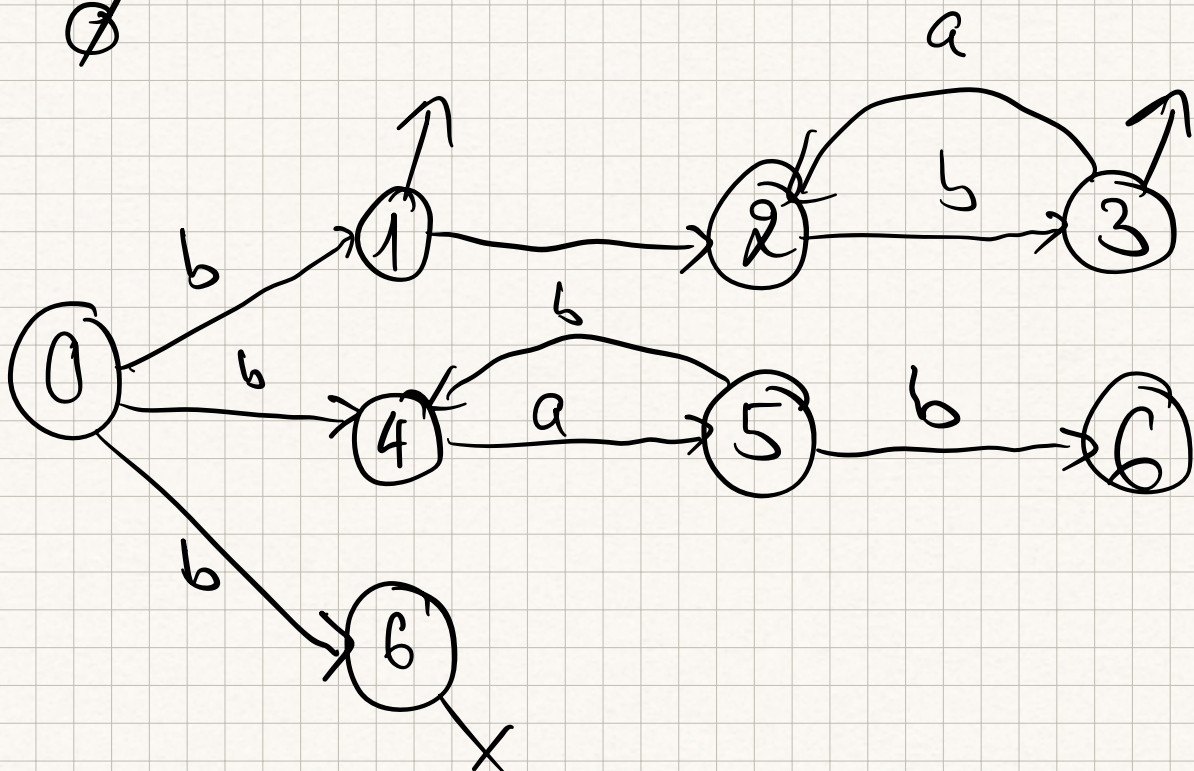


Glushkov

$$b(ab)^* + (ba)^*b$$

$$= b_1(a_2b_3)^* + (b_4a_5)^*b_6$$

| | SUCC | | |
|-------------|-------------|-------|-------|
| \emptyset | b_1 | b_4 | b_6 |
| b_1 | a_2 | | |
| a_2 | b_3 | | |
| b_3 | a_2 | | |
| b_4 | a_5 | | |
| a_5 | b_4 | b_6 | |
| b_6 | \emptyset | | |



Ex 1 Examen

$$(a^*(ab+ba)^* + (bb)^*)^*$$

$$= (a_1^*(a_2 b_3 + b_4 a_5)^* + (b_6 b_7)^*)^*$$

SUCC

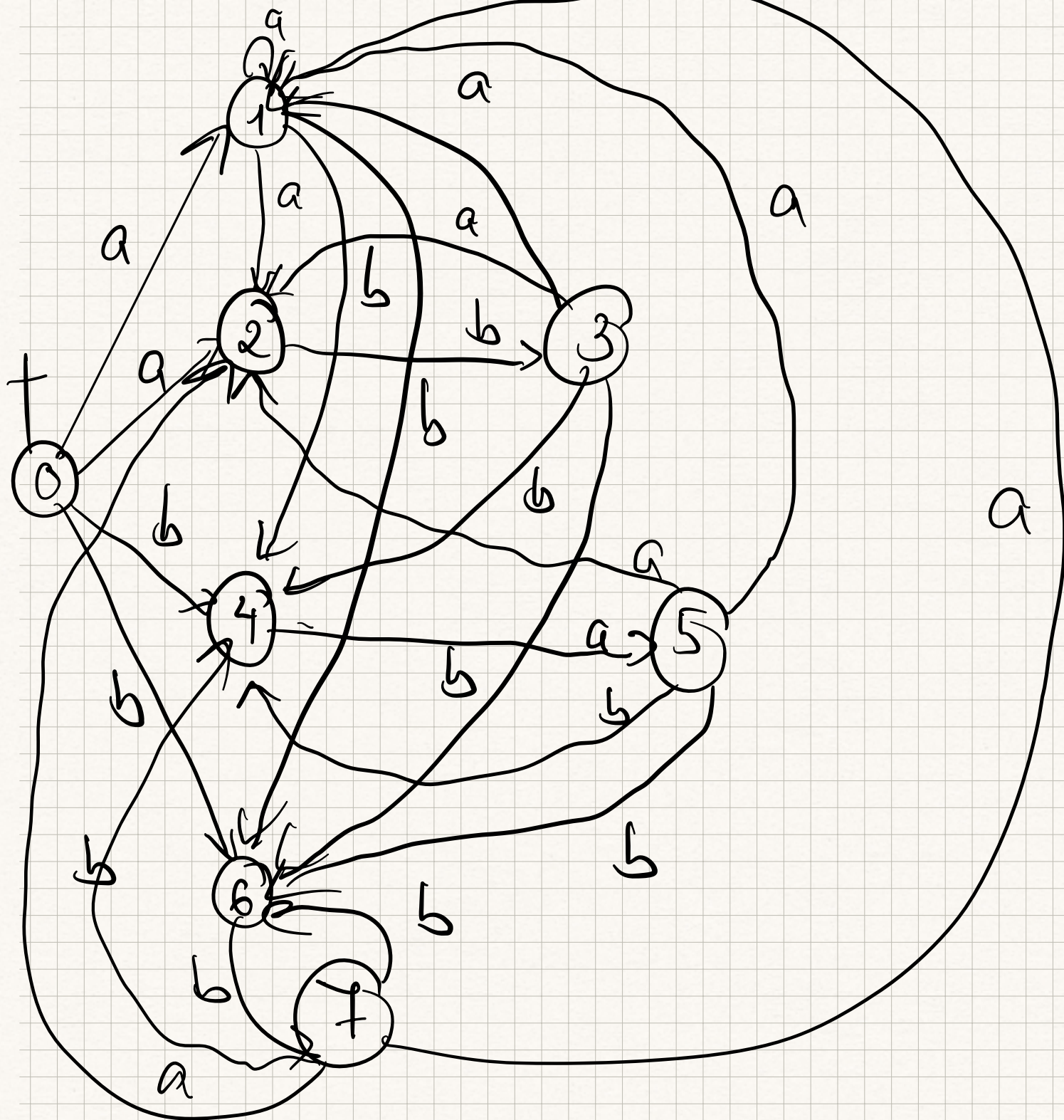
| | a_1 | a_2 | b_4 | b_6 |
|-------------|-------|-------|-------|-------|
| \emptyset | a_1 | a_2 | b_4 | b_6 |
| a_1 | a_1 | a_2 | b_4 | b_6 |
| a_2 | b_3 | | | |
| b_3 | a_1 | a_2 | b_4 | b_6 |
| b_4 | a_5 | | | |
| a_5 | a_1 | a_2 | b_4 | b_6 |
| b_6 | b_7 | | | |
| b_7 | a_1 | a_2 | b_4 | b_6 |

$$\text{first}(r') = \{a_1, a_2, b_4, b_6\}$$

$$\text{last}(r') = \{a_1, b_3, a_5, b_7\}$$

$$\text{Next}(r) = (\text{last}, \text{first})$$

$$\text{Next}(r) = (a_1, a_1) (a_1, a_2) ($$



Ex TD 4/

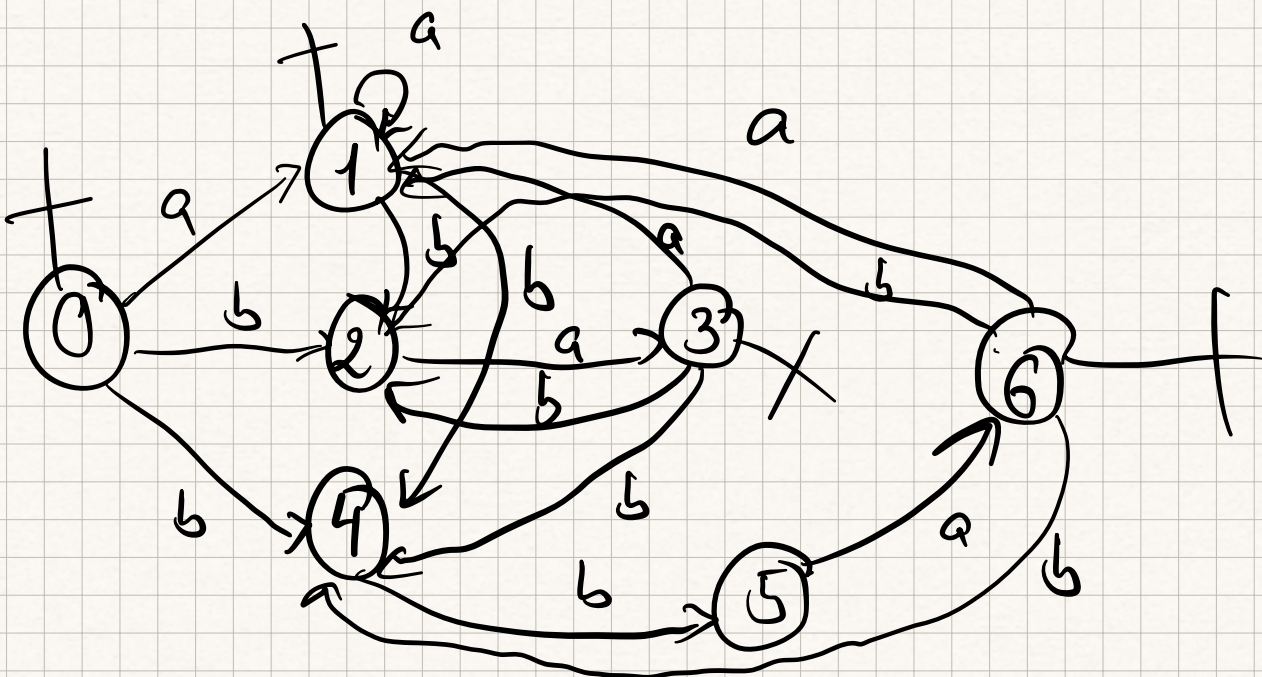
$$\begin{aligned} \mathcal{L}(A) &= (a + ba + bba)^+ \\ &= (a_1 + b_2 a_3 + b_4 b_5 a_6)^+ \end{aligned}$$

SUCC

| \emptyset ^{first} | a_1 | b_2 | b_4 |
|------------------------------|-------|-------|-------|
| a_1 | a_1 | b_2 | b_4 |
| b_2 | a_3 | | |
| a_3 | a_1 | b_2 | b_4 |
| b_4 | b_5 | | |
| b_5 | a_6 | | |
| a_6 | a_1 | b_2 | b_4 |

$$\begin{aligned} \text{first}(r) &= \{a_1, b_2, b_4\} \\ \text{last}(r) &= \{a_1, a_3, a_6\} \end{aligned}$$

$$\text{Next}(r) = (\text{Last}, \text{Next})$$



$$(a^*(ab+ba)^* + (bb)^*)^*$$

$$(\underline{a_1}^* (a_2 b_3 + \underline{b_4} a_5)^* + (\underline{b_6} b_7)^*)^*$$

