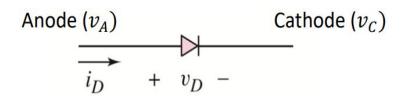
### Lecture 9

Diode models & Rectifiers

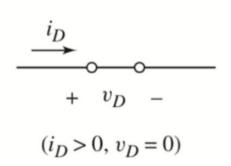
### Review: Ideal Diode Model

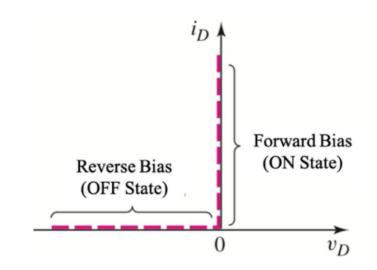


OFF State: Open circuit

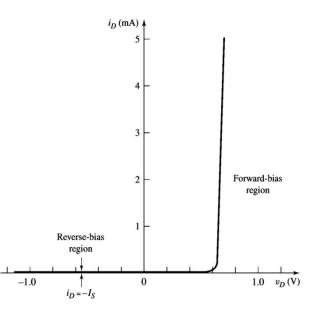
$$\begin{array}{c}
i_D = 0 \\
 & \longrightarrow \\
 & + v_D - \\
 & (v_D < 0, i_D = 0)
\end{array}$$

ON State: Short circuit





### Real diode



I-V characteristics of a real diode

Relation between diode current and diode voltage:

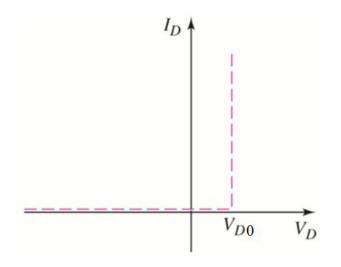
$$i_D = I_S \left( e^{\frac{v_D}{\eta V_T}} - 1 \right)$$

where  $v_D$  (=  $v_A - v_C$ ) is the voltage across the diode,  $i_D$  is the current through the diode (from anode to cathode) and  $V_T$ , called the thermal voltage, is a temperature dependent constant. For temperature T = 300K,  $V_T = 25 \text{ mV}$ .

 $\eta$  is called the ideality factor (try to recall, you measured this in the lab!)

### Modeling the real diode

- 1. Ideal diode model
- 2. Constant voltage drop (CVD) model
- 3. CVD+R model



OFF State: Open circuit

$$\begin{array}{c}
i_D = 0 \\
+ v_D -
\end{array}$$

$$(v_D < V_{D0}, i_D = 0)$$

ON State: Voltage source

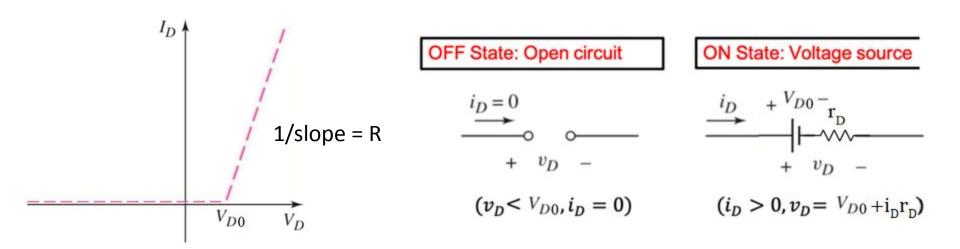
$$V_{D0} - V_{D0} - V_{D0} - V_{D0}$$

$$(i_D > 0, v_D = V_{D0})$$

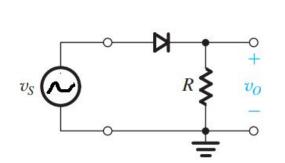
### Modeling the real diode

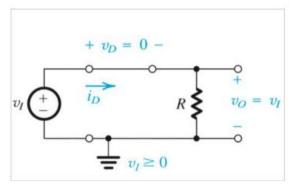
- 1. Ideal diode model
- 2. Constant voltage drop (CVD) model

