

# Package Delivery on “Double 11” Day

## Project for Algorithm and Complexity

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**Abstract.** Package delivery is such a significant problem nowadays. The convenience and speediness of online shopping highly rely on an efficient and well-organized delivery network. Meanwhile, the delivery companies always want to reduce the cost of transportation while winning high rates from customers. The problem can be modelled as min-cost commodity flows over time. The characteristics of such kind of problem are networks with capacities and transit times. We also have other properties like the priority of orders of commodities, the ordering time and transportation restrictions with respect to special kinds of commodities. However, such kind of problems is really hard to solve. Though static  $s$ - $t$  flow problem can be solved in polynomial time, the problem we encountered is almost NP-Hard with enormous input size. Thus, we came up with some approximations to get good feasible solutions, applied these algorithms in different scenes and compared their performance.

**Keywords:** Package Delivery, Network Flow, Routing, Flow over time.

## 1 Symbol Table

Define all the symbols that will be used later.

**Table 1.** Symbol Table

Symbol	Attribute
<i>city</i>	<i>index, kind(large/small/hub), capacity</i>
<i>tool</i>	<i>departure_city, arrival_city, time, average_delay, departure_time, unit_cost</i>
<i>commodity</i>	<i>index, unit_weight</i>
<i>order</i>	<i>seller_city, purchaser_city, order_time, commodity_index, amount, emergency</i>

## 2 Problem 1

### 2.1 Problem Analysis

In this part SF Express has its substations on all 656 cities covered in the orders. We came up with a network model. Regard *city* as vertex and *tool* as edge, we can construct a network and simulate the transportation of orders on it. Our cost function is defined as

$$C(p) = \text{transport\_time}^{\text{rate}} \times \text{transport\_cost}$$

Here  $p$  is the path that a particular order takes. And we evaluate the path using our cost function by the time the order takes from the time it was made to the time the package was sent to the consumer. We add an exponential *rate* to represent the weight of time in the cost function.

The problem is an *NPO* problem, we give the formal definition as follows:

- *I*: The network model  $G = (V, E)$  and the set of *order*
- *sol*: A set of paths  $P$  representing the delivery scheme
- *m*:  $m(G, \text{order}) = \sum_{p \in P} C(p)$
- *goal*: *min*

We consider that the problem is not a *LP* or *ILP* problem. Because the *transport\_time* here is not linear. For example, there exist some orders that cannot be sent in the same day it was ordered. They will be delayed for several days thus the *transport\_time* of a certain order will be a piecewise function. So we defined a non-linear object function, and constructed such network model.

## 2.2 Algorithm Design

## 2.3 Theoretical Analysis

**Complexity Analysis** We implemented a modified DFS algorithm to search for optimal solutions for each order.

**Efficiency Analysis** The problem is an NP problem. We can find such a certifier that given a delivery scheme we can verify the correctness order-by-order. The procedure will take polynomial time and thus the problem is NP.

## 2.4 Performance Evaluation

# 3 Problem 2

## 3.1 Problem Analysis

In this section, we set some hubs in some cities. Hubs can gather packages and send them together to the same city with lower unit cost. However, the packages gathered together at a hub to one destination can only be sent by one transportation tool. We defined some new symbols

We consider it's an *NPO* problem as well.

**Table 2.** Problem 2 Symbols

Symbol	Definition
$\hat{C}$	The cost of setting a hub, a constant
$discount$	The discount rate on the cost when packages are sent from the same hub, $discount \in (0, 1)$
$\#hub$	The number of hubs
$H$	The set of cities where hubs are set

- $I$ : The network model  $G = (V, E)$ , the set of *order*, the set of hubs  $H$
- $sol$ : A set of paths  $P$  representing the delivery scheme
- $m$ :  $m(G, order, H, \hat{C}, discount) = \sum_{p \in P} C(p)$
- $goal$ :  $min$

## 3.2 Algorithm Design

First, we designed the algorithm to choose suitable cities to set hubs. Then, we designed the algorithm to find a new delivery scheme.

