathode

Anode voltage: V_A

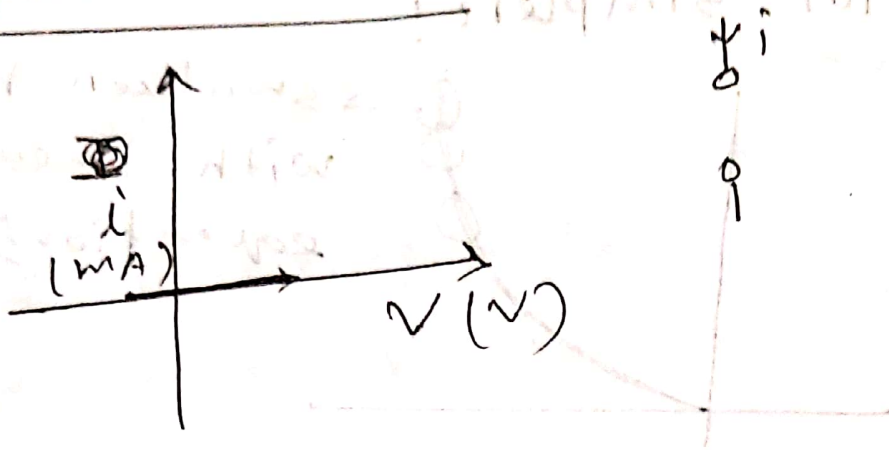
Cathode " : V_B

1) $V_A > V_B$: Forward Bias

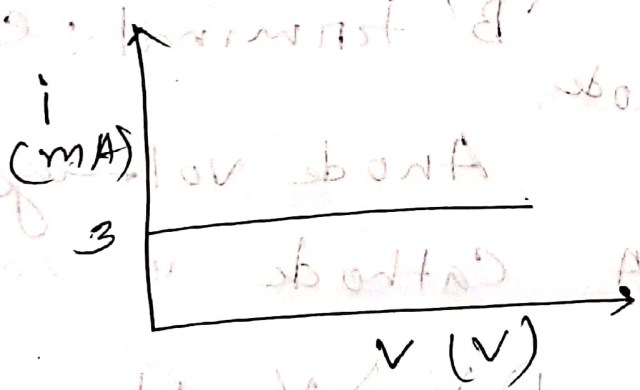
2) $V_A < V_B$: Reverse Bias

Some Basic graphs:

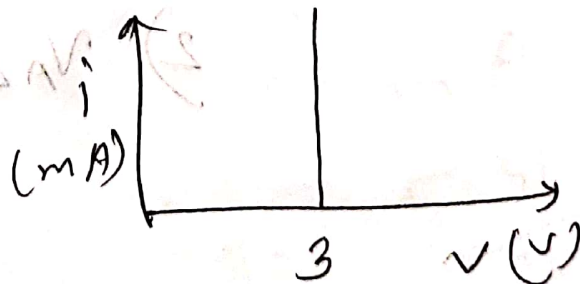
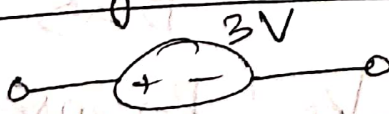
Open circuit:



Current source:



Voltage source:



The $i-v$ plot for a Generic non-linear device :



To make calculations easier —



Example 1