SUCC

| \emptyset | a_1 | a_2 | b_4 | b_6 |
|---------------|-------|-------|-------|-------|
| $\boxed{a_1}$ | a_1 | a_2 | b_4 | b_6 |
| a_2 | b_3 | | | |
| $\boxed{b_3}$ | a_1 | a_2 | b_4 | b_6 |
| b_4 | a_5 | | | |
| $\boxed{a_5}$ | a_1 | a_2 | b_4 | b_6 |
| b_6 | b_7 | | | |
| $\boxed{b_7}$ | a_1 | a_2 | b_4 | b_6 |

$$\times \underline{\text{first}}(r) = \{a_1, a_2, b_4, b_6\}$$

$$\times \underline{\text{last}}(r) = \{a_1, b_3, a_5, b_7\}$$

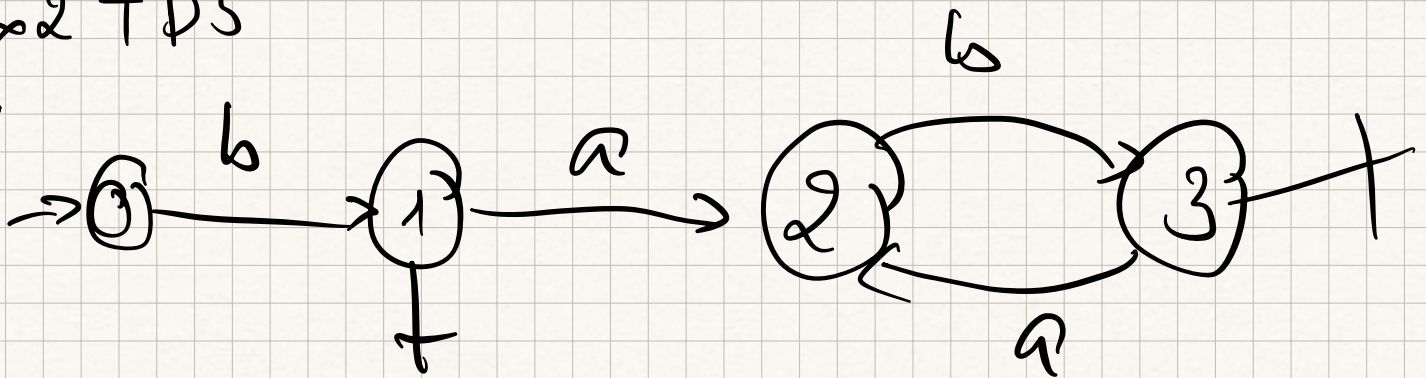
$$\times \text{Next}(r) = (\text{last}, \text{first})$$

$$\text{Next}(r) \\ (a_2, b_3)$$

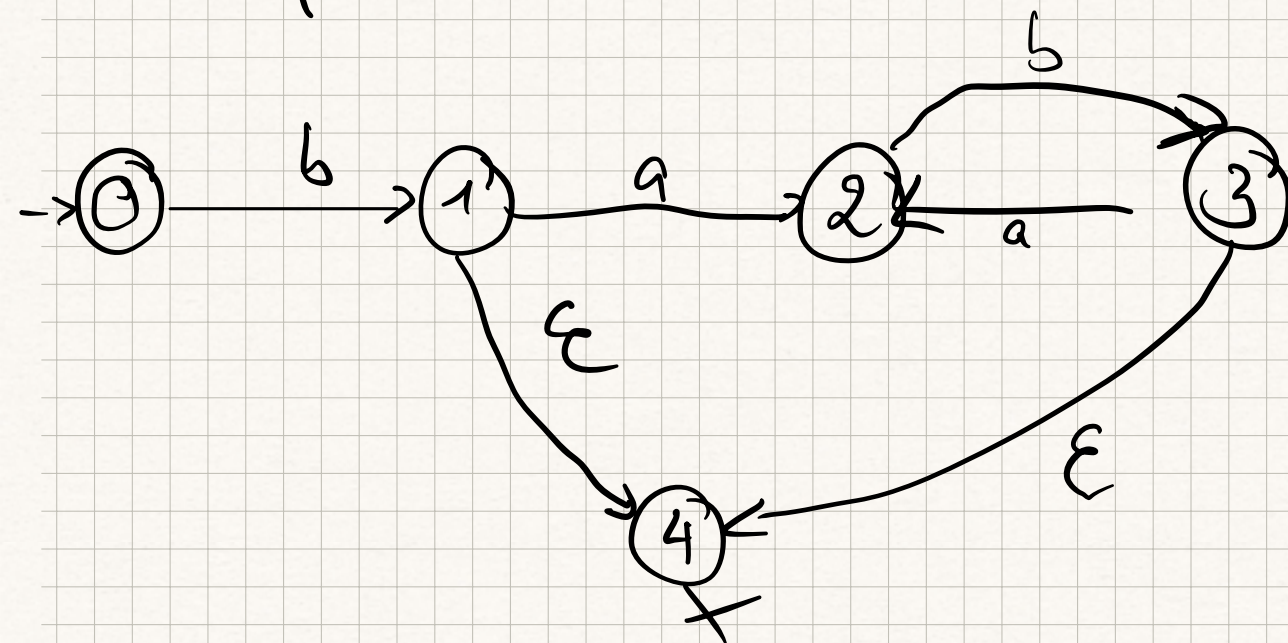
Brozowski

Ex 2 T D 5

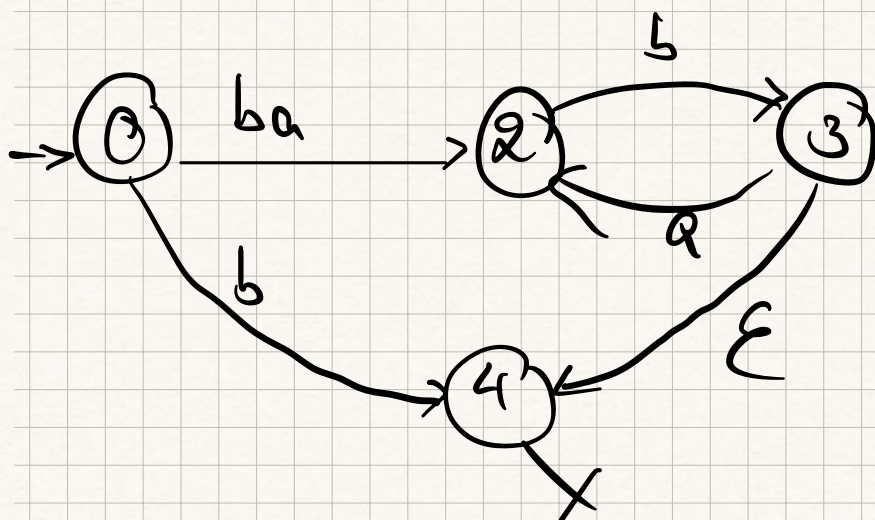
14



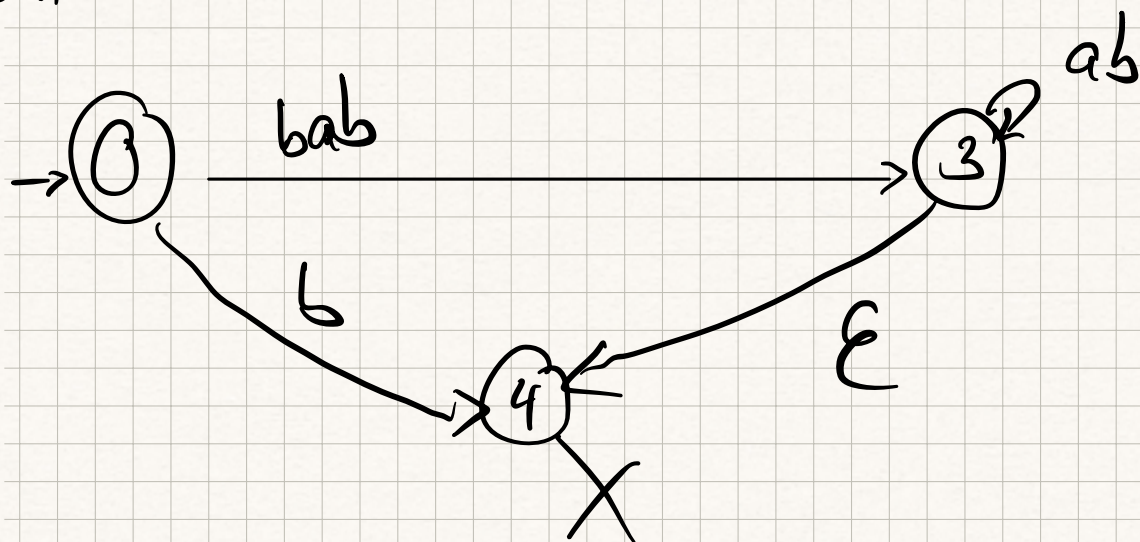
On modifie automate :



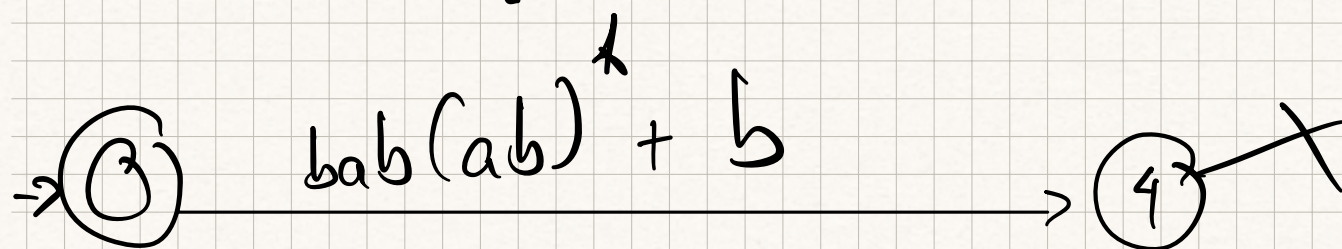
On élimine 1 :



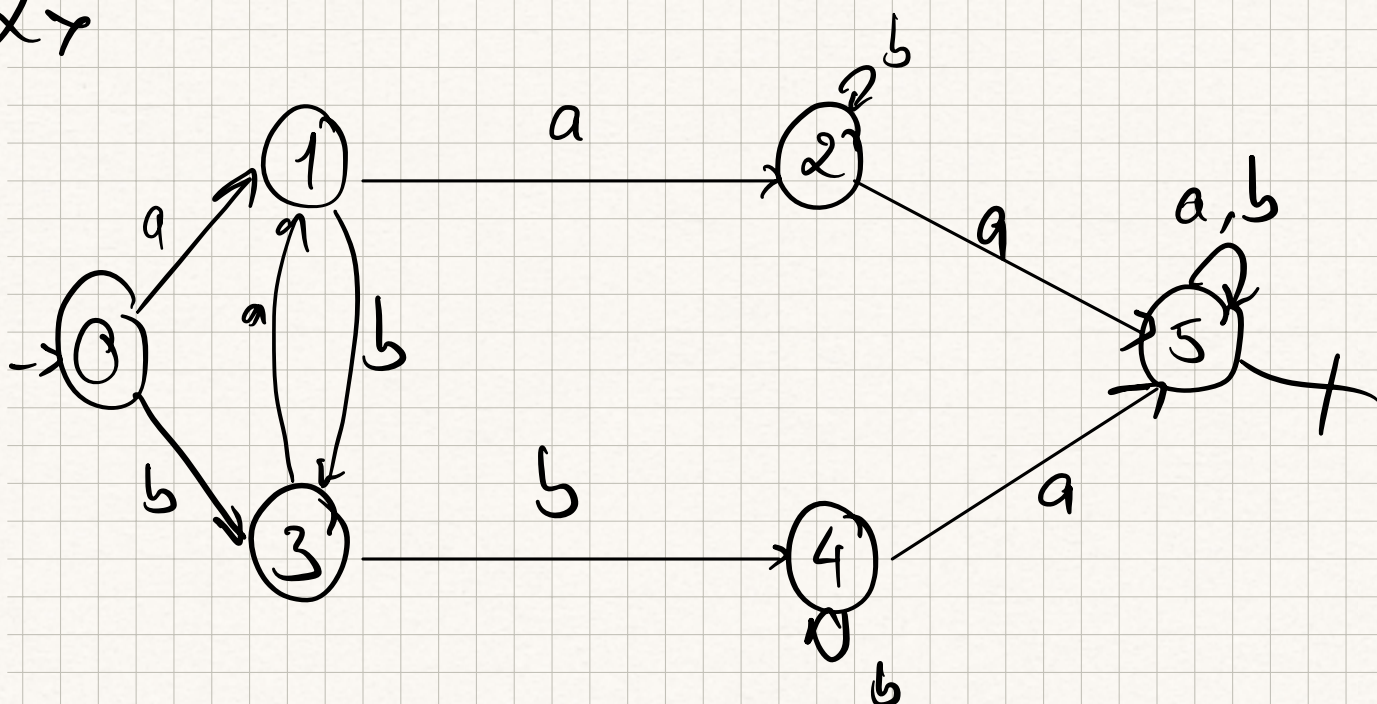
On élimine 2 :