## 3.3 Theoretical Analysis

**Complexity Analysis**

**Efficiency Analysis**

### 3.4 Performance Evaluation

## 4 Problem 3

### 4.1 Problem Analysis

### 4.2 Algorithm Design

### 4.3 Theoretical Analysis

### 4.4 Performance Evaluation

## 5 Problem 4

### 5.1 Problem Analysis

### 5.2 Algorithm Design

### 5.3 Theoretical Analysis

### 5.4 Performance Evaluation

## 6 First Section

### 6.1 A Subsection Sample

Please note that the first paragraph of a section or subsection is not indented. The first paragraph that follows a table, figure, equation etc. does not need an indent, either.

Subsequent paragraphs, however, are indented.

**Sample Heading (Third Level)** Only two levels of headings should be numbered. Lower level headings remain unnumbered; they are formatted as run-in headings.

*Sample Heading (Fourth Level)* The contribution should contain no more than four levels of headings. Table 3 gives a summary of all heading levels.

**Table 3.** Table captions should be placed above the tables.

Heading level	Example	Font size and style
Title (centered)	<b>Lecture Notes</b>	14 point, bold
1st-level heading	<b>1 Introduction</b>	12 point, bold
2nd-level heading	<b>2.1 Printing Area</b>	10 point, bold
3rd-level heading	<b>Run-in Heading in Bold.</b> Text follows	10 point, bold
4th-level heading	<i>Lowest Level Heading.</i> Text follows	10 point, italic

Displayed equations are centered and set on a separate line.

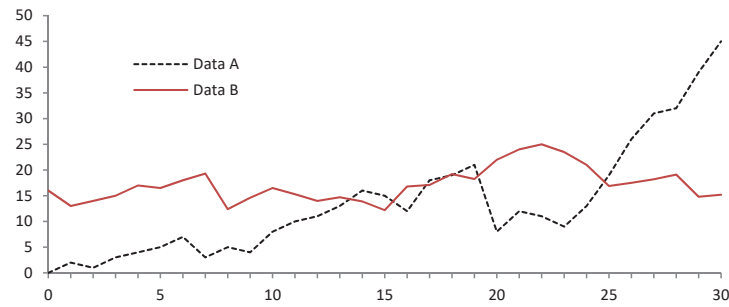
$$x + y = z \quad (1)$$

Please try to avoid rasterized images for line-art diagrams and schemas. Whenever possible, use vector graphics instead (see Fig. 1).

**Theorem 1.** *This is a sample theorem. The run-in heading is set in bold, while the following text appears in italics. Definitions, lemmas, propositions, and corollaries are styled the same way.*

*Proof.* Proofs, examples, and remarks have the initial word in italics, while the following text appears in normal font.

For citations of references, we prefer the use of square brackets and consecutive numbers. Citations using labels or the author/year convention are also acceptable. The following bibliography provides a sample reference list with entries for journal articles [1], an LNCS chapter [2], a book [3], proceedings without editors [4], and a homepage [5]. Multiple citations are grouped [1,2,3], [1,3,4,5].



**Fig. 1.** A figure caption is always placed below the illustration. Please note that short captions are centered, while long ones are justified by the macro package automatically.

## Acknowledgements

Here is your acknowledgements. You may also include your feelings, suggestion, and comments in the acknowledgement section.

## References

1. Author, F.: Article title. Journal **2**(5), 99–110 (2016)
2. Author, F., Author, S.: Title of a proceedings paper. In: Editor, F., Editor, S. (eds.) CONFERENCE 2016, LNCS, vol. 9999, pp. 1–13. Springer, Heidelberg (2016).
3. Author, F., Author, S., Author, T.: Book title. 2nd edn. Publisher, Location (1999)
4. Author, A.-B.: Contribution title. In: 9th International Proceedings on Proceedings, pp. 1–2. Publisher, Location (2010)
5. LNCS Homepage, <http://www.springer.com/lncs>. Last accessed 4 Oct 2017