**Investigating a real-time Hydraulic Erosion Simulation to be used for terrain generation in games**

1 Introduction

This portfolio project will contain an investigation into real-time hydraulic erosion when creating realistic terrain in video games and a program that will use techniques found in the investigation to create a real-time hydraulic erosion simulation. Terrain is one of the most important aspects of emulating a realistic virtual experience whether it’s in a computer game that requires a large-scale terrain for an open world experience, a movie that requires a fantasy style location that might be too dangerous to film in or a training simulation that requires the most realistic environment to help train people.

1.1 Aims and Goals

What needs to be achieved

* Aims – quite broad
* Objectives – very specific

2 Literature Review

General tips:

* Use diagrams, but be aware that for important stuff for your project you really need to explain in your own words

Extra sections here:

* Real world stuff
  + Include diagrams, pictures etc (all fully referenced)
* How have scientists modelled this?

2.1 Terrain

(INTRO CAN BE FINISHED LATER)

Generating realistic terrain for games is a long and time-consuming process. To solve this problem developers have found quicker and more effective ways for generating realistic terrain. When talking about terrain generation the first step is how that data is represented. Terrain data can be represented with two main models. These being a volumetric model and an elevation model.

2.1.1 Terrain Representation

The elevation model can be described with either an elevation function or a discrete heightfield. The most commonly used method is the discrete heightfield. The discrete heightfield uses a two-dimensional grid to represent the altitude of each position. This means that it is unable to recreate suspended materials like overhangs, caves, and arches. But it is a lot less data heavy which allows a simulation to be ran a lot faster with more area to work with. Elevation functions use a formula that can generate a point of altitude at any point in terrain. This allows for a program to generate multiple points to create a terrain of any size required.[2]

The volumetric model is similar to the elevation model but instead of using two-dimensional space it uses voxels which allow for a three-dimensional space where each cell represents a material at a particular position. This allows for the use of features like overhangs, caves, and arches. Volumetric models are very data heavy which makes them slower to run. There are ways to optimize the data structure by using compression techniques like Sparse Voxel Octrees to reduce the memory cost. This is done using an octree. An octree is where a three-dimensional space gets recursively divided into subspaces of children nodes until each voxel only contains one point or multiple point of similar data.[1] This technique can be used in open world games which require real time interaction.

2.1.2 Terrain Generation

When creating terrain there are two main ways for acquiring the terrain data. These being data sets and procedural generation. Data sets can be created by artists modelling the terrain in a 3D modelling software or by collecting data from the real world. There are also ways for users to input a small amount of detail into a program which then outputs a model based on the users input. Procedural generation is a method where programs generate their own data with no user input to be used for terrain. (start explaining about each type \-(:/)-/ )

Noise is essentially a function that generates a set of random numbers. It is used in multiple different procedural generation methods. But random numbers on their own aren’t what you want when modelling terrain. What a noise function does is it takes white noise, which is a source of random uniformly distributed numbers with no correlation whatsoever between successive numbers and gives it a structure or pattern to then be used. White noise can be generated by a random physical process, such as the thermal noise that occurs within many analogue electronic systems.[7]

There are multiple different functions that can be used with handling noise. One famous function is the Perlin noise function discovered by Ken Perlin in 1983[8] which was then improved in 2001 by Ken Perlin again who called it simplex noise[9].

Fractals are defined as sets that exhibit self-similarity under scaling. This means when you zoom in on a fractal pattern, the same pattern will repeat itself over and over again. There are many different fractal algorithms that have been discovered each with their own unique properties and characteristics. Fractals can be described by using a property called a fractal dimension. Fractal dimensions allow for real number to be used to describe a dimension. For example, 2.3, 2 being the second dimension and .3 being the fractal increment. The fractal increment determines the roughness of the fractal with 0 being flat and .999 being rough. The equation for finding a fractal dimension was discovered by Benoit Mandelbrot.[3] This equation being:

D = log(N) / log(1 / r)

Where D is the fractal dimension, N is the amount an object can be divided and r being the ratio how much the object has been divided. A good example to show this would be the von Koch snowflake curve which was known as an “early mathematical monster” where a simple line segment is divided into thirds and the middle third is replaced by two segments forming part of an equilateral triangle. At the next stage in the construction each of these 4 segments are replaced by 4 new segments with length 1/3 of their parent according to the original pattern. This then is repeated over and over again yielding the von Koch curve.

(PICTURE OF THE SNOWFLAKE CURVE)

So with the amount the object gets divided being 4, each of these section is scaled down by 1/3. The equation for the von Koch snowflake curve would be D = log(4) / log(3). This means that the fractal dimension equals 1.26. There are a few different ways these fractals can be used to generate terrain. One of them being Multifractals. What this does is it takes a Noise function adds an offset to it and then multiplies it by the power of the lacunarity which is the change in scale between successive levels of detail and the fractal dimension. It then repeats this over a given number of octaves which is the number of scales at which you’re adding in smaller details.[5][6]

2.2 Water/Fluid Simulation

Most fluids in animation are governed by the Navier-Stokes equations. These equations are a set of partial differential equations that are supposed to hold throughout the fluid. The Navier-Stokes equations are split into two equations. One being the momentum equation and the other being the incompressibility equation. The momentum equation is derived from newtons second law where mass times acceleration equals force. The momentum equation has been adapted for flow. This is done by including viscosity, pressure and velocity force related to time. The equation looks like this:

