

The Zener diode is specified as

$$V_{Z0} = 3V$$

$$P_Z = 0.5W$$

$$I_{ZK} = 1mA$$

The load current can vary from $0mA$ to $50mA$.

⊗ The source has a nominal value of $5V$ and can vary $\pm 10\%$.

ⓐ Find $V_s(\min)$, $V_s(\max)$, $I_L(\min)$, $I_L(\max)$

ⓑ Solⁿ: $10\% \text{ of } 5V = 0.5V$

$$\therefore V_s(\min) = 5 - 0.5 = 4.5V$$

$$V_s(\max) = 5 + 0.5 = 5.5V$$

$$I_L(\min) = 0 \text{ mA}$$

$$I_L(\max) = 50mA.$$

(b) What is the worst case values of I_L , I_Z and V_S ?

Solⁿ: In worst case, I_{ZK} will flow through the Zener diode. [If the current falls below this, the regulation will not be maintained]

$$KCL \Rightarrow I_Z = I_S - I_L$$

$$\text{and } I_S = \frac{V_S - V_L}{R_S}$$

So, I_Z is minimum when I_L is maximum and V_S is minimum.

\therefore Worst case \Rightarrow

$$I_L = I_L(\text{max}) = 50 \text{ mA}$$

$$I_Z = I_Z(\text{min}) = I_{ZK} = 1 \text{ mA}$$

$$V_S = V_S(\text{min}) = 4.5 \text{ V}$$

(c) For worst case, what is the value of I_S ?

Solⁿ: $I_S = I_Z + I_L = 50 + 1 = 51 \text{ mA}$.

~~(d) For worst case,~~

(d) Forz worst case, what is the value of V_R ?

Solⁿ: In worst case scenario, the Zener diode will barely maintain its voltage.

~~So $V_L = V_Z$~~

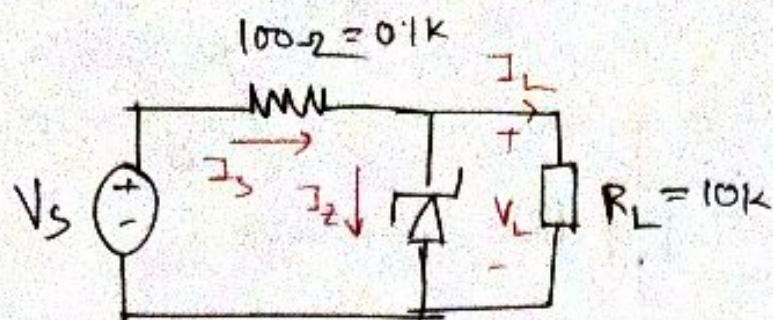
$$\text{So, } V_L = V_Z = V_Z + I_Z r_Z = 3V.$$

$$\begin{aligned}\therefore V_R &= V_S - V_L \\ &= 4.5 - 3 \\ &= 1.5V\end{aligned}$$

(e) Find the value of R_S , for which the Zener diode maintains regulation in worst case scenario.

$$\underline{\text{Sol}^n}: R_S = \frac{V_R}{I_Z} = \frac{1.5}{51} \approx 30 \Omega.$$

(2)



Zener diode specification: $V_{Z0} = 3V$

$$r_z = 0.2$$

$$I_{ZK} = 1mA$$

Find the minimum value of V_s for which the Zener diode maintain its regulation.

Solⁿ: In worst case scenario, $I_z = I_{ZK} = 1mA$.

$$\therefore V_L = V_z = V_{Z0} + I_z r_z = 3V$$

$$\therefore I_L = \frac{V_L}{R_L} = \frac{3V}{10K\Omega} = 0.3mA$$

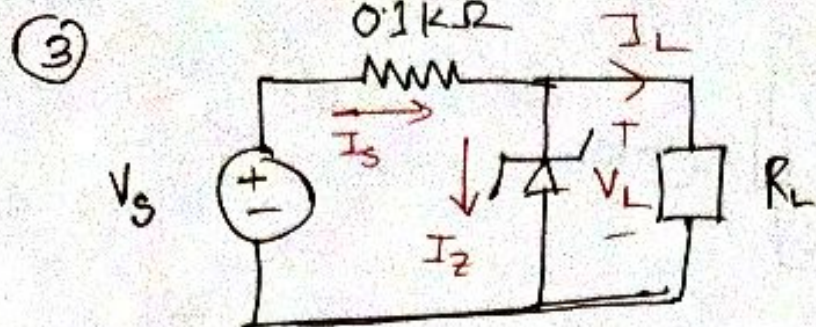
$$\therefore I_s = I_z + I_L \quad (\text{KCL})$$