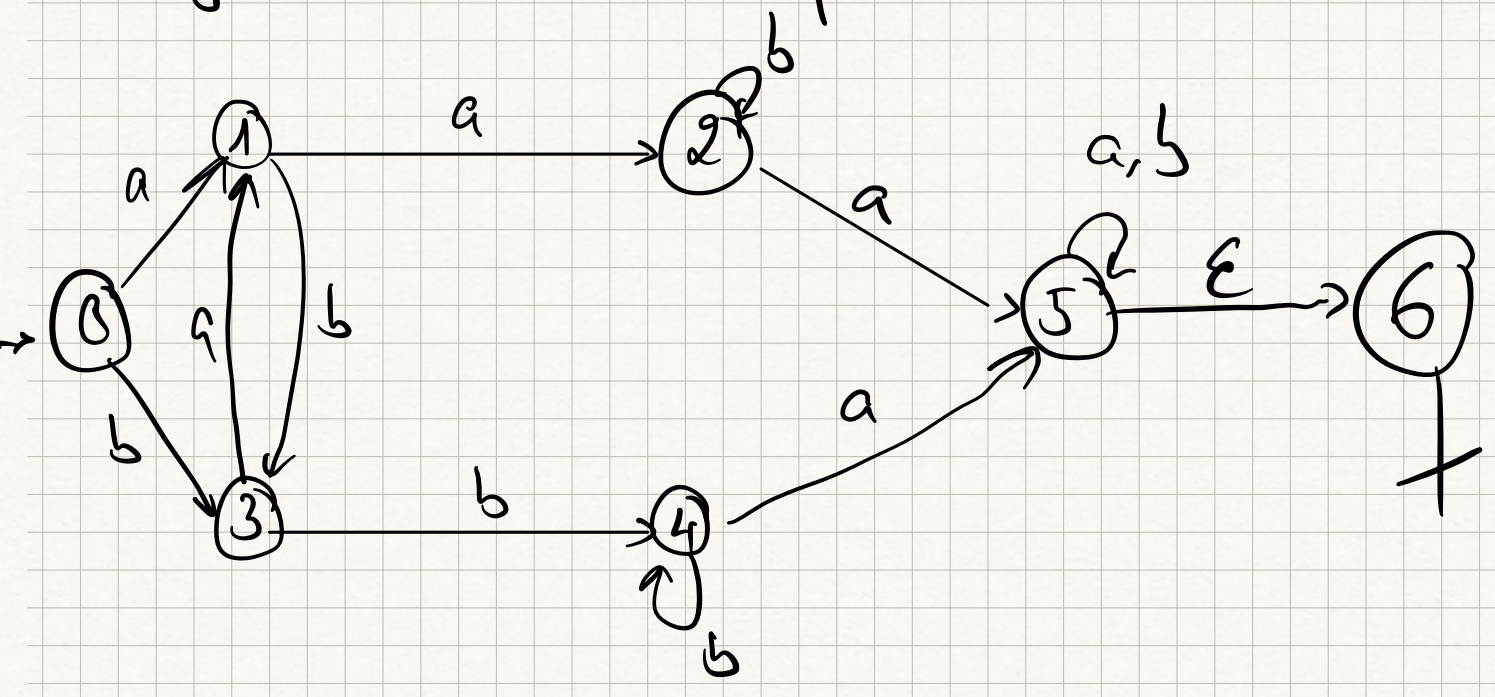
On élimine 3 :