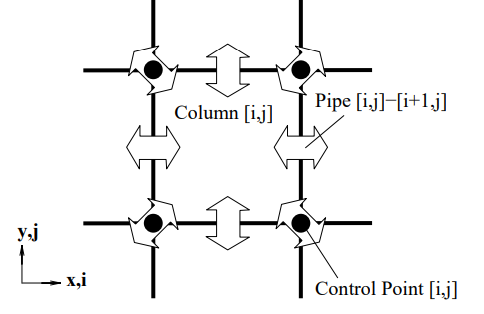
The p is the density of the fluid, du/dt is the time dependent velocity, P being the pressure, v being the dynamic viscosity and F being any forces interacting with the fluid which in most cases is usually gravity. The incompressibility equation is to state that the continuity does not change, and that mass is conserved. The equation looks like this:

The first part of this equation is the divergence, and the u is the velocity vector field. This equation describes how the mass of a fluid across the field must never change therefor has to be zero.[10][11]

(somewhat of an intro probably need more)

Now that we have talked about the Navier-Stokes equations we can talk about the methods used to simulate water. When simulating water there are two main approaches to tracking the fluid. These being the Eularian approach and the Lagrangian approach. The Lagrangian approach, which was named after the mathematician Lagrange, labels each point in a fluid as a separate particle with its own position and velocity. This is well known as a particle system. One of the most common particle systems is called Smooth Particle Hydrodynamics which was discovered by R.A.Gingold and J.J.Monaghan in 1977[12]. The Eularian approach, which was named after the mathematician Euler, takes a different approach. Instead of tracking each particle it tracks a fixed point in space and tracks the fluid density and pressure of that fixed position. This is also known as a grid-based approach. There are multiple grid-based methods used when simulating fluids. One of these being the Pipe Model method which was discovered by James F. O’Brien and Jessica K. Hodgins[14] and was then later adapted to run faster on a GPU by Xing Mei, Philippe Decaudin and Bao-Gang Hu. There are of course many more.[15]

Smooth Particle Hydrodynamics is one of the most commonly used particle-based simulation methods. It works by first identifying the properties of each particle. It does this by acquiring all the neighbouring particles within the kernel radius. Computes the kernel weight at the centres of the neighbouring particles. Finds the weight of the physical quantity carried by the neighbouring particles by the kernel values and then sums the values obtained. This method then uses a simplified version of the Navier-Stokes equation to calculate the motion.[13]

The Pipe Model method is a grid-based water simulation method that uses virtual pipes that connect neighbouring cells to transfer water between them. It stores its data on a two-dimensional grid where the height of the water is stored in each position on the grid. Each cell is connected eight ways to every neighbouring cell and looks like this:

Picture from [14]

To transfer water, it calculates the pressure between each pipe to measure which direction the water will flow. The equation to determine the flow in the pipes are derived from the physical laws of hydrostatic pressure. The static pressure of the grid cell at position [i, j] would be:

Where is the density of the fluid, g is the acceleration due to gravity, is the set atmospheric pressure in the system, is external forces that don’t include gravity like objects hitting the surface of the water, and is the height of the grid cell at [i, j]. To then solve the acceleration of a pipe it uses an equation that’s derived from Newtons second law being F = ma. Which looks like:

Where is the pipe connecting a grid cell to a neighbouring grid cell, c is the cross-sectional area of the pipe, and m is the mass of the fluid in the pipe. The mass of the fluid in the pipe can be expressed with , where l is the length of the pipe. Assuming that the set atmospheric pressure is a constant this equation can then be rewritten as:

To calculate the flow in the pipe it then assumes that the acceleration over a time step is constant which then gives us the equation:

To then calculate the net volume change of a time step it uses the equation:

After this at the end of each time step all grid cells are tested to see if any are at a negative volume. If so, then all the pipes that are removing water are scaled back. This is repeated until all grid cell volumes are positive.[14]

The Shallow Water equations are a set of partial differential equations that describe the behaviour of water waves in shallow areas of water. These equations are derived from the Navier-Stoke equations and make a few assumptions about the simulated water. One assumption being that the horizontal length of the water is greater than the vertical length. It also assumes that the vertical velocities of the water are very minimal.

When it comes to how efficient a water simulation is, both particle-based and grid-based methods have their own advantages and disadvantages. Particle-based methods only require for you to simulate where water is precent, while using a grid-based method requires the entire world space to be simulated at all time steps. But particle-based methods find difficulties with large bodies of water as it would require thousands of particles to be simulated each time step. This shows that particle-based methods are better suited to small bodies of water whilst grid-based methods are more efficient at running larger bodies of water such as rivers, canals, or oceans/waves. This has led to people investigating hybrid methods that utilize the advantages of both methods. A paper made by Nuttapong Chentanez and Matthias Müller investigates creating one such method. They do this by first simulating water on a two-dimensional height field using the shallow water equations. Then they detect when the height field struggles to simulate and generate particles at that point. The particles then later get removed when they’re enter a point on the height field that can simulate again.

2.3 Erosion Algorithms

(INTRO TO EROSION)

There are multiple different types of erosion in the real world that can be simulated. These include weathering and denudation. Weathering is a small-scale erosion that usually effects stones and rocks. Denudation is an erosion process that mostly results in shaping the surface of an area causing rivers, valleys, or canyons.

Weathering can be split up into two sections. Chemical and thermal. Chemical weathering is the process when moisture makes contact with the surface of a material causing a chemical change. Thermal weathering is the process at which the change in temperature causes material to expand and retracted allowing cracks to form.

Denudation can be split into three sections. Gravity conditioned movement, splash erosion and fluvial erosion. Gravity conditioned movement is when loose material such as soil, gravel or sand moves when it reaches an equilibrium between the gravity and its inner tension. Splash erosion can be described as when raindrops make impact with a material like sand causing an indent in its place. And finally fluvial erosion is the process at which flowing water interacts with the landscape it is flowing down causing material to be remove from the surface being forced down stream with the water.

**Heading: games implemented**

* Talk about specific games and how they implement their methods (where known)

3 Design

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References

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