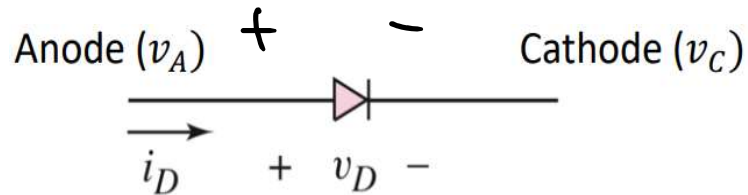


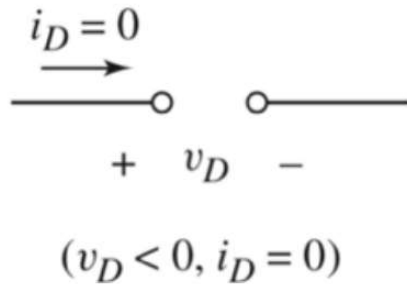
# Lecture 9

## Rectifiers & Filtering

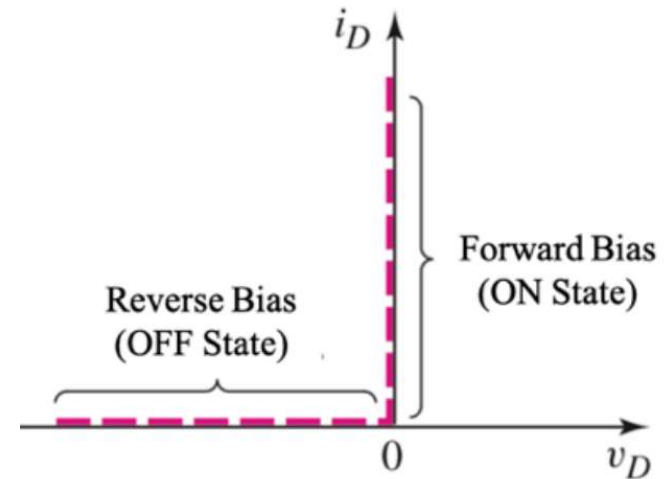
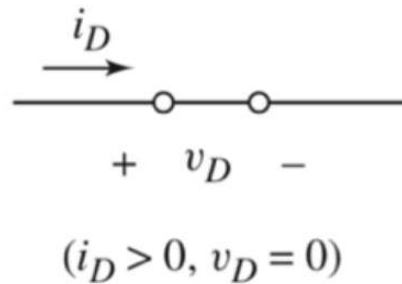
# Ideal Diode Model



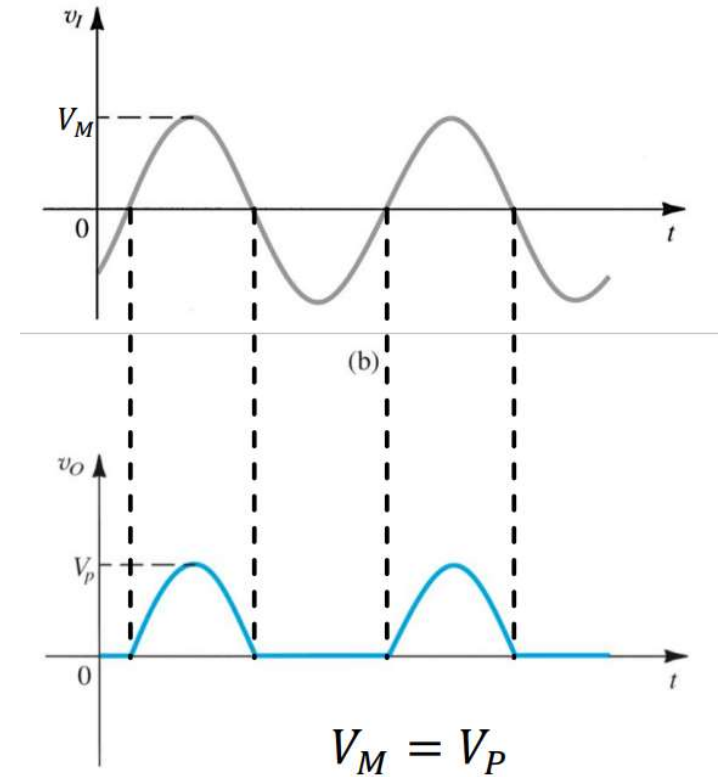
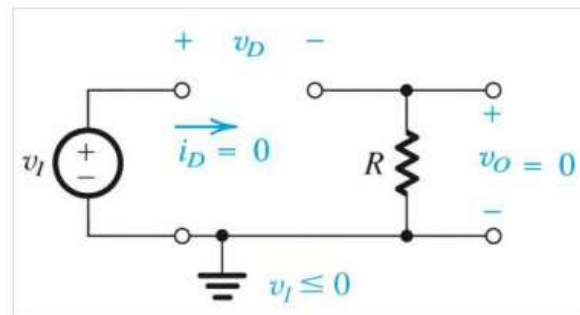
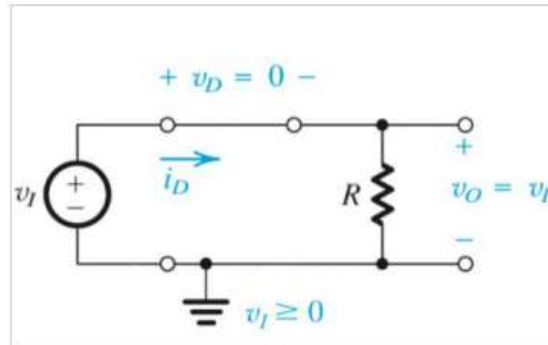
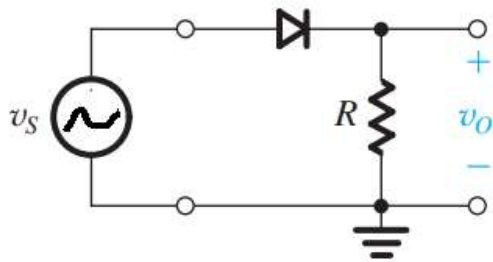
**OFF State: Open circuit**

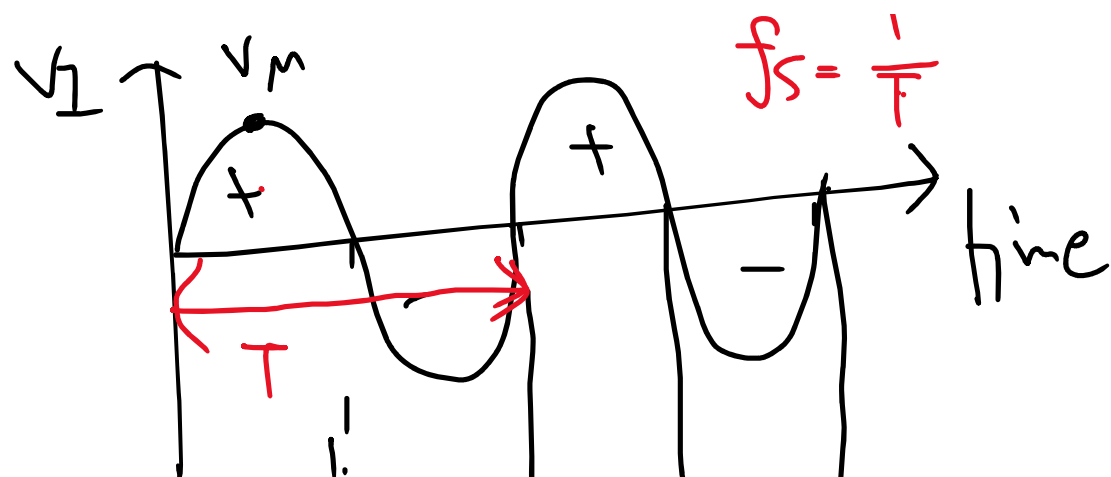


**ON State: Short circuit**



# Half-wave rectifier (ideal diode model)





$$V_1 = V_m \sin(\omega t)$$

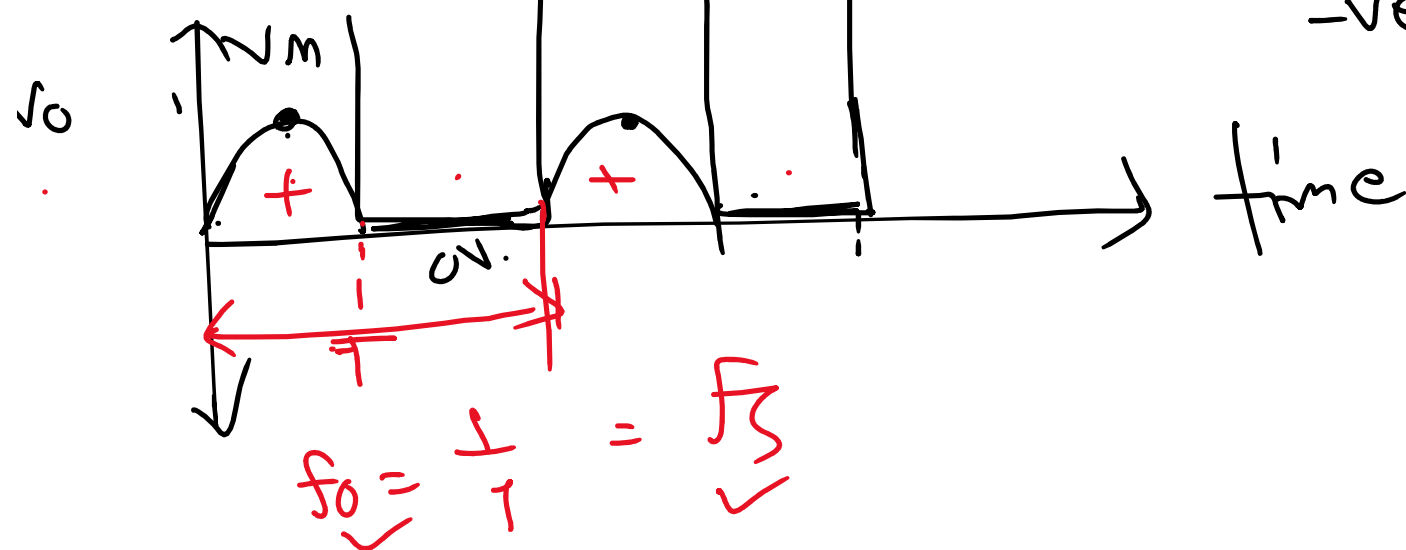
for half-cycle  $V_1 > 0 \rightarrow \text{on}$