$$= 1.3mA$$

$$I_s = \frac{V_s - V_L}{0.1K} = 1.3mA$$

$$\Rightarrow \frac{V_s - 3}{0.1K} = 1.3mA$$

$$\Rightarrow \boxed{V_s = 3.13V} \quad \therefore \boxed{V_s(\min) = 3.13V}$$



Zener diode specification: $V_Z = 3V$,

$$r_Z = 0.2$$

$$I_{ZK} = 1mA$$

The source V_s has a nominal value of 5V and can vary $\pm 10\%$.

Find the worst case/minimum value of R_L so that regulation is maintained.

Solⁿ: In worst case, $I_Z = I_{Z(min)} = I_{ZK} = 1mA$

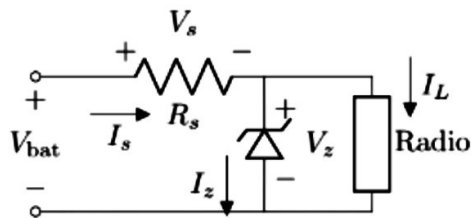
$$V_L = V_Z = V_Z + I_Z r_Z = 3V$$

In worst case, $V_s = V_s(min) = 5 - 10\% = 5 - 0.5 = 4.5V$

$$\therefore I_s = \frac{V_s - V_L}{0.1k} = \frac{4.5 - 3}{0.1k} = 15mA$$

$$\begin{aligned} \therefore I_L &= I_s - I_Z \text{ [KCL]} \\ &= 15 - 1 \\ &= 14mA \end{aligned}$$

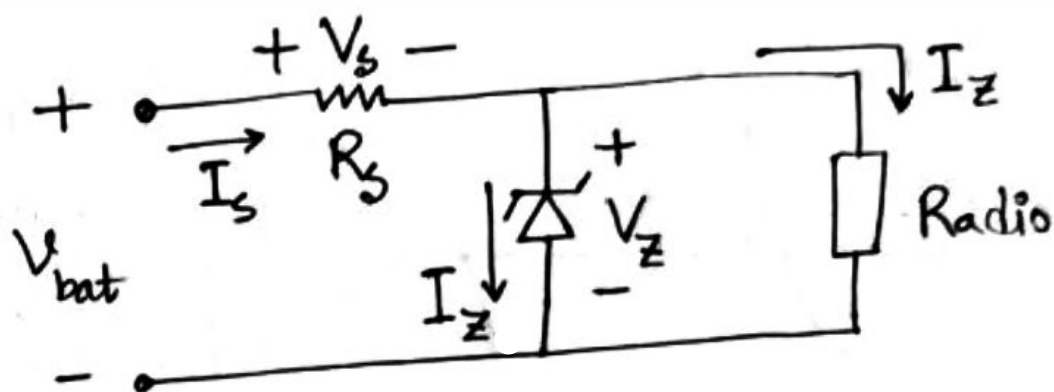
$$\therefore R_L = \frac{V_L}{I_L} = \frac{3V}{14mA} \approx 214\Omega$$



The circuit above is a voltage regulator used to power a car radio (which requires ≈ 9 V) from the car battery, V_{bat} whose voltage may vary between 11 and 13.6 V. The current in the radio, I_L , will vary between 0 (off) to 9 mA (full volume). The Zener diode in the circuit is specified with parameter $V_{z0} = 9$ V, $r_z = 0.05$ k Ω , and $I_{zk} = 1$ mA.

- Identify** the worst-case conditions and **calculate** the Zener current (I_z), Zener voltage (V_z), the input voltage (V_{bat}), and the load current (I_L) in this worst-case scenario. [1+1+1+1+1]
- Calculate** the current (I_s) and the voltage (V_s) the input resistor R_s in the worst-case scenario. [2]
- Design** the circuit, i.e., find the value of R_s , such that even in the worst-case scenario voltage regulation is maintained. Calculate the line regulation for this circuit. [2+1]

(5)