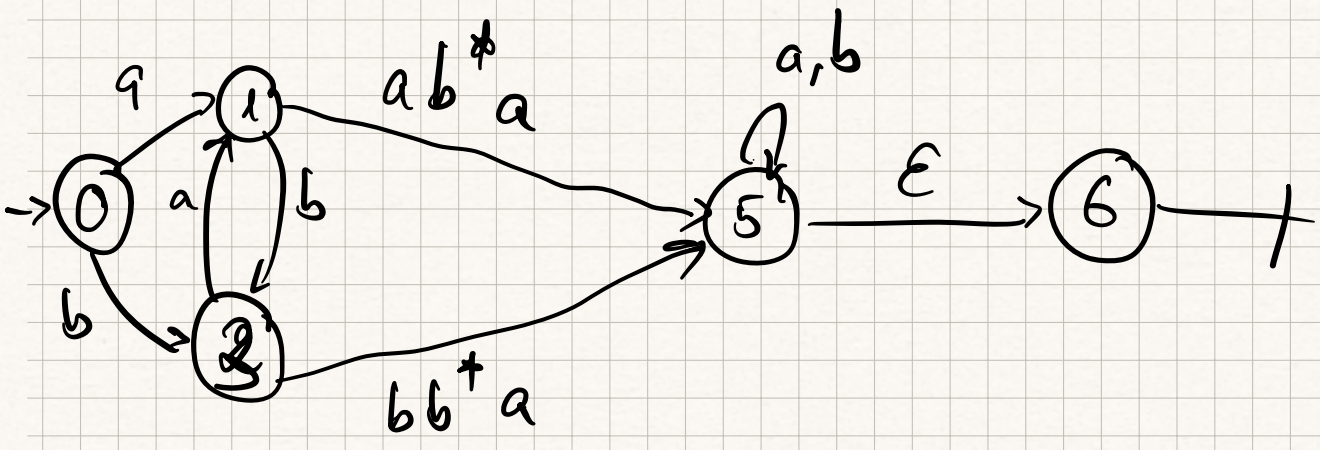
27



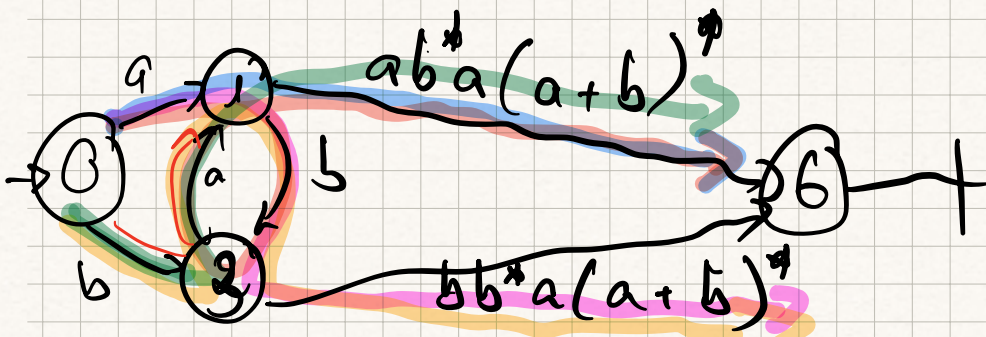
On rajoute une étape



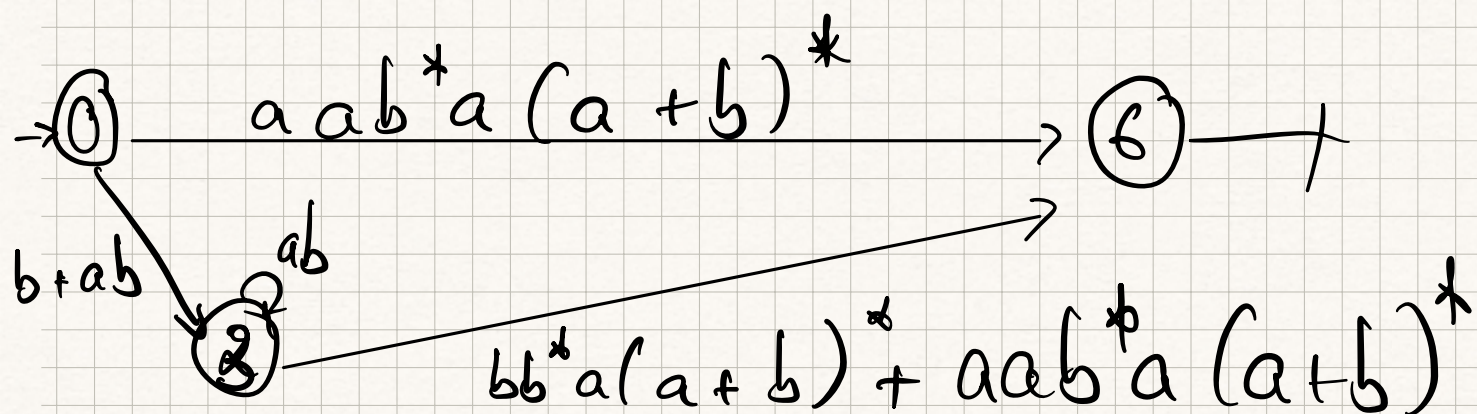
On élimine 2 et 4



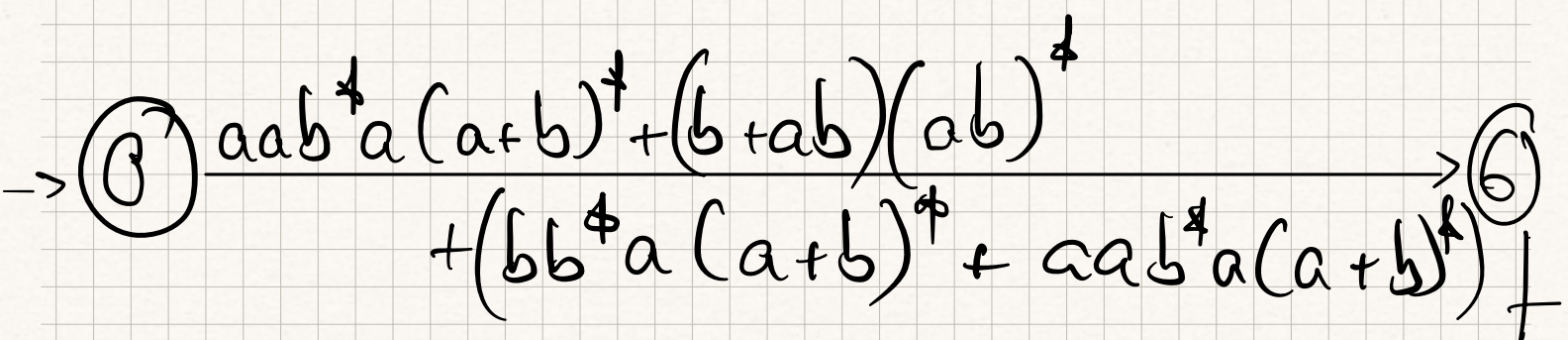
On élimine 5



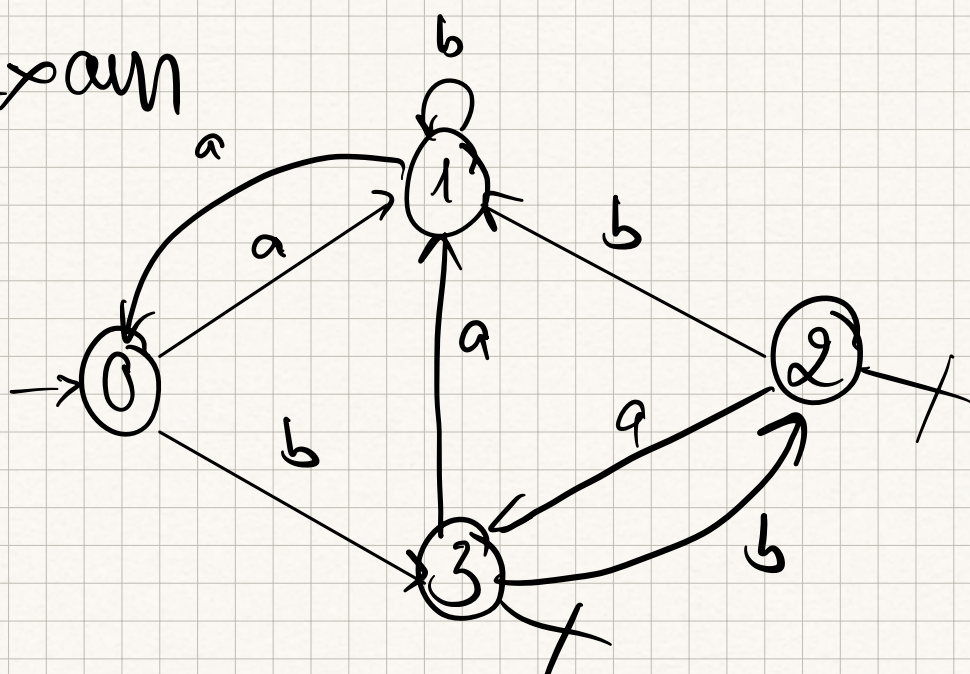
On élimine 1

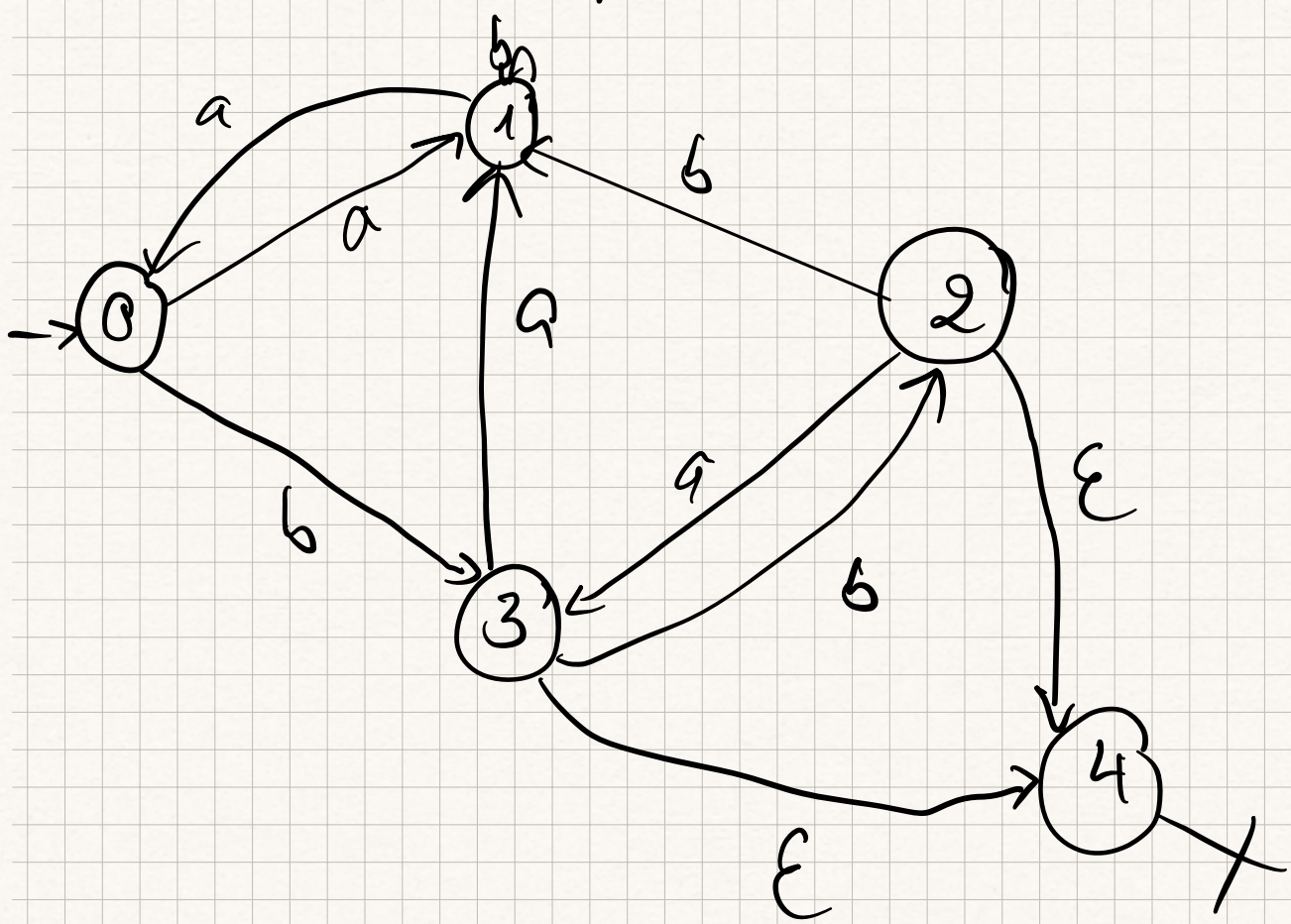


On élimine 3

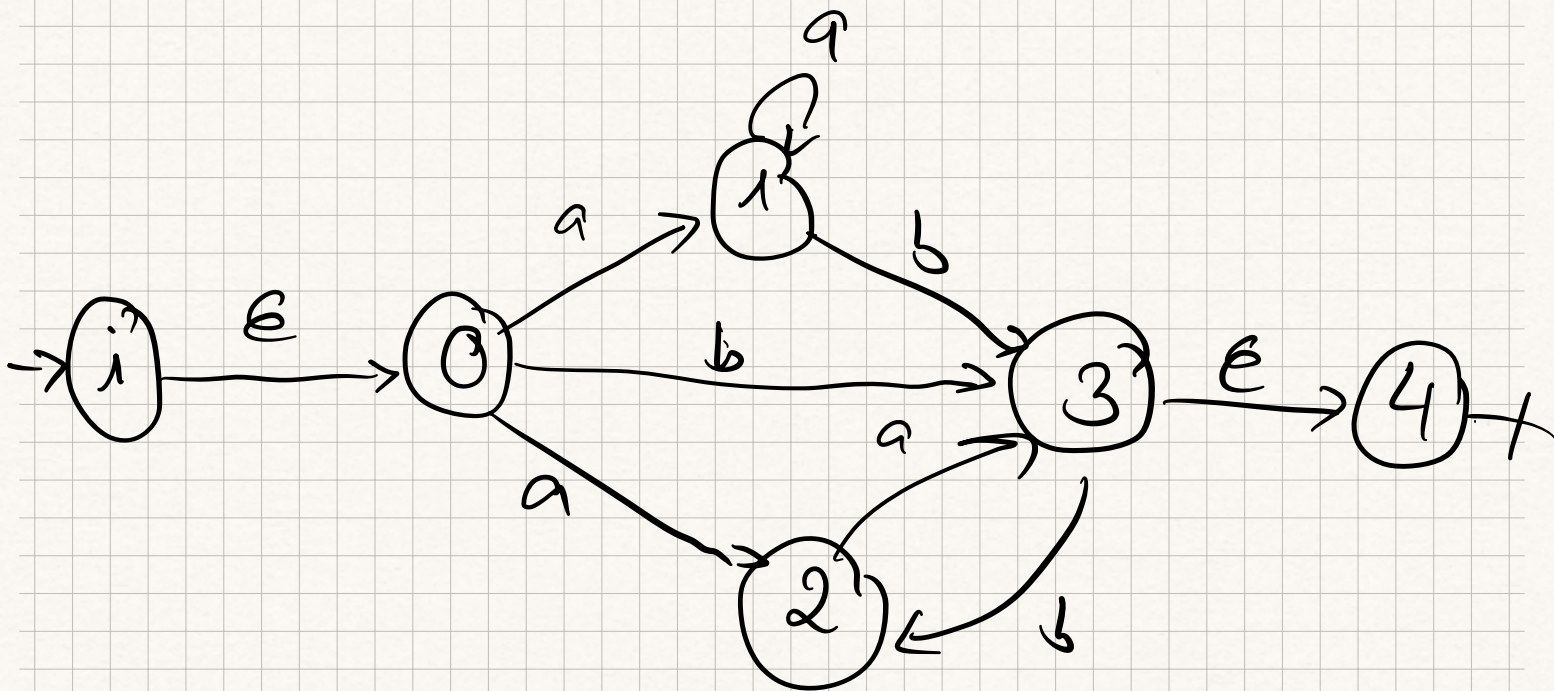
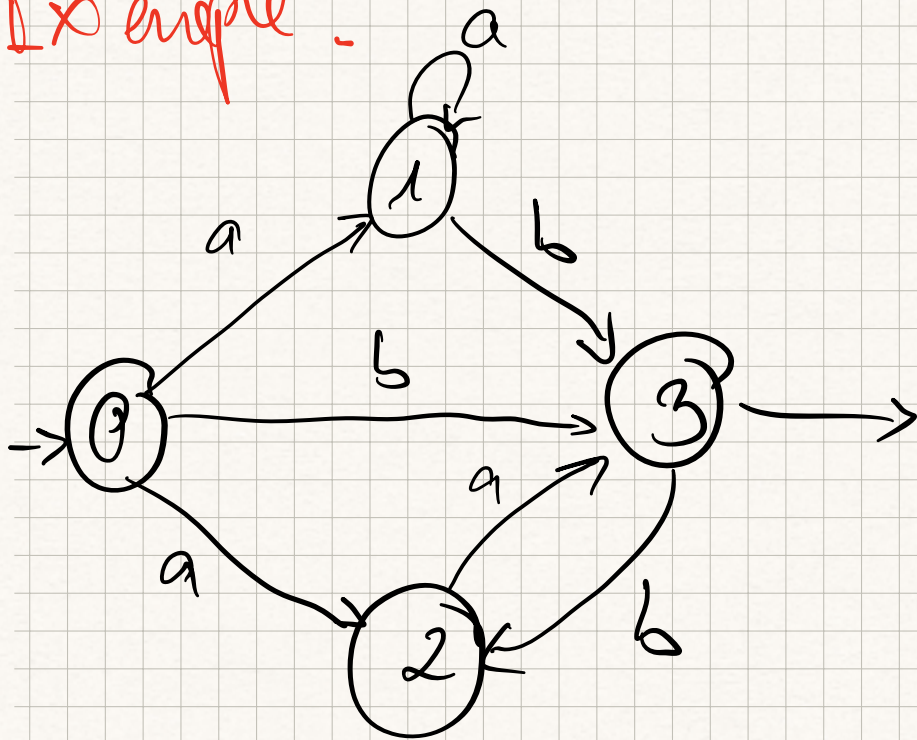