$$V_o = V_1$$

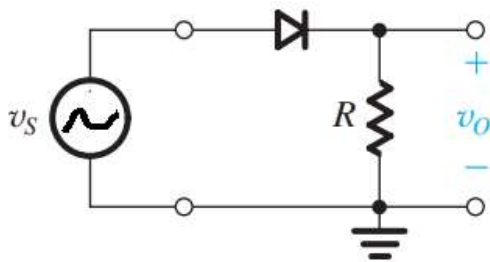
for half-cycle  $V_1 < 0 \rightarrow$

$V_o < 0 \rightarrow \text{off}$

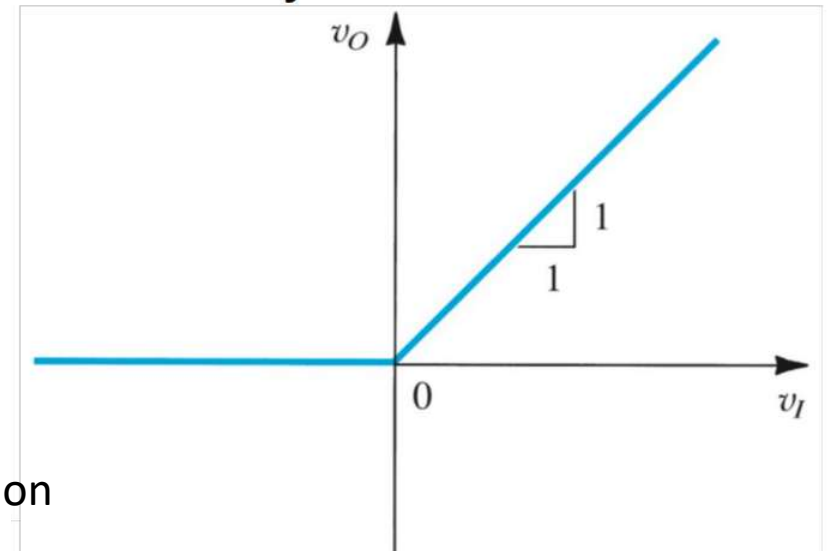
$$V_o = 0$$



# Half-wave rectifier (ideal diode model)



**Transfer Characteristics**



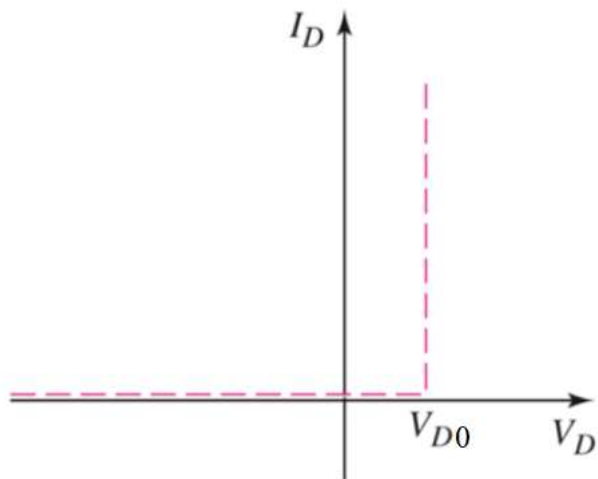
When  $V_i > 0$ , Diode on  $\rightarrow V_o = V_i \rightarrow y=mx$  type relation

where slope,  $m = 1$

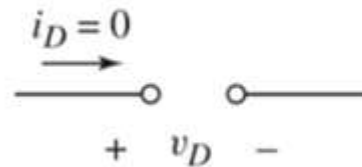
$V_i < 0$ , Diode off  $\rightarrow V_o = 0$  V

# Modeling the real diode

## Constant voltage drop (CVD) model

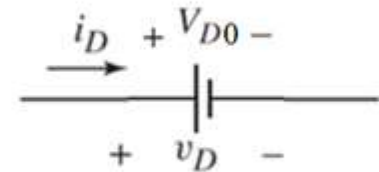


OFF State: Open circuit



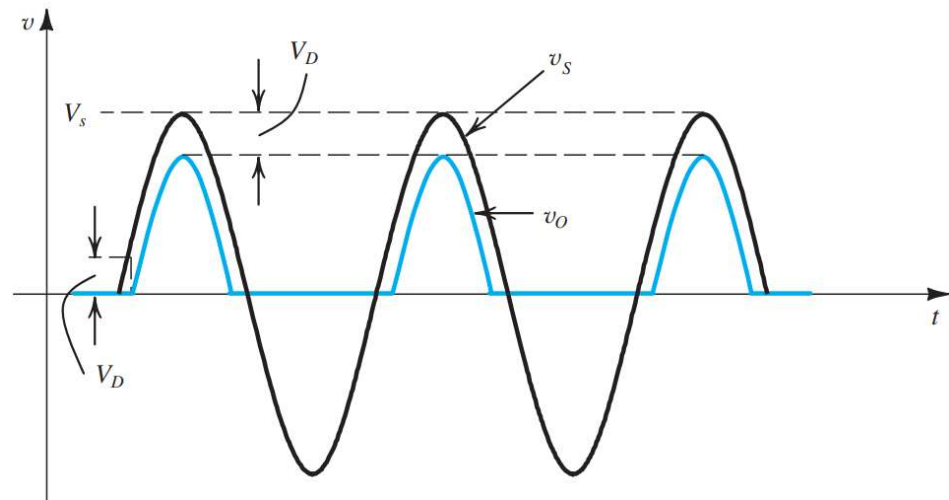
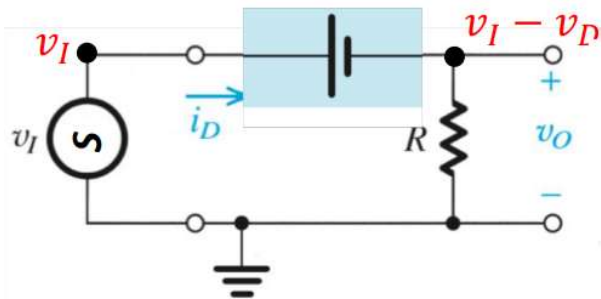
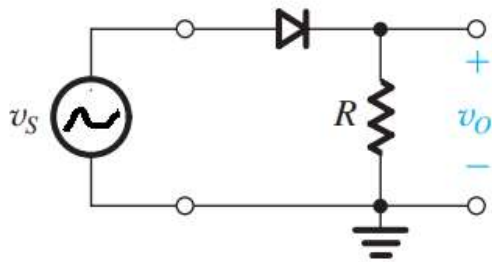
$$(v_D < V_{D0}, i_D = 0)$$