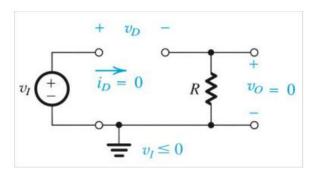
#### 3. CVD+R model

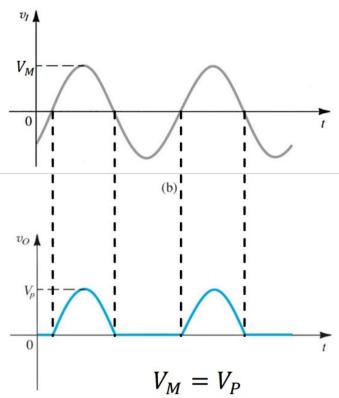


### Half-wave rectifier (ideal diode model)

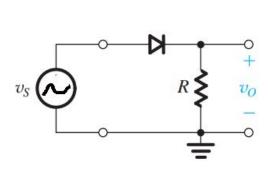


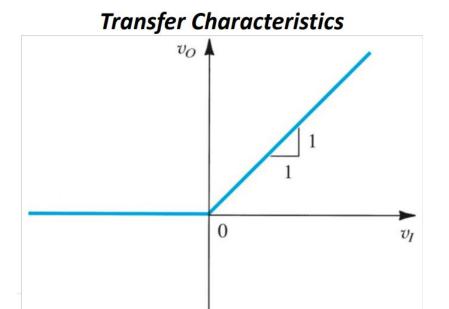




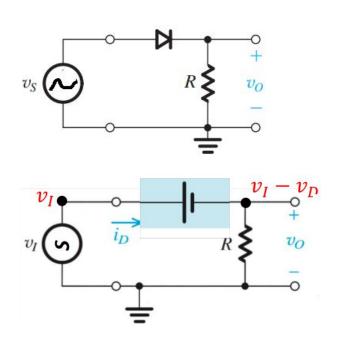


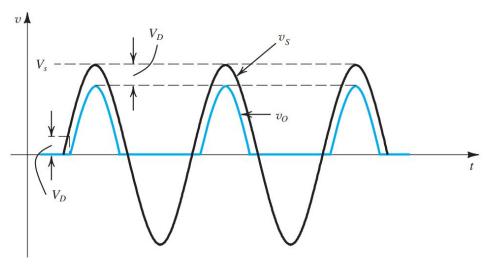
### Half-wave rectifier (ideal diode model)





## Half-wave rectifier (CVD model)





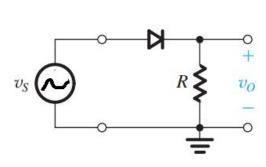
$$v_{I} = V_{M} \sin \omega t$$

$$v_{O} = V_{M} \sin \omega t - V_{D}$$

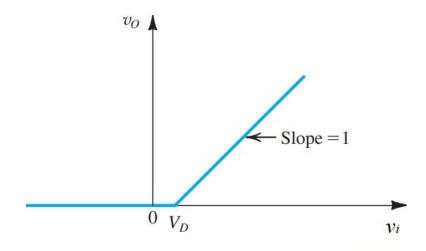
$$V_{D} = peak \ of \ output$$

$$= V_{M} - V_{D}$$

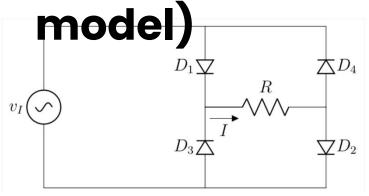
## Half-wave rectifier (CVD model)