Exan

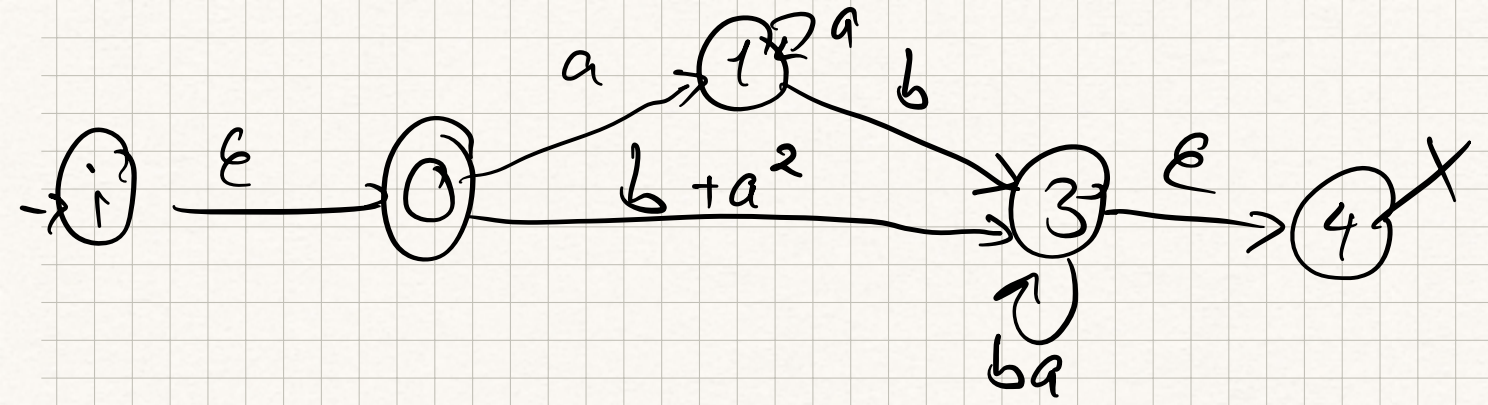




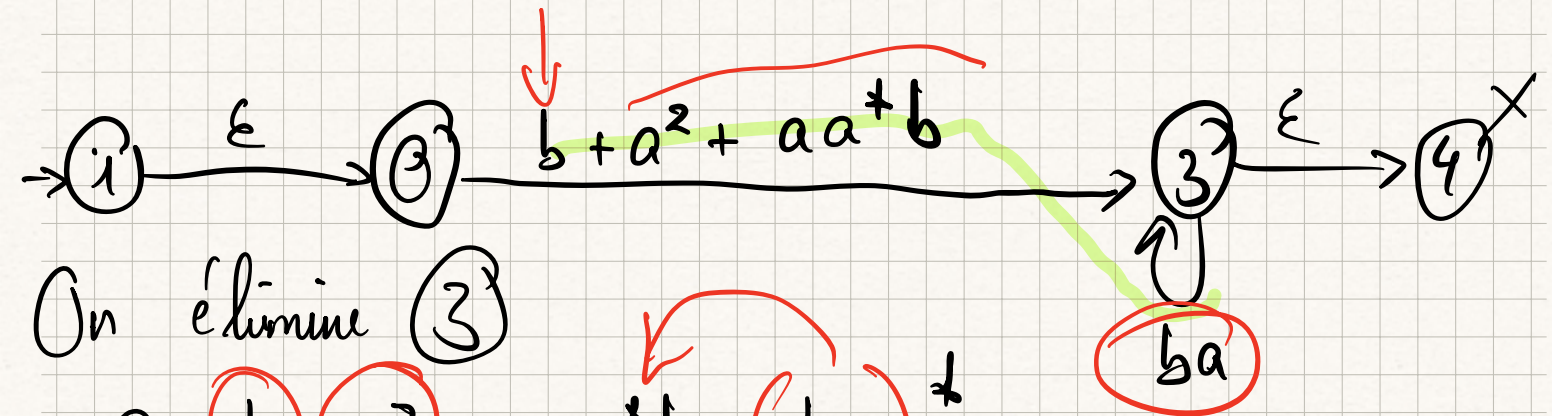
Example :



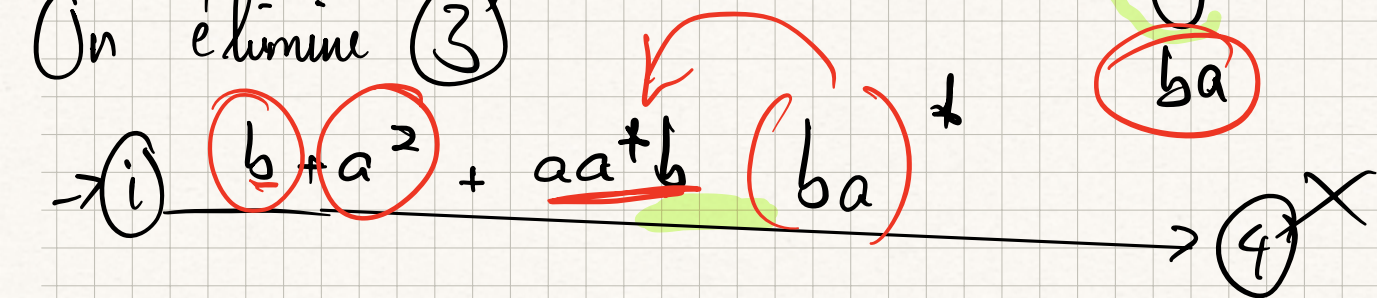
On eliminate (2)