ON State: Voltage source



$$(i_D > 0, v_D = V_{D0})$$

# Half-wave rectifier (CVD model)



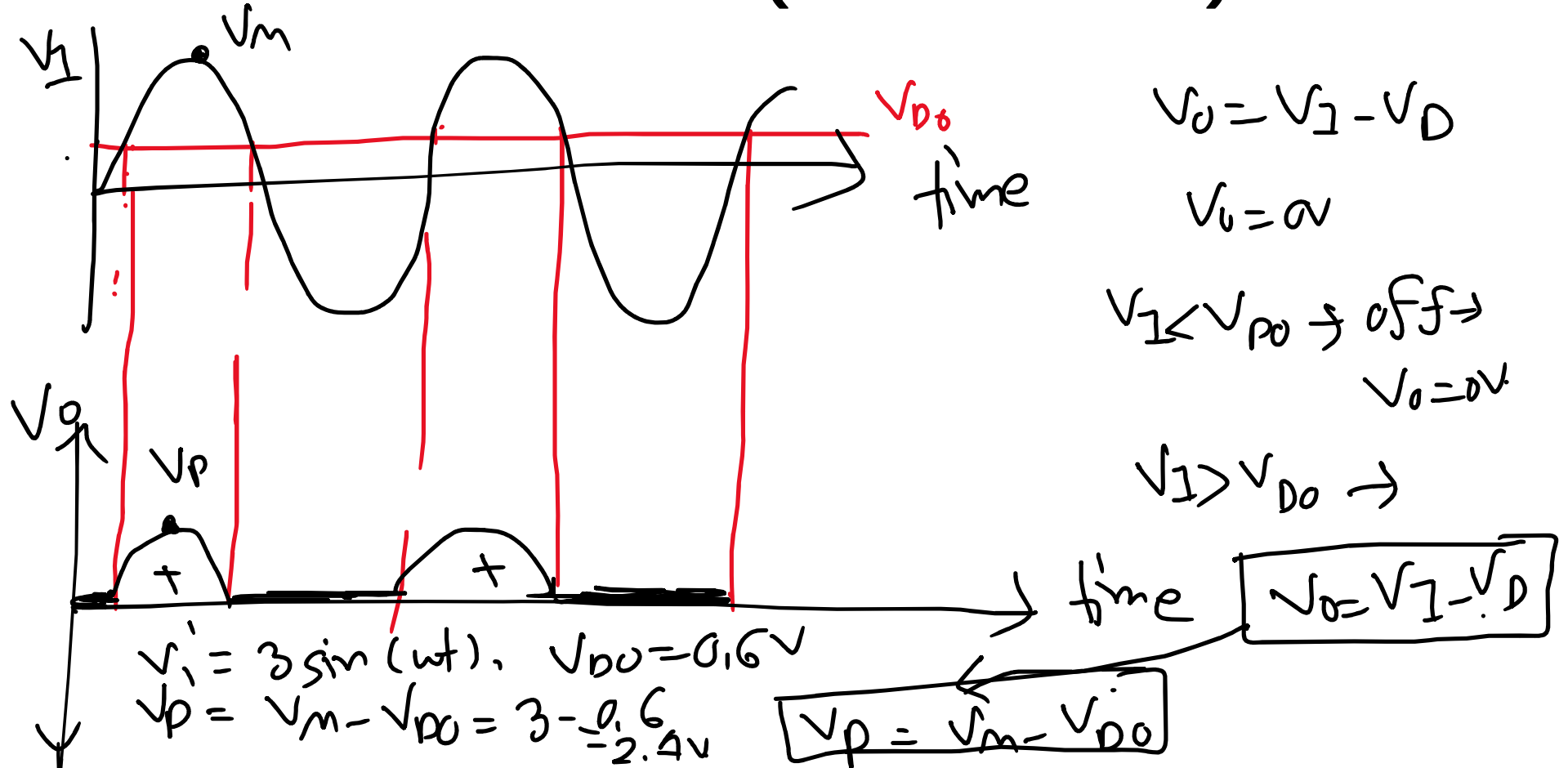
$$v_I = V_M \sin \omega t$$

$$v_O = V_M \sin \omega t - V_D$$

$$V_p = \text{peak of output}$$

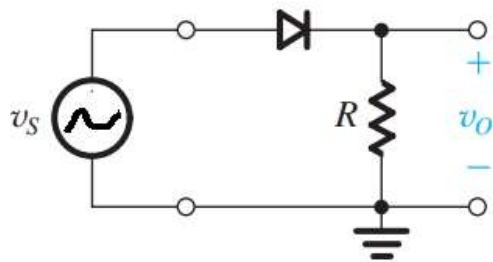
$$= V_M - V_D$$

# Half-wave rectifier (CVD model)





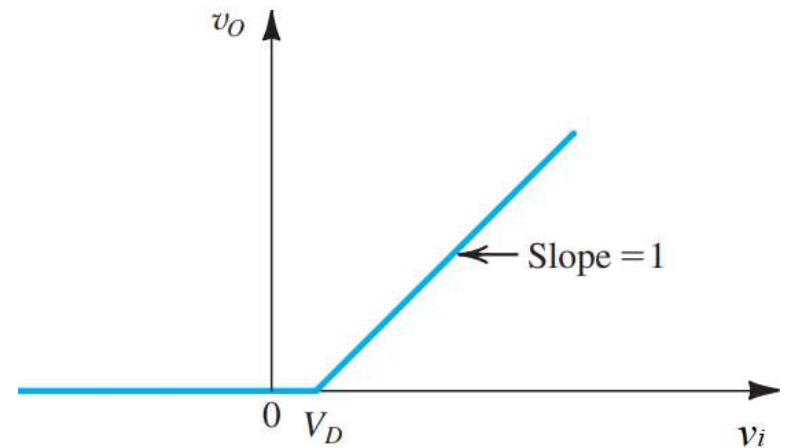
# Half-wave rectifier (CVD model)



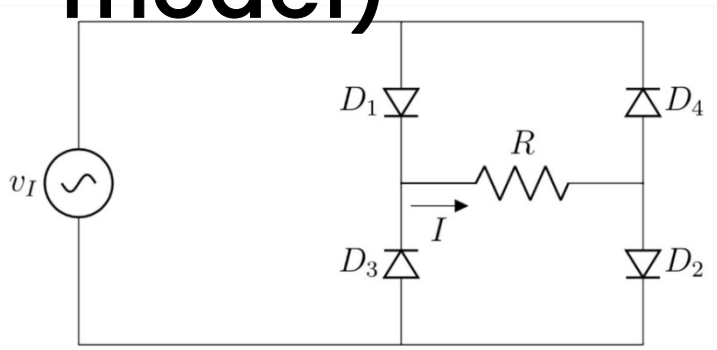
When  $V_i > V_{D0}$ , Diode on  $\rightarrow V_o = V_i - V_{D0} \rightarrow y = mx + c$  type relation where slope,  $m = 1$

$V_i < V_{D0}$ , Diode off  $\rightarrow V_o = 0 \text{ V}$

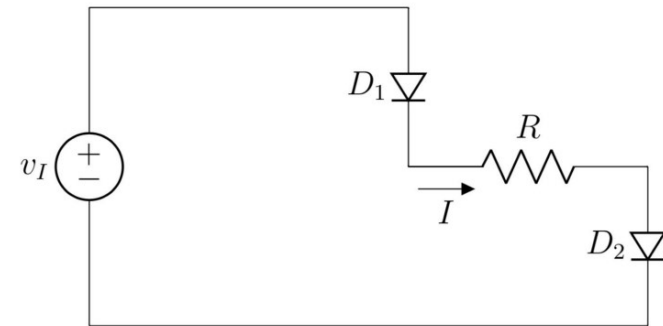
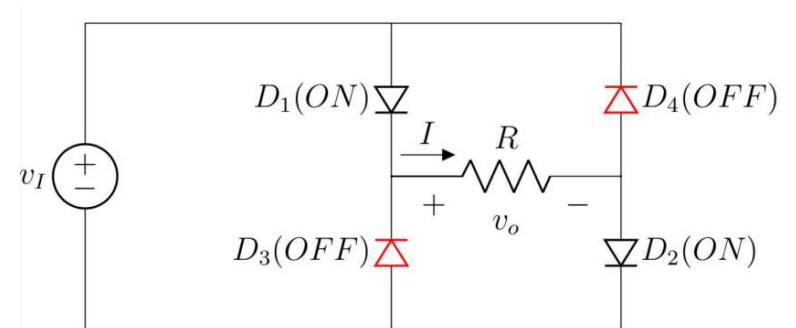
*Transfer Characteristics*



# Full-wave rectifier (ideal diode & CVD model)

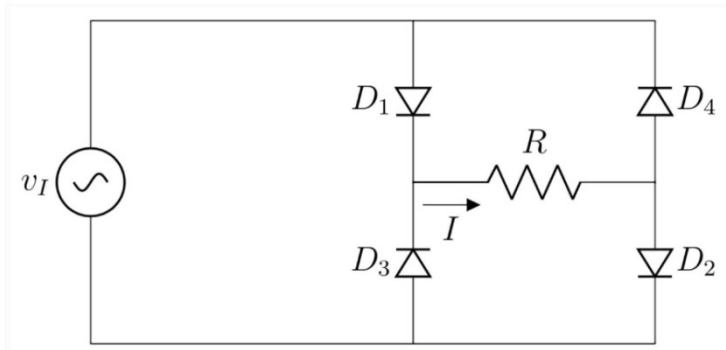


(+) half-cycle

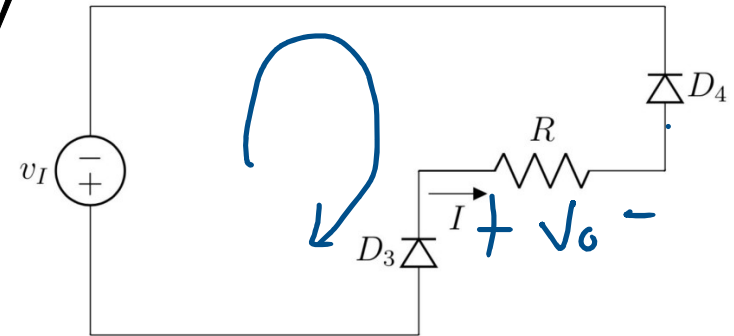
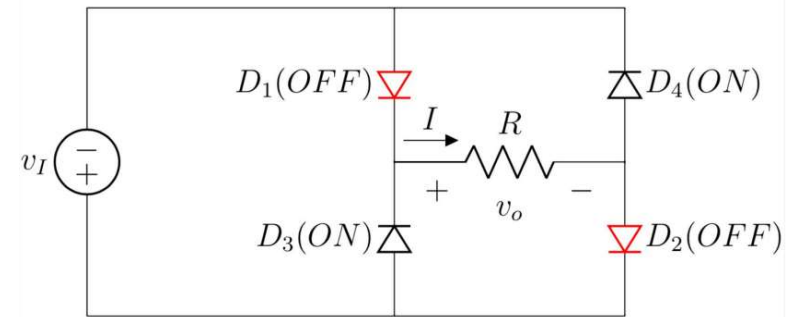


