

## Chapter 3 Homework

### QUESTIONS

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**10. Does the odometer of a car measure a scalar or a vector quantity? What about the speedometer?**

The odometer of a car measures a scalar quantity. The speedometer also measures a scalar quantity.

**16. A projectile is launched at an upward angle of  $30^\circ$  to the horizontal with a speed of 30m/s. How does the horizontal component of its velocity 1.0s after launch compare with its horizontal component of velocity 2.0s after launch, ignoring air resistance? Explain.**

The projectile will be farther away after 2 seconds than it is at 1 second. Its velocity in the horizontal direction will not change, though, because the force of gravity will only have an effect on the vertical velocity.

**17. A projectile has the least speed at what point in its path?**

A projectile has the least speed at the apex of its climb and the termination of its path.

**19. A person sitting in an enclosed train car, moving at a constant velocity, throws a ball straight up into the air in her reference frame.**

**(a) Where does the ball land?**

The ball lands where it started on the train.

**(b) Where does the ball land if the car accelerates?**

The ball lands in the negative x direction in relation to its starting position in the train's reference frame.

**(c) Where does the ball land if the car decelerates?**

In the train's reference frame, the ball will land +x from where it started.

**(d) Where does the ball land if the car rounds a curve?**

In this case, the ball will land offset by some value of z and likely an offset of x as well.

**(e) Where does the ball land if the car moves with constant velocity but is open to the air?**

Assuming air resistance, the ball will land behind its starting position, that is the -x direction.

### **MISCONCEPTION QUESTIONS**

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**4. Which of the following equations correctly expresses the relation between vectors  $\vec{A}$ ,  $\vec{B}$ , and  $\vec{C}$ , shown in Fig 3-36?**

(b)  $\vec{B} = \vec{A} + \vec{C}$

**6. A bullet fired horizontally from a rifle begins to fall**

(a) as soon as it leaves the barrel

**9. Two balls having different speeds roll off the edge of a horizontal table at the same time. Which hits the floor sooner?**

(c) Both the same.

**10. You are riding in an enclosed train car moving at 90km/h. If you throw a baseball straight up, where will the baseball land?**

(c) In your hand.

**11. Which of the three kicks in Fig. 3-38 is in the air for the longest time? They all reach the same maximum height  $h$ . Ignore air resistance.**

(c)

**13. A hunter is aiming horizontally at a monkey who is sitting in a tree. The monkey is so terrified when it sees the gun that it falls off the tree. At that very instant, the hunter pulls the trigger. What will happen?**

(d) It depends on how far the hunter is from the monkey.

## PROBLEMS

1. A car is driven 245 km west and then 118 km southwest ( $45^\circ$ ). What is the displacement of the car from the point of origin (magnitude and direction)? Draw a diagram.

| $\vec{v}$ | $v_x$   | $v_y$  |
|-----------|---------|--------|
| West      | -245    |        |
| Southwest | -83.44  | -83.44 |
| Total     | -328.44 | -83.44 |

$$\tan^{-1}\left(\frac{-83.44}{-328.44}\right) = 14.25$$

$$R = \sqrt{(-83.44)^2 + (-328.44)^2} = 338.9$$

$$\text{Displacement} = 338.9 \angle 14.25^\circ \text{ Southwest}$$

2. If  $V_x = 9.40$  units and  $V_y = -6.80$  units, determine the magnitude and direction of  $\vec{V}$

$$\tan^{-1}\left(\frac{9.40}{-6.80}\right) = -54.1^\circ$$

$$V_r = \sqrt{9.40^2 + 6.80^2} = 11.6$$

$$\vec{V} = 11.6 \angle 54.1^\circ \text{ south of east}$$

8. An airplane is traveling 815 km/h in a direction  $41.5^\circ$  west of north.

(a) Find the components of the velocity vector in the northerly and westerly directions.

$$\cos(41.5) = \frac{y}{815} \implies y = 815(\cos(41.5)) = 610.4$$

610.4 km/h North

$$\sin(41.5) = \frac{x}{815} \implies x = 815(\sin(41.5)) = 540.0$$

540.0 km/h West

(b) How far north and how far west has the plane traveled after 1.75 h?