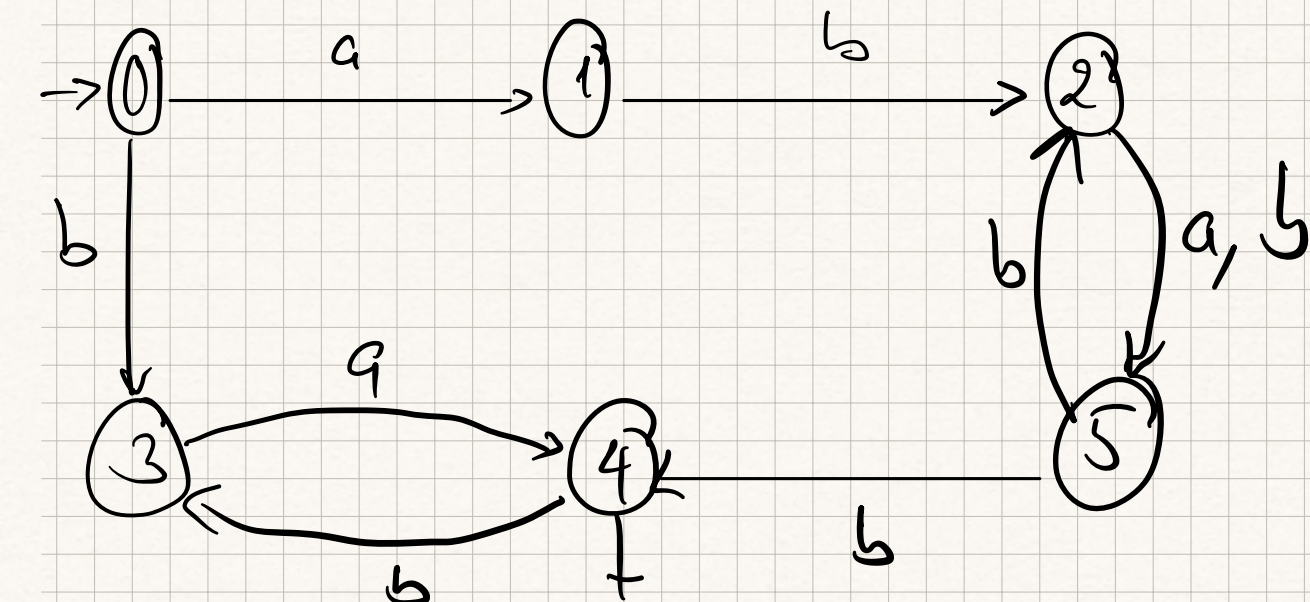
On élimine 1

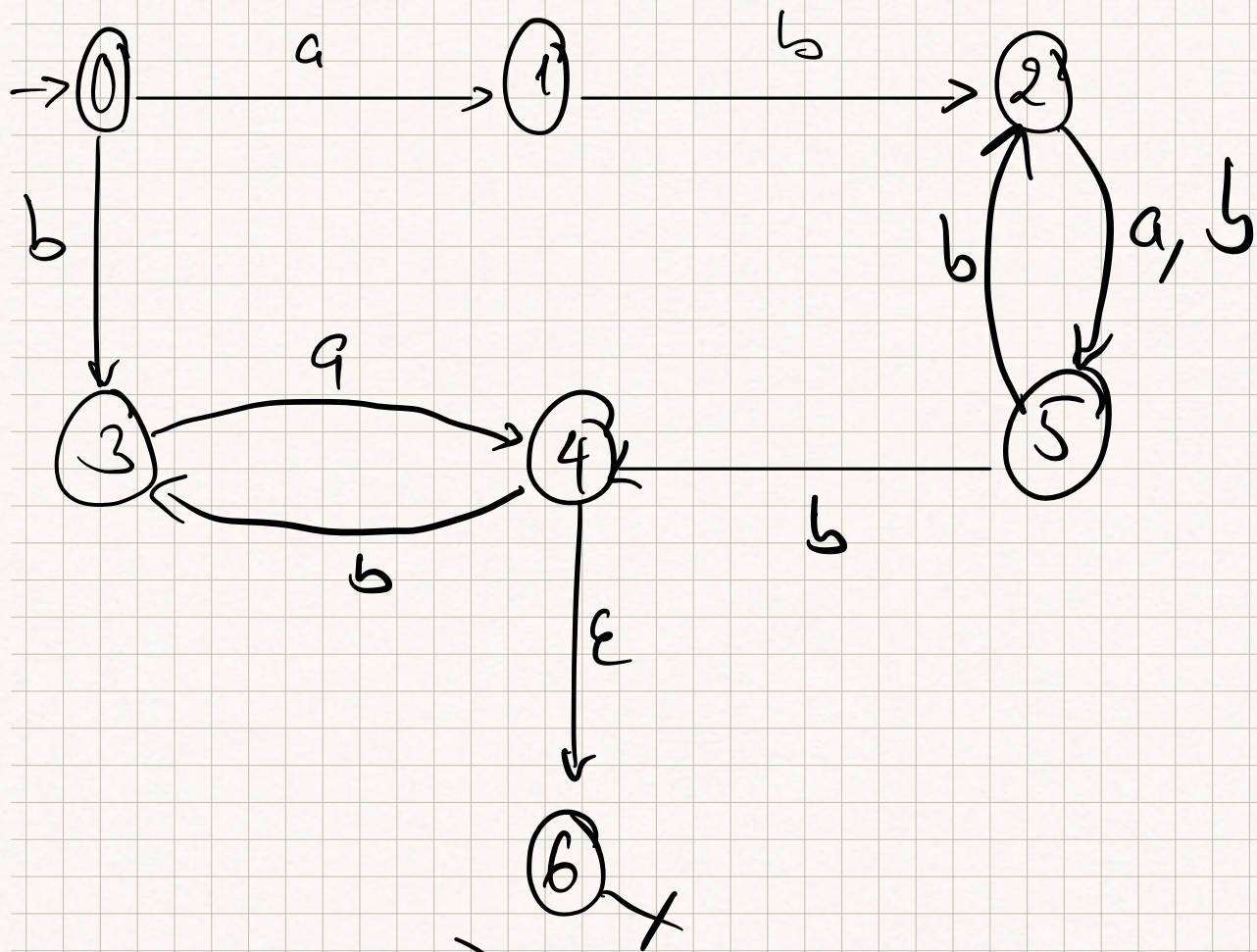


On élimine 3

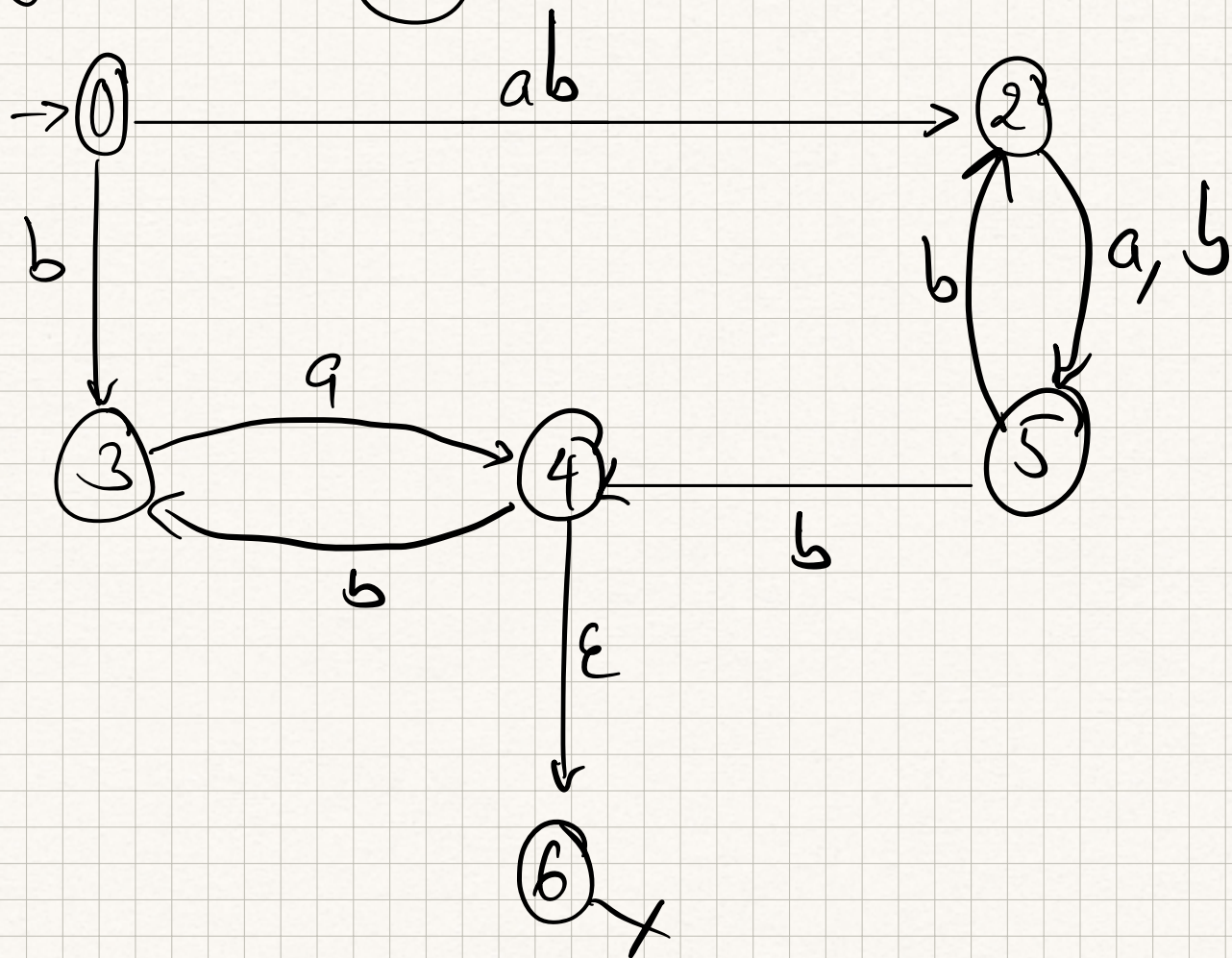


Exemple

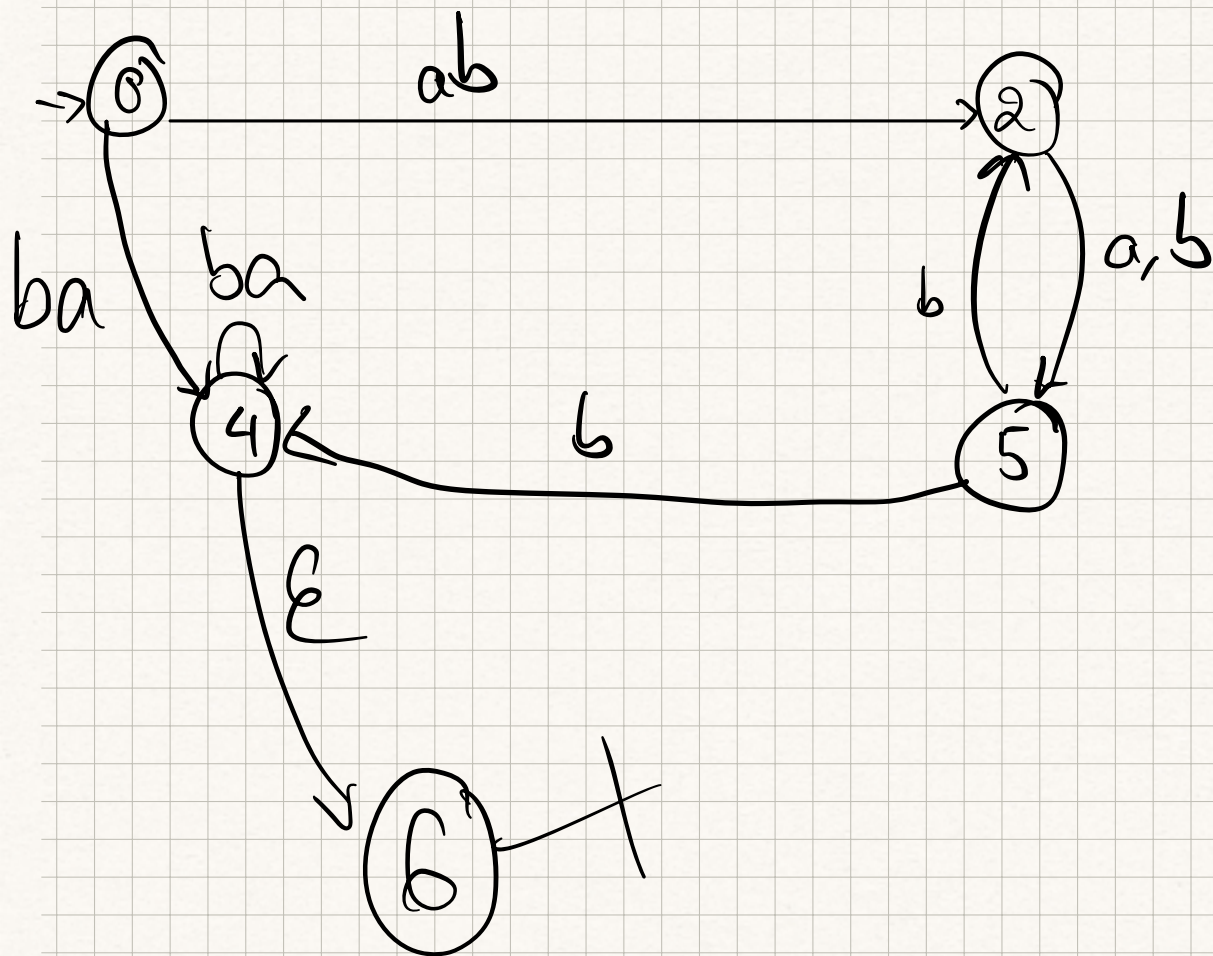




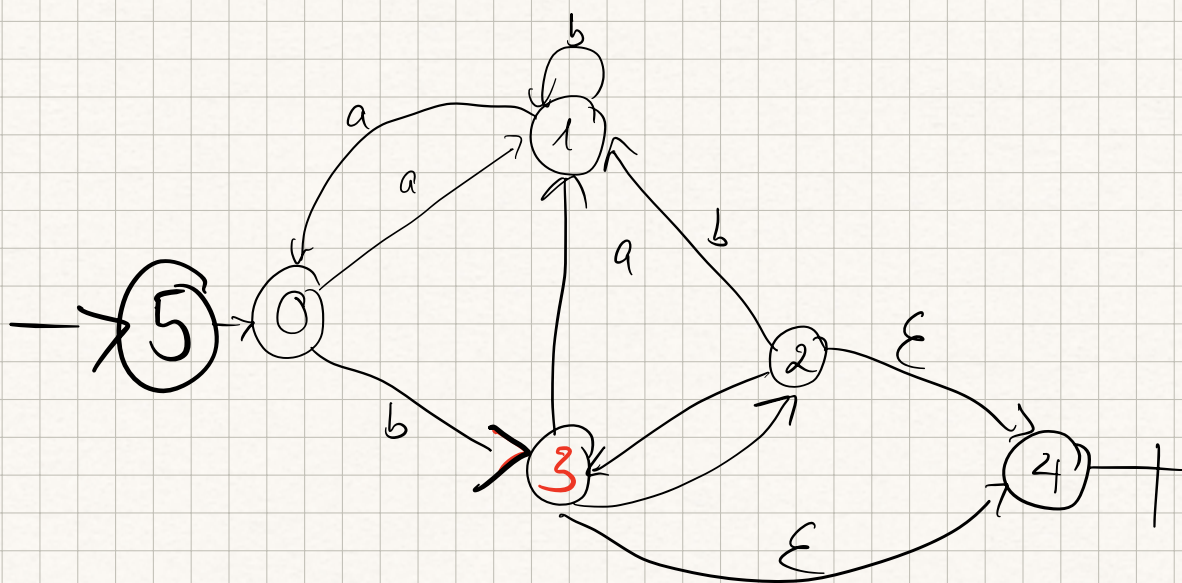
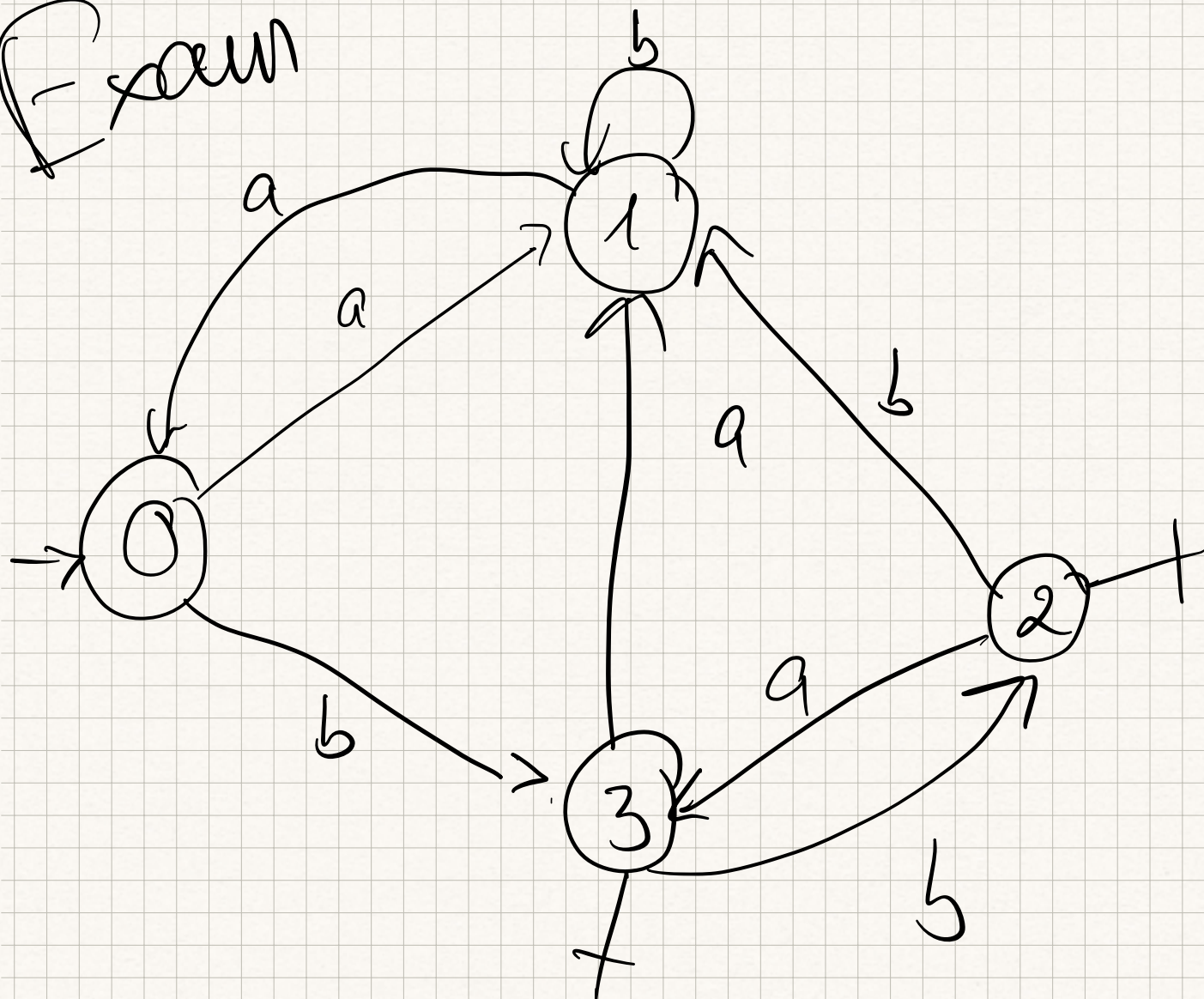
On eliminate (1)



