## Laplace transform of differential equations: MX-3202

Wednesday, 7 February 2024 11:13 am

$$\mathcal{L}\left[\frac{df}{dt}\right] = sF(s) - f(0-) \qquad \mathcal{L}\left[Y(t)\right] = Y(s) \\
\mathcal{L}\left[\frac{d^{2}f}{dt^{2}}\right] = s^{2}F(s) - sf(0-) - f'(0-) \qquad \mathcal{L}\left[Y'(t)\right] = sY(s) - Y(o) \\
\mathcal{L}\left[\frac{d^{2}f}{dt^{2}}\right] = s^{n}F(s) - \sum_{k=1}^{n} s^{n-k}f^{k-1}(0-) \qquad \mathcal{L}\left[Y''(t)\right] = s^{2}Y(s) - sY(o) - Y'(o) \\
\mathcal{L}\left[Y'''(t)\right] = s^{3}Y(s) - s^{2}Y(o) - sY'(o) - Y''(o) \\
\mathcal{L}\left[Y'''(t)\right] = s^{4}Y(s) - s^{3}Y(o) - s^{2}Y(o) - sY'(o) \\
\mathcal{L}\left[\frac{d^{5}f}{dt^{5}}\right] = \mathcal{L}\left[Y''''\right] = s^{5}Y(s) - s^{4}Y(o) - s^{3}Y'(o) - s^{2}Y''(o) \\
\mathcal{L}\left[\frac{d^{5}f}{dt^{5}}\right] = s^{5}F(s)$$

$$\int \frac{d^2y}{dt^2} + 12\frac{dy}{dt} + 32y = 32u(t)$$

$$\int \int \frac{s^2}{(s)} - \frac{sy(s)}{s} + \frac{32}{s} \left[\frac{y_{(s)}}{s}\right] = \frac{32}{s}$$
initial conditions
$$\int \frac{d^2y}{dt^2} + 12\frac{dy}{dt} + 32y = 32u(t)$$

$$\int \int \frac{s^2}{(s)} - \frac{32}{s} + \frac{32}{s} \int \frac{y_{(s)}}{s} + \frac{32}{s} \int \frac{y_{(s)}}$$

$$Y(5) \left[ 5^2 + 125 + 32 \right] = \frac{32}{5}$$

$$\gamma_{(s)} = \frac{32}{s(s^2+12s+32)}$$

$$\left[ \int_{0}^{2x} \frac{d^{2}x}{dt^{2}} + 4\frac{dx}{dt} + 5x = 1 \right] \Rightarrow \left[ \int_{0}^{2x} \frac{dx}{dt} + 5x = 1 \right] \Rightarrow \left[ \int_{0}$$