$$v_o = v_I - 2V_D$$

# Full-wave rectifier (ideal diode & CVD model)

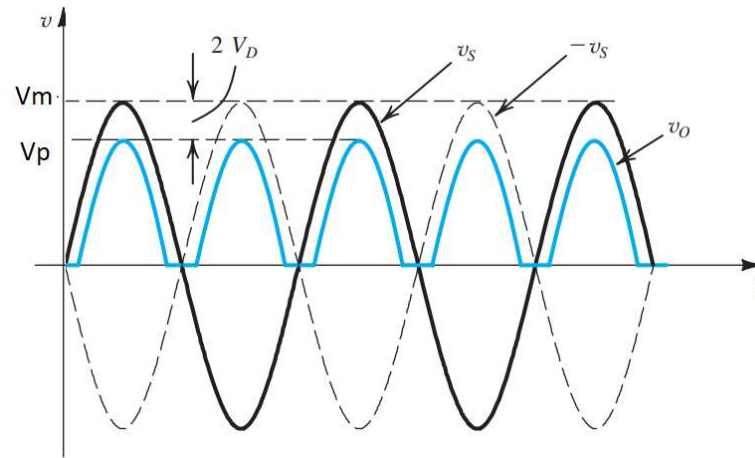
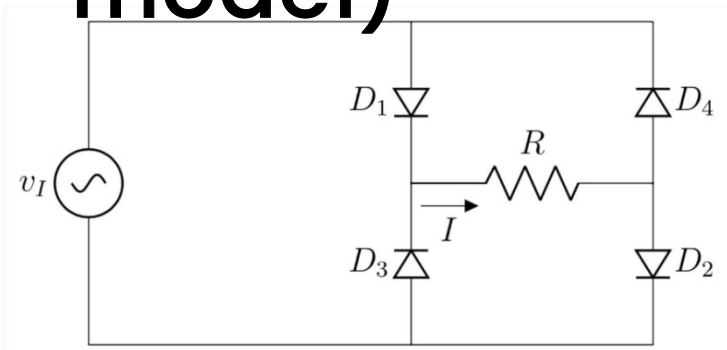