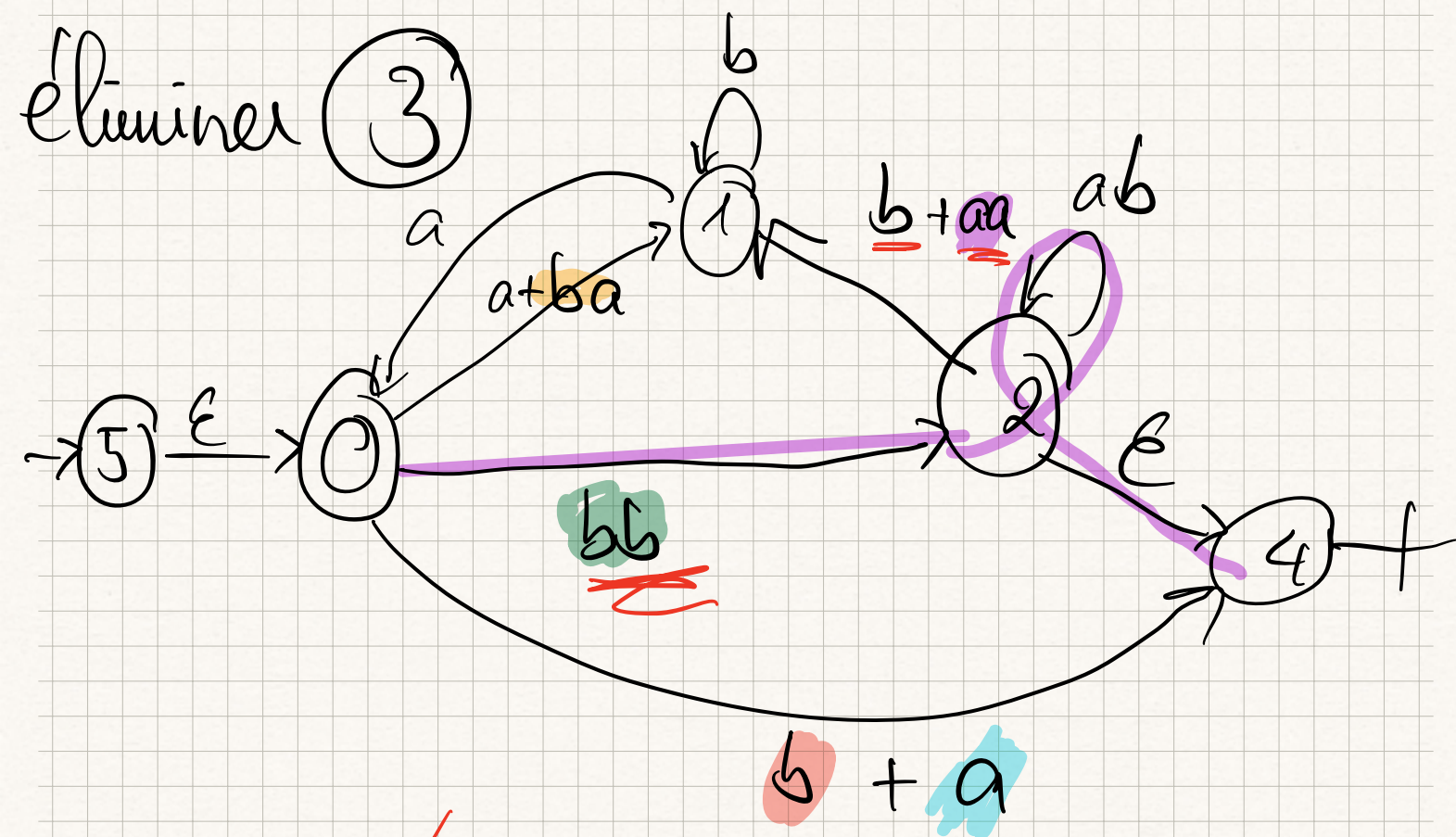
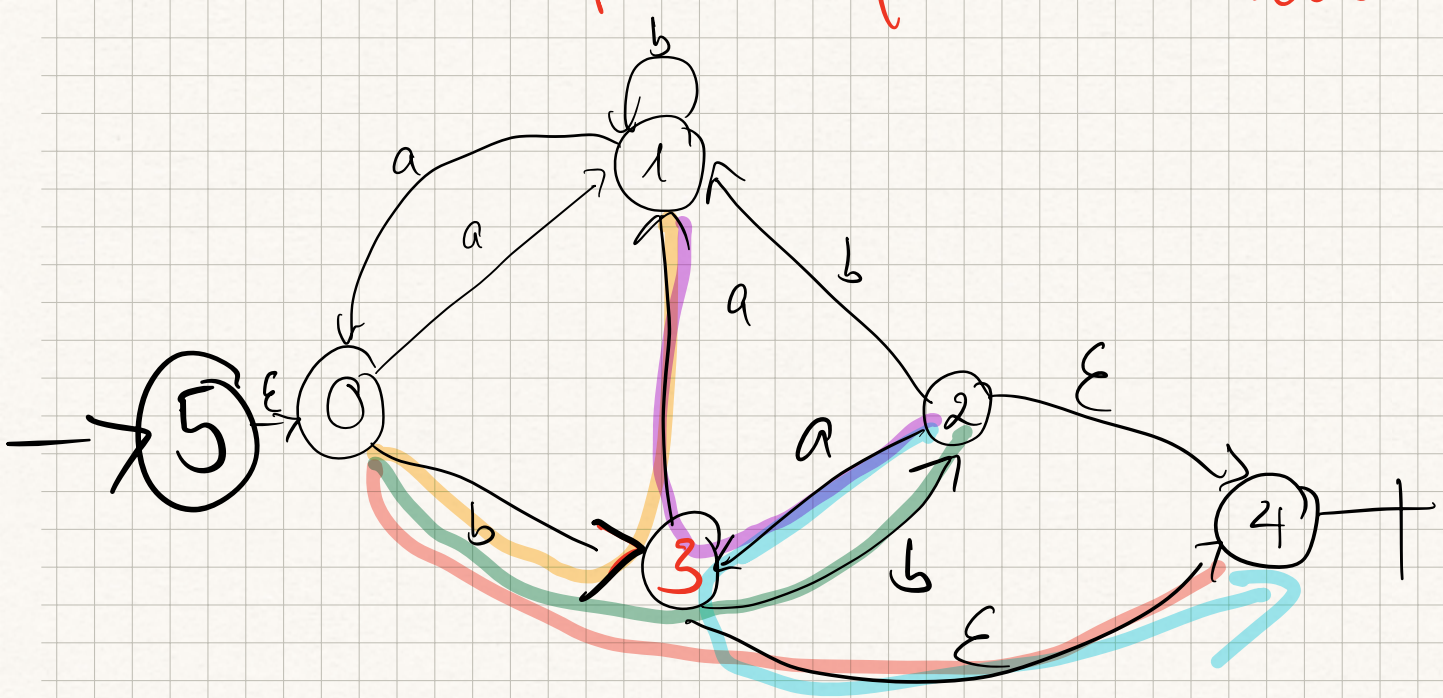
On eliminate (3)



Exemple

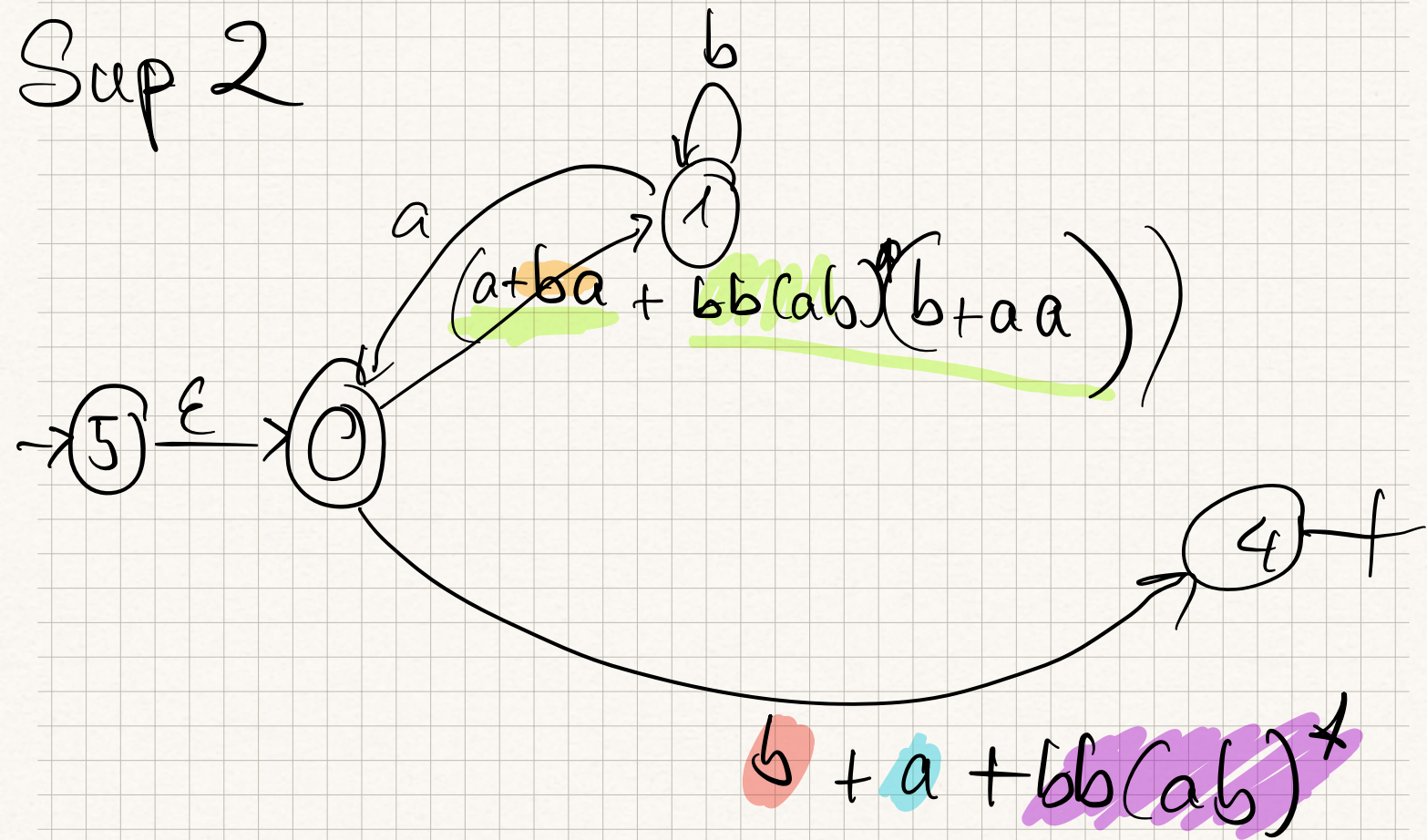


Etat initial : pas de fleches entrante

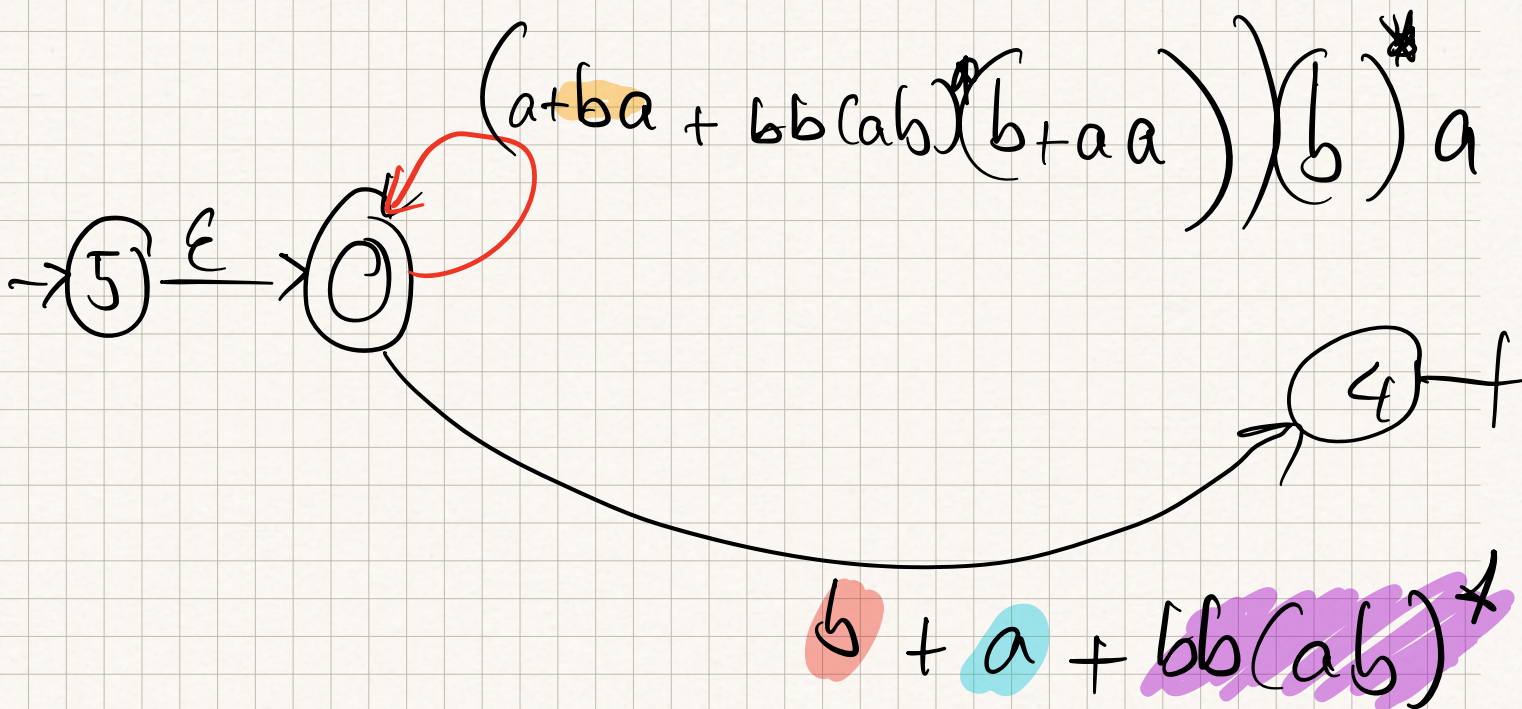


$$\frac{a+ba}{\checkmark} + \frac{bb(ab)^*b}{\checkmark} + \frac{aa}{\checkmark}$$