$$610.4 \times 1.75 = 1068.2$$

1068.2 km North

$$540.0 \times 1.75 = 945$$

945 km West

9. The summit of a mountain, 2450 m above base camp, is measured on a map to be 4580 m horizontally from the camp in a direction  $38.4^\circ$  west of north. What are the components of the displacement vector from camp to summit? What is its magnitude? Choose the x axis east, y axis north, and z axis up.

$$\sin 38.4 = \frac{x}{4580} \Rightarrow x = 4580 \sin 38.4 \Rightarrow x = 2844.9 \text{ m}$$

$$\cos 38.4 = \frac{y}{4580} \Rightarrow y = 4580 \cos 38.4 \Rightarrow y = 3589.3 \text{ m}$$

z: 2450m

magnitude: 4580m

10. Three vectors magnitudes are given in arbitrary units. Determine the sum of the three vectors. Give the resultant in terms of

(a) components

| Vector    | Resultant | Degree | Calculations   | $\vec{V}_x$ | $\vec{V}_y$ |
|-----------|-----------|--------|--|-------------|-------------|
| $\vec{A}$ | 42.0      | 28.0   | $\vec{A}_x = 42 \cos(28)$<br>$\vec{A}_y = 42 \sin(28)$   | 37.08       | 19.72       |
| $\vec{B}$ | 29.7      | 56.0   | $\vec{B}_x = 29.7 \cos(56.0)$<br>$\vec{B}_y = 29.7 \sin(56.0)$   | -16.61      | 24.62       |
| $\vec{C}$ | 31.0      |        |  |             | -31.0       |
| $\vec{D}$ | 24.43     | 33.09  | $\vec{D}_x = 37.08 - 16.61$<br>$\vec{D}_y = 19.72 + 24.62 - 31.0$<br>$\tan^{-1}\left(\frac{13.34}{20.47}\right)$<br>$\vec{D}_R = \sqrt{(13.34)^2 + (20.47)^2}$ | 20.47       | 13.34       |

(b) magnitude and angle with the +x axis

$$\vec{D} = 24.43 \angle 33.09^\circ$$

32. A tiger leaps horizontally from a 7.5-m-high rock with a speed of 3.0m/s. How far from the base of the rock will he land?

$$\Delta y = v_{0y}t - \frac{1}{2}gt^2 \Rightarrow -7.5 = -4.9t^2 \Rightarrow \sqrt{\frac{-7.5}{-4.9}} = t = 1.24 \text{ s}$$

$$\Delta x = v_{x0}t \Rightarrow \Delta x = 3.0(1.24) \Rightarrow \Delta x = 3.72 \text{ m}$$

**34. A ball is thrown horizontally from the roof of a building 7.5m tall and lands 9.5m from the base. What was the ball's initial speed?**

$$\Delta y = v_{0y}t - \frac{1}{2}gt^2 \implies -7.5 = -4.9t^2 \implies \sqrt{\frac{-7.5}{-4.9}} = t = 1.24s$$

$$v_{0x} = \frac{\Delta x}{t} \implies v_{0x} = \frac{9.5}{1.24} \implies v_{0x} = 7.66m/s$$

**36. A football is kicked at ground level with a speed of 18.0m/s at an angle of 31.0° to the horizontal. How much later does it hit the ground?**

$$R = \frac{v_0^2 \sin 2\theta}{g} \implies R = \frac{18.0^2 \sin(62)}{9.8} \implies R = 1.62m$$

$$\Delta x = v_{0x}t \implies t = \frac{\Delta x}{v_{0x}} \implies t = \frac{1.62}{18.0} \implies t = 0.09s$$

**47. A rescue plane wants to drop supplies to isolated mountain climbers on a rocky ridge 265m below. If the plane is traveling horizontally with a speed of 125km/h, how far in advance of the recipients (horizontal distance) must the goods be dropped?**

Given:

$$\Delta y = -265m$$

$$v_{x0} = 34.72m/s = \left( \frac{125km}{h} \times \frac{1h}{3600s} \times \frac{1000m}{1km} \right)$$

Find:  $\Delta x$

$$\Delta y = v_{y0}t - \frac{1}{2}gt^2 \implies -265 = -4.9t^2 \implies t = \sqrt{\frac{-265}{-4.9}} \implies t = 7.354$$

$$\Delta x = v_{x0}t \implies \Delta x = (34.72m/s)(7.354s) \implies \Delta x = 255.3m$$