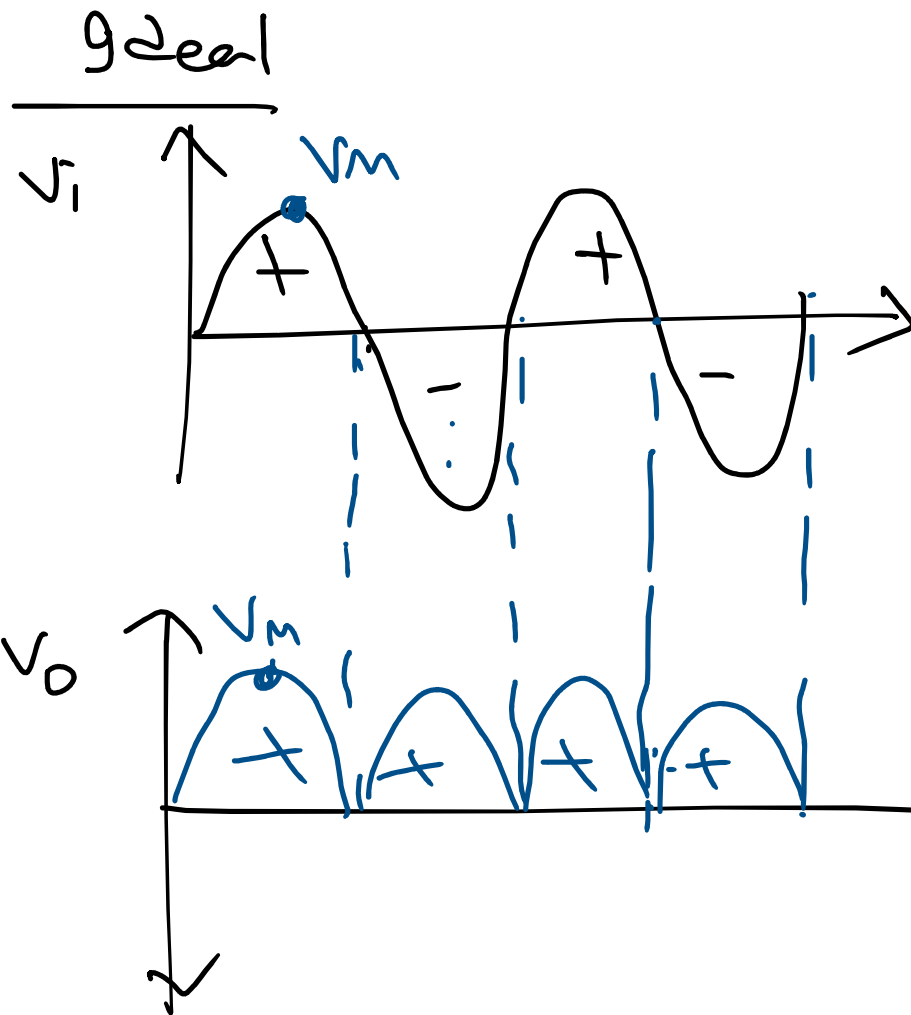
(-) half-cy



$$v_o = -v_I - 2V_D$$

# Full-wave rectifier (ideal diode & CVD model)





trve half  $\rightarrow V_o = V_i$

-ve half  $\rightarrow \underline{V_o = -V_i}$

time

$$V_p = V_m$$

time

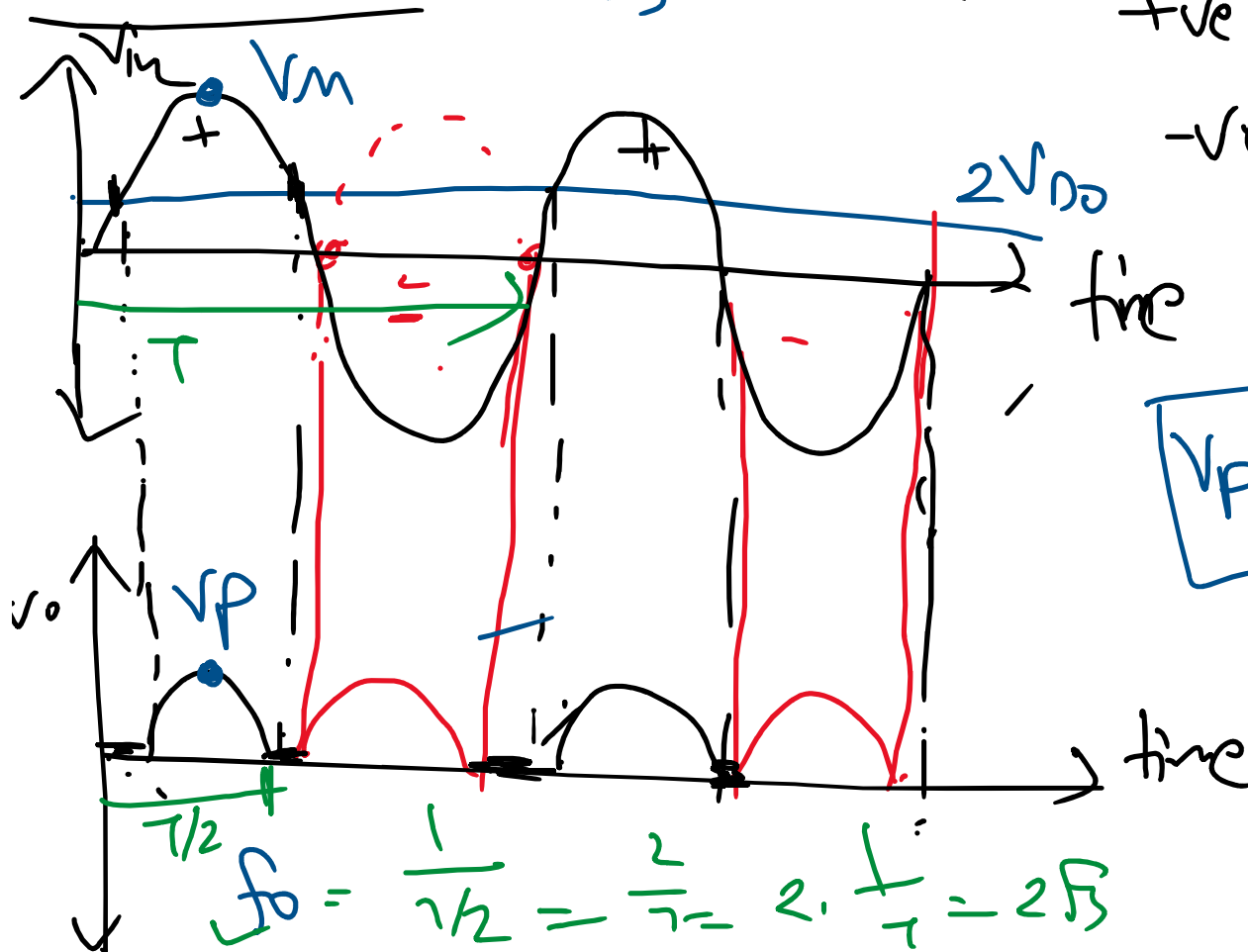
CVP model

$f_s$

$$V_i' > 2V_{D0}$$

$$+ve \text{ half} \rightarrow V_o = V_i' - 2V_{D0}$$

$$-ve \text{ " } \rightarrow V_o = -V_i' - 2V_{D0}$$

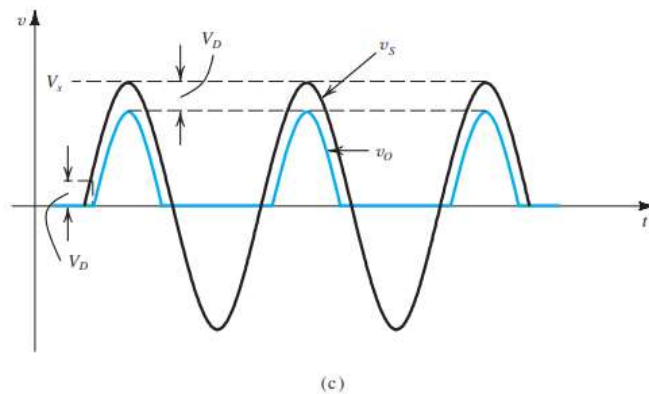
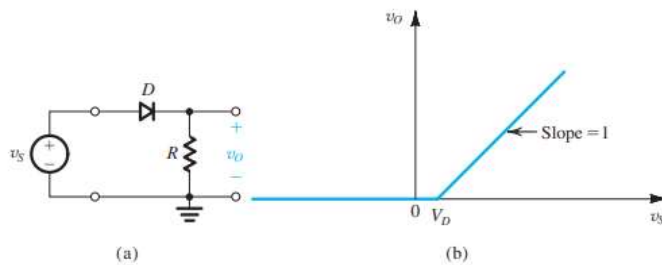


fire

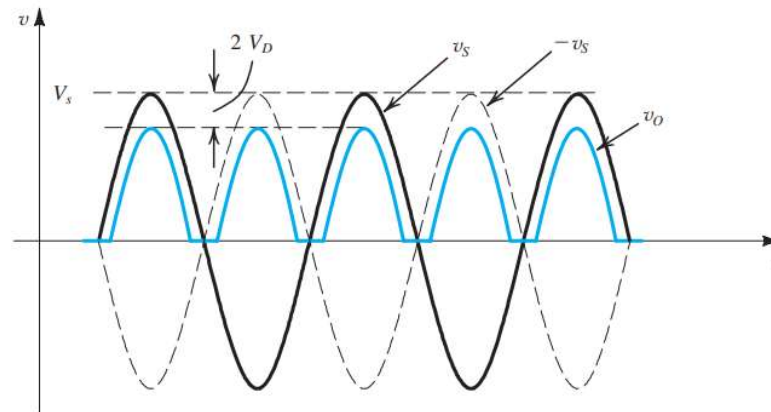
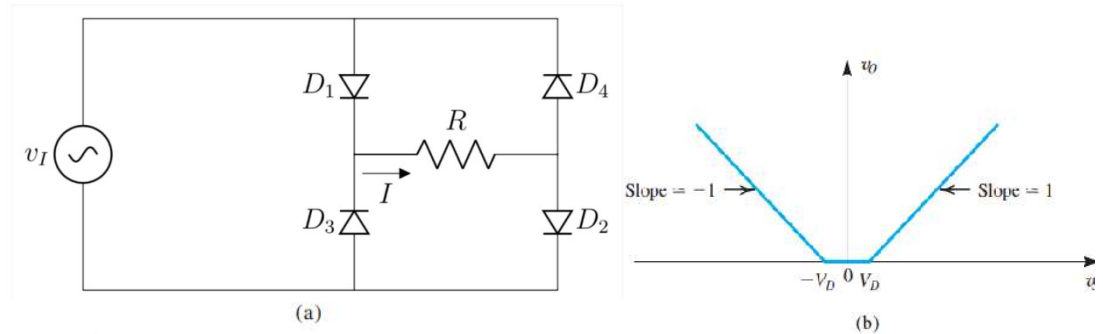
$$V_p = V_m - 2V_{D0}$$

$$f_o = f_s$$

# Half-wave and Full-wave rectifier



**Half-wave**



**Full-wave**

$$V_{in} = 5 \sin(200\pi t) \rightarrow V_m \sin(\omega t)$$

$$HW \rightarrow (CVD) \rightarrow V_p, f_0 = ? \quad V_{DO} = 0.3V$$

$$FW \rightarrow (CVD) \rightarrow V_p, f_0 = ?$$

a) HW       $\omega = 2\pi f$        $V_m = 5V$

$$\omega = 200\pi = 2\pi f_3 \quad \therefore f_3 = \frac{200\pi}{2\pi} = 100 \text{ Hz}$$

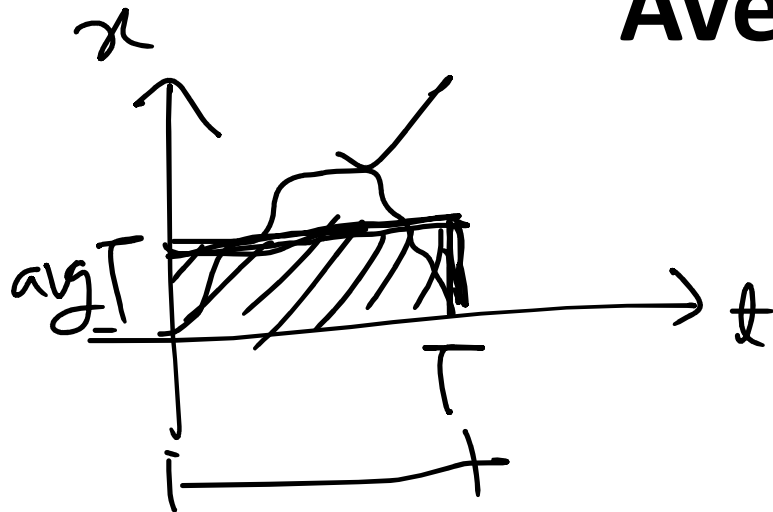
$$V_p = V_m - V_{DO} = 5 - 0.3 = 4.7V$$

b) FW       $f_0 = 2f_3 = 200 \text{ Hz}, V_p = V_m - 2V_{DO}$

$$= 5 - 2 \times 0.3 = 4.4V$$

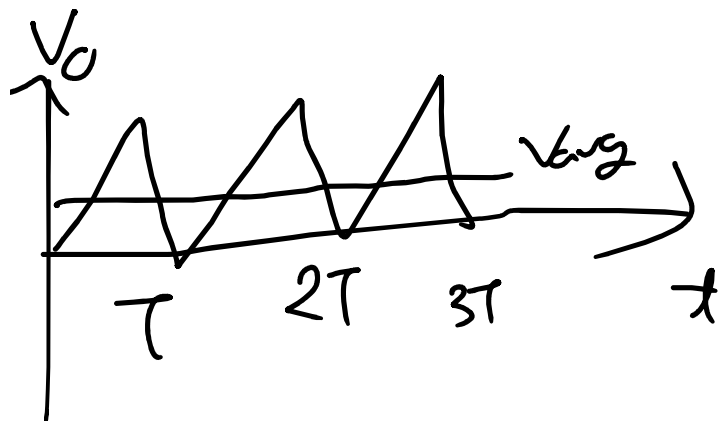


# Average Value



$$\text{area} = \int_0^T x \, dt$$

$$\text{area} = \text{avg} \times T = \int_0^T x \, dt$$



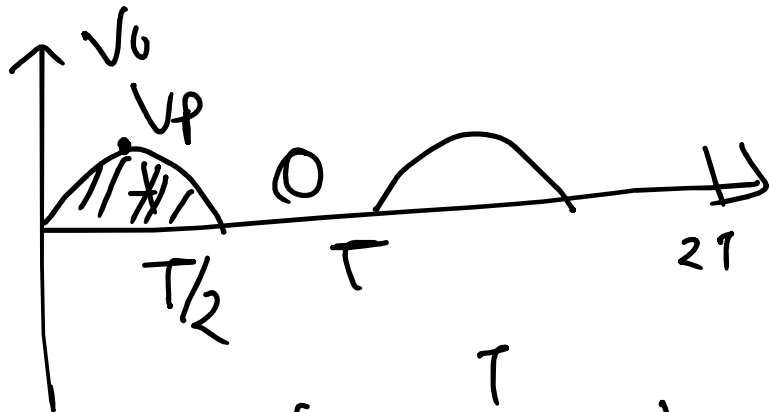
$$\Rightarrow \text{avg} = \frac{1}{T} \int_0^T x \, dt$$

$$v_{\text{avg}} = \frac{1}{T} \int_0^T v_o \, dt$$

# Average Value of Rectifier Output

	HW	FW	
$V_P$	$V_m - V_{D_0}$	$V_m - 2V_{D_0}$	
$V_{AV}$	$\frac{1}{\pi} V_m$	$\frac{2}{\pi} V_m$	← Ideal
$V_{AV}$	$\frac{1}{\pi} V_m - \frac{1}{2} V_{D_0}$	$\frac{2}{\pi} V_m - 2V_{D_0}$	← Real