Given that, $V_{bat} = 11\text{ v} \sim 13.6\text{ v}$

$$I_L = 0 \sim 9\text{ mA}$$

$$V_{z0} = 9\text{ v}, r_z = 0.05\text{ k}\Omega, I_{zk} = 1\text{ mA}$$

(a) Worst case conditions:

$$(1) V_{bat(\min)} = 11\text{ v}.$$

$$(2) I_{z(\min)} = I_{zk} = 1\text{ mA}.$$

$$\text{So, } I_z = 1\text{ mA. (Ans)} \quad V_{bat} = 11\text{ v. (Ans)}$$

$$V_z = V_{z0} + I_z r_z$$

$$\hookrightarrow V_z = 9 + 1 \times 10^{-3} \times 0.05 \times 10^3$$

$$\hookrightarrow V_z = 9.05\text{ v. (Ans)}$$

$$I_L = I_{L(\max)} = 9\text{ mA}.$$

⑤ Applying KVL we get, $V_{bat} = V_s + V_z$

$\hookrightarrow V_s = V_{bat} - V_z$

$\hookrightarrow V_s = (11 - 9.05) \text{ V}$

$\hookrightarrow V_s = 1.95 \text{ V} \text{ (Ans)}$

Applying KCL we get,

$$I_s = I_z + I_L$$

$$\hookrightarrow I_s = (1 + 9) \text{ mA}$$

$$\hookrightarrow I_s = 10 \text{ mA} \text{ (Ans)}$$

$$\textcircled{c} \quad R_s = \frac{V_s}{I_s} = \frac{1.95}{10 \times 10^{-3}} = 195 \Omega. \text{ (Ans)}$$

Line Regulation,

$$\frac{\Delta V_L}{\Delta V_{bat}} = \frac{r}{r+R}$$

$$= \frac{0.05 \times 10^3}{0.05 \times 10^3 + 195} \text{ V/V}$$

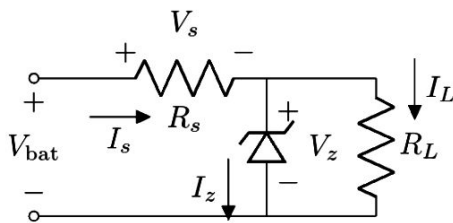
$$= 0.20408 \text{ V/V}$$

$$= 204.08 \text{ mV/V. (Ans)}$$

here,

$$r = r_2 = 0.05 \text{ k}\Omega$$

$$R = R_s = 195 \Omega$$



The circuit above is a voltage regulator used to power a load R_L from a battery V_{bat} . For this circuit, $R_s = 0.2 \text{ k}\Omega$, $R_L = 2 \text{ k}\Omega$, $V_{z0} = 4 \text{ V}$, $r_z = 0 \text{ }\Omega$, and $I_{zk} = 0.5 \text{ mA}$.

- Identify** the zener current I_z in the worst-case scenario. In this worst-case scenario, **calculate** the zener voltage V_z , load current I_L and input current I_s . [5]
- Design** the circuit, *i.e.*, find the minimum value of the input voltage V_{bat} such that, voltage regulation is maintained even in the worst-case scenario. [3]
- Determine** whether the circuit will maintain regulation if V_{bat} is increased. If yes, **argue** if it should be increased or not. [2]

1) (a) Worst case

$$I_Z = I_{ZK} = \boxed{0.5 \text{ mA}}$$

$$V_Z = V_{Z0} + I_Z r_Z$$
$$= \boxed{4 \text{ V}}$$

$$I_L = \frac{V_Z}{R_L} = \frac{4}{2} = \boxed{2 \text{ mA}}$$

$$I_S = I_Z + I_L$$
$$= \boxed{2.5 \text{ mA}}$$

1) (b) $V_{\text{bat}} = V_S + V_Z$

$$= I_S R_S + V_Z$$
$$= \boxed{1.5 \text{ V}}$$

1) (c) Line regulation = $\frac{r_Z}{R_S + r_Z}$

Load „ = $-\frac{r_Z R_S}{R_S + r_Z}$

Neither of the regulations depends on V_{bat} . So, if V_{bat} is increased, regulation will be maintained.

$$\text{Now, } V_{\text{bat}} = (I_Z + I_L) R_S + V_Z$$
$$= \left(I_Z + \frac{V_Z}{R_L} \right) R_S + V_Z$$

$V_{\text{bat}} \uparrow \quad I_Z \uparrow \therefore I_Z > I_{ZK} \rightarrow$ ensures breakdown.
working as regulator.