Sup 2

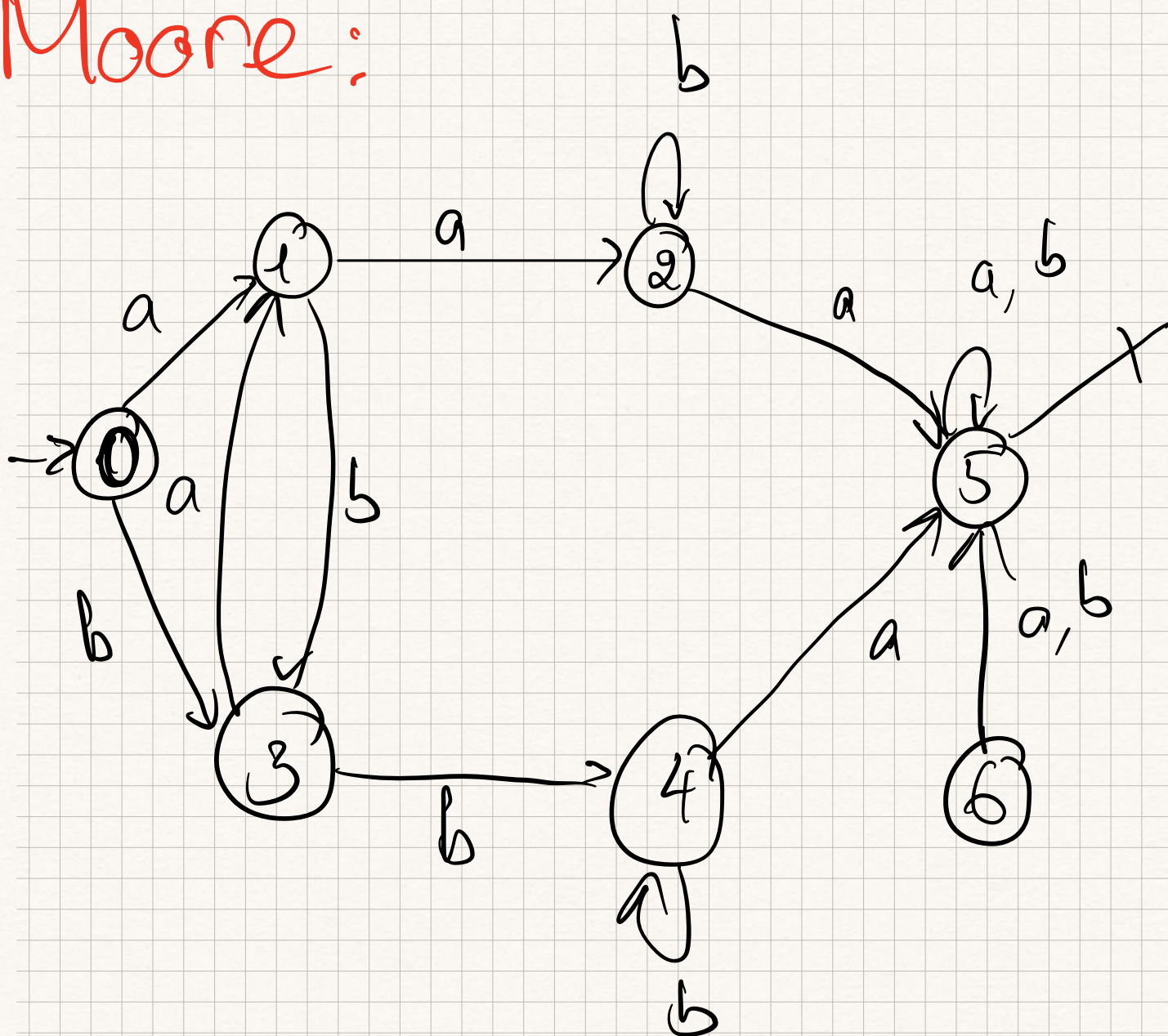


Supp 1



→ ⑤ $((a+ba+bb(ab)^*(b+aa)(b)^*a)^*(b+a+bb(ab)^*))$ → ④

Moore:



| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|---|--------------|
| a | 1 | 2 | 5 | 1 | 5 | 5 | |
| b | 3 | 3 | 2 | 4 | 4 | 5 | |

b n'est pas accessible. On enlève 6

$\{0, 1, 2, 3, 4, 5\}$ $\{5\}$

(a sépare 3 et 4)

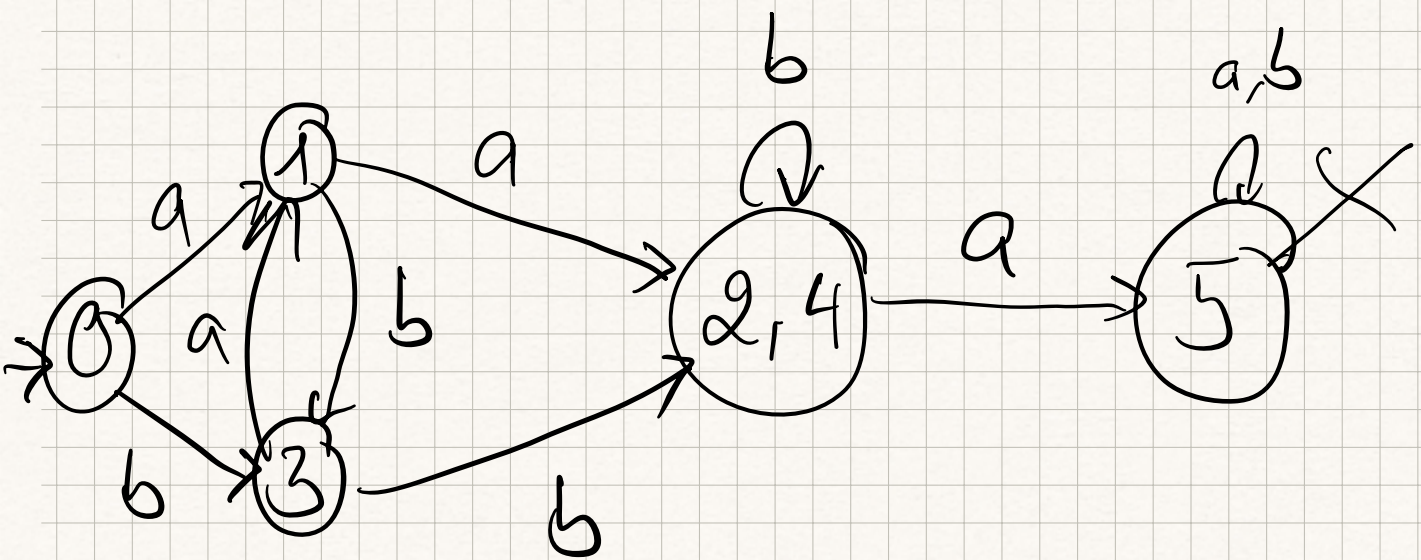
$\{0, 1, 3\}$ $\{2, 4\}$ $\{5\}$

(a sépare 1 et 3)

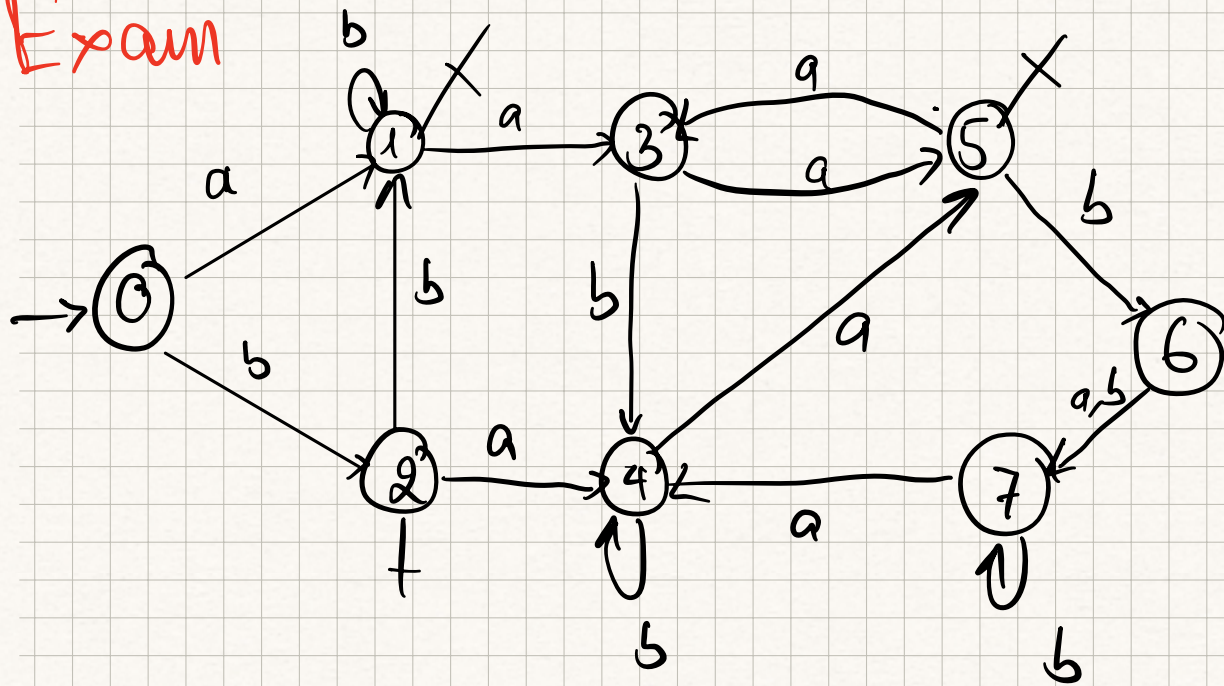
$\{0, 3\}$ $\{1\}$ $\{2, 4\}$ $\{5\}$

(b sépare 0 et 3)

$\{0\}$ $\{3\}$ $\{1\}$ $\{2, 4\}$ $\{5\}$



Exam



| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---|---|---|---|---|---|---|---|---|
| a | 1 | 3 | 4 | 5 | 5 | 3 | 7 | 4 |
| b | 2 | 1 | 1 | 4 | 4 | 6 | 7 | 7 |

Séparer états finaux et les autres

{0, 3, 4, 6, 7} {1, 2, 5}

b sépare 2 et 5

{ 1, 2 } { 5 } { 0, 3, 4, 6, 7 }

a sépare 0 et 3

{ 0, 6, 7 } { 3, 4 } { 1, 2 } { 5 }

a sépare 0 et 6

{ 0 } { 3, 4 } { 1, 2 } { 5 } { 6, 7 }

a sépare 6 et 7

{ 0 } { 3, 4 } { 1, 2 } { 5 } { 6 }
{ 7 }