## Average Value of HW Rectifier Output (Ideal)



$$V_{in} = V_m \sin(\omega t)$$

Diode on  $\Rightarrow V_o = V_{in}$   
 " off  $\Rightarrow V_o = 0$

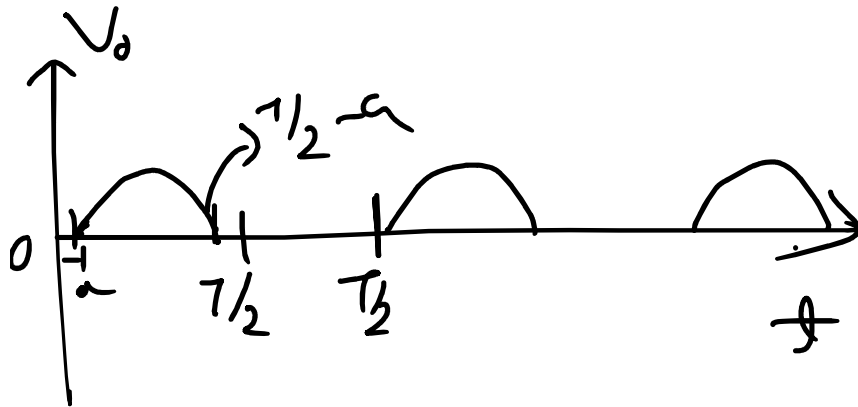
$$\begin{aligned} \text{avg} &= \frac{1}{T} \int_0^T V_o dt = \frac{1}{T} \int_0^T V_{in} dt \\ &= \frac{1}{T} \int_0^{T/2} V_m \sin \omega t dt \end{aligned}$$

$$\omega = 2\pi f = \frac{2\pi}{T}$$

## Average Value of HW Rectifier Output (Ideal)

$$\begin{aligned}
 &= \frac{V_m}{T} \times \frac{1}{\omega} \left[ \cos \omega t \right]_0^{T/2} \\
 &= \frac{V_m}{T} \times \frac{-T}{2\pi} \left[ \cos \frac{2\pi}{T} \times \frac{T}{2} - \cos 0 \right] \\
 &= \frac{-V_m}{2\pi} \left[ \cos \pi - 1 \right] \\
 &= \frac{-V_m}{2\pi} \times [-1 - 1] = \frac{-V_m}{2\pi} \times -2 \\
 &\boxed{V_{avg} = \frac{V_m}{\pi}} \quad \checkmark
 \end{aligned}$$

## Average Value of HW Rectifier Output (CVD)



$$V_o = V_m' - V_{D0}$$

$$avg = \frac{1}{T} \int_0^T V_o dt$$

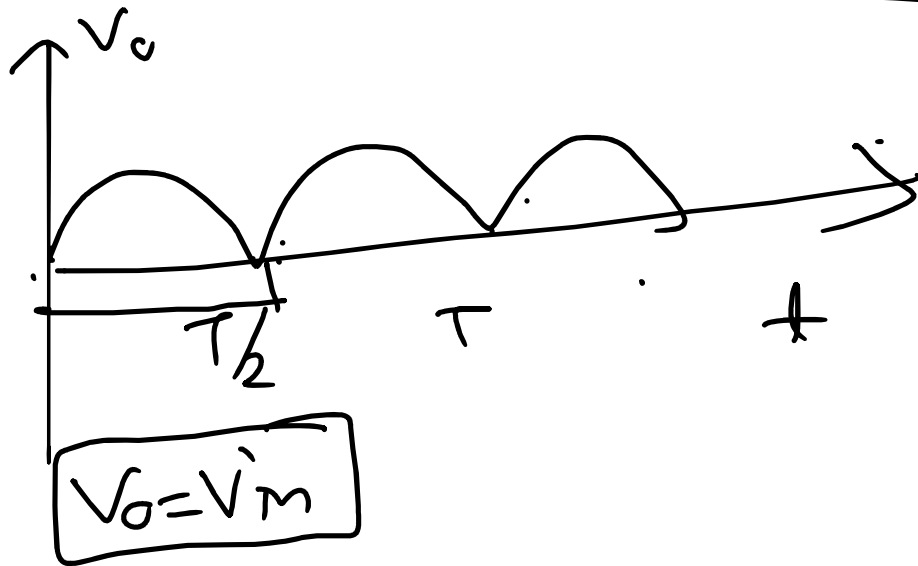
$$= \frac{1}{T} \int_0^{T/2} V_m' - V_{D0} dt$$

$$= \frac{1}{T} \int_0^{T/2} V_m \sin \omega t - V_{D0} dt$$

$$= \frac{V_m}{\pi} - \frac{1}{T} \int_0^{T/2} V_{D0}$$

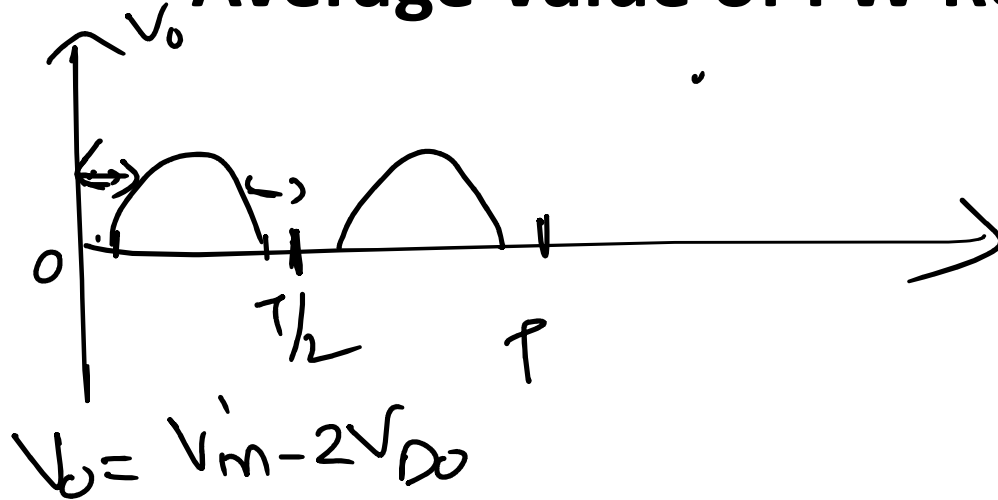
$$= \frac{V_m}{\pi} - \frac{V_{D0}}{2}$$

## Average Value of FW Rectifier Output (ideal)



$$\begin{aligned} \text{avg} &= \frac{1}{T/2} \int_0^{T/2} v_m dt \\ &= \frac{2}{T} \int_0^{T/2} V_m \sin \omega t dt \\ &= 2 \times \frac{V_m}{\pi} = \frac{2V_m}{\pi} \end{aligned}$$

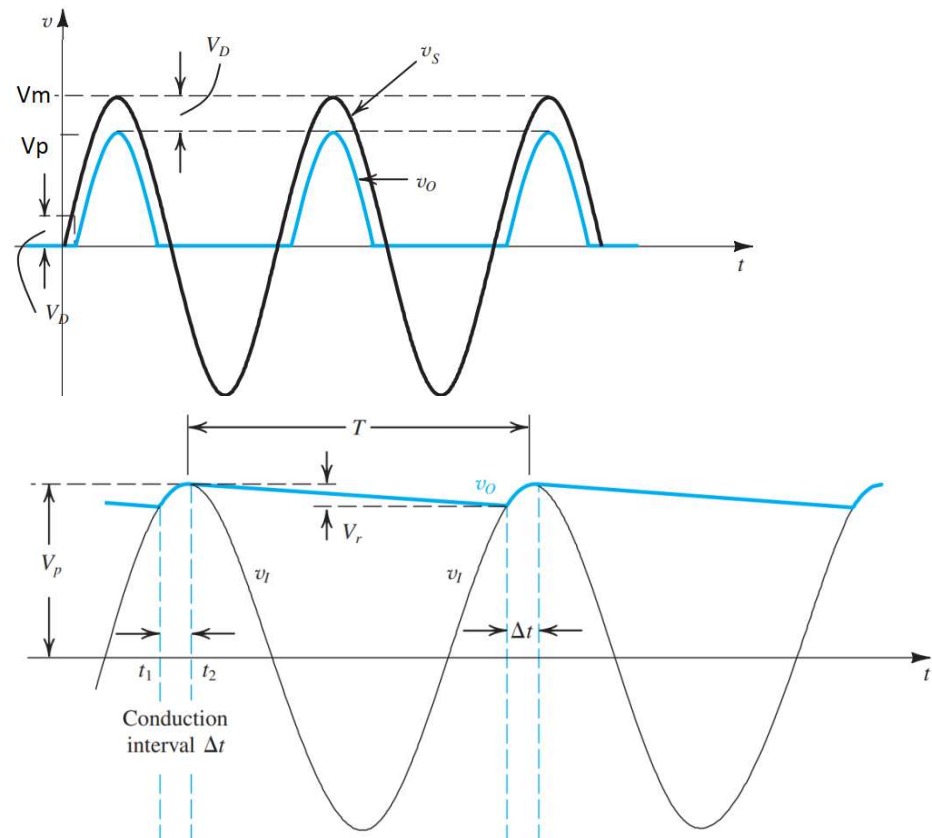
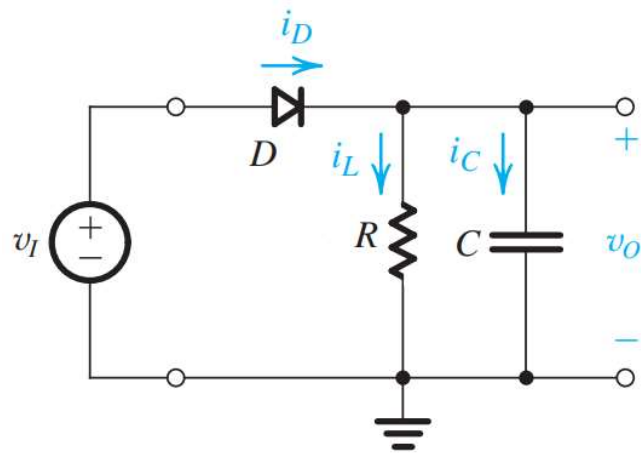
## Average Value of FW Rectifier Output (CVD)



$$\begin{aligned} \text{avg} &= \frac{1}{(T/2)} \int_0^{T/2} V_o \, dt \\ &= \frac{2}{T} \int_0^{T/2} (V_m - 2V_{D0}) \, dt \end{aligned}$$

