

Exam 1 - Chapters 1 - 4 & Notes

1. What is 23_{base6} minus 23_{base4} ? Express the answer in base 10.

$$23_6 = 3(6^0) + 2(6^1) = 3 + 12 = 15_{10}$$

$$23_4 = 3(4^0) + 2(4^1) = 3 + 8 = 11_{10}$$

$$15 + 11 = 26_{10}$$

2. Find the value of the following 8-bit two's complement binary number: 11001010

$$11001010 - 1 = 11001001$$

$$\text{Inversion } 00110110$$

$$00110110 = 2^1 + 2^2 + 2^4 + 2^5 = 2 + 4 + 16 + 32 = 54$$

$$11001010 = -54$$

3. Using the Hamming Algorithm with EVEN parity, find the position of the error and the corrected data string.

1001 0001 0010

100100010010

$$p1 = ? 0 0 0 0 1 = 1$$

$$p2 = ? 0 00 01 = 1$$

$$p3 = ? 000 0 = 0$$

$$p4 = ? 0010 = 1$$

12 4 8

100100010010

11 0 1

$$*X X * = 6$$

bit 6 incorrect

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100101010010

$$p1 = ? 0 0 0 0 1 = 1$$

$$p2 = ? 0 10 01 = 0$$

$$p3 = ? 010 0 = 1$$

$$p4 = ? 0010 = 1$$

12 4 8

100101010010

10 1 1

Position of error \rightarrow 6

Corrected Data String \rightarrow 1001 0101 0010

4. List all the ordered pairs that make the following expression true:

$$\neg(\neg A + \neg B)$$

$$\neg\neg A * \neg\neg B \text{ DeMorgan's}$$

$$A * B \text{ Double Negation}$$

The ordered pair that makes this expression true is (1,1)

A	B	Value
0	0	0
1	0	0
0	1	0
1	1	1

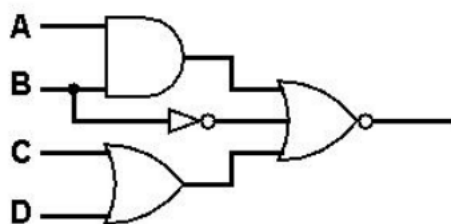
5. Write the Boolean expression in Sum of Product (SOP) form represented by the truth table below

A	B	C	Output
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

6. Write the simplified (minimized) expression for the boolean function defined by the following Karnaugh Map (KMap) in Sum of Product (SOP) form.

		yz			
		00	01	11	10
wx	00	0	1	0	1
	01	0	1	1	1
	11	1	1	0	0
	10	1	1	0	1

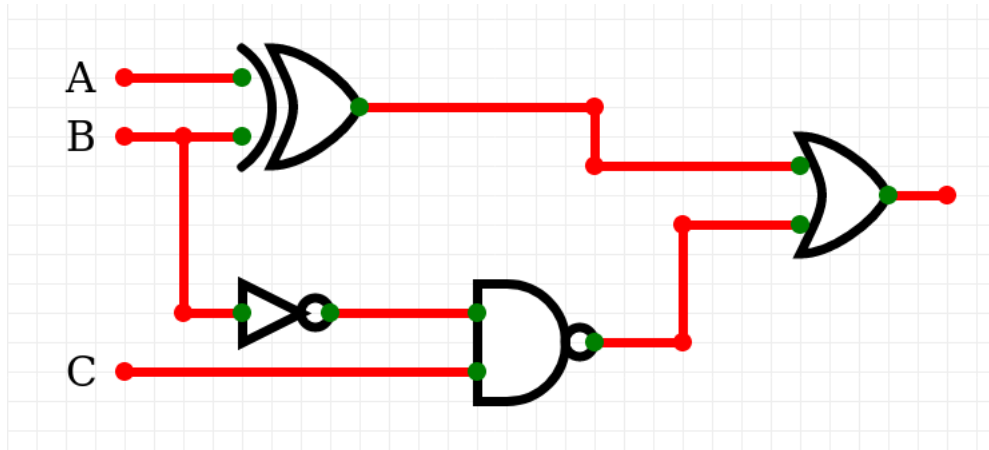
7. What is the Boolean Expression represented by the digital circuit?



$$\neg[(A * B) + \neg B + (C + D)]$$

8. Draw the circuit diagram for the following expression:

$$(A \oplus B) + \neg(\neg B * C)$$



9. What is the final value of C when the program is run?

A	DC	4	# label A defined as 4
B	DC	120	# label B defined as 120
C	DC	0	# label C defined as 0
TOP	LOAD	C	# C in the accumulator
	ADD	=1	# ACC += 1
	STORE	C	# C = 1
	LOAD	C	# C in ACC
	SUB	A	# ACC = 1 - 4 = -3
	SUB	A	# ACC = -3 - 4 = -7
	SUB	A	# ACC = -7 - 4 = -11
	STORE	B	# B = -11
	LOAD	B	# ACC = -11
	SUB	A	# ACC = -11 - 4 = -15
	BG	TOP	# Does not Branch to TOP because !(ACC>0)
	END		# END

The final value of C is 1