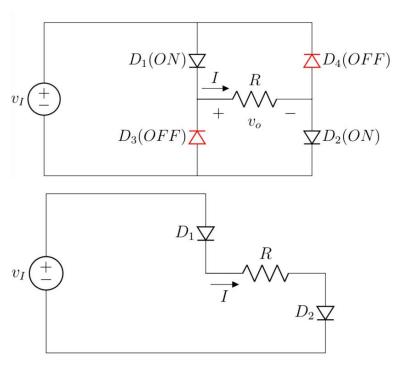
#### **Transfer Characteristics**



# Full-wave rectifier (ideal diode & CVD

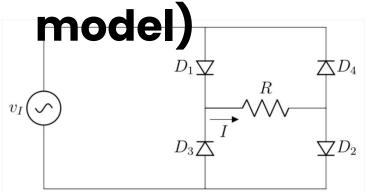


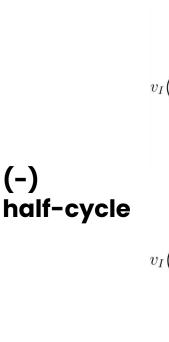
(+) half-cycle

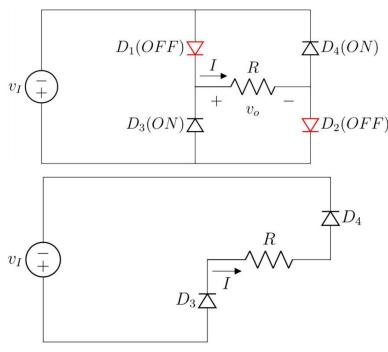


$$v_o = v_I - 2V_D$$

# Full-wave rectifier (ideal diode & CVD

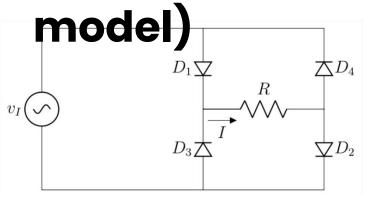


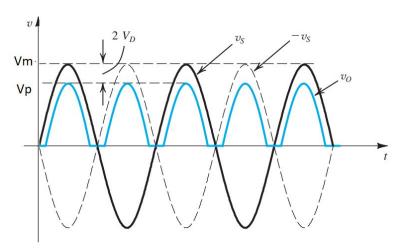




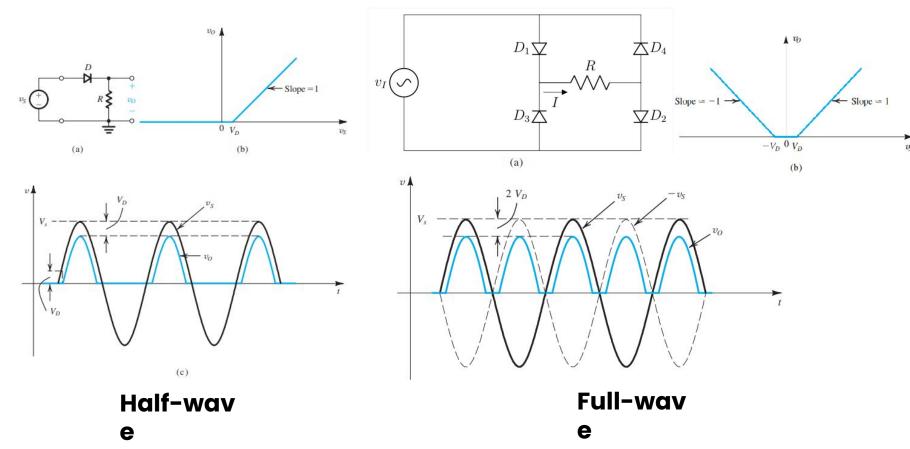
$$v_o = -v_I - 2V_D$$

Full-wave rectifier (ideal diode & CVD

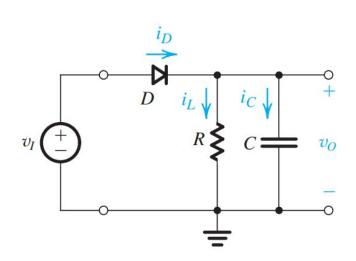


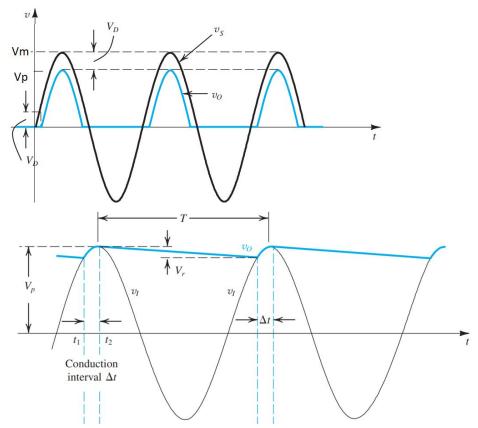


### Half-wave and Full-wave rectifier

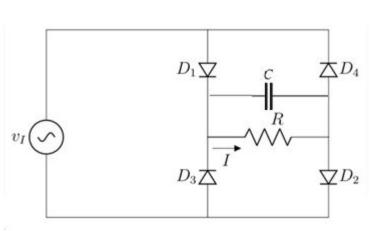


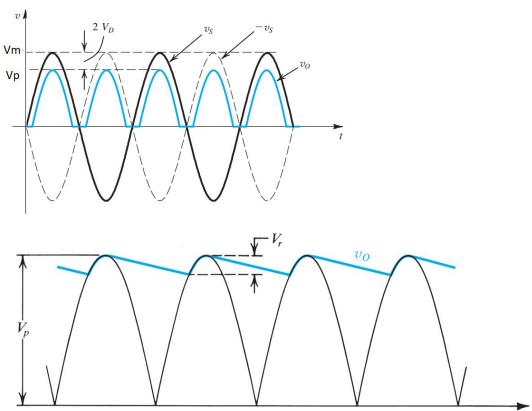
### Filtering: Half-wave rectifier





### Filtering: Full-wave rectifier





### Without capacitor

Rectifier	i/p peak	o/p peak	average
H/W	V <sub>M</sub>	V <sub>p</sub>	$V_{avg} = V_{DC} = \frac{1}{\pi} V_{M} - \frac{1}{2} V_{Do}$
F/W	V <sub>M</sub>	$V_{p}$	$V_{avg} = V_{DC} = \frac{2}{\pi}V_{M} - 2V_{Do}$

# With capacitor

Rectifier	i/p peak	o/p peak	frequency	Ripple voltage	average
H/W	V <sub>M</sub>	$V_p = V_M - V_{Do}$	f <sub>r</sub> =f <sub>i</sub>	$V_r = \frac{V_p}{f_r R C}$	$V_{avg} = V_{DC} = V_p - \frac{1}{2}V_r$
F/W	$V_{M}$	$V_P = V_M - 2V_{Do}$	$f_r=2f_i$	$V_r = \frac{V_p}{f_r R_C}$	$V_{avg} = V_{DC} = V_{P} - \frac{1}{2}V_{r}$

$$I_{o,avg} = V_{o,avg}/R$$
,  $V_{rms} = V_p/\sqrt{2}$ 

### **Example**



A voltage waveform  $v_i = 8sin(2000\pi t)V$  is input to a full-wave rectifier. A resistance of  $R = 50k \Omega$  is connected at the load. [Assume that the diodes used in the circuit have a forward drop of 0.8V].

(a) Draw the circuit of the full wave rectifier. Label the input and output voltages properly.

(b) Draw the waveforms of the input and output voltages. What are the peak values of input and output? Show them in the graph.

[1+1]

[1]

(c) Find the average voltage measured at the output.

[1]



# Thank you