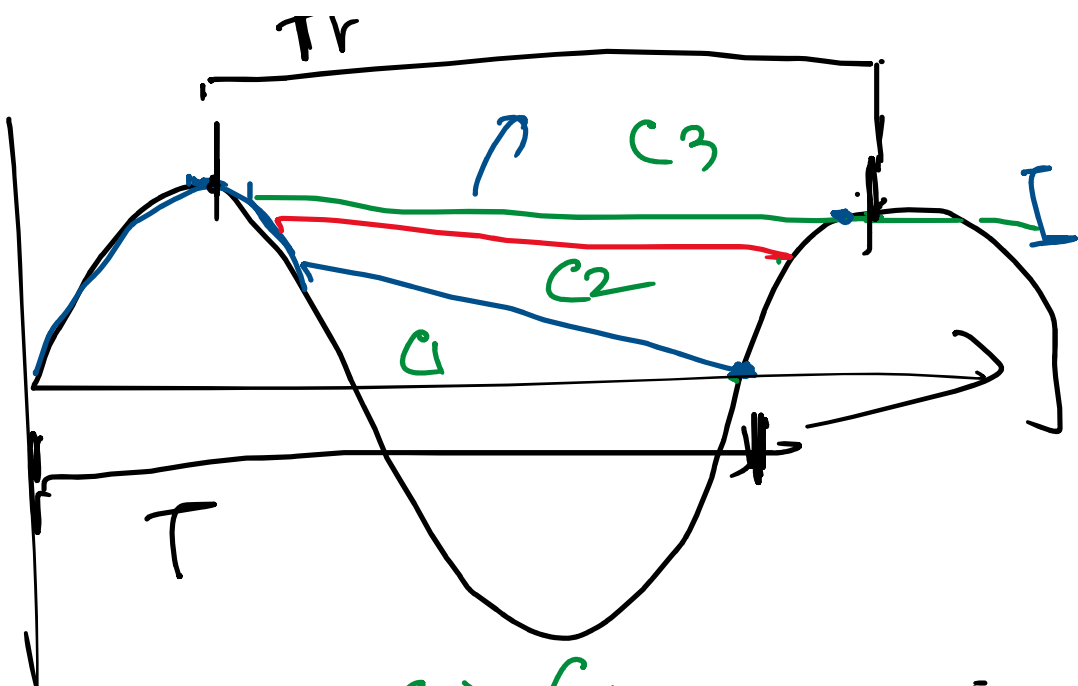
$$= \frac{2V_m}{T} - 2V_{D0}$$

# Filtering: Half-wave rectifier



From Microelectronic Circuits by Adel S. Sedra & Kenneth C. Smith: Chapter 4. 7th edition. Published by Oxford University Press. Used for educational purposes only.

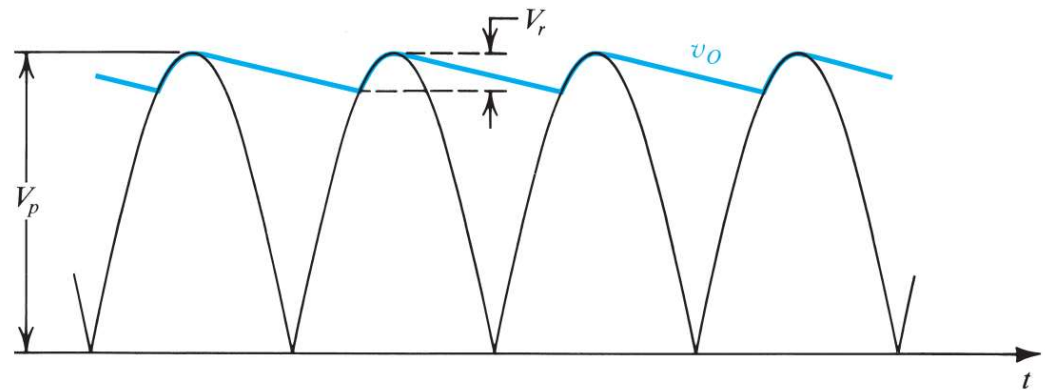
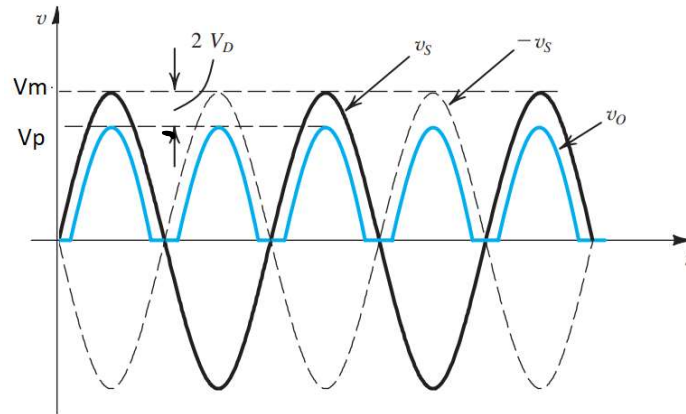
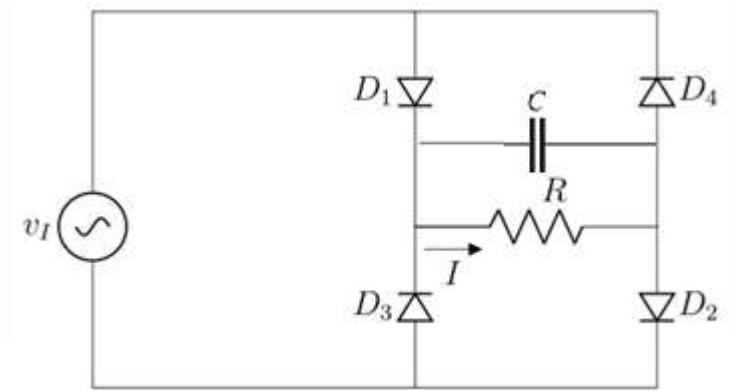




a)  $C_1, C_2, C_3$   
 b) which capacitor?

a)  $C_3 > C_2 > C_1$   
 b)  $C_3$

# Filtering: Full-wave rectifier



### Without capacitor

Rectifier	i/p peak	o/p peak	average
H/W	$V_M$	$V_P$	$V_{avg}=V_{DC}=\frac{1}{\pi}V_M-\frac{1}{2}V_{Do}$
F/W	$V_M$	$V_P$	$V_{avg}=V_{DC}=\frac{2}{\pi}V_M-2V_{Do}$

### With capacitor

Rectifier	i/p peak	o/p peak	frequency	Ripple voltage	average
H/W	$V_M$	$V_P=V_M-V_{Do}$	$f_r=f_i$	$V_r=\frac{V_P}{f_r R C}$	$V_{avg}=V_{DC}=V_P-\frac{1}{2}V_r$
F/W	$V_M$	$V_P=V_M-2V_{Do}$	$f_r=2f_i$	$V_r=\frac{V_P}{f_r R C}$	$V_{avg}=V_{DC}=V_P-\frac{1}{2}V_r$

$$I_{o,avg}=V_{o,avg}/R, V_{rms}=V_p/\sqrt{2}$$

## Example

A voltage waveform  $v_i = 8\sin(2000\pi t)V$  is input to a full-wave rectifier. A resistance of  $R = 50k\ \Omega$  is connected at the load. [Assume that the diodes used in the circuit have a forward drop of  $0.8V$ ].

(a) Draw the circuit of the full wave rectifier. Label the input and output voltages properly. [1]

(b) Draw the waveforms of the input and output voltages. What are the peak values of input and output? Show them in the graph. [1+1]

(c) Find the average voltage measured at the output. [1]

d) Draw VTC curve with proper labelling.

e) If  $1\mu F$  capacitor is connected in parallel with the resistor, what will be the average output voltage then?

$$b) \text{ input} \rightarrow V_m = 8V$$

$$\text{out} \rightarrow V_p = V_m - 2V_{D1} = 8 - 2 \times 0.8 = 6.4V$$

$$W = 2000 \text{ \AA}$$

$$\Rightarrow 2\pi f = 2000 \text{ \AA}$$

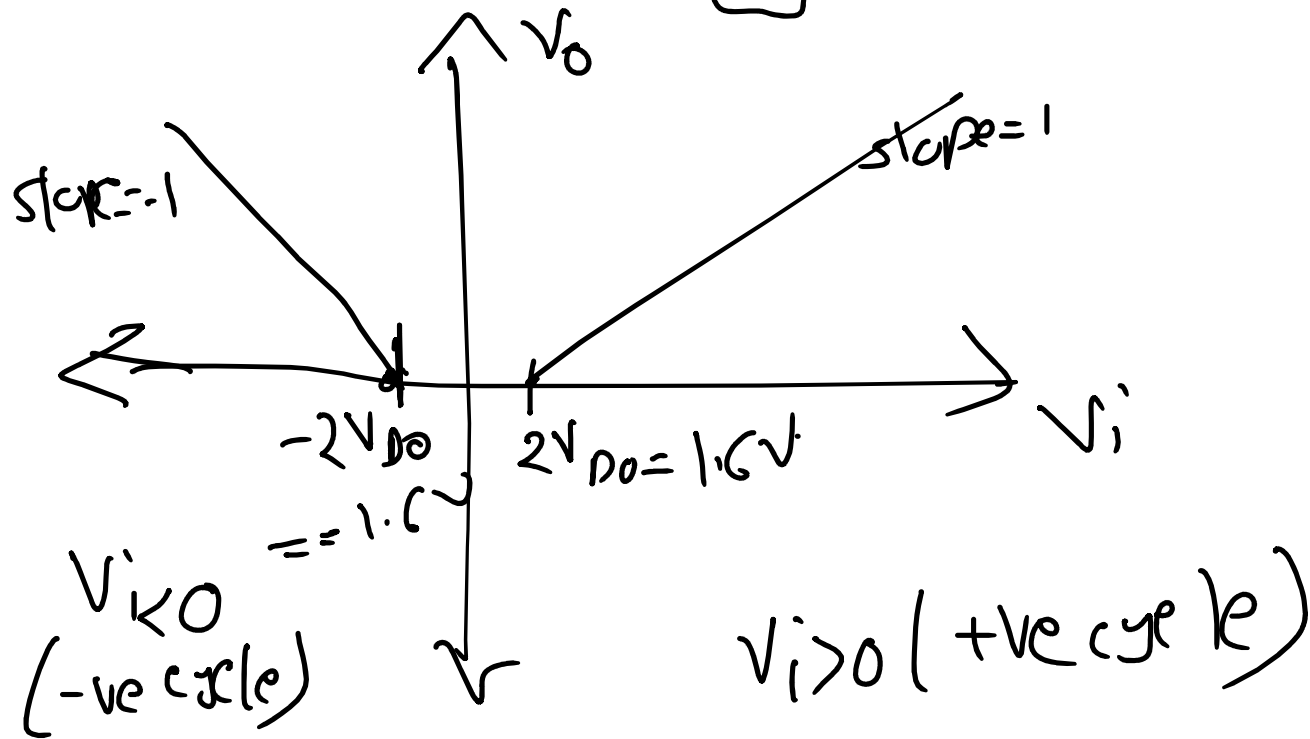
$$\therefore f = 1000 \text{ THz} \\ = 1 \text{ PHz}$$

$$f_0 = 2f = 2 \text{ PHz}$$

$$c) \text{ FW (c.v.d):}$$

$$\begin{aligned} \text{avg} &= \frac{2V_m}{h} - 2V_{D1} \\ &= \frac{2 \times 8}{h} - 2 \times 0.8 \\ &= \underline{\underline{3.4 \text{ eV}}} \end{aligned}$$

d) +ve cycle  $\rightarrow V_o = V_{in} - 2V_{D0} \rightarrow y = mx + c$   
 -ve "  $\rightarrow V_o = -V_{in} - 2V_{D0} \rightarrow y = mx + c$



e) Filtering

$$V_{avg} = V_p - V_r/2$$

$$V_r = \frac{V_p}{f_r RC}$$

$$6.4$$

$$\Rightarrow V_r = \frac{6.4}{2000 \times 50 \times 10^3 \times 1 \times 10^{-6}}$$

$$= 0.064V$$

$$f_r = 2f_s = f_0$$

$$= 2kHz$$

$$R = 5k\Omega$$

$$C = 1\mu F$$

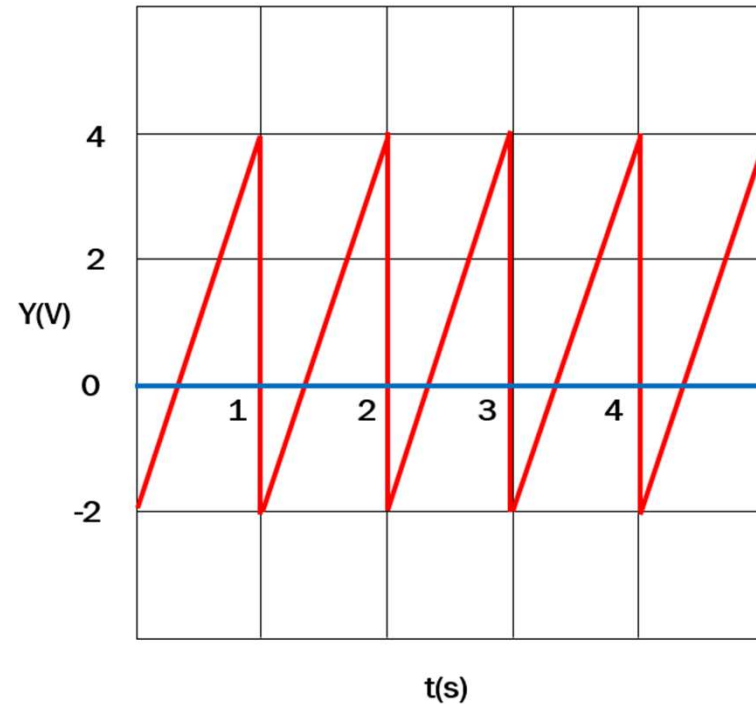
[6.4, 0.064]

~~1μF, 5μF~~  
 $V_r$   $V_r$

$$V_{avg} = V_p - V_r/2$$

$$= 6.4 - \frac{0.064}{2}$$

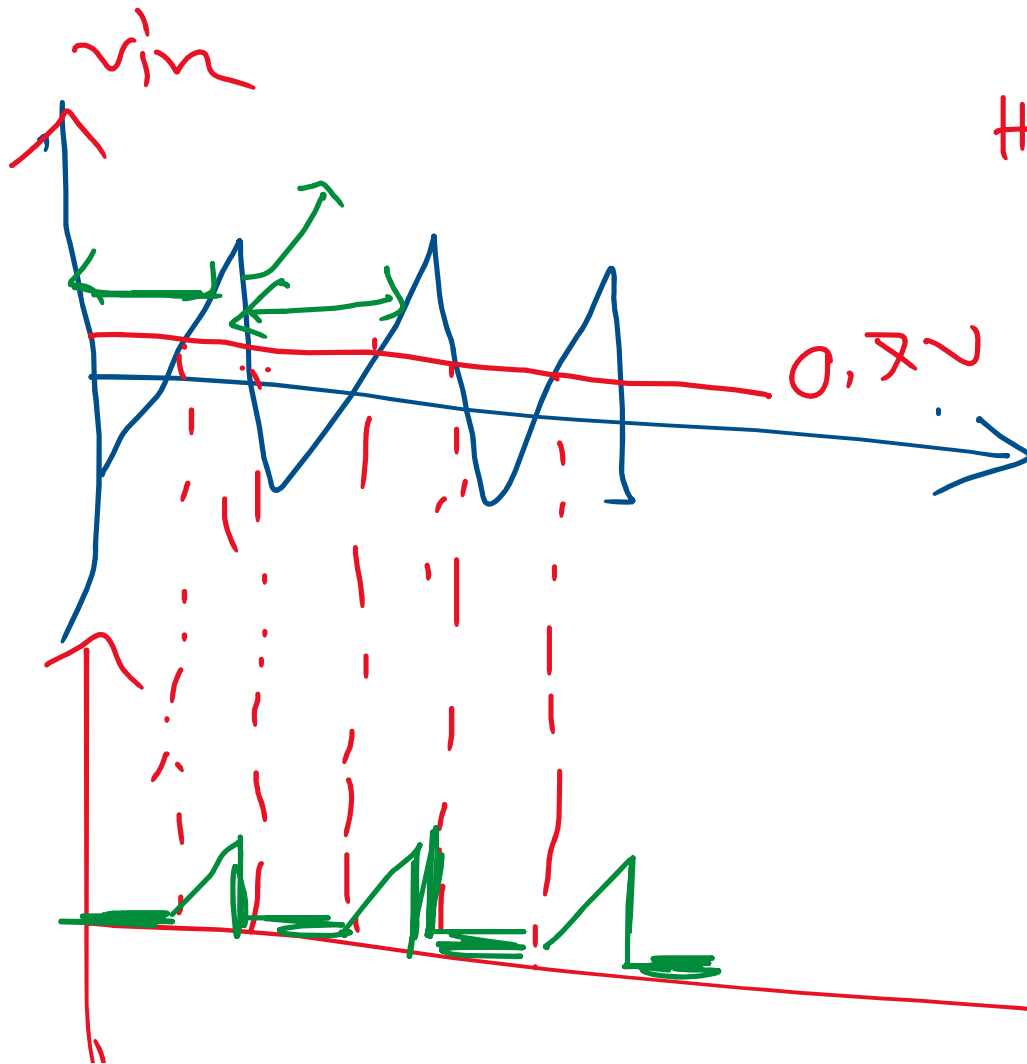
$$= 6.3 \text{ -- } V$$



The input of a Half-wave rectifier is exhibited in the Figure above and output load resistance is  $R = 5 \text{ k}\Omega$ . Silicon diodes are used in this circuit for which the forward drop is  $V_{D0} = 0.7 \text{ V}$ .

- i. Show the input and output waveforms.
- ii. Draw the VTC curve





HW (eVD) :

$$\begin{cases} v_i > v_{DD} \rightarrow v_o = v_i - v_{DD} \\ v_i < v_{DD} \rightarrow v_o = 0V \end{cases}$$

# Thank you